

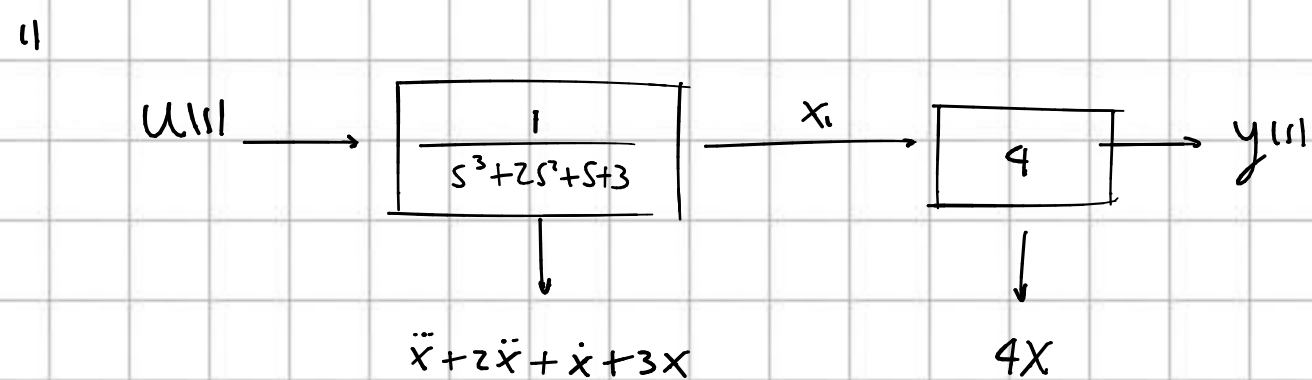
# Taller

$$1) G(s) = \frac{4}{s^3 + 2s^2 + s + 3}$$

$$2) G(s) = \frac{4s}{s^3 + 2s^2 + s + 3}$$

$$3) G(s) = \frac{6s^2 + 4s + 2}{s^4 - s^3 + 2s + 3}$$

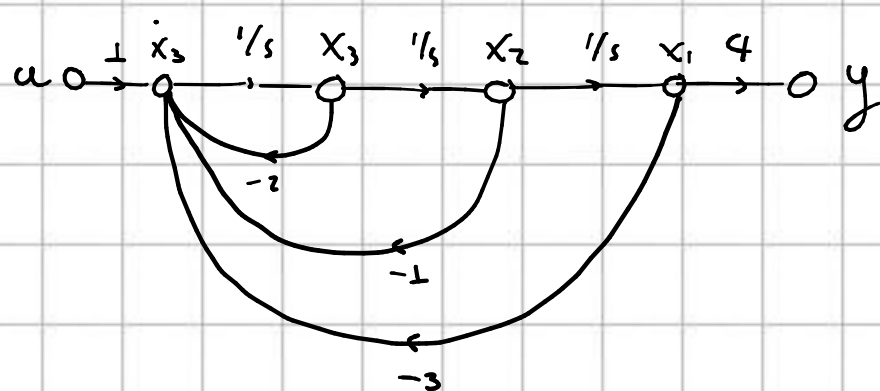
## Desarrollo



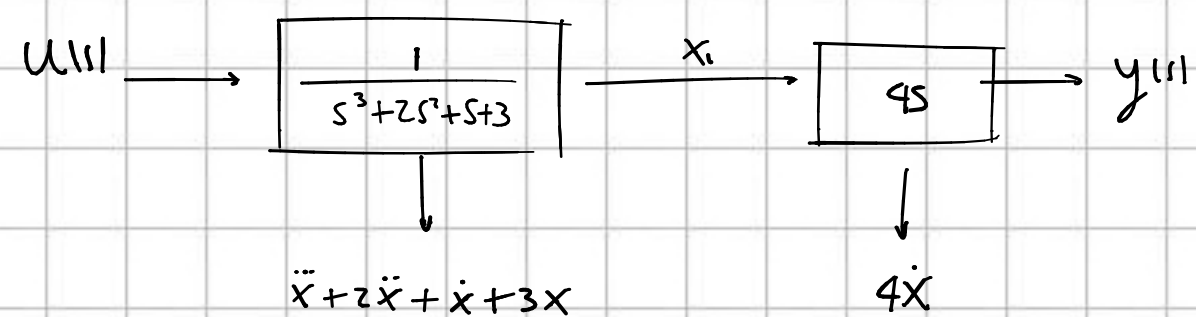
$$\begin{aligned} x &= x_1 & \dot{x}_3 + 2x_3 + x_2 + 3x_1 &= u & 4x_1 &= y \\ \dot{x} &= x_2 & \dot{x}_3 &= u - 2x_3 - x_2 - 3x_1 \\ \ddot{x} &= x_3 & & & \\ \ddot{\ddot{x}} &= \dot{x}_3 & & & \\ & & y &= 4x_1 \end{aligned}$$

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -3 & -1 & -2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} u$$

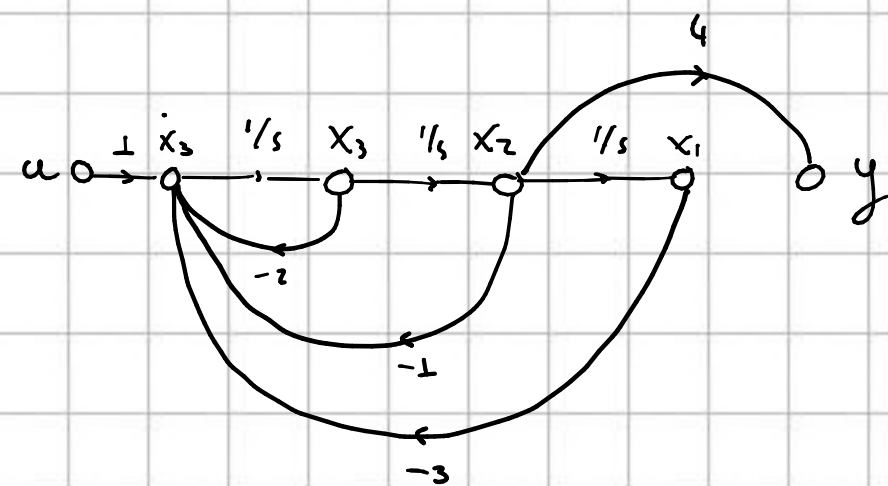
$$y = \begin{bmatrix} 4 & 0 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$



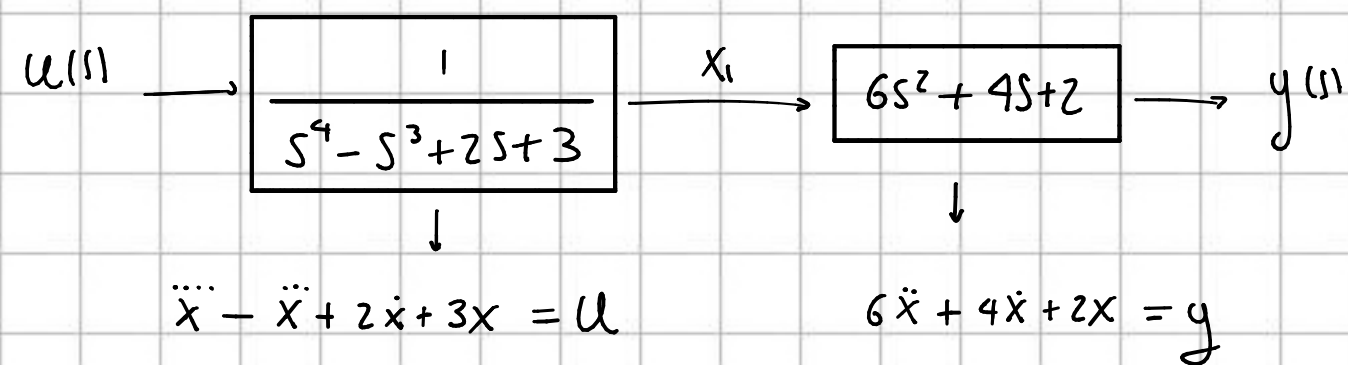
2)



$$\begin{aligned} x &= x_1 & \dot{x}_3 + 2x_3 + x_2 + 3x_1 &= u & 4x_2 &= y \\ \dot{x} &= x_2 & \dot{x}_3 &= u - 2x_3 - x_2 - 3x_1 \\ \ddot{x} &= x_3 & & & \\ \ddot{\ddot{x}} &= \dot{x}_3 & & & \\ & & y &= 4x_2 \end{aligned}$$



$$3) G(s) = \frac{6s^2 + 4s + 2}{s^4 - s^3 + 2s + 3}$$



$$\begin{aligned} x &= x_1 & \dot{x}_4 - x_4 + 2x_2 + 3x_1 &= u & 6x_3 + 4x_2 + 2x_1 &= y \\ \dot{x} &= x_2 = \dot{x}_1 & \dot{x}_4 &= u + x_4 - 2x_2 - 3x_1 \\ \ddot{x} &= x_3 = \dot{x}_2 & & & \\ \ddot{\ddot{x}} &= x_4 = \dot{x}_3 & & & \\ \ddot{\ddot{\ddot{x}}} &= \dot{x}_4 & & & \end{aligned}$$

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \\ \dot{x}_4 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ -3 & -2 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} u$$

$$y = \begin{bmatrix} 2 & 4 & 6 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix}$$

