IST ACM-ICPC Notebook 2016-17

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Common Stuff

1	Common Stun			
	1.1	Default code	1	
	1.2	Priority Queue	1	
2	Geometry			
	2.1	Convex hull	1	
	2.2	Miscellaneous geometry	2	
	2.3	Java geometry	3	
	2.4	3D geometry	4	
3	Numerical algorithms			
	3.1	Number theory (modular, Chinese remainder, linear Diophantine)	4	
	3.2	Fast Fourier transform	5	
	3.3	Fast Fourier transform (C++)	5	
	3.4	Simplex algorithm	6	
4	Gra	ph algorithms	7	
	4.1	Fast Dijkstra's algorithm - Stanford	7	
	4.2	Strongly connected components - Stanford	7	
	4.3	Eulerian path - Stanford	7	
	4.4	Bellman Ford (Shortest path with negative edges)	7	
	4.5	Floyd-Wrashall (All-pairs shortest path)	8	
	4.6	Prim (MST)	8	
	4.7	Kruskal - Stanford	8	
	4.8	Maximum Bipartite Matching	8	
	4.9	Ford-Fulkerson (Max Flow)	9	
	4.10	Edmonds-Karp (Max Flow)	9	
	4.11	Strongly Connected Components	9	
5	Stri	ngs	9	
	5.1	Suffix array - Stanford	9	
	5.2	Knuth-Morris-Prath (String matching)	10	
6	Data	a structures 1	0	
•	6.1		10	
	6.2		10	
	6.3	·	10	
	6.4		11	
	6.5	* *	12	
	6.6		12	
	0.0	Lowest common ancestor		

1 Common Stuff

1.1 Default code

```
#include <bits/stdc++.h>
#define _ ios_base::sync_with_stdio(0);cin.tie(0);
#define FOR(i,a,b) for (int i=(a);i<(b);i++)
#define SZ(x) ((int)(x).size())
using namespace std;</pre>
```

1.2 Priority Queue

2 Geometry

2.1 Convex hull

```
// Compute the 2D convex hull of a set of points using the monotone
         chain
                     Eliminate redundant points from the hull if
        REMOVE_REDUNDANT is
// #defined.
// Running time: O(n log n)
       INPUT: a vector of input points, unordered.

OUTPUT: a vector of points in the convex hull, counterclockwise,
        starting
with bottommost/leftmost point
#include <cstdio>
#include <cassert>
#include <vector>
#include <algorithm>
#include <cmath>
// BEGIN CUT
#include <map>
// END CUT
using namespace std;
#define REMOVE_REDUNDANT
typedef double T;
const T EPS = 1e-7;
struct PT {
  PT(T x, T y) : x(x), y(y) {}
bool operator<(const PT &rhs) const { return make_pair(y,x) <
    make_pair(rhs.y,rhs.x); }
bool operator=-(const PT &rhs) const { return make_pair(y,x) ==</pre>
           make_pair(rhs.y,rhs.x); }
};
T cross(PT p, PT q) { return p.x*q.y-p.y*q.x; }
T area2(PT a, PT b, PT c) { return cross(a,b) + cross(b,c) + cross(c,a)
#ifdef REMOVE_REDUNDANT
bool between(const PT &a, const PT &b, const PT &c) {
   return (fabs(area2(a,b,c)) < EPS && (a.x-b.x)*(c.x-b.x) <= 0 && (a.y-b.y)*(c.y-b.y) <= 0);</pre>
#endif
void ConvexHull(vector<PT> &pts) {
   sort(pts.begin(), pts.end());
pts.erase(unique(pts.begin(), pts.end()), pts.end());
    <= 0) dn.pop_back();
      up.push_back(pts[i]);
      dn.push_back(pts[i]);
   for (int i = (int) up.size() - 2; i >= 1; i--) pts.push_back(up[i]);
#ifdef REMOVE_REDUNDANT
   if (pts.size() <= 2) return;
dn.clear();
dn.push_back(pts[0]);</pre>
   dn.push_back(pts[1]);
dn.push_back(pts[1]);
for (int i = 2; i < pts.size(); i++) {
   if (between(dn[dn.size()-2], dn[dn.size()-1], pts[i])) dn.pop_back</pre>
      dn.push_back(pts[i]);
   if (dn.size() >= 3 && between(dn.back(), dn[0], dn[1])) {
    dn[0] = dn.back();
    dn.pop_back();
   pts = dn;
#endif
// The following code solves SPOJ problem #26: Build the Fence (BSHEEP)
int main() {
   int t;
scanf("%d", &t);
for (int caseno = 0; caseno < t; caseno++) {</pre>
      int n;
      scanf("%d", &n);
vector<PT> v(n);
for (int i = 0;
vector<PT> h(v);
                              i < n; i++) scanf("%lf%lf", &v[i].x, &v[i].y);
      map PT, int> index;
for (int i = n-1; i >= 0; i--) index[v[i]] = i+1;
ConvexHull(h);
      double len = 0:
      double len = 0;
for (int i = 0; i < h.size(); i++) {
  double dx = h[i].x - h[(i+1)%h.size()].x;
  double dy = h[i].y - h[(i+1)%h.size()].y;
  len += sqrt(dx*dx*dy*dy*dy);</pre>
      if (caseno > 0) printf("\n");
printf("%.2f\n", len);
for (int i = 0; i < h.size(); i++) {
   if (i > 0) printf(" ");
   printf("%d", index[h[i]]);
```

```
}
   printf("\n");
}
}
// END CUT
```

2.2 Miscellaneous geometry

```
// C++ routines for computational geometry.
 #include <iostream>
 #include <vector>
#include <cmath>
 #include <cassert>
 using namespace std;
 double INF = 1e100;
 struct PT {
       double x, y;
     double x, y;
PT() {}
PT() {}
PT(double x, double y) : x(x), y(y) {}
PT(const PT &p) : x(p.x), y(p.y) {}
PT operator + (const PT &p) const { return PT(x+p.x, y+p.y); }
PT operator - (const PT &p) const { return PT(x-p.x, y-p.y); }
PT operator * (double c) const { return PT(x*c, y*c); }
PT operator / (double c) const { return PT(x/c, y/c); }
// rotate a point CCW or CW around the origin
PT RotateCCW90(PT p) { return PT(-p.y,p.x); }
PT RotateCW90(PT p) { return PT(p.y,-p.x); }
 PT RotateCCW(PT p, double t) {
   return PT(p.x*cos(t)-p.y*sin(t), p.x*sin(t)+p.y*cos(t));
 // project point c onto line through a and b
 // assuming a != b
PT ProjectPointLine(PT a, PT b, PT c) {
       return a + (b-a) *dot(c-a, b-a) /dot(b-a, b-a);
// project point c onto line segment through a and b
PT ProjectPointSegment (PT a, PT b, PT c) {
    double r = dot(b-a,b-a);
    if (fabs(r) < EPS) return a;</pre>
       if (rabs(f) < bra) /r;
r = dot(c-a, b-a)/r;
if (r < 0) return a;
if (r > 1) return b;
return a + (b-a)*r;
   // compute distance from c to segment between a and b
 double DistancePointSegment(PT a, PT b, PT c) {
  return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
// compute distance between point (x,y,z) and plane ax+by+cz=d double DistancePointPlane(double x, double y, double z, double d), double d)
       return fabs(a*x+b*y+c*z-d)/sqrt(a*a+b*b+c*c);
// determine if lines from a to b and c to d are parallel or collinear
bool LinesParallel(PT a, PT b, PT c, PT d) {
   return fabs(cross(b-a, c-d)) < EPS;</pre>
bool LinesCollinear(PT a, PT b, PT c, PT d) {
  return LinesParallel(a, b, c, d)
  && fabs(cross(a-b, a-c)) < EPS</pre>
                    && fabs(cross(c-d, c-a)) < EPS;
   // determine if line segment from a to b intersects with
// determine if fine segment from a to a linear to be a linea
                    return false;
              return true:
       if (cross(d-a, b-a) * cross(c-a, b-a) > 0) return false;
if (cross(a-c, d-c) * cross(b-c, d-c) > 0) return false;
       return true;
 \begin{subarray}{lll} // & compute intersection of line passing through a and b \end{subarray}
 // with line passing through c and d, assuming that unique
 // intersection exists; for segment intersection, check if
// segments intersect first
 PT ComputeLineIntersection(PT a, PT b, PT c, PT d) {
       b=b-a; d=c-d; c=c-a;
```

```
assert(dot(b, b) > EPS && dot(d, d) > EPS);
     return a + b*cross(c, d)/cross(b, d);
  // compute center of circle given three points
 PT ComputeCircleCenter(PT a, PT b, PT c) {
     b= (a+b) /2;
c= (a+c) /2;
     return ComputeLineIntersection(b, b+RotateCW90(a-b), c, c+RotateCW90(
                   a-c));
// determine if point is in a possibly non-convex polygon (by William // Randolph Franklin); returns 1 for strictly interior points, 0 for // strictly exterior points, and 0 or 1 for the remaining points. // Note that it is possible to convert this into an *exact* test using // integer arithmetic by taking care of the division appropriately // (making sure to deal with signs properly) and then by writing exact // tests for checking point on polygon boundary bool PointInPolygon(const vector<PT> &p, PT q) {
     pol PointInPolygon(const vector<PT> &p, PT q) {
    bool c = 0;
    for (int i = 0; i < p.size(); i++) {
        int j = (i+1) &p.size();
        if ((p[i].y <= q.y && q.y < p[j].y ||
        p[j].y <= q.y && q.y < p[i].y) &&
        q.x < p[i].x + (p[j].x - p[i].x) * (q.y - p[i].y) / (p[j].y - p[i].y) / (p[j].y - p[i].y)</pre>
                             ].y))
               c = !c;
     return c:
// determine if point is on the boundary of a polygon
bool PointOnPolygon(const vectorPTP &p, PT q) {
   for (int i = 0; i < p.size(); i++)
   if (dist2(ProjectPointSegment(p[i], p[(i+1)*p.size()], q), q) < EPS</pre>
               return true;
          return false;
 // compute intersection of line through points a and b with // circle centered at c with radius r>0 vector<PT> CircleLineIntersection(PT a, PT b, PT c, double r) {
      vector<PT> ret;
     b = b-a:
      a = a-c;
     a = a-c;
double A = dot(b, b);
double B = dot(a, b);
double C = dot(a, a) - r*r;
double D = B*B - A*C;
if (D < -EPS) return ret;</pre>
     ret.push_back(c+a+b*(-B+sqrt(D+EPS))/A);
if (D > EPS)
           ret.push_back(c+a+b*(-B-sqrt(D))/A);
 // compute intersection of circle centered at a with radius r
// with circle centered at b with radius R
vector<PT> CircleCircleIntersection(PT a, PT b, double r, double R) {
     vector<PT> ret;
double d = sqrt(dist2(a, b));
     double d = sqrt(dist2(a, b));
if (d > rR || d+min(r, R) < max(r, R)) return ret;
double x = (d*d-R*R+r*r)/(2*d);
double y = sqrt(r*r-x*x);
PT v = (b-a)/d;
ret.push_back(a+v*x + RotateCCW90(v)*y);</pre>
     if (y > 0)
           ret.push_back(a+v*x - RotateCCW90(v)*y);
     return ret;
 // This code computes the area or centroid of a (possibly nonconvex)
// polygon, assuming that the coordinates are listed in a clockwise or
// counterclockwise fashion. Note that the centroid is often known as
// the "center of gravity" or "center of mass".
double ComputeSignedArea(const vector<PT> &p) {
     double area = 0;
for(int i = 0; i < p.size(); i++) {
   int j = (i+1) % p.size();
   area += p[i].x*p[j].y - p[j].x*p[i].y;</pre>
     return area / 2.0;
 double ComputeArea(const vector<PT> &p) {
     return fabs(ComputeSignedArea(p));
 PT ComputeCentroid(const vector<PT> &p) {
      PT c(0,0);
     fi c(,0);
double scale = 6.0 * ComputeSignedArea(p);
for (int i = 0; i < p.size(); i++) {
   int j = (i+1) % p.size();
   c = c + (p[i]+p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);</pre>
     return c / scale;
  // tests whether or not a given polygon (in CW or CCW order) is simple
// tests whether or not a given polygon (in CW or CC
bool IsSimple(const vector<PT> &p) {
    for (int i = 0; i < p.size(); i++) {
        for (int k = i+1; k < p.size(); k++) {
            int j = (i+1) % p.size();
            int l = (k+1) % p.size();
            if (i == l || j == k) continue;
            if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
            return false;</pre>
                    return false;
```

```
return true:
int main() {
   // expected: (-5,2)
cerr << RotateCCW90(PT(2,5)) << endl;</pre>
        expected: (5,-2)
   cerr << RotateCW90(PT(2.5)) << endl;</pre>
   // expected: (-5.2)
   cerr << RotateCCW(PT(2,5),M_PI/2) << endl;</pre>
    // expected: (5,2)
   cerr << ProjectPointLine(PT(-5,-2), PT(10,4), PT(3,7)) << endl;</pre>
    // expected: (5,2) (7.5,3) (2.5,1)
   << ProjectPointSegment(PT(-5,-2), PT(2.5,1), PT(3,7)) << endl;
   // expected: 6.78903
   cerr << DistancePointPlane(4,-4,3,2,-2,5,-8) << endl;
    // expected: 1 0 1
   // expected: 1 1 1 0
           << SegmentsIntersect(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) << " "
<< SegmentsIntersect(PT(0,0), PT(2,4), PT(4,3), PT(0,5)) << " "
<< SegmentsIntersect(PT(0,0), PT(2,4), PT(2,-1), PT(-2,1)) << " "</pre>
            << SegmentsIntersect(PT(0,0), PT(2,4), PT(5,5), PT(1,7)) << endl
    // expected: (1,2)
   cerr << ComputeLineIntersection(PT(0,0), PT(2,4), PT(3,1), PT(-1,3))
           << endl;
   cerr << ComputeCircleCenter(PT(-3,4), PT(6,1), PT(4,5)) << endl;</pre>
   v.push_back(PT(0,0));
v.push_back(PT(5,0));
   v.push back(PT(5,5));
   // expected: 1 1 1 0 0
cerr << PointInPolygon(v, PT(2,2)) << " "
           << PointInPolygon(v, PI(2,2)) << " "
<< PointInPolygon(v, PT(2,0)) << " "
<< PointInPolygon(v, PT(0,2)) << " "</pre>
           << PointInPolygon(v, PT(0,2)) << " "
<< PointInPolygon(v, PT(5,2)) << " "
<< PointInPolygon(v, PT(2,5)) << endl;</pre>
   << PointOnPolygon(v, PI(0,2)) << " "
<< PointOnPolygon(v, PI(5,2)) << " "
<< PointOnPolygon(v, PI(2,5)) << endl;</pre>
        expected: (1,6)
                         (5,4) (4,5)
blank line
                         (4,5) (5,4) blank line
                         (4,5) (5,4)
   (4,3) (3,4)
vector<PT> u = CircleLineIntersection(PT(0,6), PT(2,6), PT(1,1), 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
   ror (int i = 0; i < u.size(); i++) cerr << u[i] < " -; cerr << endi;
u = CircleLineIntersection(PT(0,9), PT(9,0), PT(1,1), 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endi;
u = CircleCircleIntersection(PT(1,1), PT(10,10), 5, 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endi;</pre>
   u = CircleCircleIntersection(PT(1,1), PT(8,8), 5, 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(4.5,4.5), 10, sqrt(2.0)/2.0)</pre>
   for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(4.5,4.5), 5, sqrt(2.0)/2.0);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
   // area should be 5.0
   // area should be 5.0
// centroid should be (1.1666666, 1.166666)
PT pa[] = { PT(0,0), PT(5,0), PT(1,1), PT(0,5) };
vector<PT> p(pa, pa+4);
PT c = ComputeCentroid(p);
cerr << "Area: " << ComputeArea(p) << endl;
cerr << "Centroid: " << c << endl;</pre>
```

2.3 Java geometry

```
// In this example, we read an input file containing three lines, each // containing an even number of doubles, separated by commas. The first two
```

```
// lines represent the coordinates of two polygons, given in
        counterclockwise
          clockwise) order, which we will call "A" and "B". The last line
// contains a list of points, p[1], p[2], ...
// Our goal is to determine:
      (1) whether B - A is a single closed shape (as opposed to multiple
shapes)
       (2) the area of B-A
(3) whether each p[i] is in the interior of B-A
// INPUT:
     0 0 10 0 0 10
0 0 10 10 10 0
// OUTPUT:
       The area is singular.
     The area is 25.0
Point belongs to the area.
      Point does not belong to the area.
import java.util.*:
import java.awt.geom.*;
import java.io.*;
public class JavaGeometry {
       // make an array of doubles from a string
     // make an array of doubles from a string
static double[] readPoints(String s) {
   String[] arr = s.trim().split("\\s+");
   double[] ret = new double[arr.length];
   for (int i = 0; i < arr.length; i++) ret[i] = Double.
        parseDouble(arr[i]);</pre>
            return ret;
      // make an Area object from the coordinates of a polygon
     // make an itea Object Item the Cooltainates of a polygon
static Area makeArea (double[] pts) {
   Path2D.Double p = new Path2D.Double();
   p.moveTo (pts[0], pts[1]);
   for (int i = 2; i < pts.length; i += 2) p.lineTo(pts[i], pts[i]);</pre>
                   +1]);
            p closePath();
            return new Area(p);
      // compute area of polygon
      static double computePolygonArea(ArrayList<Point2D.Double> points)
            Point2D.Double[] pts = points.toArray(new Point2D.Double[points
           size()];
double area = 0;
for (int i = 0; i < pts.length; i++){
   int j = (i+1) % pts.length;
   area += pts[i].x * pts[j].y - pts[j].x * pts[i].y;</pre>
            return Math.abs(area)/2;
      // compute the area of an Area object containing several disjoint
      static double computeArea(Area area) {
           double computerred (area area) (
double totArea = 0;
PathIterator iter = area.getPathIterator(null);
ArrayList<Point2D.Double> points = new ArrayList<Point2D.Double
                    >();
            while (!iter.isDone()) {
                  double[] buffer = new double[6];
switch (iter.currentSegment(buffer)) {
                  case PathIterator.SEG_MOVETO:
case PathIterator.SEG_LINETO:
                        points.add(new Point2D.Double(buffer[0], buffer[1]));
                  case PathIterator.SEG CLOSE:
                        totArea += computePolygonArea(points);
points.clear();
                        break:
                  iter.next();
           return totArea:
      // notice that the main() throws an Exception -- necessary to
     // avoid wrapping the Scanner object for file reading in a // try { ... } catch block.

public static void main(String args[]) throws Exception {
            Scanner scanner = new Scanner(new File("input.txt"));
           // also,
// Sca
                 Scanner scanner = new Scanner (System.in);
           double[] pointsA = readPoints(scanner.nextLine());
double[] pointsB = readPoints(scanner.nextLine());
Area areaA = makeArea(pointsA);
Area areaB = makeArea(pointsB);
            areaB.subtract(areaA);
// also,
                 areaB.exclusiveOr (areaA);
                  areaB.add (areaA);
areaB.intersect (areaA);
            // (1) determine whether B - A is a single closed shape (as
                      opposed to multiple shapes)
           boolean isSingle = areaB.isSingular();
            // also,
// areaB.isEmpty();
```

```
if (isSingle)
    System.out.println("The area is singular.");
else
     System.out.println("The area is not singular.");
// (2) compute the area of B - A
System.out.println("The area is " + computeArea(areaB) + ".");
   (3) determine whether each p[i] is in the interior of B - A
while (scanner.hasNextDouble()) {
   double x = scanner.nextDouble();
     assert (scanner.hasNextDouble()):
    double y = scanner.nextDouble();
    if (areaB.contains(x,y)) {
    System.out.println ("Point belongs to the area.");
    } else {
         System.out.println ("Point does not belong to the area.
}
// Finally, some useful things we didn't use in this example:
     Ellipse2D.Double ellipse = new Ellipse2D.Double (double x,
                                                             double w.
       double h):
       creates an ellipse inscribed in box with bottom-left
        and upper-right corner (x+y,w+h)
     Rectangle2D.Double rect = new Rectangle2D.Double (double x
```

creates a box with bottom-left corner (x,y) and upper-

// Each of these can be embedded in an Area object (e.g., new

double w

2.4 3D geometry

, double h):

corner (x+y, w+h)

```
public class Geom3D {
  // distance between parallel planes aX + bY + cZ + d1 = 0 and
  // aX + bY + cZ + d2 = 0
public static double planePlaneDist (double a, double b, double c,
     double d1, double d2) {
return Math.abs(d1 - d2) / Math.sqrt(a*a + b*b + c*c);
  // distance from point (px, py, pz) to line (x1, y1, z1)-(x2, y2, z2) // (or ray, or segment; in the case of the ray, the endpoint is the // first point)
  public static final int LINE = 0;
public static final int SEGMENT = 1;
  public static final int RAY = 2;
public static double ptLineDistSq(double x1, double y1, double z1,
       double x2, double y2, double z2, double px, double py, double pz,
     double pd2 = (x1-x2)*(x1-x2) + (y1-y2)*(y1-y2) + (z1-z2)*(z1-z2);
     double x, y, z;
if (pd2 == 0) {
  x = x1;
  y = y1;
  z = z1;
}
        double u = ((px-x1)*(x2-x1) + (py-y1)*(y2-y1) + (pz-z1)*(z2-z1))
       Gouple u = ((px-x1)*(x2-x1) - pd2;

x = x1 + u * (x2 - x1);

y = y1 + u * (y2 - y1);

z = z1 + u * (z2 - z1);

if (type != LINE && u < 0) {
          x = x1;
y = y1;
        if (type == SEGMENT && u > 1.0) {
  x = x2;
          y = y2;
z = z2;
       }
     return (x-px) * (x-px) + (y-py) * (y-py) + (z-pz) * (z-pz);
  public static double ptLineDist(double x1, double y1, double z1
       double x2, double y2, double z2, double px, double py, double pz, int type) \{
     return Math.sqrt(ptLineDistSq(x1, y1, z1, x2, y2, z2, px, py, pz,
            type));
```

3 Numerical algorithms

3.1 Number theory (modular, Chinese remainder, linear Diophantine)

```
// This is a collection of useful code for solving problems that
// involve modular linear equations. Note that all of the
// algorithms described here work on nonnegative integers.
#include <iostream>
#include <rostream>
#include <vector>
#include <algorithm>
using namespace std:
typedef vector<int> VI;
typedef pair<int, int> PII;
// return a % b (positive value)
int mod(int a, int b) {
    return ((a%b) + b) % b;
.
 // computes gcd(a,b)
int gcd(int a, int b) {
     while (b) { int t = a%b; a = b; b = t; }
              return a;
// computes lcm(a,b)
int lcm(int a, int b) {
   return a / gcd(a, b)*b;
 // (a^b) mod m via successive squaring
int powermod(int a, int b, int m)
              int ret = 1;
              while (b)
                           if (b & 1) ret = mod(ret*a, m);
a = mod(a*a, m);
                            b >>= 1:
              return ret;
// returns g = gcd(a, b); finds x, y such that d = ax + by int extended_euclid(int a, int b, int &x, int &y) {
              int xx = y = 0;
int yy = x = 1;
              while (b)
                             int q = a / b;
                            int t = b; b = a%b; a = t;
t = xx; xx = x - q*xx; x = t;
t = yy; yy = y - q*yy; y = t;
              return a;
// finds all solutions to ax = b (mod n)
VI modular_linear_equation_solver(int a, int b, int n) {
             ret.push_back(mod(x + i*(n / g), n));
              return ret;
// computes b such that ab = 1 (mod n), returns -1 on failure int mod_inverse(int a, int n) {
              int x, y;
int g = extended_euclid(a, n, x, y);
if (g > 1) return -1;
// Chinese remainder theorem (special case): find z such that
// z % m1 = r1, z % m2 = r2. Here, z is unique modulo M = lcm(m1, m2). // Return (z, M). On failure, M = -1.
// Return (z, M). On failure, M = -1.
PII chinese_remainder_theorem(int m1, int r1, int m2, int r2) {
    int s, t;
    int g = extended_euclid(m1, m2, s, t);
    if (r1%g != r2%g) return make_pair(0, -1);
    return make_pair(mod(s*r2*m1 + t*r1*m2, m1*m2) / g, m1*m2 / g);
// Chinese remainder theorem: find z such that // z \$ m[i] = r[i] for all i. Note that the solution is // unique modulo M = lcm_i (m[i]). Return (z, M). On // failure, M = -1. Note that we do not require the a[i]'s
// to be relatively prime.
PII chinese_remainder_theorem(const VI &m, const VI &r) {
              PII ret = make_pair(r[0], m[0]);
for (int i = 1; i < m.size(); i++) {
```

```
ret = chinese_remainder_theorem(ret.second, ret.first,
                       m[i], r[i]);
if (ret.second == -1) break;
            return ret;
}
// computes x and y such that ax + by = c
// returns whether the solution exists
bool linear_diophantine(int a, int b, int c, int &x, int &y) {
           if (!a && !b)
                       if (c) return false;
x = 0; y = 0;
return true;
           if (!a)
                       if (c % b) return false;
x = 0; y = c / b;
return true;
            if (!b)
                       if (c % a) return false;
x = c / a; y = 0;
                       return true;
           int g = gcd(a, b);
if (c % g) return false;
x = c / g * mod_inverse(a / g, b / g);
y = (c - a*x) / b;
            return true:
int main() {
            // expected: 2
           cout << gcd(14, 30) << endl;
           int x, y;
int g = extended_euclid(14, 30, x, y);
cout << g << " " << x << " " << y << endl;
           // expected: 95 451
VI sols = modular_linear_equation_solver(14, 30, 100);
for (int i = 0; i < sols.size(); i++) cout << sols[i] << " ";</pre>
           cout << endl;
            // expected: 8
            cout << mod_inverse(8, 9) << endl;</pre>
            // expected: 23 105
           PII ret = chinese_remainder_theorem(VI({ 3, 5, 7 }), VI({ 2, 3,
           2 }));
cout << ret.first << " " << ret.second << endl;
           ret = chinese_remainder_theorem(VI({ 4, 6 }), VI({ 3, 5 }));
cout << ret.first << " " << ret.second << endl;</pre>
            if (!linear_diophantine(7, 2, 5, x, y)) cout << "ERROR" << endl</pre>
           ; cout << x << " " << y << endl;
           return 0;
}
```

3.2 Fast Fourier transform

```
#include <cassert>
#include <cstdio>
#include <cmath>
struct cpx
  cpx(double aa):a(aa),b(0){}
   cpx (double aa, double bb) :a (aa), b (bb) {}
  double a;
  double modsq(void) const
    return a * a + b * b;
  cpx bar(void) const
    return cpx(a, -b);
cpx operator +(cpx a, cpx b)
  return cpx(a.a + b.a, a.b + b.b);
cpx operator *(cpx a, cpx b)
  return cpx(a.a * b.a - a.b * b.b, a.a * b.b + a.b * b.a);
cpx operator / (cpx a, cpx b)
  cpx r = a * b.bar();
  return cpx(r.a / b.modsq(), r.b / b.modsq());
cpx EXP (double theta)
```

```
return cpx(cos(theta),sin(theta));
const double two_pi = 4 * acos(0);
// in:
// out:
                       input array
output array
// out. Output alray
// step: (SET TO 1) (used internally)
// size: length of the input/output (MUST BE A POWER OF 2)
// dir: either plus or minus one (direction of the FFT)
// RESULT: out[k] = \sum_{[j=0]^{(size - 1)} in[j] * exp(dir * 2pi * i * j
void FFT(cpx *in, cpx *out, int step, int size, int dir)
    if(size < 1) return;
if(size == 1)</pre>
        out[0] = in[0];
        return;
    FFT(in, out, step * 2, size / 2, dir);
FFT(in + step, out + size / 2, step * 2, size / 2, dir);
for(int i = 0; i < size / 2; i++)</pre>
       }
// f[0...N-1] and g[0..N-1] are numbers
\label{eq:continuous_series} \begin{split} // &f[0\ldots N-1] \text{ and } g[0\ldots N-1] \text{ are numbers} \\ // &\text{Want to compute the convolution h, defined by} \\ // &h[n] = \text{sum of } f[k]g[n-k] \; (k=0,\ldots,N-1) \; . \\ // &\text{Here, the index is cyclic; } f[-1] = f[N-1], \; f[-2] = f[N-2], \; \text{etc.} \\ // &\text{Let } F[0\ldots N-1] \; \text{be } FFT(f), \; \text{and similarly, define } G \; \text{and } H. \\ // &\text{The convolution theorem says } H[n] = F[n]G[n] \; (\text{element-wise product}) \; . \\ // &\text{To compute } h[j \; \text{in } O(N \; \log N) \; \text{time, do the following:} \\ // &\text{1. Compute } F \; \text{and } G \; (\text{pass dir = 1 as the argument}) \; . \\ // &\text{2. Get } H \; \text{by element-wise multiplying } F \; \text{and } G \; . \\ // &\text{3. Get } h \; \text{by taking the inverse } FFT \; (\text{use dir = -1 as the argument}) \\ &\text{and } * \text{dividing by } N*. \; DO \; NOT \; FORGET \; THIS \; SCALING \; FACTOR.} \end{split}
    printf("If rows come in identical pairs, then everything works.\n");
    cpx A[8];
cpx B[8];
    FFT(a, A, 1, 8, 1);
FFT(b, B, 1, 8, 1);
    for(int i = 0; i < 8; i++)
        printf("%7.21f%7.21f", A[i].a, A[i].b);
    printf("\n");
for(int i = 0; i < 8; i++)</pre>
         for (int j = 0; j < 8; j++)
            Ai = Ai + a[j] * EXP(j * i * two_pi / 8);
        printf("%7.21f%7.21f", Ai.a, Ai.b);
    printf("\n");
   cpx AB[8];
for(int i = 0; i < 8; i++)
   AB[i] = A[i] * B[i];
cpx aconvb[8];
FFT(AB, aconvb, 1, 8, -1);
for(int i = 0; i < 8; i++)
   aconvb[i] = aconvb[i] / 8;
for(int i = 0; i < 8; i++)</pre>
        printf("%7.21f%7.21f", aconvb[i].a, aconvb[i].b);
    printf("\n");
for(int i = 0; i < 8; i++)</pre>
         cox aconvbi(0,0);
         for (int j = 0; j < 8; j++)
             aconvbi = aconvbi + a[j] * b[(8 + i - j) % 8];
        printf("%7.21f%7.21f", aconvbi.a, aconvbi.b);
    printf("\n");
    return 0;
```

3.3 Fast Fourier transform (C++)

```
// Convolution using the fast Fourier transform (FFT). // // INPUT: // a[1...n] // b[1...m]
```

```
//
// OUTPUT:
            c[1...n+m-1] such that c[k] = sum_{i=0}^{n} k a[i] b[k-i]
// Alternatively, you can use the DFT() routine directly, which will // zero-pad your input to the next largest power of 2 and compute the
#include <iostream>
#include <!ostream
#include <vector>
#include <complex>
using namespace std;
typedef long double DOUBLE;
typedef complex<DOUBLE> COMPLEX;
typedef vector<DOUBLE> VD;
typedef vector<COMPLEX> VC;
struct FFT {
     VC A;
   int n. L:
    int ReverseBits(int k) {
       int ret = 0;
for (int i = 0; i < L; i++)</pre>
          ret = (ret << 1) | (k & 1);
k >>= 1;
       return ret:
   void BitReverseCopy(VC a) {
   for (n = 1, L = 0; n < a.size(); n <<= 1, L++) ;
   A.resize(n);
   for (int k = 0; k < n; k++)
    A[ReverseBits(k)] = a[k];</pre>
   VC DFT(VC a, bool inverse) {
   BitReverseCopy(a);
   for (int s = 1; s <= L; s++) {
      int m = 1 << s;
      COMPLEX wm = exp(COMPLEX(0, 2.0 * M_PI / m));
      if (inverse) wm = COMPLEX(1, 0) / wm;
      for (int k = 0; k < n; k += m) {
         COMPLEX w = 1;
         for (int j = 0; j < m/2; j++) {
            COMPLEX t = w * A[k + j + m/2];
            COMPLEX t = a A[k + j];
            A[k + j] = u + t;
            A[k + j] = u - t;
            w = w * wm;
      }
}</pre>
             }
          }
       if (inverse) for (int i = 0; i < n; i++) A[i] /= n;</pre>
     // c[k] = sum_{\{i=0\}^k} a[i] b[k-i]
   VD Convolution(VD a, VD b) {
  int L = 1;
  while ((1 << L) < a.size()) L++;
  while ((1 << L) < b.size()) L++;</pre>
       int n = 1 << (L+1);
       VC aa, bb;
       VC AA = DFT(aa, false);
VC BB = DFT(bb, false);
       for (size_t i = 0; i < AA.size(); i++) CC.push_back(AA[i] * BB[i]);</pre>
       VC cc = DFT(CC, true);
       for (int i = 0; i < a.size() + b.size() - 1; i++) c.push_back(cc[i</pre>
                 ].real());
       return c;
}:
int main() {
  double a[] = {1, 3, 4, 5, 7};
  double b[] = {2, 4, 6};
   VD c = fft.Convolution(VD(a, a + 5), VD(b, b + 3));
    // expected output: 2 10 26 44 58 58 42 for (int i = 0; i < c.size(); i++) cerr << c[i] << " ";
   cerr << endl:
   return 0:
```

3.4 Simplex algorithm

```
// Two-phase simplex algorithm for solving linear programs of the form // maximize c^T x
```

```
subject\ to Ax <= b
// INPUT: A -- an m x n matrix
                b \ -- \ an \ m-dimensional \ vector
                c -- an n-dimensional vector
                x -- a vector where the optimal solution will be stored
// OUTPUT: value of the optimal solution (infinity if unbounded // above, nan if infeasible)
/// To use this code, create an LPSolver object with A, b, and c as // arguments. Then, call Solve(x).
#include <iostream>
#include <iomanip>
#include <vector>
#include <cmath>
#include <limits>
using namespace std;
typedef long double DOUBLE;
typedef vector<DOUBLE> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
const DOUBLE EPS = 1e-9;
struct LPSolver {
  int m, n;
VI B, N;
VVD D;
   LPSolver (const VVD &A, const VD &b, const VD &c) :
      m(b.size()), n(c.size()), N(n + 1), B(m), D(m + 2, VD(n + 2)) {

for (int i = 0; i < m; i++) for (int j = 0; j < n; j++) D[i][j] = A

[i][j];
     [1][j];
for (int i = 0; i < m; i++) { B[i] = n + i; D[i][n] = -1; D[i][n +
    1] = b[i]; }
for (int j = 0; j < n; j++) { N[j] = j; D[m][j] = -c[j]; }
N[n] = -1; D[m + 1][n] = 1;</pre>
  void Pivot(int r, int s) {
  double inv = 1.0 / D[r][s];
  for (int i = 0; i < m + 2; i++) if (i != r)
    for (int j = 0; j < n + 2; j++) if (j != s)
        D[i][j] -= D[r][j] * D[i][s] * inv;
  for (int j = 0; j < n + 2; j++) if (j != s) D[r][j] *= inv;
  for (int i = 0; i < m + 2; i++) if (i != r) D[i][s] *= -inv;
        D[r][s] = inv:</pre>
      swap(B[r], N[s]);
  bool Simplex(int phase) {
  int x = phase == 1 ? m + 1 : m;
      while (true) {
         }
if (D[x][s] > -EPS) return true;
int r = -1;
for (int i = 0; i < m; i++) {
    if (D[i][s] < EPS) continue;
    if (r = -1 || D[i][n + 1] / D[i][s] < D[r][n + 1] / D[r][s] ||
        (D[i][n + 1] / D[i][s]) == (D[r][n + 1] / D[r][s]) && B[i] <
        B[r]) r = i;
}</pre>
         if (r == -1) return false;
         Pivot(r, s);
   DOUBLE Solve(VD &x) {
      int r = 0;
      int r = 0;
for (int i = 1; i < m; i++) if (D[i][n + 1] < D[r][n + 1]) r = i;
if (D[r][n + 1] < -EPS) {
   Pivot(r, n);
   if (!Simplex(1) || D[m + 1][n + 1] < -EPS) return -numeric_limits</pre>
         if (!Simplex(2)) return numeric_limits<DOUBLE>::infinity();
     x = VD(n);
for (int i = 0; i < m; i++) if (B[i] < n) x[B[i]] = D[i][n + 1];
return D[m][n + 1];
int main() {
   const int m = 4;
   const int n = 3;
   { -1, -5, 0 },
{ 1, 5, 1 },
{ -1, -5, -1 }
   DOUBLE _{b[m]} = \{ 10, -4, 5, -5 \};
```

```
DOUBLE _c[n] = { 1, -1, 0 };

VVD A(m);

VD b(_b, _b + m);

VD c(_c, _c + n);

for (int i = 0; i < m; i++) A[i] = VD(_A[i], _A[i] + n);

LPSolver solver(A, b, c);

VD x;

DOUBLE value = solver.Solve(x);

cerr << "VALUE: " << value << endl; // VALUE: 1.29032
cerr << "SOLUTION:"; // SOLUTION: 1.74194 0.451613 1

for (size_t i = 0; i < x.size(); i++) cerr << " " << x[i];

return 0;
```

4 Graph algorithms

4.1 Fast Dijkstra's algorithm - Stanford

```
// Implementation of Dijkstra's algorithm using adjacency lists // and priority queue for efficiency.
// Running time: O(|E| log |V|)
#include <queue>
#include <cstdio>
using namespace std;
const int INF = 2000000000;
typedef pair<int, int> PII;
int main() {
            vector
t i = 0; i < n,
int M;
scanf("%d", &M);
for (int j = 0; j < M; j++) {
    int vertex, dist;
    scanf("%d%d", &vertex, &dist);
    edges[i].push_back(make_pair(dist, vertex)); //
    note order of arguments here</pre>
             // use priority queue in which top element has the "smallest" \ensuremath{\textit{priority}}
            priority
priority_queue<PII, vector<PII>, greater<PII> > Q;
vector<int> dist(N, INF), dad(N, -1);
Q.push(make_pair(0, s));
             dist[s] = 0;
            dist[s] = 0;
while (!Q.empty()) {
   PII p = Q.top();
   Q.pop();
   int here = p.second;
   if (here == t) break;
                         if (dist[here] != p.first) continue;
                         for (vector<PII>::iterator it = edges[here].begin(); it
                                     = edges[here].end(); it++) {
if (dist[here] + it->first < dist[it->second])
                                                  dist[it->second] = dist[here] + it->
                                                  first;
dad[it->second] = here;
Q.push(make_pair(dist[it->second], it->
                                                          second));
            return 0;
Sample input:
3 1 4 3 3 4 1
2 0 1 2 3
Expected:
4 2 3 0
```

4.2 Strongly connected components - Stanford

```
#include < memory.h >
struct edge{int e, nxt;};
int V, E;
edge e[MAXE], er[MAXE];
int sp[MAXV], spr[MAXV];
int group_cnt, group_num[MAXV];
bool v[MAXV];
int stk[MAXV];
void fill_forward(int x)
   int i:
   for(i=sp[x];i;i=e[i].nxt) if(!v[e[i].e]) fill_forward(e[i].e);
   stk[++stk[0]]=x;
void fill_backward(int x)
   v[x]=false;
  group_num[x]=group_cnt;
for(i=spr[x];i;i=er[i].nxt) if(v[er[i].e]) fill_backward(er[i].e);
void add_edge(int v1, int v2) //add edge v1->v2
  e [++E].e=v2; e [E].nxt=sp [v1]; sp [v1]=E;
er[ E].e=v1; er[E].nxt=spr[v2]; spr[v2]=E;
void SCC()
  met i,
stk[0]=0;
memset(v, false, sizeof(v));
for(i=1;i<=V;i++) if(!v[i]) fill_forward(i);</pre>
  for(i=:;ix-v;i+r) if(:v[:], ifit_forward(:),
group_cnt=0;
for(i=stk[0];i>=1;i--) if(v[stk[i]])(group_cnt++; fill_backward(stk[i]))
```

4.3 Eulerian path - Stanford

```
struct Edge;
typedef list<Edge>::iterator iter;
struct Edge
           int next_vertex;
iter reverse_edge;
           Edge(int next_vertex)
                        :next_vertex(next_vertex)
const int max vertices = ;
int num_vertices;
list<Edge> adj[max_vertices];
                                                          // adjacency list
vector<int> path;
void find_path(int v)
            while(adj[v].size() > 0)
                        int vn = adj[v].front().next_vertex;
                        adj[vn].erase(adj[v].front().reverse_edge);
adj[v].pop_front();
find_path(vn);
           path.push_back(v);
void add_edge(int a, int b)
            adi[a].push front(Edge(b));
           adj[a].pusn_front(toge(b));
iter ita = adj[a].begin();
adj[b].push_front(Edge(a));
iter itb = adj[b].begin();
ita->reverse_edge = itb;
itb->reverse_edge = ita;
```

4.4 Bellman Ford (Shortest path with negative edges)

4.5 Floyd-Wrashall (All-pairs shortest path)

4.6 Prim (MST)

```
//Complexidade: O(E log V)
//Dados iniciais: pair<distancia, vertice> na lista de adjacencia
//Dados finais:
            d[v] -> distancia da aresta que liga a MST ao vertice v
            parent[v] -> vertice a que esta ligado o vertice v totalweight -> peso total da arvore
#include <vector>, <set>
#define NVERTICES 10010
vector< pair<int,int> > adjlist[NVERTICES];
vector pair<int, int > heap;
int d[NVERTICES], parent[NVERTICES], totalweight;
void add(int cost, int v, int p) {
    if(cost(dy]) {
        parent[v]=p;
}
                         heap.erase(pair<int,int>(d[v], v));
                         d[v]=cost;
                         heap.insert(pair<int,int>(d[v], v));
void prim(int root) {
            memset(d, 0x3f, sizeof(d)); // 0x3f3f3f3f > 1.000.000.000
            memset(parent, -1, sizeof(parent));
             totalweight=0;
            totalweight=0;
add(0, root, -1);
while(!heap.empty()) {
    pair<int, int> cur = *heap.begin();
    totalweight+=d[cur.second];
    d[cur.second]=0; //vertex in MST
                         heap.erase(heap.begin()); //pop closest vertex
for(unsigned int i=0; i<adjlist[cur.second].size(); i</pre>
                                     -) //for each neighbour add(adjlist[cur.second][i].first, adjlist[cur.
                                             second][i].second, cur.second); //add/
}
```

4.7 Kruskal - Stanford

```
.
Uses Kruskal's Algorithm to calculate the weight of the minimum
       spanning
forest (union of minimum spanning trees of each connected component) of a possibly disjoint graph, given in the form of a matrix of edge
       weights
(-1 if no edge exists). Returns the weight of the minimum spanning
forest (also calculates the actual edges - stored in T). Note: uses a disjoint-set data structure with amortized (effectively) constant time
union/find. Runs in O(E*log(E)) time.
#include <iostream>
#include <vector>
#include <algorithm>
#include <queue>
using namespace std;
typedef int T:
struct edge
  int u, v;
  T d;
};
struct edgeCmp
  int operator()(const edge& a, const edge& b) { return a.d > b.d; }
```

```
int find(vector \langle int \rangle \& C, int x) { return (C[x] == x) ? x : C[x] = find
        (C, C[x]); }
T Kruskal (vector <vector <T> >& w)
  int n = w.size();
  T weight = 0;
  vector <int> C(n), R(n);
for(int i=0; i<n; i++) { C[i] = i; R[i] = 0; }</pre>
  priority queue <edge, vector <edge>, edgeCmp> E;
  for(int i=0; i<n; i++)
  for(int j=i+1; j<n; j++)
   if(w[i][j] >= 0)
          e.u = i; e.v = j; e.d = w[i][j];
          E.push(e);
  while (T.size() < n-1 && !E.empty())</pre>
     edge cur = E.top(); E.pop();
     int uc = find(C, cur.u), vc = find(C, cur.v);
if(uc != vc)
       T.push_back(cur); weight += cur.d;
        if(R[uc] > R[vc]) C[vc] = uc;
        else if(R[vc] > R[uc]) C[uc] =
else { C[vc] = uc; R[uc]++; }
  return weight;
int main()
  int wa[6][6] = {
     { 0, -1, 2, -1, 7, -1 },
 { -1, 0, -1, 2, -1, -1 },
 { 2, -1, 0, -1, 8, 6 },
 { -1, 2, -1, 0, -1, -1 },
     { 7, -1, 8, -1, 0, 4 },
{ -1, -1, 6, -1, 4, 0 } };
  vector <vector <int> > w(6, vector <int>(6));
  for(int i=0; i<6; i++)
for(int j=0; j<6; j++)</pre>
        w[i][j] = wa[i][j];
  cout << Kruskal(w) << endl;
  cin >> wa[0][0];
```

4.8 Maximum Bipartite Matching

```
// Time Complexity: O( V * E ) which at most is O(V^3) // Input: adjency list graph graph[i] has all the nodes j to which node
i can be connected
//Output:
             - matchL[m] (right vertex to which left vertex m is matched, -1
         - \mathsf{matchR}[n] (left vertex to which right vertex n is matched, -1 if not matched)
            - nmatches (number of matches)
#include <cstring>
#include <vector>
#define MAX 410
vector<int> graph[MAX];
bool seen[MAX];
int matchL[MAX], matchR[MAX], nmatches;
int nLeft, nRight;
bool findmatch(int leftv) {
    for(int i=0; i<(int)graph[leftv].size(); i++) {
        int rightv = graph[leftv][i];
        if (seen[rightv]) continue;
}</pre>
                        matchR[rightv]=leftv;
matchL[leftv]=rightv;
                                   return true;
            return false;
void bpm() {
           memset (matchL, -1, sizeof(matchL));
memset (matchR, -1, sizeof(matchR));
memset (seen, 0, sizeof(seen));
            nmatches=0:
            for(int i=0; i<nLeft; i++) {</pre>
                       findmatch(i);
memset(seen, 0, sizeof(seen));
```

4.9 Ford-Fulkerson (Max Flow)

4.10 Edmonds-Karp (Max Flow)

4.11 Strongly Connected Components

```
// Time Complexity: O(V + E)
// Input: adjlist
// Output: set of SCC
#include <vector>, <stack>
#define N 100
struct NODE {
        int index, lowlink;
};
int n, ind;
```

```
NODE nodes[N];
stack<int> st:
bool instack[N];
vector<vector<int> > adjlist, SCC;
void connect(int v) {
           int w:
           int w;
nodes[v].index = nodes[v].lowlink = ind++;
st.push(v);
instack[v] = true;
for (int i=0; i<SZ(adjlist[v]); i++) {
    w = adjlist[v][i];
    if (!nodes[w].index) {
        connect(w);
}</pre>
                                    connect(w);
nodes[v].lowlink = min(nodes[v].lowlink, nodes[
                                            w].lowlink);
                        else if (instack[w])
                                   nodes[v].lowlink = min(nodes[v].lowlink, nodes[
    w].index);
            if (nodes[v].lowlink == nodes[v].index) {
                        for(w = -1; w != v; ) {
    w = st.top(); st.pop();
    instack[w] = false;
                                    tmp.push back(w);
                        SCC.push_back(tmp);
           }
void tarjan() {
           for (int i=0; i<n; i++) if (!nodes[i].index) connect(i);</pre>
```

5 Strings

5.1 Suffix array - Stanford

```
// Suffix array construction in O(L \log^2 L) time. Routine for // computing the length of the longest common prefix of any two // suffixes in O(\log L) time.
// OUTPUT: array suffix[] such that suffix[i] = index (from 0 to L-1) // of substring s[i...L-1] in the list of sorted suffixes.
                That is, if we take the inverse of the permutation suffix
                we get the actual suffix array.
#include <vector>
#include <string>
using namespace std;
struct SuffixArray {
  const int L:
  string s;
vector<vector<int> > P;
   vector<pair<int,int>,int> > M;
  SuffixArray(const string &s) : L(s.length()), s(s), P(1, vector<int>(
     L, 0)), M(L) {

for (int i = 0; i < L; i++) P[0][i] = int(s[i]);

for (int skip = 1, level = 1; skip < L; skip *= 2, level++) {
        P.push_back(vector<int>(L, 0));
for (int i = 0; i < L; i++)</pre>
        vector<int> GetSuffixArray() { return P.back(); }
  // returns the length of the longest common prefix of s[i...L-1] and
  int LongestCommonPrefix(int i, int j) {
     int longestcommonFefix(int 1, int j) {
int len = 0;
if (i == j) return L - i;
for (int k = P.size() - 1; k >= 0 && i < L && j < L; k--) {
   if (P[k][i] == P[k][j]) {</pre>
          i += 1 << k;
j += 1 << k;
len += 1 << k;
     return len;
// BEGIN CUT // The following code solves UVA problem 11512: GATTACA.
#define TESTING
#ifdef TESTING
int main() {
  int T;
cin >> T;
   for (int caseno = 0; caseno < T; caseno++) {</pre>
```

```
if (1 > len) count = 2; else count++;
        if (len > bestlen || len == bestlen && s.substr(bestpos, bestlen)
          > s.substr(i, len)) {
bestlen = len;
          bestcount = count;
bestpos = i;
     if (bestlen == 0) {
           ut << "No repetitions found!" << endl;
     } else {
              << s.substr(bestpos, bestlen) << " " << bestcount << endl;
#else
  END CUT
int main() {
   // bobocel is the 0'th suffix
// obocel is the 5'th suffix
        bocel is the 1'st suffix ocel is the 6'th suffix
  // ocel is the o'th suffix
// cel is the 2'nd suffix
// el is the 3'rd suffix
// l is the 4'th suffix
SuffixArray suffix("bobocel");
vector<int> v = suffix.GetSuffixArray();
   // Expected output: 0 5 1 6 2 3 4
  for (int i = 0; i < v.size(); i++) cout << v[i] << " ";</pre>
  cout << endl;
cout << suffix.LongestCommonPrefix(0, 2) << endl;</pre>
 / BEGIN CUT
#endif
// END CUT
```

5.2 Knuth-Morris-Prath (String matching)

```
// Time Complexity: O(len(W) + len(S))
// Input: S and W (W is the substring to search in S)
// Output: Position of the first match of W in S

#include <cstdlib>, <string>
int* compute_prefix(string w) {
    int m = w.length(), k = 0;
    int *pi = (int*)malloc(sizeof(int)*m);
    pi[0] = 0;
    for (int q=1; q<m; q++) {
        while (k > 0 && w[k] != w[q]) k = pi[k-1];
        if (w[k] == w[q]) k++;
        pi[q] = k;
    }
    return pi;
}
int kmp_match(string s, string w) {
    int *pi=compute_prefix(w);
    int q = 0, n = s.length(), m = w.length();
    for (int i=0; i<n; i++) {
        while (q > 0 && w[q] != s[i]) q = pi[q-1];
        if (w[q] == s[i]) q++;
        if (q == m) return i-m+1; // Match at pos i-m+1
    }
    return -1; // No Match
```

6 Data structures

6.1 Range Minimum Query

```
// Time Complexity: Query O(log N)
// Input:
    N -> number of values in A
// A[i] -> i-th value
// M[i] -> minimum value position for
    the interval assigned to the i-th node
//Output: Minimum value in interval [i, j]
#define MAXN 1000
#include <cstdio>
int A[MAXN], M[MAXN], N;
void init(int node, int b, int e) {
```

6.2 Binary Indexed Tree - Stanford

```
#include <iostream>
using namespace std;

#define LOGSZ 17

int tree[(1<<LOGSZ)+1];
int N = (1<<LOGSZ);

// add v to value at x
void set(int x, int v) {
    while (x < N) {
        tree[x] += v;
        x += (x & -x);
    }
}

// get cumulative sum up to and including x
int get(int x) {
    int res = 0;
    while (x) {
        res += tree[x];
        x -= (x & -x);
    }
    return res;
}

// get largest value with cumulative sum less than or equal to x;
// for smallest, pass x-1 and add 1 to result
int getind(int x) {
    int idx = 0, mask = N;
    while (mask && idx < N) {
        int t = idx + mask;
        if (x >= tree[t]) {
            idx = t;
            x -= tree[t];
        }
        mask >>= 1;
    }
    return idx;
}
```

6.3 KD-tree

```
// point structure for 2D-tree, can be extended to 3D
struct point {
      ntype x, v;
      point (ntype xx = 0, ntype yy = 0) : x(xx), y(yy) {}
};
bool operator==(const point &a, const point &b)
      return a.x == b.x && a.y == b.y;
 // sorts points on x-coordinate
bool on_x(const point &a, const point &b)
      return a.x < b.x;
// sorts points on y-coordinate
bool on_y(const point &a, const point &b)
      return a.y < b.y;</pre>
 // squared distance between points
ntype pdist2(const point &a, const point &b)
      ntvpe dx = a.x-b.x, dv = a.v-b.v;
      return dx*dx + dy*dy;
 // bounding box for a set of points
struct bbox
      ntvpe x0, x1, v0, v1;
      bbox(): x0(sentry), x1(-sentry), y0(sentry), y1(-sentry) {}
      // computes bounding box from a bunch of points
     void compute(const vector<point> &v) {
    for (int i = 0; i < v.size(); ++i) {
        x0 = min(x0, v[i].x); x1 = max(x1, v[i].x);
        y0 = min(y0, v[i].y); y1 = max(y1, v[i].y);
    }
}</pre>
      \ensuremath{//} squared distance between a point and this bbox, 0 if inside
      ntype distance (const point &p) {
           if (p.x < x0) {
    if (p.y < y0)
    else if (p.y > y1)
    else
                                              return pdist2(point(x0, y0), p);
                                              return pdist2(point(x0, y1), p);
return pdist2(point(x0, p.y), p);
            else if (p.x > x1) {
                                              return pdist2(point(x1, y0), p);
return pdist2(point(x1, y1), p);
return pdist2(point(x1, p.y), p);
                 if (p.y < y0)
else if (p.y > y1)
                 else
            else {
                 if (p.y < y0)
else if (p.y > y1)
                                              return pdist2(point(p.x, y0), p);
return pdist2(point(p.x, y1), p);
                                               return 0;
                 else
 // stores a single node of the kd-tree, either internal or leaf
struct kdnode
                            // true if this is a leaf node (has one point)
// the single point of this is a leaf
// bounding box for set of points in children
      bool leaf:
      point pt;
bbox bound;
      kdnode *first, *second; // two children of this kd-node
      kdnode() : leaf(false), first(0), second(0) {}
~kdnode() { if (first) delete first; if (second) delete second; }
      // intersect a point with this node (returns squared distance)
      ntype intersect(const point &p) {
           return bound.distance(p);
      // recursively builds a kd-tree from a given cloud of points
void construct(vector<point> &vp)
            // compute bounding box for points at this node
           bound.compute(vp);
                if we're down to one point, then we're a leaf node
           if (vp.size() == 1) {
    leaf = true;
                 pt = vp[0];
           else {
    // split on x if the bbox is wider than high (not best
                 heuristic...)
if (bound.x1-bound.x0 >= bound.y1-bound.y0)
                  sort(vp.begin(), vp.end(), on_x);
// otherwise split on y-coordinate
                 else
                       sort(vp.begin(), vp.end(), on_y);
                 // divide by taking half the array for each child
// (not best performance if many duplicates in the middle)
                 int half = vp.size()/2;
vector<point> vl(vp.begin(), vp.begin()+half);
vector<point> vr(vp.begin()+half, vp.end());
first = new kdnode(); first->construct(vl);
second = new kdnode(); second->construct(vr);
```

```
// simple kd-tree class to hold the tree and handle queries
struct kdtree
     // constructs a kd-tree from a points (copied here, as it sorts
     kdtree(const vector<point> &vp) {
          vector<point> v(vp.begin(), vp.end());
root = new kdnode();
          root->construct(v);
      kdtree() { delete root; }
     // recursive search method returns squared distance to nearest
     ntype search(kdnode *node, const point &p)
          if (node->leaf) {
               // commented special case tells a point not to find itself
if (p == node->pt) return sentry;
                    return pdist2(p, node->pt);
          ntype bfirst = node->first->intersect(p);
ntype bsecond = node->second->intersect(p);
          // choose the side with the closest bounding box to search
            // (note that the other side is also searched if needed)
          // (note that the other side is also searched if me
if (bfirst < bsecond) {
   ntype best = search(node->first, p);
   if (bsecond < best)
      best = min(best, search(node->second, p));
               return best;
          else {
               itype best = search(node->second, p);
if (bfirst < best)
    best = min(best, search(node->first, p));
               return best:
     // squared distance to the nearest
     ntype nearest(const point &p) {
   return search(root, p);
};
// some basic test code here
int main()
      // generate some random points for a kd-tree
     vector<point> vp;
for (int i = 0; i < 100000; ++i) +</pre>
          vp.push_back(point(rand()%100000, rand()%100000));
     kdtree tree(vp):
     << "Closest squared distance to ; ...
<< ")"
<< " is " << tree.nearest(q) << endl;</pre>
```

6.4 Splay tree

```
#include <cstdio>
#include <algorithm>
using namespace std;

const int N_MAX = 130010;
const int oo = 0x3f3f3f3f;
struct Node
{
   Node *ch[2], *pre;
   int val, size;
   bool isTurned;
} nodePool[N_MAX], *null, *root;

Node *allocNode(int val)
{
   static int freePos = 0;
   Node *x = &nodePool[freePos ++];
   x->val = val, x->isTurned = false;
   x->ch[0] = x->ch[1] = x->pre = null;
   x->size = 1;
```

```
inline void update (Node *x)
  x->size = x->ch[0]->size + x->ch[1]->size + 1;
inline void makeTurned(Node *x)
  if(x == null)
   inline void pushDown (Node *x)
   if(x->isTurned)
     makeTurned(x->ch[0]);
     makeTurned(x->ch[1]);
x->isTurned ^= 1;
inline void rotate(Node *x, int c)
  Node *y = x->pre;

x->pre = y->pre;

if(y->pre!= null)

y->pre->ch[y == y->pre->ch[1]] = x;

y->ch[!c] = x->ch[c];

if(x->ch[c]!= null)

x->ch[c]->pre = y;

x->ch[c] = y, y->pre = x;

update(y);

if(y == root)
  if(y == root
root = x;
             root)
void splay(Node *x, Node *p)
   while (x->pre != p)
     if(x->pre->pre == p)
  rotate(x, x == x->pre->ch[0]);
      else
        Node *y = x->pre, *z = y->pre;
if(y == z->ch[0])
           if(x == y->ch[0])
               rotate(y, 1), rotate(x, 1);
           else
             rotate(x, 0), rotate(x, 1);
         else
           if(x == y->ch[1])
  rotate(y, 0), rotate(x, 0);
           else
             rotate(x, 1), rotate(x, 0);
  update(x);
void select(int k, Node *fa)
  Node *now = root;
   while(1)
      pushDown (now);
     int tmp = now->ch[0]->size + 1;
if(tmp == k)
     else if(tmp < k)</pre>
        now = now->ch[1], k -= tmp;
     else

now = now->ch[0];
   splay(now, fa);
Node *makeTree(Node *p, int 1, int r)
     return null;
  int mid = (1 + r) / 2;
Node *x = allocNode(mid);
  x->pre = p;
x->ch[0] = makeTree(x, 1, mid - 1);
x->ch[1] = makeTree(x, mid + 1, r);
update(x);
  return x;
int main()
  int n, m;
null = allocNode(0);
null->size = 0;
root = allocNode(0);
   root->ch[1] = allocNode(oo);
root->ch[1]->pre = root;
   update (root):
   scanf("%d%d", &n, &m);
```

```
root->ch[1]->ch[0] = makeTree(root->ch[1], 1, n);
splay(root->ch[1]->ch[0], null);

while(m --)
{
   int a, b;
   scanf("%d%d", &a, &b);
   a ++, b ++;
   select(a - 1, null);
   select(b + 1, root);
   makeTurned(root->ch[1]->ch[0]);
}

for(int i = 1; i <= n; i ++)
{
   select(i + 1, null);
   printf("%d ", root->val);
}
```

6.5 Lazy segment tree

```
public class SegmentTreeRangeUpdate {
    public long[] leaf;
           public long[] update;
public int origSize;
public SegmentTreeRangeUpdate(int[] list)
                     regmentifeexamgeopdate(int[] list)
origSize = list.length;
leaf = new long[4*list.length];
update = new long[4*list.length];
build(1,0,list.length-1,list);
           public void build(int curr, int begin, int end, int[] list)
                      if(begin == end)
                                 leaf[curr] = list[begin];
                                 int mid = (begin+end)/2;
                                 build(2 * curr, begin, mid, list);
build(2 * curr + 1, mid+1, end, list);
leaf[curr] = leaf[2*curr] + leaf[2*curr+1];
           public void update(int begin, int end, int val) {
         update(1,0,origSize-1,begin,end,val);
           public void update(int curr, int tBegin, int tEnd, int begin,
                   int end, int val) {
  if(tBegin >= begin && tEnd <= end)</pre>
                                 update[curr] += val;
                      else
                                 val);

if(tEnd >= begin && mid+1 <= end)
                                           update(2*curr+1, mid+1, tEnd, begin, end, val);
                      }
           public long query(int begin, int end) {
   return query(1,0,origSize-1,begin,end);
           public long query(int curr, int tBegin, int tEnd, int begin,
                  if(2*curr < update.length){</pre>
                                                      update[2*curr] += update[curr];
update[2*curr+1] += update[curr
                                            update[curr] = 0;
                                 return leaf[curr];
                                  leaf[curr] += (tEnd-tBegin+1) * update[curr];
                                 if(2*curr < update.length) {
    update[2*curr] += update[curr];
    update[2*curr+1] += update[curr];</pre>
                                 update[curr] = 0:
                                 int mid = (tBegin+tEnd)/2;
long ret = 0;
if(mid >= begin && tBegin <= end)</pre>
                                           ret += query(2*curr, tBegin, mid, begin
                                 return ret;
        }
}
```

6.6 Lowest common ancestor

const int max_nodes, log_max_nodes;

```
int num_nodes, log_num_nodes, root;
vector<int> children[max_nodes];
                                                            // children[i] contains the
children of node i
int A[max_nodes][log_max_nodes+1];
        int L[max_nodes];
    node i and the root
// floor of the binary logarithm of n int lb(unsigned int n) \,
      if(n==0)
     if (n==0)
  return -1;
int p = 0;
if (n >= 1<<16) { n >>= 16; p += 16; }
if (n >= 1<< 8) { n >>= 8; p += 8; }
if (n >= 1<< 4) { n >>= 4; p += 4; }
if (n >= 1<< 2) { n >>= 2; p += 2; }
if (n >= 1<< 1) {
  p += 1; }</pre>
      return p;
void DFS(int i, int 1)
      L[i] = 1;
for(int j = 0; j < children[i].size(); j++)
    DFS(children[i][j], 1+1);</pre>
}
int LCA(int p, int q)
      // ensure node p is at least as deep as node q if (L[p] < L[q])
            swap(p, q);
      // "binary search" for the ancestor of node p situated on the same
level as q
for(int i = log_num_nodes; i >= 0; i--)
if(L[p] - (1<<i) >= L[q])
p = A[p][i];
      if(p == q)
            return p;
```

```
// "binary search" for the LCA
    for (int i = log_num_nodes; i >= 0; i--)
    if(A[p][i] != -1 && A[p][i] != A[q][i])
            p = A[p][i];
            q = A[q][i];
   return A[p][0];
int main(int argc,char* argv[])
   // read num_nodes, the total number of nodes
log_num_nodes=lb(num_nodes);
   for(int i = 0; i < num_nodes; i++)</pre>
       int p;
        // read p, the parent of node i or -1 if node i is the root
       root = i;
   else
A[i][j] = -1;
   // precompute L
DFS(root, 0);
   return 0;
```