

# L<sup>A</sup>T<sub>E</sub>X Workshop Exercise Sheet

December 2022

**Exercise 1:** Reproduce the following: A **number** is a mathematical object used to count, measure, *and* label. The original examples are the natural numbers 1, 2, 3, 4, and so forth. Other categories of numbers include:

- Rational numbers:  $\frac{1}{2}$
- Transcendental numbers:  $\pi$
- Irrational numbers:  $\sqrt{2}$ ,  $\sqrt[3]{2}$
- Real numbers:  $1$
- Complex numbers:  $a + bi$

**Exercise 2:** Reproduce the following:

$$(\forall \varepsilon > 0) (\exists \delta > 0) (\forall x \in \mathbb{R}) (0 < |x - p| < \delta \implies |f(x) - L| < \varepsilon)$$

**Exercise 3:** Reproduce the following (the images can be found [here](#) and [here](#)):



(a) A trivial statement



(b) A funny meme

Figure 1: Truer words have never been spoken.

$\times$	<b>1</b>	<b>i</b>	<b>j</b>	<b>k</b>
<b>1</b>	1	i	j	k
<b>i</b>	i	-1	-k	-j
<b>j</b>	j	-k	-1	i
<b>k</b>	k	j	-i	-1

Table 1: Quaterinon multiplication table

**Exercise 4:** Math expression

$$\exists n \geq 3, x, y, z \in \mathbb{N} \mid x^n + y^n = z^n \quad (1)$$

This result follows naturally from the argument in Figure ??, and we leave it as an exercise to the reader.✓

**Exercise 5:** Matrices and Tables

$$\begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ -\sin(\theta) & \cos(\theta) \end{bmatrix}$$

$$\begin{pmatrix} k \\ 1 \\ 1 \end{pmatrix} = \alpha \times \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} + \beta \times \begin{pmatrix} 0 \\ 0 \\ k \end{pmatrix}$$

**Exercise 6:** Prove that if  $n^2$  is even, then  $n$  is even.

**Challenge:** Let  $A$  be the set of solvable problems in polynomial time by a deterministic Turing machine and  $B$  the set of solvable problems in polynomial time by a non-deterministic Turing machine. Is  $A = B$ ?

**Reward:** €100