

Questão 2 - capítulo 4

EMANUELE GUSE

a) Binário: $[0, 1048575]$

- | | | |
|-------------------|---|--------------------|
| A) $[0, 1062346]$ | ✓ | eficiência = 100% |
| B) $[0, 1007759]$ | ✗ | eficiência = 96,1% |
| C) $[0, 949343]$ | ✗ | eficiência = 90,5% |
| D) $[0, 2097023]$ | ✓ | eficiência = 100% |
| E) $[0, 1047552]$ | ✗ | eficiência = 99,9% |

b) $m = 3$

- A) $400 + 2000 + 2500 \cdot 3 = 9900$
- D) $1000 + 1200 + 1670 \cdot 3 = 7210$ ✓

Ao triplicar o atraso de multiplicação se somam aos outros atrasos, o conjunto modular D é o mais veloz.

c) $n = 7$

$$D = 2^7, 2^7 - 1, 2^7 + 1$$

$$X = \{x_{20}, x_{19}, \dots, x_1, x_0\}$$

$$x = x_6 x_5 x_4 x_3 x_2 x_1 x_0 \sim N_1$$

$$x_{13} x_{12} x_{11} x_{10} x_9 x_8 x_7 \sim N_2$$

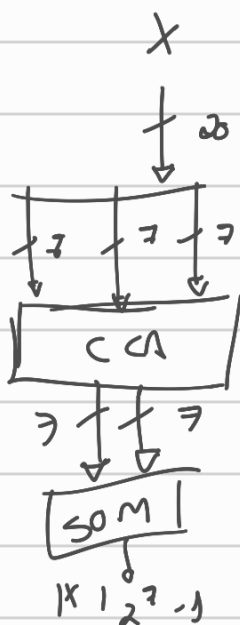
$$x_{20} x_{19} x_{18} x_{17} x_{16} x_{15} x_{14} \sim N_3$$

$$2^7: N_1 \rightarrow \{x_6, x_5, x_4, x_3, x_2, x_1, x_0\}$$

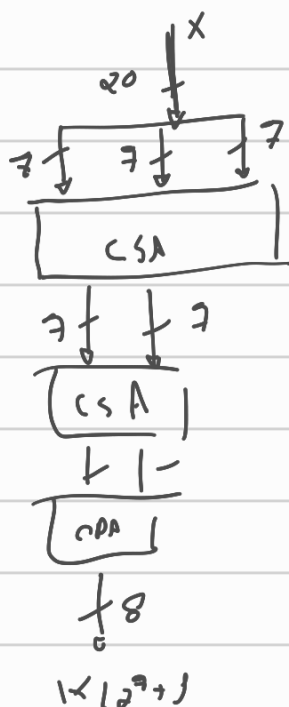
$$2^7 - 1: |N_1 + N_2 + N_3|_{2^7 - 1}$$

$$2^7 + 1: |N_1 + N_2 + N_3|_{2^7 + 1} = |N_0 - N_1 + N_2|_{2^7 + 1}$$

$$2^7 - 1:$$



$$2^7 + 1:$$



d)

$$m_1 = 2^7$$

$$m_2 = 2^7 - 1$$

$$m_3 = 2^7 + 1$$

$$\hat{m}_1 = (2^7 - 1)(2^7 + 1) = 2^{14} - 1$$

$$\hat{m}_2 = 2^7(2^7 + 1) = 2^{14} + 2^7$$

$$\hat{m}_3 = (2^7 - 1)2^7 = 2^{14} - 2^7$$

$$|\hat{m}_1^{-1}| m_1 = 2^7 - 1$$

$$|\hat{m}_2^{-1}| m_2 = 2^6$$

$$|\hat{m}_3^{-1}| m_3 = 2^6 + 1$$

$$V_1 = \frac{(2^7 - 1)(2^{14} - 1) - 1}{2^7} = \frac{2^{21} - 2^7 - 2^{14} - 1}{2^7} = 2^{14} - 2^7 + 1$$

$$V_2 = \frac{2^6 \cdot 2^7 (2^7 + 1)}{2^7} = 2^{13} + 2^6$$

$$V_3 = (2^6 + 1) \cdot 2^7 (2^7 - 1) = 2^{13} + 2^6 - 1$$

$$2^{13} \quad 2^{12} \quad \overbrace{2^{11}}^{2^7} \quad 2^{10} \quad 2^9 \quad 2^8 \quad 2^7 \quad 2^6 \quad 2^5 \quad 2^4 \quad 2^3 \quad 2^2 \quad 2^1 \quad 2^0$$

$$A \quad \overline{r_{1,5}} \quad \overline{r_{1,5}} \quad \overline{r_{3,4}} \quad \overline{r_{3,3}} \quad \overline{r_{1,2}} \quad \overline{r_{1,1}} \quad \overline{r_{3,6}} \quad r_{2,0} \quad r_{2,6} \quad r_{2,5} \quad r_{2,4} \quad r_{2,3} \quad r_{2,2} \quad r_{2,1}$$

$$B \quad r_{0,0} \quad r_{2,6} \quad r_{2,5} \quad r_{2,4} \quad r_{2,3} \quad r_{2,2} \quad r_{2,1} \quad r_{3,7} \quad r_{3,6} \quad r_{3,5} \quad r_{3,4} \quad r_{3,3} \quad r_{3,2} \quad r_{3,1}$$

$$C \quad r_{3,0} \quad r_{3,6} \quad r_{3,5} \quad r_{3,4} \quad r_{3,3} \quad r_{3,2} \quad r_{3,1} \quad r_{2,1} \quad \overline{r_{3,3}} \quad \overline{r_{3,6}} \quad \overline{r_{3,5}} \quad \overline{r_{3,4}} \quad \overline{r_{3,3}} \quad \overline{r_{3,4}} \quad \overline{r_{2,0}}$$

$$D \quad r_{3,7} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0$$

