

# SMALL CELL NETWORKS: SPEED BASED POWER ALLOCATION

by

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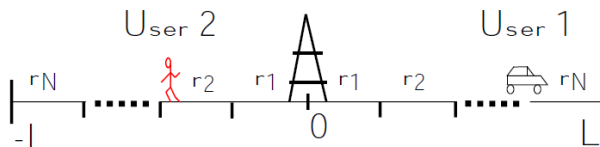
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# Outline

- Problem description
- Speed dependent performance measure
- Maximum velocity supported by system
- Optimal power: finite number of classes
- Continuous optimal power law
- Numerical results
- Conclusions and future directions

# Problem description

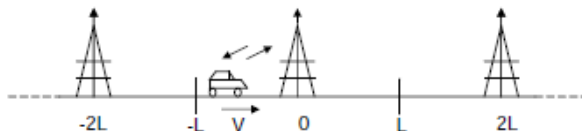


User 1: Receives rate  $r_N$   
 User 2: Receives rate  $r_2$

- Short radius cell network.
- Good service to cell edge users.

## Problem description contd..

- Mobility management.
- Increase in handover rate.
- Unacceptable rate of call drop.
- Optimal cell size increases with velocity.
- Increase power.



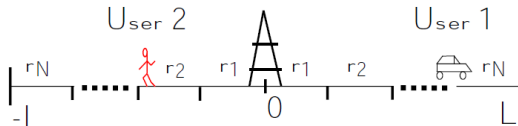
# Power allocation

- Allocate power based on speed.
  - Finite number of velocity classes.
    - Allocate equal power to each class.
  - Continuous power allocation.
    - Allocate power based on exact speed.
- Discrete law converges to continuous one.

## Assumptions

- No interference.
- Symmetry in both directions.
- User speed does not change during call.

# Notations and Terminology



- $2N$  disjoint segments  $\{A_n\}_{n \in \mathbb{N}}$ .

$$A_n := \left[ \frac{(n-1)L}{N}, \frac{nL}{N} \right] \mathbf{1}_{\{n>0\}} + \left[ \frac{nL}{N}, \frac{(n+1)L}{N} \right] \mathbf{1}_{\{n<0\}}$$

$$\mathbb{N} := \{-N, \dots, -1, 1, \dots, N\}$$

- Rate regions  $\mathbb{R} := \{r_1, \dots, r_N\}$ 
  - Decreasing set
- Path loss factor  $\beta$

# Notations and Terminology

- Poisson Arrivals
  - External arrivals
    - Arrival from external world ( $\lambda_e$ ).
  - Handover arrivals
    - sub-stream of external arrivals whose service is not completed in the previous cell ( $\lambda_h$ ).
- Velocity of user ( $V$ )
- Number of bytes to be transmitted  $S \sim \text{expo}(\mu)$
- Resources
  - $K$  number of servers.
- Probabilistic arrival in each segment
  - Position of arrival with distribution  $\Pi := \{\pi_n\}_n$
- Information to initiate the HO
  - extra bytes to be exchanged:  $s_h \ll S$

## Speed dependent performance measure

- Hand over probability
  - Probability of External call handing over ( $P_{e,ho}$ )
  - Probability of HO call again handing over ( $P_{h,ho}$ )
- Expected service time
- HO arrival rate ( $\lambda_{h,L}$ )
- Overall expected service time

$$\bar{b} = \left( \frac{\lambda_L}{\lambda_L + \lambda_{h,L}} b_e + \frac{\lambda_{h,L}}{\lambda_L + \lambda_{h,L}} b_h \right).$$



## Speed dependent performance measure

- Load factor ( $\rho$ )

$$\rho = \frac{1}{K}(\lambda_L + \lambda_{h,L})\bar{b}.$$

- Busy probability (M/G/K/K queue)

$$P_{Busy} = \frac{\rho^K / K!}{\sum_{k=0}^K \rho^k / k!} \quad (\text{Erlang loss formulae})$$

### Claim

*Optimizers of  $\rho$  and  $P_{busy}$  are same.*

# Maximum velocity supported by system

Useful communication is possible only if

$$g^N(L) > s_h \quad a.s.$$

## Theorem

*When  $\beta > 1$ , there exists a limit on the maximum velocity that can be supported by the system for a given power  $P$*

$$V_{lim}(P) := \frac{1}{s_h} r_0 \sum_{n=-N}^N |n|^{-\beta} P d_0^{1-\beta}. \quad \square$$

## Optimal power: Finite number of classes

- Divide users in  $I$  disjoint intervals based on speed

### Theorem

Assume  $C_{h,ho} - \mu s_h C_{e,ho} > 0$  and assume that the following matrix is positive definite,

$$\mathcal{P}_V := \begin{bmatrix} p_1 + \frac{p_1^2}{p_I} & \frac{p_1 p_2}{p_I} & \dots & \frac{p_1 p_{I-1}}{p_I} \\ \frac{p_1 p_2}{p_I} & p_2 + \frac{p_2^2}{p_I} & \dots & \frac{p_2 p_{I-1}}{p_I} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{p_1 p_{I-1}}{p_I} & \frac{p_{I-1} p_2}{p_I} & \dots & p_{I-1} + \frac{p_{I-1}^2}{p_I} \end{bmatrix} > 0.$$

Then the power allocation that minimizes  $\rho$  while satisfying the average power constraint equals:

$$P_i^*(L; \bar{P}) = \bar{P} + \frac{\mu s_h L^{\beta-1}}{C_{h,ho}} \left( \frac{1}{\Upsilon_i} - \sum_j p_j \frac{1}{\Upsilon_j} \right). \quad (1)$$

# Continuous optimal power law

- Accurate estimate of velocity.

Optimal power law that optimizes load factor  $\rho$ , and satisfies

$$\int_{V_{min}}^{V_{max}} P(v) p_V(v) d(v) \leq \bar{P}.$$

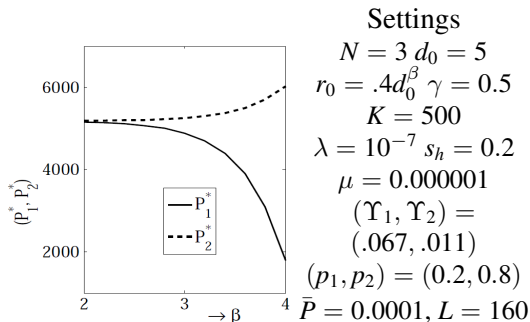
## Theorem

*The power function  $P^*(.)$  that optimizes  $\rho$ , while satisfying the average power constraint equals:*

$$P^*(v) = \bar{P} + \frac{1}{C_{h,ho}} \mu s_h L^{\beta-1} (v - E[V]). \quad \square \quad (2)$$

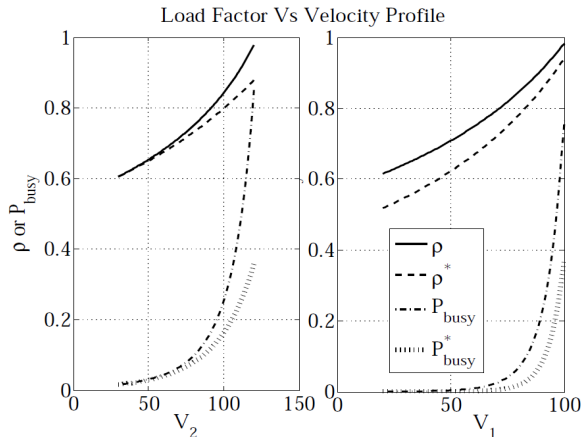
# Numerical results

- More the losses (path-loss factor) are, more diverse the two allocated powers are.



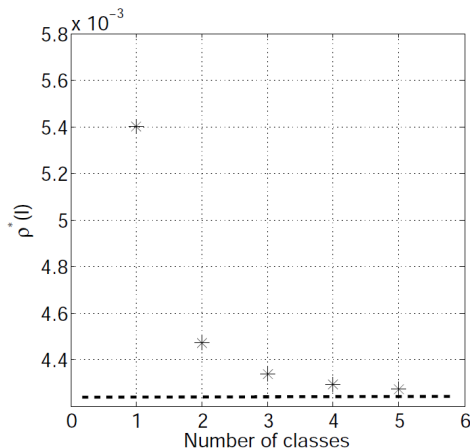
Power allocated optimally to two user classes

# Numerical results contd...



Comparison of performance with and without optimal  
power allocation

# Numerical results contd...



$\rho^*$  decreases with number of classes and approaches to continuous law

# Conclusions

- Model to incorporate speed based design variation in allocated power.
- Closed form expression for optimal power allocation.
  - optimal for busy/drop probability
  - Discrete power law
  - continuous power law (fine optimal power control)
- Linear variation in optimal power with user speed
- Large improvement in busy probability with optimal power law
- Best improvement with continuous power law.



# Thank you!!!