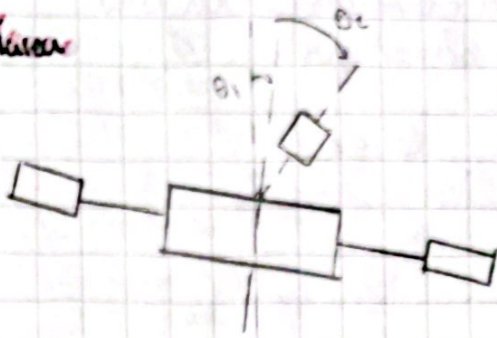
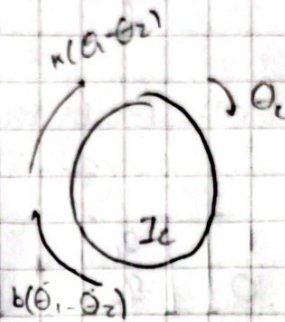
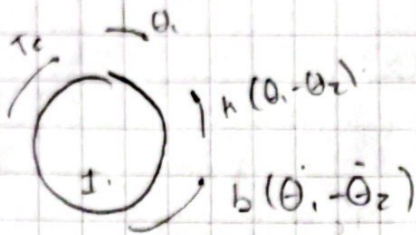
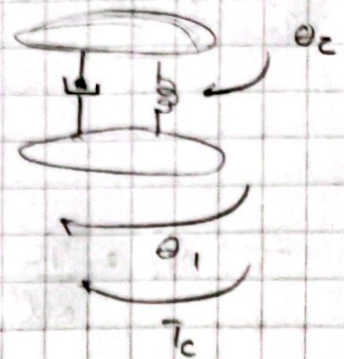


Answer



$\theta_c$ : Sensor

$\theta_1$ : Body



$$I_1 \ddot{\theta}_1 - k(\theta_1 - \theta_2) - b(\dot{\theta}_1 - \dot{\theta}_2) = I_1 \ddot{\theta}_1$$

$$b(\dot{\theta}_1 - \dot{\theta}_2) + k(\theta_1 - \theta_2) = I_2 \ddot{\theta}_2$$

$$\ddot{\theta}_1 = \frac{T_c}{I_1} - \frac{k}{I_1}(\theta_1 - \theta_2) - \frac{b}{I_1}(\dot{\theta}_1 - \dot{\theta}_2)$$

$$q_1 = \theta_1 \quad q_2 = \theta_2$$

$$\ddot{q}_1 = \frac{T_c}{I_1} - \frac{k}{I_1} q_2 + \frac{k}{I_1} q_3 - \frac{b}{I_1} \dot{q}_2 + \frac{b}{I_1} \dot{q}_3 \quad (1)$$

$$\dot{q}_2 = \dot{\theta}_1 = \dot{q}_1 \quad \dot{q}_4 = \dot{\theta}_2 = \dot{q}_3$$

$$\ddot{q}_2 = \ddot{\theta}_1 = \ddot{q}_1 \quad \ddot{q}_4 = \ddot{\theta}_2 = \ddot{q}_3$$

$$\ddot{q}_2 = \frac{b}{I_2}(\dot{q}_1 - \dot{q}_2) + k(q_1 - q_2)$$

$$\ddot{q}_4 = \frac{b}{I_2} \dot{q}_2 - \frac{b}{I_2} \dot{q}_4 + k q_1 - k q_3 \quad (2)$$

$$\begin{bmatrix} \ddot{q}_1 \\ \ddot{q}_2 \\ \ddot{q}_3 \\ \ddot{q}_4 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ -\frac{k}{I_1} & -\frac{b}{I_1} & \frac{k}{I_1} & \frac{b}{I_1} \\ 0 & 0 & 1 & 1 \\ k & \frac{b}{I_2} & -k & -\frac{b}{I_2} \end{bmatrix} \begin{bmatrix} q_1 \\ q_2 \\ q_3 \\ q_4 \end{bmatrix} + \begin{bmatrix} 0 \\ 1/I_1 \\ 0 \\ 0 \end{bmatrix} T_c$$

$\theta_1 = q_1 \quad \quad \quad \theta_2 = q_3$