Rule 0.4 (Refactoring Loops with Repeated Computations)

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 \begin{bmatrix} [\dots] \\ \textbf{contract } A \ \{ \\ [\dots] \\ \textbf{function } f(pds) \ \{ \\ [\dots] \\ \textbf{for}(init; \ cond; \ update) \ \{ \\ stmts[expr] \\ \} \\ stmts' \\ \} \\ [\dots] \\ \}
```

where

expr is an expression that is loop-invariant (yields the same result in every iteration);

T is the type of the computed expression expr;

local is a local variable of type T used to cache the computation result;

stmts[expr] represents statements inside the loop that use expr;

stmts[local] represents the same statements with expr replaced by local;

init, cond, and update are the loop initialization, condition, and update expressions; stmts' represents statements following the loop.

provided

expr does not depend on the loop variable or any value modified within the loop;

expr is side-effect free (does not modify state or call external functions);

The value of *expr* remains constant throughout all loop iterations;

No variable in expr is modified between the assignment to local and the loop execution.

Invariant:

Let s_i and s'_i be the initial state of A and A', respectively.

Let s_f and s'_f be the state reached by A and A', respectively, after A.f() and A'.f() are executed from s_i and s'_i , respectively.

Then, the coupling invariant is

$$\forall s_i, s_i' : (s_i = s_i') \rightarrow (s_f = s_f')$$