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DarthKnight's blog

Algorithm Gym :: Data structures

DARTHKNIGHT BLOG TEAMS SUBMISSIONS GROUPS CONTESTS PROBLEMSETTING

By DarthKnight, 5 years ago, , ,

Today I want to introduce you some very very useful data structures.

In this lecture, we are trying to improve your data structures skills, stay with us and click on **read more**. Important data structures :

Trees

Trees are one of the most useful data structures. A tree is a connected-acyclic graph. There are too many types of trees, like: rooted trees, weighted trees, directed trees, tries, etc.

Partial sum

There are two types of problems solvable by partial sum.

1.Problems which you are asked to answer some queries about the sum of a part of elements (without modify queries).

Solution of all of this problems are the same. You just need to know how to solve one of them.

Example : You are asked some queries on an array $a_1, a_2, ...a, n$. Each query give you numbers l and r and you should print $a_l + a_{l+1} + ... + a_r$.

Solution : You need to build another array $s_1, s_2, ..., s_n$ which $s_i = a_1 + a_2 + ... + a_i$ and answer is $s_r - s_{l-1}$.

2.Problems which you are asked to perform some queries asking you to modify a part of elements (without printing queries.)

Solution of all of this problems are the same. You just need to know how to solve one of them.

Example : You need to perform some queries on an array $a_1, a_2, ...a, n$. Each query give you numbers l, r and v and for each i such that $l \le i \le r$ you should increase a_i by v, and then after performing all queries, you should print the whole array.

Solution : You should have another array $p_1, p_2, ..., p_n$ which, all of its members are initially 0, for each query, you should increase p_l by v and decrease p_{r+1} by v.

An then, for each i, starting from 1 you should increase p_i by p_{i-1} . So, final array would be $a_1+p_1, a_2+p_2, ..., a_n+p_n$.

Hard problem of partial sum : Troynacci Query

Disjoint sets

Disjoint sets are also useful data structures. Using them is fast and easy. We use theme in many algorithms, like Kruskal's and Prim's.

Disjoint sets, or DSU (Disjoint Sets Union) as their name, are sum sets. Imagine we have some boxes and some tools and initially each tool is in one box. Mostly, we are given some queries and ask to merge two boxes or print the members of a box or find which box is some tool in.

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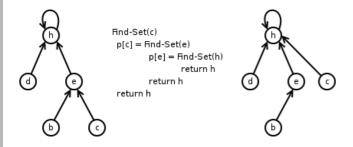
Urvatullo12345 → <u>Tutorial for problem 4a</u> Watermelon!

For rest of these, let's consider that initially there is exactly one tool in a box. That is, we have n tools and n boxes and initially, tool number i is in box number i.

For this propose, we can use so many containers.Like:

Trees

Trees are the most useful containers for DSU. For each vertex, we keep it's parent (and parrent of the root is -1). So, initially are parents are set to -1, and we have queries to find the root of each box(having the root, we can easily find the box's index) and queries for merging two trees. For better time complexity, every time we want to find the root of each vertex, we set it's parent to the root for the next queries. And while merging, we always want to minimize the height of the tree, so when we want to merge the boxes, it's like we put all the tools of the box with fewer tools in the other box.



The best way I've seen to code this kind of DSU, is style of bmerry: (C++)

In the code above, for each root v, par[v] equals the negative of number of tools in that box.

Arrays, vectors

We keep tools in a vector (or an array) and when we have a query to merge two boxes, we put all the tools of the box with fewer tools in the other box.

The time complexity is good because for each tool, we take and put it in an other box at most log(n) times (each time the size of the vector will be at least doubled).

So time complexity would be O(n.log(n)).

Sets (red-black trees)

Other way is to keep them in a red-black tree (in C++ it's set). We do exactly like vectors, so time complexity would be $O(n.log^2(n))$. (One log is for inserting).

Problems: Hamro and tools, TROY Query (Join the group ACM-OI first)

Tries

Tries are some kind of rooted trees in which each edge has a character on it. Actually, trie is some kind of DFA (Determining Finite Automata). For a bunch of strings, their trie is the smallest rooted tree with a character on each edge and each of these strings can be build by writing down the characters in the path from the root to some node.

It's advantage is, LCP (Longest Common Prefix) of two of these strings is the LCA (Lowest Common Ancestor) of their nodes in the trie(a node that we can build the string by writing down the characters in the path from the root to that node).

```
PikMike → Educational Codeforces Round 78
[Rated for Div. 2] ©
\begin{array}{l} \textbf{fakeacc007} \rightarrow \underline{\text{Need assistance in solving:}} \\ \underline{\text{Minimum number of swaps to make a string}} \end{array}
palindrome 6
xiaowuc1 → USACO 2019-2020 First
Contest 🐠
  love_Hoang_Yen → 2019 ICPC Asia
Danang Regional is now on Kattis
p_six \rightarrow From when to when was rng_58 the
admin of topcoder?
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Codeforces
It_Wasnt_Me → help on 195D - Analyzing
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mahmoud\_acm \rightarrow \underline{mathematical\ expectation}
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#277.5 (Div. 2) Editorial [A-D for now]
\textbf{bvd} \rightarrow \underline{2019 \ ICPC \ North \ American \ Regionals}
— Problem Archive 
\textbf{MikeMirzayanov} \rightarrow \underline{\textbf{Technocup 2020 -}}
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606: Editorial 📡
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codeforces global round 6 (1266D)
                                           Detailed →
```

Problem: A lot of games

Suffix array

Suffix array is a data structure that helps you sort all the suffixes in lexicography order.

This array consists of integers, the beginning of suffixes.

There are two ways to achieve this goal:

One) Non-deterministic algorithm : Use Robin-Carp and for check if a suffix is lexicographically less than another one, find their LCP using binary search + hash and then check the next character after their LCP.

```
Code:
```

```
namespace HashSuffixArray
{
        const int
                MAXN = 1 << 21;
        typedef unsigned long long hash;
        const hash BASE = 137;
        int N:
        char * S;
        int sa[MAXN];
        hash h[MAXN], hPow[MAXN];
        #define getHash(lo, size) (h[lo] - h[(lo) + (size)] * hPow[size])
        inline bool sufCmp(int i, int j)
                int lo = 1, hi = min(N - i, N - j);
                while (lo <= hi)
                        int mid = (lo + hi) >> 1;
                        if (getHash(i, mid) == getHash(j, mid))
                                lo = mid + 1;
                        else
                                 hi = mid - 1;
                return S[i + hi] < S[j + hi];</pre>
        }
        void buildSA()
                N = strlen(S);
```

```
hPow[0] = 1;
                 for (int i = 1; i <= N; ++i)</pre>
                         hPow[i] = hPow[i - 1] * BASE;
                 h[N] = 0;
                 for (int i = N - 1; i >= 0; --i)
                         h[i] = h[i + 1] * BASE + S[i], sa[i] = i;
                 stable_sort(sa, sa + N, sufCmp);
        }
} // end namespace HashSuffixArray
Two) Deterministic algorithm : We sort them log(MaxLength) steps, in the i - th step
(counting from 0), we sort them according to their first 2^i characters and put the suffixes whit
the same prefix with 2^i characters in the same buckets.
Code:
Suffix array O(n lg^2 n)
LCP table O(n)
#include <cstdio>
#include <algorithm>
#include <cstring>
using namespace std;
#define REP(i, n) for (int i = 0; i < (int)(n); ++i)
namespace SuffixArray
        const int MAXN = 1 << 21;</pre>
        char * S;
        int N, gap;
        int sa[MAXN], pos[MAXN], tmp[MAXN], lcp[MAXN];
        bool sufCmp(int i, int j)
                 if (pos[i] != pos[j])
                         return pos[i] < pos[j];</pre>
                 i += gap;
                 return (i < N && j < N) ? pos[i] < pos[j] : i > j;
        }
        void buildSA()
                 N = strlen(S);
                 REP(i, N) sa[i] = i, pos[i] = S[i];
                for (gap = 1;; gap *= 2)
                 {
                         sort(sa, sa + N, sufCmp);
                         REP(i, N-1) tmp[i+1] = tmp[i] + sufCmp(sa[i], sa[i])
+ 1]);
                         REP(i, N) pos[sa[i]] = tmp[i];
                         if (tmp[N - 1] == N - 1) break;
                }
        }
        void buildLCP()
                 for (int i = 0, k = 0; i < N; ++i) if (pos[i] != N - 1)
                 {
                         for (int j = sa[pos[i] + 1]; S[i + k] == S[j + k];)
```

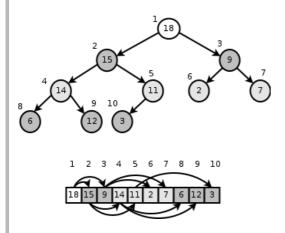
```
++k;
lcp[pos[i]] = k;
if (k)--k;
}
} // end namespace SuffixArray
```

(Codes by mukel)

Heaps

A heap is a binary rooted tree (a rooted tree that each node has at most 2 children) and each vertex has a value.

Heap property: Heap usually has a property, like the value of each vertex is equal to or greater than the value of its child(ren) (we call this a max heap). We can use heaps in heap sort.

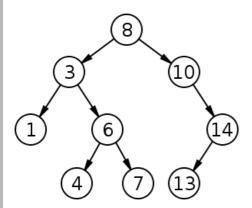


Fibonacci heaps

A fibonacci heap is a kind of heap with better complexities. We don't need to know what a fibonacci heap is.C++ already has one, priority_queue.

Binary Search Tree (BST)

A binary search tree (BST) is a binary rooted tree that every node has a value, and for each node, the value of every node in its left child's subtree is less than its value and the value of every node in its right child's subtree is greater than that. Usually we perform some queries on BSTs, like inserting, deleting, asking and



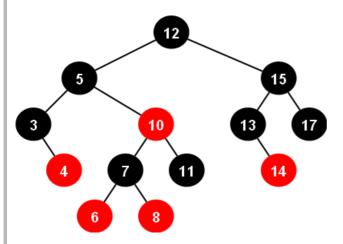
Binary search trees are too useful.

Red-black trees

A red-black tree is a kind of BST that after each query, BST will be balanced in such a way that it's height remains O(log(n)).

C++ already has a red-black tree inside, set

You can read about them in C++ references.



Unfortunately, set has not any function to find the k - th smallest minimum or find the index of an element, bust there is a data structure in C++ with does it in O(log(n))(also contains all set functions), tree:

```
#include<bits/stdc++.h>
#include<ext/pb_ds/assoc_container.hpp>
#include<ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
using namespace std;
template <typename T>
using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
tree_order_statistics_node_update>;
int main(){
        ordered_set<int> s;
        s.insert(1);
        s.insert(3);
        cout << s.order_of_key(2) << endl; // the number of elements in the s</pre>
Less than 2
        cout << *s.find_by_order(0) << endl; // print the 0-th smallest number</pre>
in s(0-based)
(Thanks to Swift for syntax using!)
This works even in C++ 98!
```

SQRT Decomposition

You can read more about it, just google sgi STL.

Suppose we have an array $a_1, a_2, ..., a_n$ and $k = \sqrt{n}$. We partition this array into k pieces each containing k elements of a.

Doing this, we can do a lot of things in $O(\sqrt{n})$. Usually we use them in the problems with modify and ask queries.

Problems: Holes, DZY Loves Colors, RMQ (range minimum query) problem

Sparse Table

The main problem that we can solve is RMQ problem, we have an array $a_1, a_2, ..., a_n$ and some queries. Each query gives you numbers l and r ($l \le r$) and you should print the value of $min(a_l, a_{l+1}, ..., a_r)$.

Solving using Sparse Table : For each i that $1 \le i \le n$ and for each j that $0 \le j$ and $i+2^j-1 \le n$, we keep the value of $min(a_i,a_{i+1},...,a_{i+2^j-1})$ in st[i][j] (preprocess) : (code is 0-based)

And then for each query, first of all, find the maximum x such that $2^x \le r - l + 1$ and answer is $min(st[l][x], st[r - 2^x + 1][x])$.

So, the main idea of Sparse Table, is to keep the value for each interval of length 2^k (for each k).

You can use the same idea for LCA problem and so many other problems.

So preprocess will be in O(n.log(n)) and query will be in O(1)

Problems: Strip, GCDSSQ, LCM Query.

Heavy light decomposition

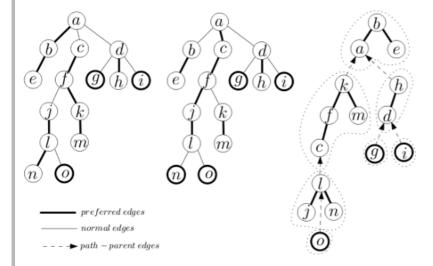
Heavy light decomposition is a way to partition a tree's vertices (or edges) in a good way.

In this kind of decomposition, we have some chains, and each vertex belongs to only one chain.

If vertex v is the parent of u size_of_subtree_of(v)/2 < size_of_subtree_of(u), u and v are in a chain and we call the edge uv, heavy, otherwise light.

There is at most one such child for each vertex v. If we consider the path from any vertex v to the root, there will be at most log(n) light edges there (go from v to the root, every time we see a light edge, size of subtree will be at least doubled). So, the number of chains on the way = O(log(n)).

In each of these chains, we can contain a container or another data structure like segment tree or etc.



Problem: GRASS PLANTING

Fenwick

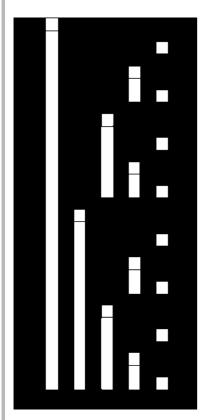
Suppose that we have n elements numbered from 1 to n.

Fenwick or BIT(Binary Indexed Tree) is a data structure with n nodes that node number i has some information about elements in the interval (i - i & -i, i].

Actually, you don't need to know what each node contains. The only thing you should know, it this (then you can change and convert it):

We have an array $a_1, a_2, ..., a_n$ and all of them are initially 0. We are gives some queries, 1.increase a_p by val and print $a_1+a_2+...+a_p$.

Only thing you should know is that how to solve this problem using Fenwick (and then you can change it and solve so many problems).



We perform each query in O(log(n)). Code : (1-based)

Please note that it should be **1-based**. It can't be done 0-based.

Problems: Inversions, Pashmak and Parmida's problem, BST.

Segment tree

We have an array of elements and some queries on intervals. So, we will be glad if we can split this interval to O(log(n)) intervals that we have actually some information about them.

Segment tree does that for you. Segment tree is a tree that each of it's nodes belongs to an interval.

Root of the tree belongs to the interval [0, n) (0-based).

Each node, has 0 or two children. Left and right. If a node's interval is [l,r) and $l+1\neq r$, the interval of its children will be [l,mid) and [mid,r) in order where $mid=\frac{l+r}{2}$, so the height of this tree will be $O(\log(n))$.



Each node has an index, we consider that root has index 1 and the children of a vertex x will have indices 2x and 2x+1 in order.

Segment tree is the most useful data structure and every problem solvable by Fenwick is also solvable by Segment tree.

If the size of the root's interval is n, segment tree could have up to 4n nodes.

To split an interval to some nodes of this tree, we will act like this:

Suppose that S is the set of nodes which their union is [x,y) and no two different nodes in S have nonempty intersection.

A node i with interval [l,r) is in S if and only if $x \le l \le r \le y$ and if it has a parent with interval [b,e), x > l or r > y.

```
C++ code:
```

Example:

We have an array $a_1, a_2, ..., a_n$ and q queries. There are 2 types of queries.

- 1. S l r, Print $a_l, a_{l+1}, ..., a_r$
- 2. Mp x, Modify a_p to x, it means $a_p = x$.

First of all we need to build the segment tree, for each node we keep the sum of its interval, for node i we call it s[i], so we should build the initial segment tree.

So, before reading the queries, we should call build() .

```
Modify function:
void modify(int p,int x,int id = 1,int l = 0,int r = n){
        s[id] += x - a[p];
                                l = r - 1 = p
        if(r - 1 < 2){ //
                 a[p] = x;
                 return ;
        }
        int mid = (1 + r)/2;
        if(p < mid)</pre>
                 modify(p, x, id * 2, 1, mid);
        else
                 modify(p, x, id * 2 + 1, mid, r);
}
(We should call modify(p, x))
Ask for sum function:
int sum(int x,int y,int id = 1,int l = 0,int r = n){
        if(x >= r or 1 >= y) return 0;
        if(x <= 1 && r <= y)     return s[id];</pre>
        int mid = (1+r)/2;
        return sum(x, y, id * 2, 1, mid) +
                sum(x, y, id * 2 + 1, mid, r);
}
(We should call sum(l, r))
Lazy propagation
Imagine we have updates on intervals, what should we do?
Example:
We have an array a_1, a_2, ..., a_n and q queries. There are 2 types of queries.
 1. S l r, Print a_l, a_{l+1}, ..., a_r
 2. I l r x, for each i such that l \le i \le r, increase a_i by x.
We shouldn't update all the nodes in this interval, just the maximal ones, then pass it to
children when we need. This trick is called Lazy Propagation, so we should have another
array lazy (for nodes) which are initially 0 and every time we want to perform increase query,
increase lazy[id] with x.
As above, we also should have an array s for nodes.
So, build function will be same as above. But we need some more functions :
A function to update a node:
void upd(int id,int 1,int r,int x){// increase all members in this interval
by x
        lazy[id] += x;
        s[id] += (r - 1) * x;
A function to pass the update information to its children:
void shift(int id,int 1,int r){//pass update information to the children
        int mid = (1+r)/2;
        upd(id * 2, 1, mid, lazy[id]);
        upd(id * 2 + 1, mid, r, lazy[id]);
        lazy[id] = 0;// passing is done
}
```

A function to perform increase queries :

```
void increase(int x,int y,int v,int id = 1,int l = 0,int r = n){
        if(x >= r or 1 >= y)
                                return ;
        if(x <= 1 && r <= y){
                upd(id, 1, r, v);
                return ;
        shift(id, l, r);
        int mid = (1+r)/2;
        increase(x, y, v, id * 2, 1, mid);
        increase(x, y, v, id*2+1, mid, r);
        s[id] = s[id * 2] + s[id * 2 + 1];
}
(We should call increase(l r x))
A function to answer to queries asking about the sum:
int sum(int x,int y,int id = 1,int l = 0,int r = n){
        if(x >= r or 1 >= y) return 0;
                              return s[id];
        if(x <= 1 && r <= y)
        shift(id, l, r);
        int mid = (1+r)/2;
        return sum(x, y, id * 2, 1, mid) +
               sum(x, y, id * 2 + 1, mid, r);
}
```

(We should call sum(l, r))

Problems: GSS1, GSS3, MULTQ3, DQUERY, KQUERY, POSTERS, PATULJCI, New Year Domino, Copying Data, DZY Loves Fibonacci Numbers, FRBSUM

Persistent data structures

Consider we have some elements, you perform some updates on it and then, and after performing all of them, you want to have the information about the elements, after each update.

For this propose, you got a data structure and somehow, you save the version of that data structure.

The most useful data structure for this propose is segment tree, I will explain persistent segment tree and all other data structures (like Fenwick) are like that.

Persistent segment tree

Example problem :

We have an array $a_1, a_2, ..., a_n$ and at first q update queries and then u ask queries which you have to answer online.

Each update query gives you numbers p and v and asks you to increase a_p by v .

Each ask query, gives you three numbers i and x and y and asks you to print the value of $a_x + a_{x+1} + ... + a_y$ after performing i - th query.

Each update query, changes the value of O(log(n)) nodes in the segment tree, so you should keep rest of nodes (not containing p) and create log(n) new nodes. Totally, you need to have q.log(n) nodes. So, you can not use normal segment's indexing, you should keep the index of children in the arrays L and R.

If you update a node, you should assign a new index to its interval (for i - th query).

You should keep an array root[q] which gives you the index of the interval of the root ([0, n)) after performing each query and a number ir = 0 which is its index in the initial segment tree

```
(ans of course, an array s[MAX_{NODES}] which is the sum of elements in that node). Also you
should have a NEXT_FREE_INDEX = 1 which is always the next free index for a node.
First of all, you need to build the initial segment tree :
(In these codes, all arrays and queries are 0-based)
void build(int id = ir,int l = 0,int r = n){
        if(r - 1 < 2){
                 s[id] = a[1];
                 return ;
        }
        int mid = (1+r)/2;
        L[id] = NEXT_FREE_INDEX ++;
        R[id] = NEXT_FREE_INDEX ++;
        build(L[id], 1, mid);
        build(R[id], mid, r);
        s[id] = s[L[id]] + s[R[id]];
}
(So, we should call build())
Update function: (its return value, is the index of the interval in the new version of segment
tree and id is the index of old one)
int upd(int p, int v,int id,int l = 0,int r = n){
        int ID = NEXT_FREE_INDEX ++; // index of the node in new version of
segment tree
        if(r - 1 < 2){
                 s[ID] = (a[p] += v);
                 return ID;
        }
        int mid = (1+r)/2;
        L[ID] = L[id], R[ID] = R[id]; // in case of not updating the interval
of left child or right child
        if(p < mid)</pre>
                 L[ID] = upd(p, v, L[ID], l, mid);
        else
                 R[ID] = upd(p, v, R[ID], mid, r);
        return ID;
}
(For the first query (with index 0) we should run root[0] = upd(p, v, ir) and for the rest of
them, for j - th query se should run root[j] = upd(p, v, root[j-1]))
Function for ask queries:
int sum(int x,int y,int id,int l = 0,int r = n){
        if(x >= r or 1 >= y)
                                return 0;
        if(x <= 1 && r <= y)
                                 return s[id];
        int mid = (1+r)/2;
        return sum(x, y, L[id], 1, mid) +
                sum(x, y, R[id], mid, r);
(So, we should print the value of sum(x, y, root[i]))
Problems: Sign on Fence, MKTHNUM, COT, The Classic Problem
```

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thanks:)

Majid

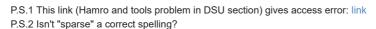
5 years ago, <u>#</u> |

← Rev. 3 **+27** ▼



Thanks for the article, especially for problems!

I didn't know that priority_queue is a Fibonacci heap. BTW, are you sure? cplusplus.com and cppreference say that push() works in logarithmic time.



→ Reply



4 years ago, <u>#</u> <u>^</u> |

A +3 V

As he said, you have to register youself in the ACM-OI group.











→ <u>Reply</u>







atique

@PrinceOfPersia, thanks for the great article. Do you have any other article on Fibonacci Heap, do you mind extending on the topic a bit with details such as inner working and implement of fibonacci heap?

→ <u>Reply</u>



<u></u> 0 🔻

Great intro. Still have 1 question. Does order_set works only in g++? How it is going to work in Visual C++?

→ <u>Reply</u>



5 years ago, # ^ |

▲ 0 ▼

 $Does\ order_set\ works\ only\ in\ g++$

Yes. It's part of SGI STL extensions of G++.



adamant

5 years ago, # | **+16**

Btw, tree isn't part of C++ standard, it is extension of GNU C++. You can read more about this data structures here and here:)

Also about persistent data structures. One can be interested in this: #TphcLk (k-th order statistics in the array segment using persistent bit trie. $O(n \log C)$. Fully online, works with negative numbers also!)

Also you can use this structure to answer all queries from this problem.

→ <u>Reply</u>



5 years ago, # <u>^</u> |

How to apply your code to the XOR query please?

speedy03



- 10

5 years ago, # <u>^</u> |

My full solution of Xor Queries: #QI8sxL

Xor query can be done greedy — we iterate through implicit bit trie of l..r subsegment and each time we try to take k-th bit in answer which is not equal to k-th bit in query.

 $\rightarrow \underline{\mathsf{Reply}}$



speedv03

Got it, thanks! The official solution is also based on trie. Any specific advantages over segment tree?

— Reply.



5 years ago, # <u>^</u> | ______ |

Actually segment tree is a kind of trie...

Trie just a bit more generic

→ <u>Rep</u>



edogrigqv2

5 years ago, <u>#</u> |

△ 0 ▼

▲ +1 ▼

△ 0 ▼

The is probably mistake in DSU implementation. par[x] += par[y]??? What is this ?

 $\rightarrow Reply$

5 years ago, # \triangle | Read it!



In the code above, for each root v, par[v] equals the negative of number of tools in that box.

So, par[x] = -sizeofbox(x), par[y] = -sizeofbox(y). so, par[x] + par[y] = -sizeofbox(x unuion y).

→ Reply



5 years ago, <u>#</u> <u>↑</u> |

<u></u> 0 🔻

Have I understood it correct now? par[v] shows the parent of v, if v is not the root, otherwise it shows negative number of nodes in group. 2 in 1 array!!!

 $\rightarrow \underline{\mathsf{Reply}}$



Yep!

→ Reply

5 years ago, # <u>^</u> |

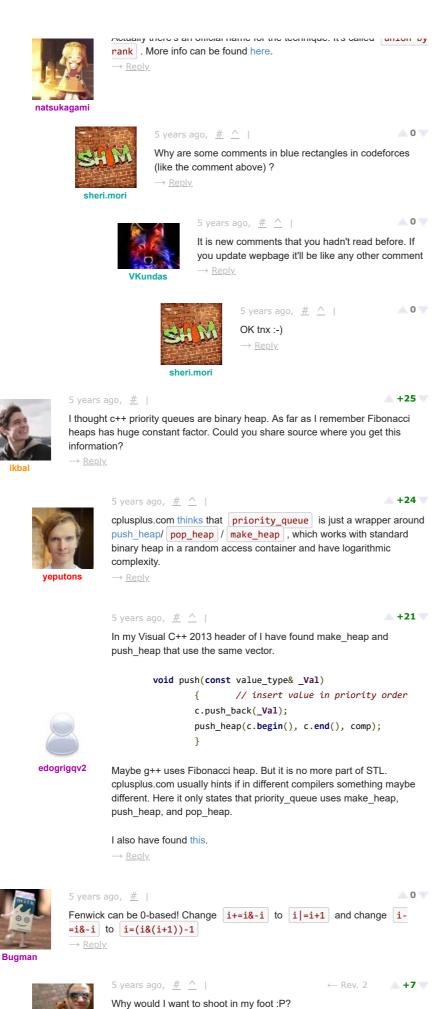
Yep!

DarthKnight

5 years ago, <u>#</u> ^ |

<u></u> 0 🔻

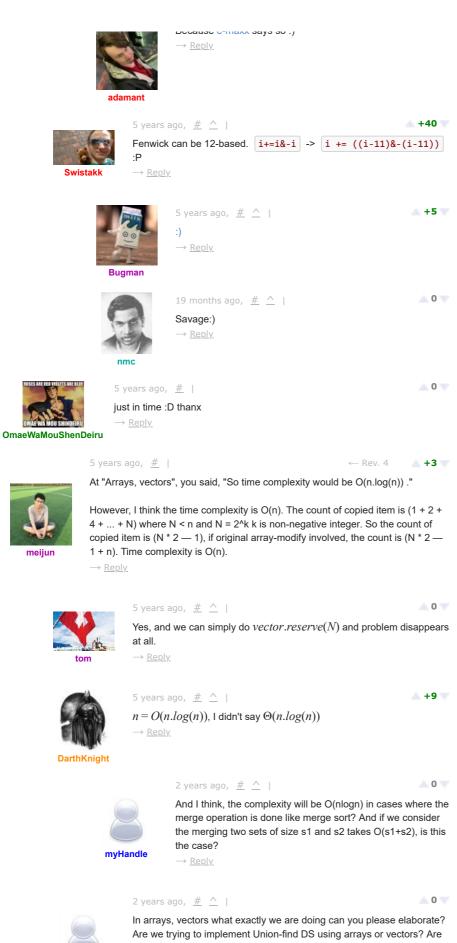
<u></u> 0 🔻



Swistakk

5 years ago, # ^ |

△ 0 ▼





we using a vector at each index? So that at max each vertex has to placed O(logn) times? Thank you.

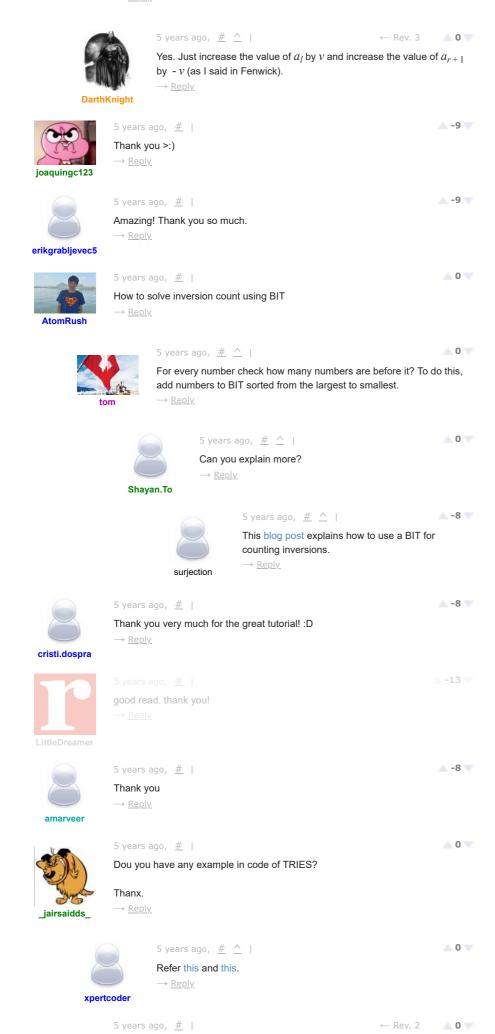
→ <u>Reply</u>

5 years ago, <u>#</u> |



In case 2 of partial sum, can you apply your formula to binary index tree if sum

within the range [I,r] is queried?







```
5 years ago, <u>#</u> |
```

Nice blog/tutorial.. it would be useful for beginners as they will get an idea of what all to study.... Would have been nice if something like this was there when I started...

<u></u> 0 🔻

← Rev. 2 **△ 0** ▼

△ 0 ▼

→ Reply



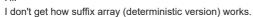
vaishious

A -8 V 5 years ago, <u>#</u> |

Good stuff. Cheers



Hi!



Could you please give me some more clear description about it?

What does "tmp" store? It seems it contains something like [0,1,...,N-1], doesn't it?!

What about "pos"?

What's the initialization of "tmp"?

Thanks...

→ Reply



```
5 years ago, <u>#</u> <u>^</u> |
```





```
5 years ago, <u>#</u> |
http://codeforces.com/blog/entry/16541
→ Reply
```

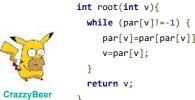
sazzad8867

```
← Rev. 3
                                                               △ 0 ▼
5 years ago, # |
```

Another problem of partial sum http://codeforces.com/problemset/problem/433/B \rightarrow Reply

5 years ago, <u>#</u> | ← Rev. 11 **△** 0 ▼

Speaking of DSU, here's the same function, but in a more understandable way.



par[v]=par[par[v]];

UPD: This is a way to compress paths, but not as efficient as the presented algorithm.

→ <u>Reply</u>



```
5 years ago, # ^ |
```

If you observe carefully, the code actually does update all the nodes in

the path which is what you want to do.



```
<u></u> 0 🔻
5 years ago, <u>#</u> <u>^</u> |
```

be the root but in crazzybeer's code it doesnt work also there is a closed bracket which leads to infinite loop

→ <u>Reply</u>



5 years ago, <u>#</u> <u>^</u> |

▲ 0 ▼

 $\label{thm:model} \begin{tabular}{ll} Mistake fixed. Now it should work. (Actually, this is the algorithm from Coursera so it works pretty well) \end{tabular}$

 $\rightarrow Repl$



CrazzyBeer

5 years ago, <u>#</u> <u>^</u> |

▲ 0 ▼

It works, but, I guess, it does a bit less work than the presented algorithm.

 $\rightarrow \underline{\mathsf{Reply}}$



5 years ago, # \wedge |

▲ 0 ▼



I see now. Thanks.

→ <u>Reply</u>

CrazzyBeer



<u></u> 0 🔻

Do you actually want to express this idea?



aaa2333333



5 years ago, $\underline{\#}$ |

△ 0 ▼

Bookmarked! Thanks for this tutorial! :)

 $\rightarrow \underline{\mathsf{Reply}}$



40

5 years ago, # |

Thank you for this Useful toturial.

ightarrow Rep



5 years ago, <u>#</u> |

△ 0 ▼

What does the modify(p, x) function do in the Segment tree section ?

→ <u>Reply</u>

suraj021



5 years ago, <u>#</u> <u>^</u> |

△ 0 ▼

"Modify a_p to x, it means $a_p = x$."

→ <u>Reply</u>



Thank

5 years ago, $\underline{\#}$ $\underline{\land}$ |

Thanks





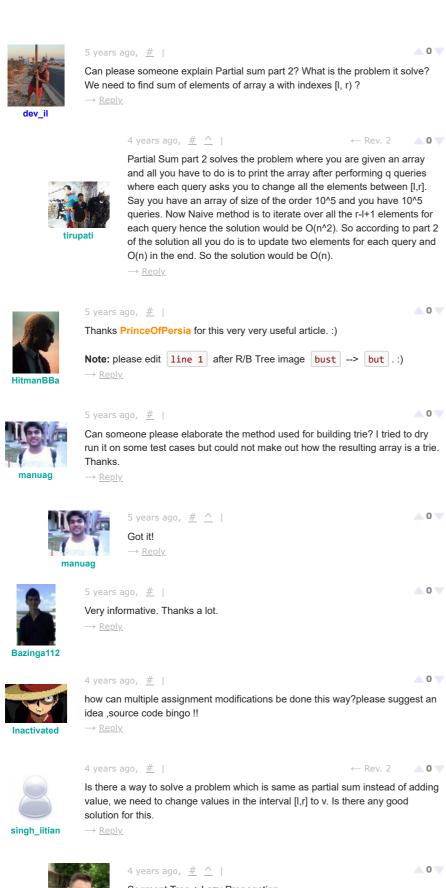
years ago, #

▲ 0 ▼

<u></u> 0 🔻

"The only thing you should know, it this (then you can change and convert it):" I think "it" has to be "is",right?

 $ightarrow ext{Reply}$ sheri.mori





Segment Tree + Lazy Propagation

slycelote

A +13 V 4 years ago, # ^ |

Astrologers proclaimed the Week of CodeChef Challenge. Amount of similar questions doubled. → Reply

A 0 V

In The persistent data structure function we should have a slidl = sll lidll + slRlidll: hefore the return statement



```
4 years ago, <u>#</u> |
```

→ Reply

A 0 V



If the size of the root's interval is n, segment tree could have up to 4n nodes. How can we justify it? When I constructed an example, I got 2n-1 nodes. In what cases it will have 4n nodes.

→ Reply

```
4 years ago, \# \triangle | \leftarrow Rev. 4 \triangle +3 \triangledown
```

Sorry, I didn't explain well in the previous post.

apaj - appiaj i apapaj, poloto ino totam atatement

First, interval tree is balanced binary tree. So first level has 1 node, second 2, third 4... i-th level has 2^(i-1) nodes.



If your interval has lenght n, you must add some extra elements till n is not a power of two (condition for balanced tree). Now the last level has m nodes (m=2^k) and higer levels have 2^(k-1) nodes, 2^(k-2) nodes... Sum of all nodes is 2^(k+1)-1. That is equal with 2m -1 nodes. The worst case is when n=2^x+1 and in that case you should have about 4n nodes, in best case if n=2^x you will have 2n-1 nodes.

I hope that now everything is clear.

 \rightarrow Reply



thank you for this useful algorithms.

is there any other posts like this?

 $\rightarrow Reply$



4 years ago, <u>#</u> |

<u></u> 0 Ψ

in Lazy propagation you had a function shift and function update.

what if we compare them?

like this:

```
inline void add(int st,int en,int v,int l=0,int r=n,int node=1){
  s[node]+=v*(en-st);
  if(l+1==r)
     return;
  else if(st>=mid(l,r))
     add(st,en,v,mid(1,r),r,(node<<1)+1);</pre>
  else if(en<=mid(l,r))</pre>
     add(st,en,v,l,mid(l,r),node<<1);</pre>
  else
add(st,mid(l,r),v,l,mid(l,r),node<<1),add(mid(l,r),en,v,mid(l,r),r,
(node<<1)+1);
}
and this is sum function:
#define mid(x,y) (x+y)/2
inline int sum(int st,int en,int l=0,int r=n,int node=1){
  if(l==st && r==en)
     return s[node];
  if(st>=mid(l,r))
     return sum(st,en,mid(l,r),r,(node<<1)+1);</pre>
  if(en \le mid(l,r))
     return sum(st,en,1,mid(1,r),node<<1);</pre>
  return
\mathsf{sum}(\mathsf{st},\mathsf{mid}(\mathsf{l},\mathsf{r}),\mathsf{l},\mathsf{mid}(\mathsf{l},\mathsf{r}),\mathsf{node} \mathord{<\!\!\cdot} 1) + \mathsf{sum}(\mathsf{mid}(\mathsf{l},\mathsf{r}),\mathsf{en},\mathsf{mid}(\mathsf{l},\mathsf{r}),\mathsf{r},
```

```
(HOUESSI)TI)
}
→ Reply
4 years ago, <u>#</u> |
                                                      ← Rev. 2 △ 0 ▼
```

In the given Trie code (as posted by PrinceOfPersia), It is only possible to search for prefix, How can we search if the word exist or not?



```
public boolean search(String word) {
        int v = 0;
        for(int i = 0; i < word.length(); i++) {</pre>
            v = x[v][word.charAt(i)];
            if(v == -1 )
                return false;
        }
        // THIS WON"T WORK
        return true;
    }
→ Reply
```

4 years ago, # ^ |



You can add a boolean array, call it something like ends and initialize it to false, for each word you insert you set ends to true only in the last character of the word, so in your search method change the "return true" line to "return ends[v]". If you insert the word partition, if you look for part, it will return false, instead of true (which is what your code is doing).

 \rightarrow Reply



4 years ago, # |

△ 0 ▼



Dipanker

In the upd() function in the persistent tree, S[ID] has not been updated after the recursive calls. Add s[ID] = S[L[ID]] + S[R[ID]]; before returning ID. Thank You for such a Useful tutorial!

4 years ago, <u>#</u> |

△ 0 ▼



You put this problem PATULJCI after explaining the segment tree with lazy propagation and before (Persistent).. but I can not solve it and my friend told me he solved it using (Persistent) segment tree!!!

could you please explain how to solve it without using Persistent ?!



DarthKnight

```
4 years ago, <u>#</u> <u>^</u> |
```

△ 0 ▼

I have no idea how to solve it with persistent!!!



4 years ago, # ^ | ← Rev. 2 ▲ +1 ▼ This code is my friend's solution (OmarHashim) using

persistent,

but i wanna know how to solve it without using persistent, could you please explain or give a hint on how to solve it?!!

→ <u>Reply</u>



▲ +1 ▼ 4 years ago, # ^ |

UPD I got a O(N log N) solution with no segment tree at all, thanks:)

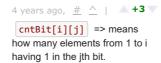
 \rightarrow Reply



A 0 V 4 years ago, <u>#</u> <u>^</u> |

anh1l1ator

FIGHO, GAIT YOU GAPIANT WHAT ARE YOU GOING , I have solved the problem using persistent segment tree(It was trivially a modification to MKTHNUM problem).



you can see it's easy to construct that table in O(nlogn) time.



then when I get query [L,R] I iterate throw bits and see if there is more than (R-L+1)/2 elements having this bit 1, if so I set it, when I done I have a number every bit in it exists in more than siz/2 elements. so it is easy to notice that either this is the answer or there is no answer at all, to check if it is the answer or not, I count how many occurrences of this number in the interval [L,R] using binary search.

△ 0 ▼

→ <u>Reply</u>



```
4 years ago, <u>#</u> |
why adding -1 to i + (1 << (j-1)) in the code of sparse table?
```

→ Reply

```
<u></u> 0 🔻
4 years ago, <u>#</u> ^ |
```

I'll try to explain on small example.



Let's say that you have array of 10 elements, and you are on 3rd. If you want to increase 5 consecutive starting from position 3 you will have to increase elements on following positions: 3, 4, 5, 6, 7. You'd probably say 'ok, from 3 to 3+5=8', but that is not correct since 3 is considered to be one of these 5 consecutive elements.

Same is with sparse table. If you want to take 2^k consecutive elements starting from position i, last element is $i+2^k-1$ which is i+(1<< k)-1.

→ <u>Reply</u>

```
2 years ago, # ^ |
                                                                 △ 0 ▼
I believe it is an error. Let say i=4, j=1.
```

Thomas_94

```
st[i][j] = min(st[i][j-1], st[i + (1 << (j-1)) - 1][j-1]);
st[4][1] = min(st[4][0], st[4][0]);
```

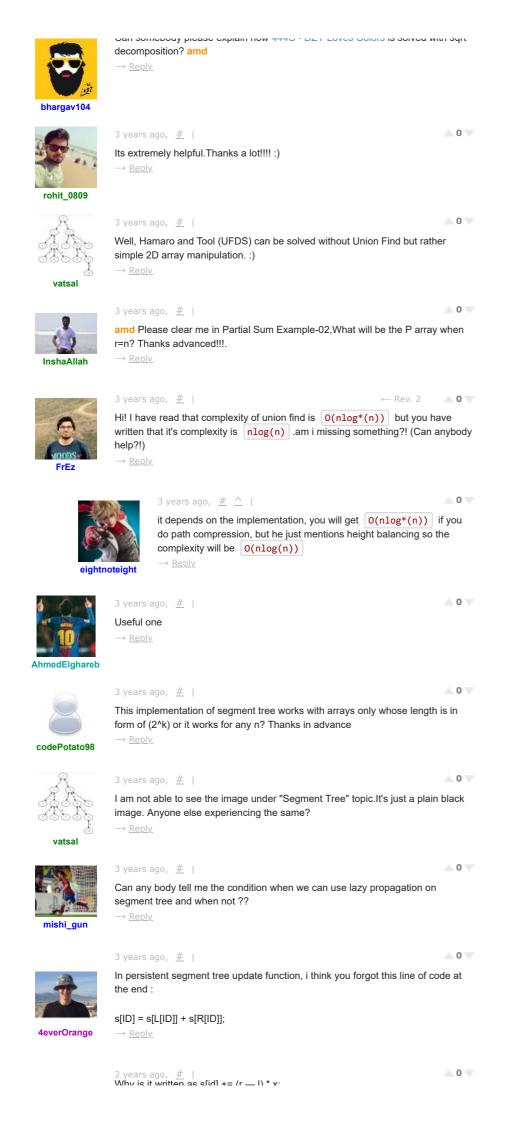
→ <u>Reply</u>

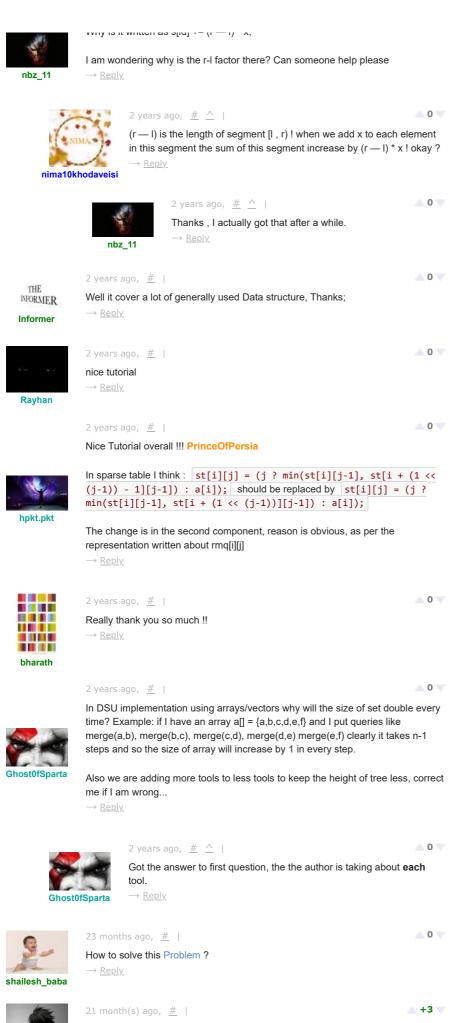


3 years ago, <u>#</u> | A +6 V wonderful toturial:) can u please write one about DP?

→ Reply







There should be this line in the end of the update function in persistence segment tree. s[ID] = s[L[ID]] + s[R[ID]]; $\rightarrow Reply$

Enigma27



brdy

```
21 month(s) ago, # |
```

http://www.usaco.org/index.php?page=viewproblem2&cpid=576

Prefix sums style range modification on trees

→ <u>Reply</u>

```
21 month(s) ago, # |
```

△ 0 ▼

△ 0 ▼

Is there somebody who knows if it's better to merge the DSUs by height instead of by size? I think the height is more important because I think the complexity of the operating "finding the root" has more to do with the height of the tree.

```
aaa2333333
```



In a control to the control

5 months ago, # $^{\wedge}$ |

△ 0 ▼

In a lot of questions, we need the size of the sets.

Hence for the template, i would personally prefer 'union by size' over 'union by rank'.

 \rightarrow Reply



- 6- - - 0 - - -

← Rev. 2 **▲ -11**

after 3 years,now its 2018,and this blog is still read by many...thank you **DarthPrince**

→ Reply



Dobul

17 months ago, # |

△ 0 ▼

Thank you so much for this useful tutorial. Especially that DSU implementation — In the code above, for each root v, par[v] equals the negative of the number of tools in that box., love the way the how par doubles as the size/rank array, requiring only one array. Saved it as one of my snippets:)

 $\rightarrow \underline{\mathsf{Repl}}_{\mathsf{y}}$



harrypotter0

14 months ago, # |

_ 0 ▼

@DarthPrince Could you provide your implementation(code) of segment tree for a few problems as I loved this code by ou and finding it real challenge to find a similar implementation for solving a problem. Thanks in advance:)

 \rightarrow Reply

12 months ago, # |

_ 0 _

OFBEING CHUTTA IS A

Hi there, I am trying to solve this problem with sparse table, I am getting TLE on

this problem.

Here is what I tried. Can soneone solve this problem with sparse table

arrypotter0 Thanks in advance.

manks in advance

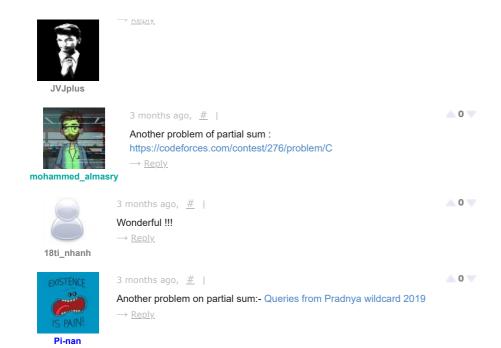
→ <u>Reply</u>

12 months ago, # |

← Rev. 2

△ 0 ▼

@DarthPrince There is a typo mistake in the example of segment tree, it should be S I r, Sum (al, al + 1, ..., ar) instead of S I r, Print (al, al + 1, ..., ar).



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The only programming contests Web 2.0 platform
Server time: Dec/19/2019 11:22:09^{UTC+5.5} (h1).
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