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**Rule 0.4** *(Refactoring Loops with Repeated Computations)*


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<pre> [...]  <b>contract</b> A {    [...]   <b>function</b> f(pds) {      [...]     <b>for</b>(init; cond; update) {        stmts[expr]      }      stmts'    }    [...] } </pre>	=	<pre> [...]  <b>contract</b> A' {    [...]   <b>function</b> f(pds) {      [...]     T local = expr;      <b>for</b>(init; cond; update) {        stmts[local]      }      stmts'    }    [...] } </pre>
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**where**

*expr* is an expression that is loop-invariant (yields the same result in every iteration);

*T* is the type of the computed expression *expr*;

*local* is a local variable of type *T* used to cache the computation result;

*stmts[expr]* represents statements inside the loop that use *expr*;

*stmts[local]* represents the same statements with *expr* replaced by *local*;

*init*, *cond*, and *update* are the loop initialization, condition, and update expressions;

*stmts'* represents statements following the loop.

**provided**

*expr* does not depend on the loop variable or any value modified within the loop;

*expr* is side-effect free (does not modify state or call external functions);

The value of *expr* remains constant throughout all loop iterations;

No variable in *expr* is modified between the assignment to *local* and the loop execution.

**Invariant:**

Let  $s_i$  and  $s'_i$  be the initial state of *A* and *A'*, respectively.

Let  $s_f$  and  $s'_f$  be the state reached by *A* and *A'*, respectively, after *A.f()* and *A'.f()* are executed from  $s_i$  and  $s'_i$ , respectively.

Then, the coupling invariant is

$$\forall s_i, s'_i . (s_i = s'_i) \rightarrow (s_f = s'_f)$$


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