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Demosttración Tarea

Demosttrar que en sistemas que operan en: 16% de overshoot

$$0,16 = e^{-\frac{\zeta \pi}{\sqrt{1-\zeta^2}}} \quad \text{Donde } \zeta = 0,504$$

$$\rightarrow \ln(0,16) = \frac{\zeta \pi}{\sqrt{1-\zeta^2}}$$

$$= \ln^2(0,16) = \frac{\zeta^2 \pi^2}{1-\zeta^2}$$

$$= \ln^2(0,16) - \ln^2(0,16) \zeta^2 = \zeta^2 \pi^2$$

$$= \ln^2(0,16) = \zeta^2 \pi^2 + \ln^2(0,16) \zeta^2$$

$$= \ln^2(0,16) = \zeta^2 (\pi^2 + \ln^2(0,16))$$

$$= \zeta = \frac{\sqrt{\ln^2(0,16)}}{\sqrt{\pi^2 + \ln^2(0,16)}} = \frac{\ln(0,16)}{\sqrt{\pi^2 + \ln^2(0,16)}}$$

$$= \zeta = 0,5039 \approx 0,504 \rightarrow \text{Valor que se pide}$$



$$\cos \phi = 0,504$$