Rule 0.25 (Cache Array Member Variables)

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 \begin{bmatrix} [\dots] \\ \textbf{contract } A \ \{ \\ [\dots] \\ \textbf{function } f(pds) \ \{ \\ [\dots] \\ \textbf{for}(init; \ cond; \ upd) \ \{ \\ stmts[arr[i]] \\ \} \\ stmts' \\ \} \\ [\dots] \\ \} \end{bmatrix} 
= \begin{bmatrix} [\dots] \\ \textbf{contract } A' \ \{ \\ [\dots] \\ \textbf{function } f(pds) \ \{ \\ [\dots] \\ \textbf{for}(init; \ cond; \ upd) \ \{ \\ T \ cache = arr[i]; \\ stmts[cache] \\ \} \\ stmts' \\ \} \\ [\dots] \\ \}
```

where

arr is an array (storage or memory) accessed within the loop;

arr[i] is an array element accessed multiple times in the loop body;

cache is a local variable of type T (reference type for storage, value type for memory) that caches arr[i];

T is the type of the array elements;

stmts[arr[i]] represents loop body statements that access arr[i] multiple times;

stmts[cache] represents the same statements with arr[i] replaced by cache;

init, cond, and upd are the loop initialization, condition, and update expressions;

pds are the parameter declarations of function f;

stmts' represents statements following the loop.

provided

The array element arr[i] is accessed multiple times within the same loop iteration;

For storage arrays, use **storage** keyword to cache references; for memory arrays, cache values;

The cached reference or value maintains consistency throughout the iteration;

No operations within the loop invalidate the cached reference (e.g., array resizing);

The caching does not introduce race conditions or affect correctness.

Invariant:

Let s_i and s'_i be the initial state of A and A', respectively.

Let s_f and s'_f be the state reached by A and A', respectively, after A.f() and A'.f() are executed from s_i and s'_i , respectively.

Then, the coupling invariant is

$$\forall s_i, s_i' : (s_i = s_i') \rightarrow (s_f = s_f')$$