Planning & Decision-making in Robotics

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Compiling Code

Command to compile

g++ planner.cpp planner_functions.cpp -o planner.out

Results and Statistics

The 5 start and goal configurations are,

| Start | Goal |
|-------------------------|-------------------------|
| 1.7, 1, 0.3, 5.6, 4.2 | 1.8, 0.2, 1.5, 2.6, 5.2 |
| 1.5, 1.9, 3.1, 1.3, 3.9 | 1.6, 0.9, 0, 5.2, 1.5 |
| 1.3, 0.7, 2.8, 1.2, 3 | 1.7, 2.3, 4, 4.1, 1.8 |
| 1.1, 0.9, 2, 1.9, 1.1 | 1.7, 6.2, 1.7, 0.4, 0.6 |
| 1.5, 1.7, 5.9, 0.1, 4.9 | 1.8, 2.5, 1.8, 1.4, 4.3 |

The four tables below show the statistics of the 4 runs for all start-goal configurations for each planner

| planner | mapName | problemInde≯ | numSteps | cost | timespent | success | numNodes |
|---------|------------|--------------|----------|------------|---------------|---------|----------|
| 0 | ./map2.txt | 0 | 33 | 22.852762 | 0.133893044 | True | 287 |
| 0 | ./map2.txt | 1 | 25 | 18.464392 | 0.08668601701 | True | 280 |
| 0 | ./map2.txt | 2 | 39 | 20.293808 | 8.321813774 | True | 2606 |
| 0 | ./map2.txt | 3 | 41 | 22.407108 | 31.190708222 | True | 4815 |
| 0 | ./map2.txt | 4 | 27 | 17.725862 | 0.069140336 | True | 240 |
| 1 | ./map2.txt | 0 | 11 | 20.404248 | 0.01008551201 | True | 69 |
| 1 | ./map2.txt | 1 | 10 | 19.739908 | 0.005698466 | True | 17 |
| 1 | ./map2.txt | 2 | 11 | 25.899614 | 0.018861024 | True | 108 |
| 1 | ./map2.txt | 3 | 42 | 51.77208 | 0.17484373301 | True | 415 |
| 1 | ./map2.txt | 4 | 34 | 34.636116 | 3.392749463 | True | 1717 |
| 2 | ./map2.txt | 0 | 32 | 20.670544 | 0.112383193 | True | 274 |
| 2 | ./map2.txt | 1 | 18 | 14.358208 | 0.00865340499 | True | 64 |
| 2 | ./map2.txt | 2 | 19 | 15.091508 | 1.845577431 | True | 1165 |
| 2 | ./map2.txt | 3 | 48 | 23.517104 | 4.844422451 | True | 1805 |
| 2 | ./map2.txt | 4 | 26 | 18.3777638 | 0.047419731 | True | 117 |
| 3 | ./map2.txt | 0 | 13 | 14.139118 | 18.35283677 | True | 10002 |
| 3 | ./map2.txt | 1 | 13 | 14.423064 | 18.364176816 | True | 10002 |
| 3 | ./map2.txt | 2 | 13 | 15.044352 | 18.298336106 | True | 10002 |
| 3 | ./map2.txt | 3 | 17 | 19.861148 | 18.26331252 | True | 10002 |
| 3 | ./map2.txt | 4 | 14 | 15.26531 | 18.32068277 | True | 10002 |

Figure 1: Stats for run 1

| planner | mapName | problemIndex | numSteps | cost | timespent | success | numNodes |
|---------|------------|--------------|----------|-------------|---------------|---------|----------|
| 0 | ./map2.txt | 0 | 17 | 16.63298 | 0.050322464 | True | 114 |
| 0 | ./map2.txt | 1 | 23 | 17.375866 | 0.02951797799 | True | 197 |
| 0 | ./map2.txt | 2 | 38 | 21.419648 | 8.233104257 | True | 2873 |
| 0 | ./map2.txt | 3 | 24 | 14.602898 | 6.54259998001 | True | 2371 |
| 0 | ./map2.txt | 4 | 52 | 22.86284 | 1.01274590401 | True | 394 |
| 1 | ./map2.txt | 0 | 45 | 47.880734 | 2.88258259301 | True | 1657 |
| 1 | ./map2.txt | 1 | 11 | 19.19138131 | 0.006947574 | True | 46 |
| 1 | ./map2.txt | 2 | 33 | 22.538644 | 0.02948758101 | True | 210 |
| 1 | ./map2.txt | 3 | 11 | 19.79566874 | 0.006154708 | True | 40 |
| 1 | ./map2.txt | 4 | 23 | 28.109756 | 0.07731675499 | True | 262 |
| 2 | ./map2.txt | 0 | 25 | 15.940134 | 0.171807885 | True | 338 |
| 2 | ./map2.txt | 1 | 21 | 15.016914 | 0.03589102899 | True | 172 |
| 2 | ./map2.txt | 2 | 38 | 24.705858 | 17.055518437 | True | 3722 |
| 2 | ./map2.txt | 3 | 54 | 31.688776 | 11.41296779 | True | 3108 |
| 2 | ./map2.txt | 4 | 29 | 16.20048 | 0.152575809 | True | 160 |
| 3 | ./map2.txt | 0 | 13 | 12.742326 | 18.741066333 | True | 10002 |
| 3 | ./map2.txt | 1 | 15 | 16.54315 | 19.41404806 | True | 10002 |
| 3 | ./map2.txt | 2 | 12 | 13.270718 | 18.908170816 | True | 10002 |
| 3 | ./map2.txt | 3 | 20 | 21.460794 | 19.240365764 | True | 10002 |
| 3 | ./map2.txt | 4 | 14 | 16.646568 | 18.600349023 | True | 10002 |

Figure 2: Stats for run 2

| planner | mapName | problemIndex | numSteps | cost | timespent | success | numNodes |
|---------|------------|--------------|----------|-------------|---------------|---------|----------|
| 0 | ./map2.txt | 0 | 22 | 18.569502 | 1.84942163101 | True | 1404 |
| 0 | ./map2.txt | 1 | 20 | 26.83138 | 0.00786997999 | True | 63 |
| 0 | ./map2.txt | 2 | 36 | 21.598546 | 0.457086173 | True | 719 |
| 0 | ./map2.txt | 3 | 64 | 36.093134 | 24.056924635 | True | 4558 |
| 0 | ./map2.txt | 4 | 32 | 19.2078946 | 0.17121946599 | True | 178 |
| 1 | ./map2.txt | 0 | 13 | 18.358096 | 0.011969981 | True | 88 |
| 1 | ./map2.txt | 1 | 9 | 19.58428731 | 0.00493412699 | True | 22 |
| 1 | ./map2.txt | 2 | 10 | 18.05793 | 0.007057326 | True | 60 |
| 1 | ./map2.txt | 3 | 13 | 12.9706638 | 0.13655618501 | True | 385 |
| 1 | ./map2.txt | 4 | 13 | 24.786318 | 0.02322423 | True | 143 |
| 2 | ./map2.txt | 0 | 56 | 21.977694 | 2.085230246 | True | 1340 |
| 2 | ./map2.txt | 1 | 36 | 24.793996 | 2.714080091 | True | 1467 |
| 2 | ./map2.txt | 2 | 32 | 20.981932 | 25.107751552 | True | 4630 |
| 2 | ./map2.txt | 3 | 39 | 19.896046 | 13.258320557 | True | 3181 |
| 2 | ./map2.txt | 4 | 27 | 16.470622 | 0.105111094 | True | 196 |
| 3 | ./map2.txt | 0 | 11 | 11.555756 | 18.561522991 | True | 10002 |
| 3 | ./map2.txt | 1 | 15 | 16.910828 | 18.435397803 | True | 10002 |
| 3 | ./map2.txt | 2 | 13 | 15.62465 | 18.40961242 | True | 10002 |
| 3 | ./map2.txt | 3 | 16 | 18.421944 | 18.426431707 | True | 10002 |
| 3 | ./map2.txt | 4 | 15 | 16.411984 | 18.816875275 | True | 10002 |

Figure 3: Stats for run 3

| planner | mapName | problemIndex | numSteps | cost | timespent | success | numNodes |
|---------|------------|--------------|----------|-------------|---------------|---------|----------|
| 0 | ./map2.txt | 0 | 34 | 22.13005 | 0.432537559 | True | 237 |
| 0 | ./map2.txt | 1 | 21 | 16.123282 | 0.00755759199 | True | 61 |
| 0 | ./map2.txt | 2 | 37 | 21.688262 | 0.733544802 | True | 874 |
| 0 | ./map2.txt | 3 | 49 | 27.8651 | 12.767764764 | True | 3553 |
| 0 | ./map2.txt | 4 | 33 | 18.7907008 | 0.060606317 | True | 164 |
| 1 | ./map2.txt | 0 | 12 | 23.36525 | 0.004996555 | True | 23 |
| 1 | ./map2.txt | 1 | 11 | 22.95762931 | 0.00548789 | True | 26 |
| 1 | ./map2.txt | 2 | 9 | 15.310102 | 0.00578063101 | True | 31 |
| 1 | ./map2.txt | 3 | 19 | 19.859134 | 0.20049359801 | True | 487 |
| 1 | ./map2.txt | 4 | 16 | 21.031646 | 0.06491227901 | True | 222 |
| 2 | ./map2.txt | 0 | 45 | 20.777726 | 0.569039922 | True | 615 |
| 2 | ./map2.txt | 1 | 38 | 19.013976 | 23.139821211 | True | 4199 |
| 2 | ./map2.txt | 2 | 37 | 21.246532 | 0.199148666 | True | 455 |
| 2 | ./map2.txt | 3 | 38 | 19.352514 | 6.08448895399 | True | 2236 |
| 2 | ./map2.txt | 4 | 55 | 17.010972 | 0.3044029 | True | 359 |
| 3 | ./map2.txt | 0 | 13 | 14.753172 | 19.404907525 | True | 10002 |
| 3 | ./map2.txt | 1 | 13 | 15.08018 | 19.188224848 | True | 10002 |
| 3 | ./map2.txt | 2 | 14 | 15.046322 | 19.912442615 | True | 10002 |
| 3 | ./map2.txt | 3 | 19 | 21.4448196 | 19.723224866 | True | 10002 |
| 3 | ./map2.txt | 4 | 14 | 15.1540226 | 19.417058969 | True | 10002 |

Figure 4: Stats for run 4

Average stats for all runs

| | RRT | RRT-Connect | RRT* | PRM |
|----------------------|------------------|------------------|-----------------|----------------|
| Avg Planning Time | 4.81075324475023 | 0.35350701055286 | 5.4627306176975 | 18.83995219985 |
| Success Rate | 70.00% | 100.00% | 70.00% | 0.00% |
| Avg Num Nodes | 1299.4 | 301.4 | 1480.15 | 10002 |
| Avg Cost | 21.17680077 | 24.3124603230769 | 19.85446499 | 15.99001131 |
| | | | l I | |
| | | | l I | |
| Std Dev Time | 8.69674422345746 | 0.95758976970943 | 8.0853923718623 | 0.52429113517 |
| Std Dev Success Rate | 0.47016234598163 | 0 | 0.4701623459816 | 0 |
| Std Dev Num Nodes | 1577.49799899781 | 494.784312392252 | 1512.4187764185 | 0 |
| Std Dev Cost | 4.85602452690235 | 9.89185591456955 | 4.2195225652285 | 2.629119280324 |

Figure 5: Average and Std Dev

RRT-Connect had the lowest average planning time, because of bi-directional growth and relaxation of the epsilon constraint. PRM had the highest average planning time, but this was only because the PRM graph is being generated during each run. Because of this, it was not able to plan within 5 seconds and had a success rate of 0. Ideally, we can generate the graph once, and then re-use it for multiple queries, which will be much faster. RRT* had a lower average cost than RRT and RRT-Connect, which was expected because of re-wiring in RRT*, which increased its average planning time. PRM had the lowest average cost, because of the large number of nodes sampled. It was always able to find a lower cost path since more nodes were sampled and added to the graph.

The hyper-parameters I used include,

- Epsilon for limiting step size. A larger step size reduced the planning time but increased the cost of the path
- A small step size for interpolating and checking collisions when joining nodes. Reducing the step size increased the time for collision checking and the overall planning time
- A goal threshold, so that whenever a node is sampled within that threshold, the algorithm tries and connect the node to the goal. Basically defining a 'goal region'. This is required because if we try and sample a single goal node, the probability for that is 0, which is why we need to define a region
- A goal bias, to periodically bias sampling directly towards the goal to speed up performance
- A search radius for the nearest neighbor search. Only nodes within that radius will be considered neighbors. A higher radius meant connecting to nodes which were further away
- A neighbor limit for PRM, to limit the branching factor of all nodes in the graph

Conclusion

- 1. Based on the above results, I believe that a PRM planner would be the best suited for this environment, provided we can pre-build and save the PRM graph. The average time for the PRM runs is high because that includes the time to sample and generate the PRM graph as well, which is happening during each run. Instead, once we have generated the graph, we can save it, and then re-use it. Searching through the PRM graph for a path will take a very short time. The average cost for the PRM runs is also the lowest.
 - This is a static environment where we might need to solve for multiple start-goal configurations, hence saving a PRM graph and then re-using it will be feasible. If we are not able to do that, and instead have to build the PRM graph during each run, then RRT or RRT-Connect will be more suitable for this environment. RRT* will take a bit more time, but will provide a lower cost solution. So if we need to plan fast, then it might not be suitable.
- 2. The issues still there in the PRM planner is that once a graph is generated, we do not change it anymore, such as in RRT*. There is no re-wiring taking place. It does not guarantee an optimal solution. If it fails to find a path, we cannot be sure if it was due to an obstacle in the environment, or just because the number of sampled nodes is less.
- 3. To improve this planner, we can perform better pre-processing while building the PRM graph, such as a more efficient implementation of the neighborhood function, or using a connected-components approach, instead of the condition limiting the maximum number of neighbors of a node. We can also use better sampling strategies while building the graph instead of sampling uniformly. This could include bias sampling towards obstacle boundaries, or use Gaussian distributions around already existing samples. We can also perform post-processing, like path shortening, to obtain better paths.

Extra Credit

The highest variance in terms of consistency of solutions for different runs with the same start and goal configurations was observed in both RRT and RRT*. They showed the maximum deviation in planning time as well as cost. One hyper-parameter that helped in decreasing the planning time was increasing the goal threshold. If the goal threshold is slightly larger, but we perform a collision-check between the second last node and the goal, it helped in reducing the planning time by a lot, since it meant a higher probability of sampling in the 'goal region'. RRT* took the most time on average (if we exclude the time of building the PRM graph), which was mainly because of the re-wiring and collision-checking process. In difficult configurations, the variation in RRT and RRT* planning times ranged from anywhere between 4 seconds and 130 seconds. This variance in planning times was much lower in PRM and RRT-Connect.