

1 Gráficos 3D

```
[1]: import numpy as np
import sympy as sp
import matplotlib.pyplot as plt
from matplotlib import cm

# Gráficos separados en novas ventás
%matplotlib qt

# Gráficos incrustados neste documento
%matplotlib inline
```

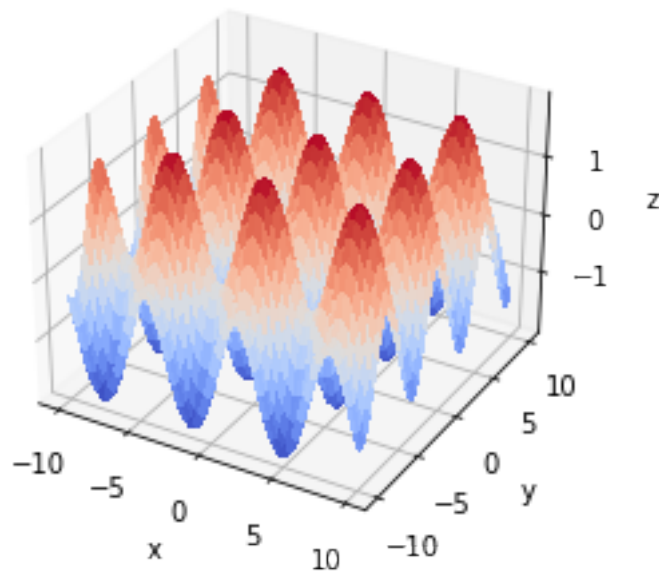
1.1 Gráficos $\mathbb{R}^2 \rightarrow \mathbb{R}$

```
[2]: # Definimos a función

fig = plt.figure()
ax = fig.gca(projection='3d')

# Definimos a superficie
X = np.arange(-10, 10, 0.1)
Y = np.arange(-10, 10, 0.1)
X, Y = np.meshgrid(X, Y)
Z = np.sin(X) + np.cos(Y)
#np.sqrt(X*Y)
#(X**2+2*Y**2)*np.exp(-X**2-Y**2)

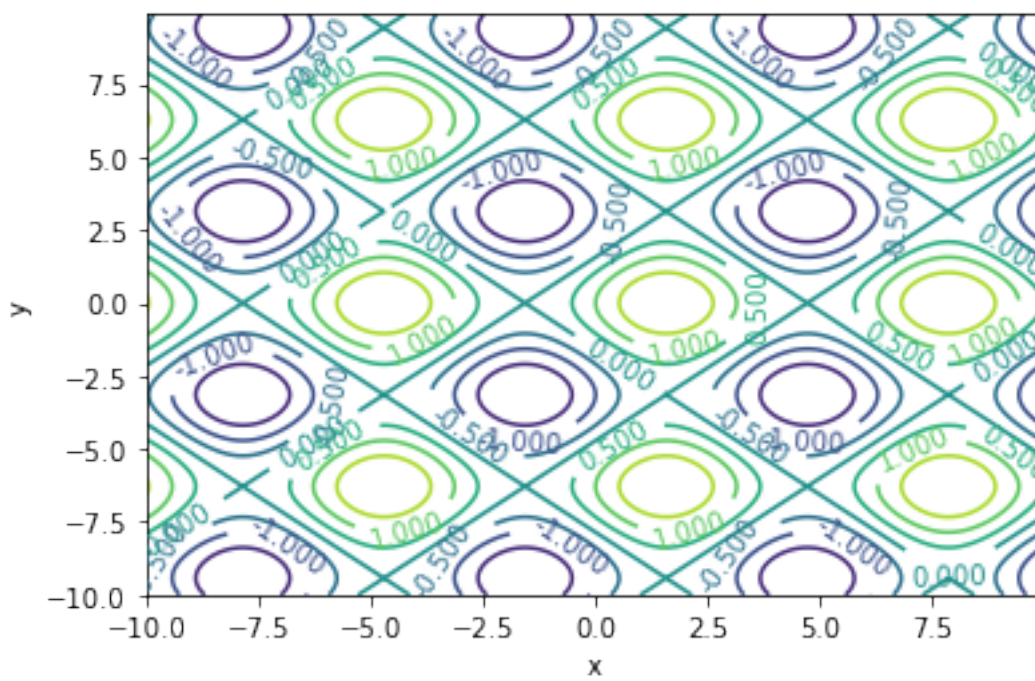
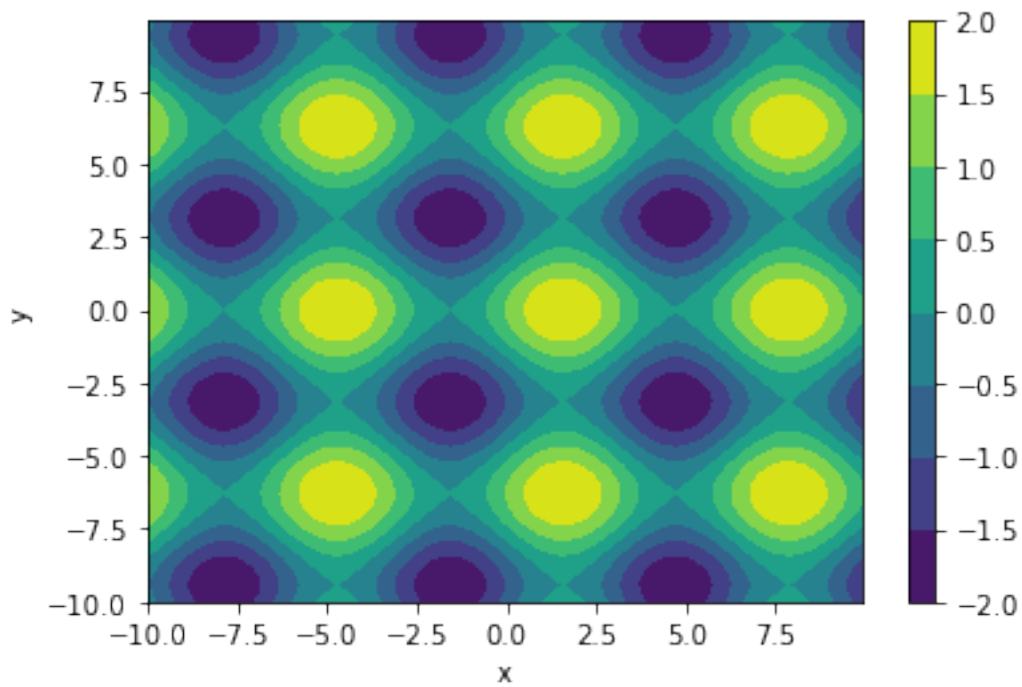
# Debuxámola.
surf = ax.plot_surface(X, Y, Z, cmap=cm.coolwarm, linewidth=0, antialiased=False)
ax.set_xlabel('x')
ax.set_ylabel('y')
ax.set_zlabel('z')
plt.show()
```



1.2 Curvas nivel

```
[3]: # Curvas de nivel (colorbar)
plt.figure()
plt.contourf(X, Y, Z)
plt.colorbar() # Engádese a barra de cores cos valores asociados
plt.xlabel('x')
plt.ylabel('y')
plt.show()

# Curvas de nivel (colorbar)
plt.figure()
figc = plt.contour(X, Y, Z)
plt.clabel(figc) # Engádese o valor numérico a cada curva de nivel
plt.xlabel('x')
plt.ylabel('y')
plt.show()
```



2 Curvas parametrizadas ($\mathbb{R} \rightarrow \mathbb{R}^2$)

```
[4]: # Curvas parametrizadas
fig = plt.figure()
ax = plt.axes(projection="3d")
# Creación dos puntos da curva
t = np.linspace(0, 3*np.pi, 100)
x_t = np.cos(t)
y_t = np.sin(t)
z_t = t
# Representación gráfica da curva 3D
p = ax.plot3D(x_t, y_t, z_t)
ax.set_xlabel('x')
ax.set_ylabel('y')
ax.set_zlabel('z')
plt.show()

# Creamos a función
t = sp.symbols('t', real=True)
expr = sp.cos(t), sp.sin(t), t
curva3d = sp.Lambda((t), expr)
curva = sp.lambdify((t), curva3d(t), "numpy") # Función numpy coa expresión da
→ curva
vtan = sp.diff(sp.cos(t), t), sp.diff(sp.sin(t), t), sp.diff(t, t)
vtanf = sp.Lambda((t), vtan)
v_curva = sp.lambdify((t), vtanf(t), "numpy") # Función numpy coa expresión do
→ vector tanxente
# Representación vectores
# Calculamos a derivada da anterior curva en t_0
t_0 = 0

fig = plt.figure()
ax = fig.add_subplot(projection='3d')
ax.plot3D(x_t, y_t, z_t) # Volvemos pintar a curva
ax.quiver(curva(t_0)[0], curva(t_0)[1], curva(t_0)[2],
          v_curva(t_0)[0], v_curva(t_0)[1], v_curva(t_0)[2], 1, color=['r']) #
→ Representación gráfica do vector tanxente en t_0
t_0 = np.pi
ax.quiver(curva(t_0)[0], curva(t_0)[1], curva(t_0)[2],
          v_curva(t_0)[0], v_curva(t_0)[1], v_curva(t_0)[2], color=['g']) #
→ Representación gráfica do vector tanxente
t_0 = 3*np.pi/2
ax.quiver(curva(t_0)[0], curva(t_0)[1], curva(t_0)[2],
          v_curva(t_0)[0], v_curva(t_0)[1], v_curva(t_0)[2], color=['m']) #
→ Representación gráfica do vector tanxente
```

```
ax.set_xlabel('x')  
ax.set_ylabel('y')  
ax.set_zlabel('z')  
plt.show()
```

