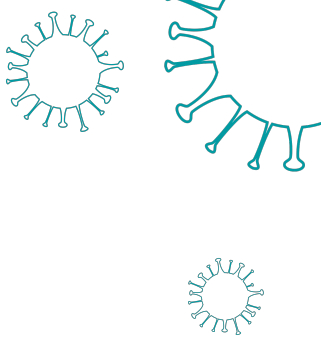


# How to allocate vaccines across countries?

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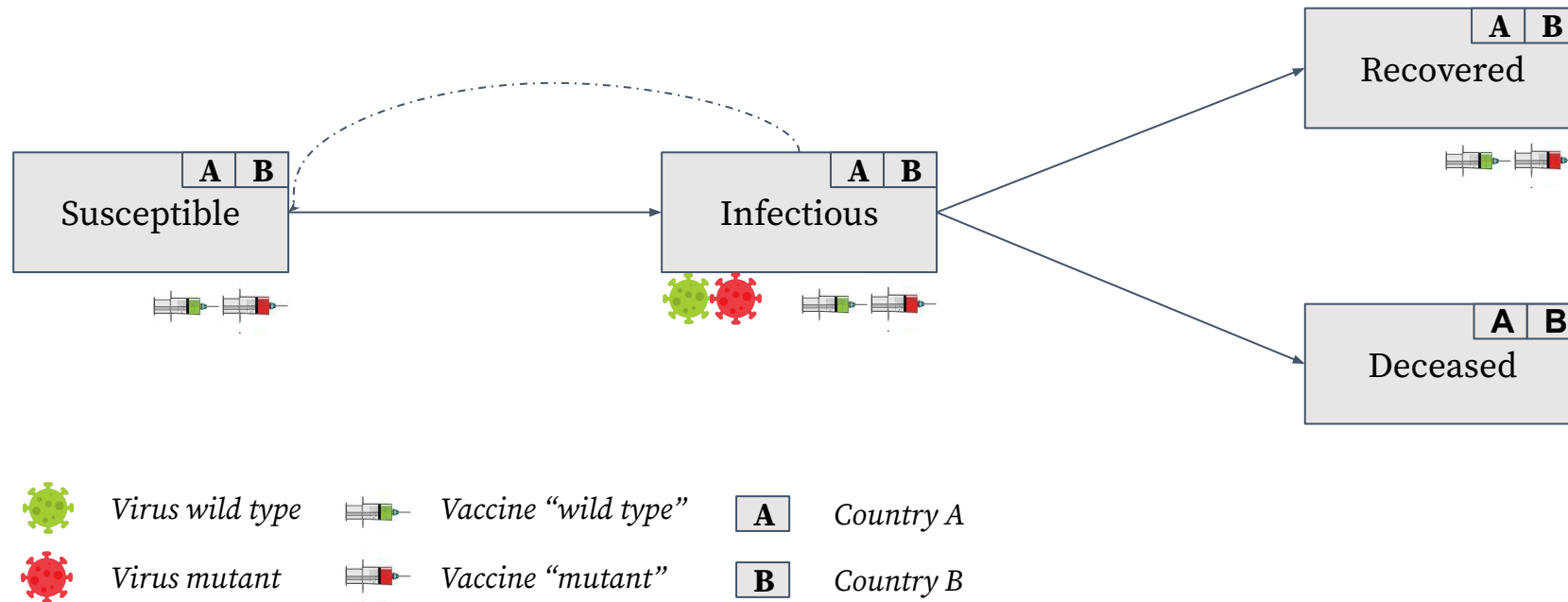
Manuel Huth  
University of Bonn

# Overview



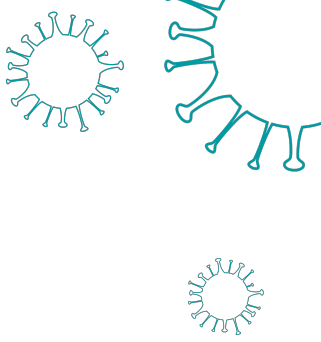
<i>General question</i>	How to efficiently allocate vaccines?
<i>Current practice</i>	Constant fraction based on population size.
<i>Our research</i>	Is there a <i>better</i> solution than the current practice?
<i>Methods</i>	Simulation of ODE compartment models.
<i>Preliminary findings</i>	In our model, a (pareto) improvement is possible.

# Model structure



**Figure 1** - Model compartments for a world with two countries A and B.

# Simulation setup

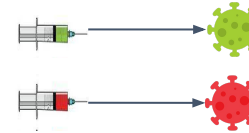


## 1) Vaccine implementation

- Continuous inflow of vaccines
- Logistically transformed cubic hermite splines.
- Domain of Polynomials are intervals with length of 14 days.

## 2) Vaccine properties

- Vaccines decrease infection probability by 80% and probability of dying by 90%.
- No cross-effectiveness of vaccines.



## 3) Parameters

- The reproduction number is  $3.0^1$  for the wild type and 3.6 for the mutant.
- Start with 8 million susceptible individuals in each country.
- Country A has one wild type and Country B has one mutant case at the start.



## 4) Objective

- Minimize the total number of deceased individuals.
- Optimize over boundary conditions of splines.
- Consider only allocations that yield a pareto improvement.

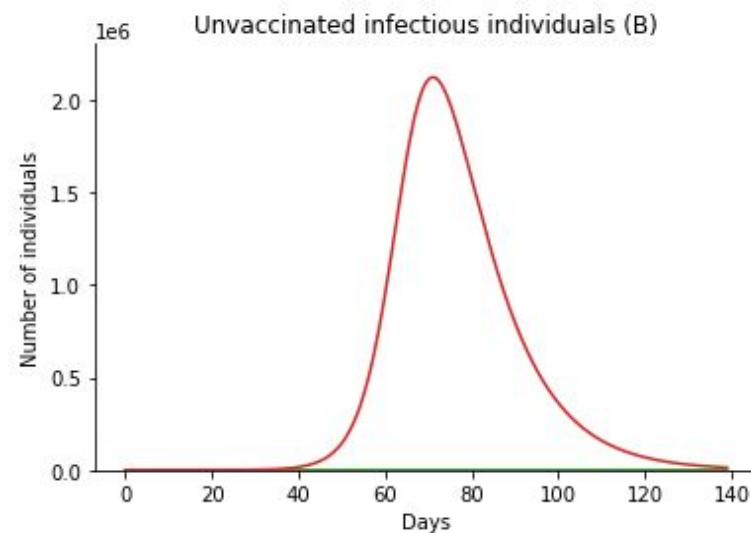
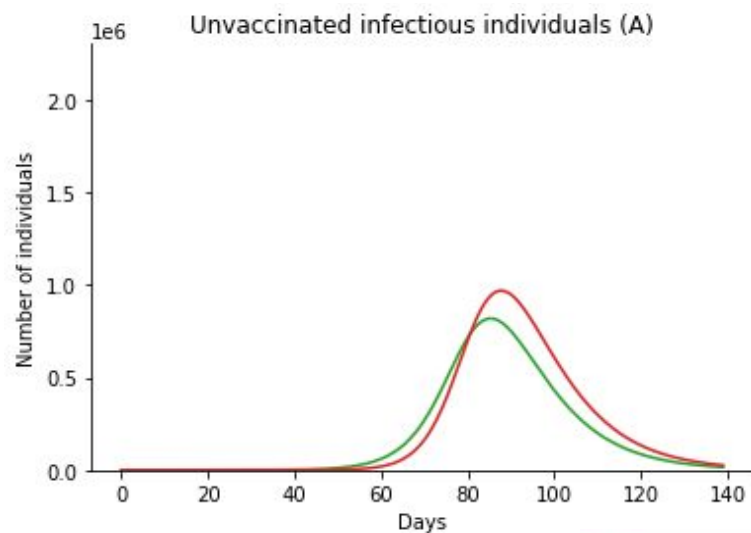
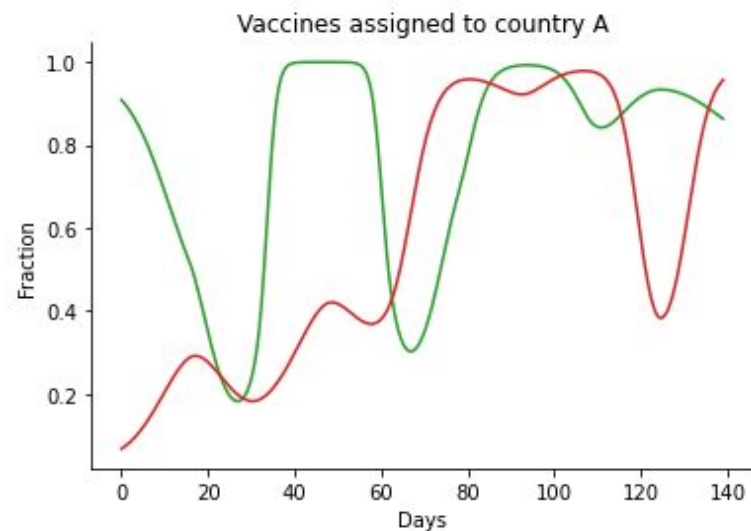
<sup>1</sup>Robert Koch Institute (2021)

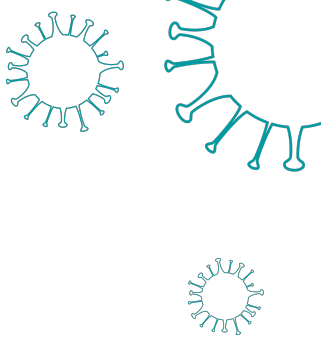
# Results for different policies

	<i>Current policy</i>	<i>Optimal policy</i>	<i>One Vaccine per country</i>
<i>Deceased country A</i>	206,562	204,607	218,045
<i>Deceased country B</i>	208,782	201,888	186,863
<i>Total</i>	414,344	406,495	404,908

**Table 1** - Deceased individual dependent on vaccination strategies.

# Optimal allocation

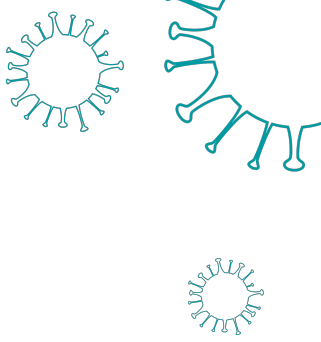




# How to allocate vaccines across countries?

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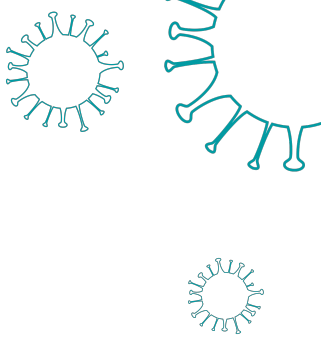
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University of Bonn



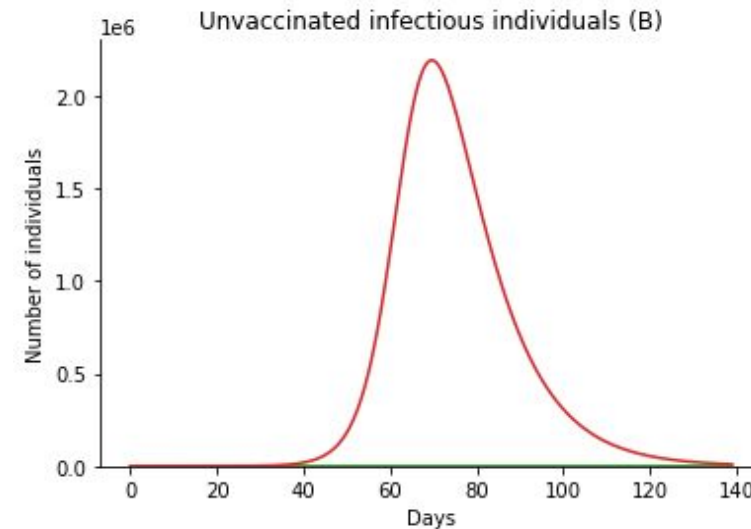
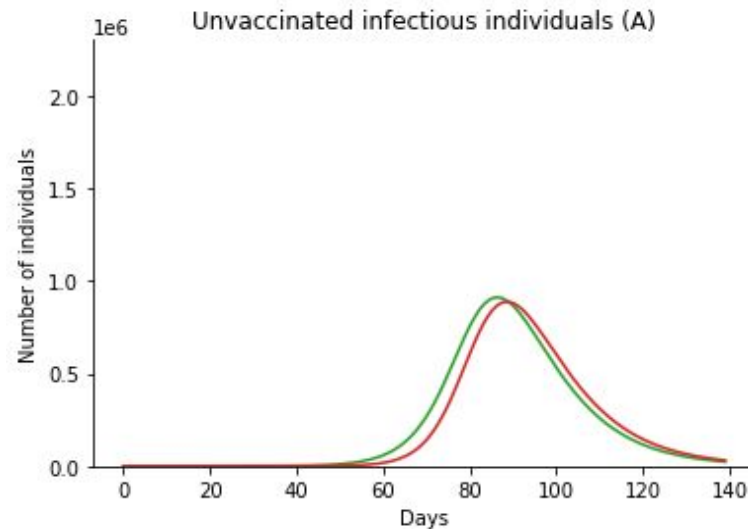
# | Additional material



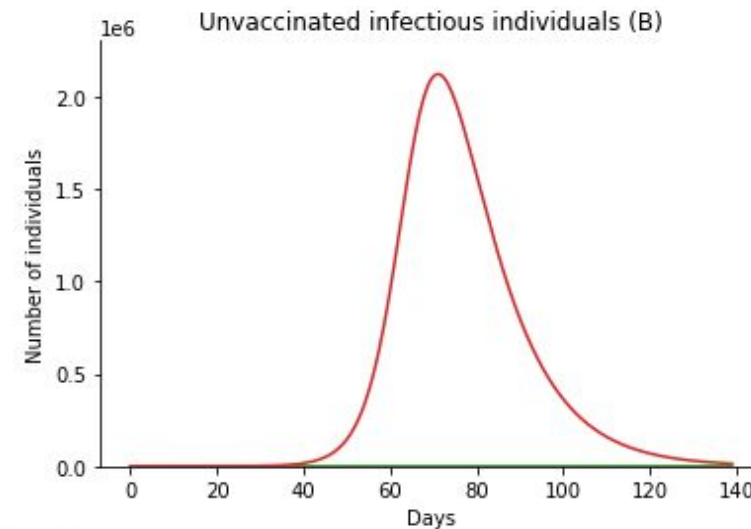
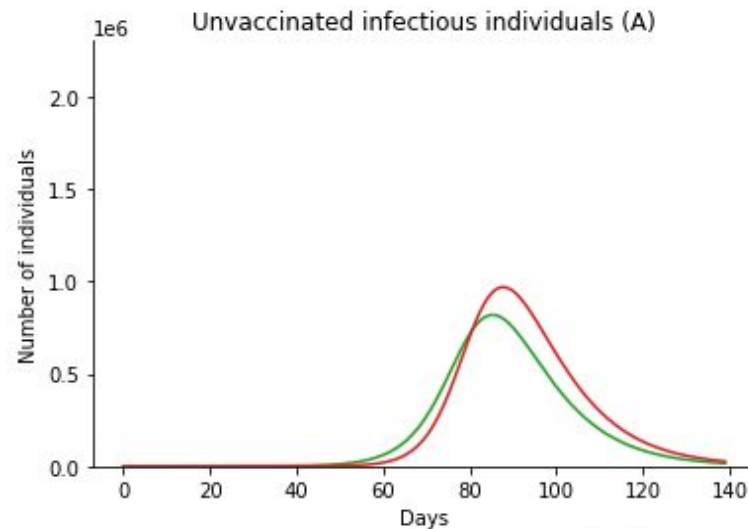
# Unvaccinated infectious individuals



Current strategy

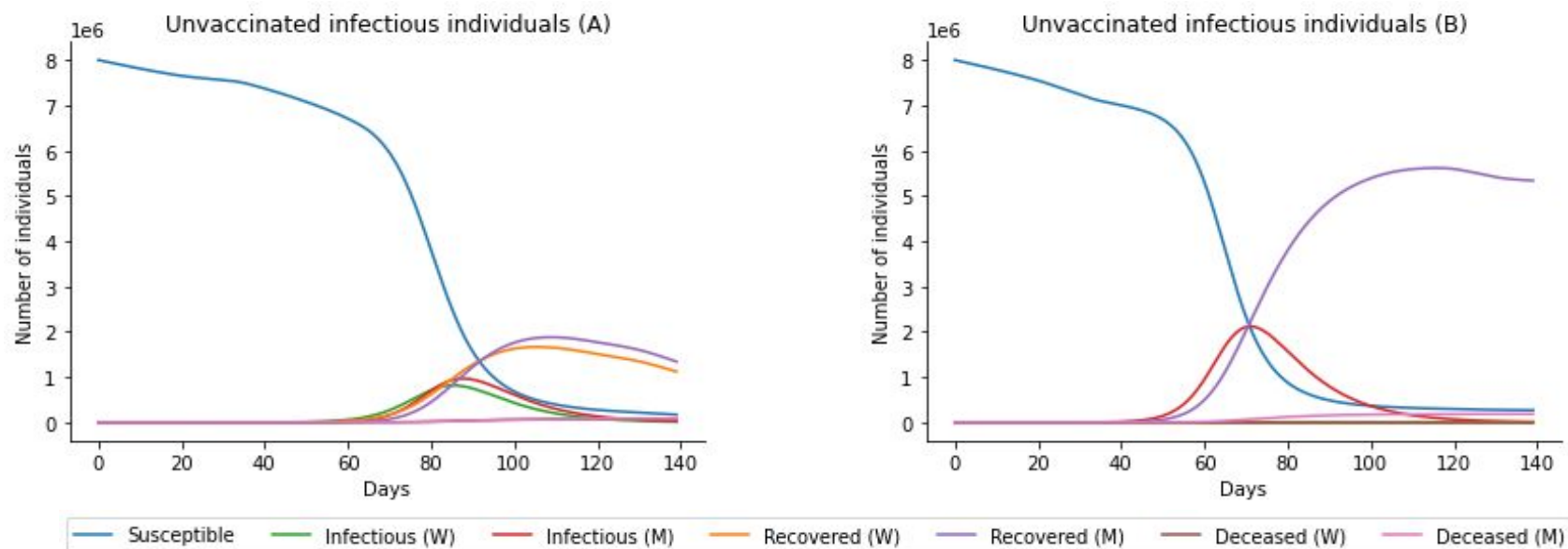
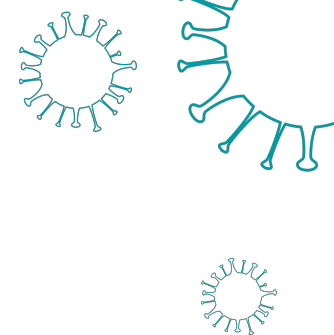


Optimal strategy



— Virus wild type — Virus mutant

# Compartments in the optimal setup



# Splines

## 1) Basis polynomials

$$b_1(t) = 2t^3 - 3t^2$$

$$b_2(t) = t^3 - 2t^2 + t$$

$$b_3(t) = -2t^3 + 3t^2$$

$$b_4(t) = t^3 - t^2$$

## 3) Polynomials

$$\begin{aligned} P_i(\theta; t) = & b_1(t') \overbrace{P_i(t_i)}^{\theta_i} \\ & + b_2(t')(t_{i+1} - t_i) P'_i(\theta; t_i) \\ & + b_3(t') \underbrace{P_{i+1}(t_{i+1})}_{\theta_{i+1}} \\ & + b_4(t')(t_{i+1} - t_i) P'_i(\theta; t_{i+1}) \end{aligned}$$

$$t' = (t - t_i) / (t_{i+1} - t_i)$$

## 2) Finite difference approximation

$$P'_1(t_1) \approx \frac{P_2(\theta; t_2) - P_1(t_1)}{t_2 - t_1}$$

$$P'_i(\theta; t_i) \approx \frac{1}{2} \left[ \frac{P_{i+1}(t_{i+1}) - P_i(t_i)}{t_{i+1} - t_i} + \frac{P_i(t_i) - P_{i-1}(t_{i-1})}{t_i - t_{i-1}} \right]$$

$$P'_z(t_{z+1}) \approx \frac{P_{z+1}(t_{z+1}) - P_z(t_z)}{t_{z+1} - t_z}$$

## 4) Exemplary spline

