



$$\theta_1 + \frac{\pi}{2} - \phi_1 + \phi_2 - \phi_3 = \theta_2 + \frac{\pi}{2}$$

$$\phi_1 + \phi_3 = \theta_1 - \theta_2 + \phi_2$$

$$\phi_1 + \phi_2 + \phi_3 = 2\phi_2 + \theta_1 - \theta_2$$

$$\frac{\partial L_{RLR}}{\partial \theta_1} = 2\rho \frac{\partial \phi_2}{\partial \theta_1} + \rho$$

$$\frac{\partial L_{RLR}}{\partial \theta_2} = 2\rho \frac{\partial \phi_2}{\partial \theta_2} - \rho$$

$$2\pi - \phi_2 = \pi - 2\alpha$$

$$\frac{\partial L_{RLR}}{\partial \theta_1} = 4\rho \frac{\partial \alpha}{\partial \theta_1} + \rho$$

$$\alpha = \cos^{-1} \left(\frac{\|C_1 C_3\|}{4\rho} \right)$$

$$= \cos^{-1} \left(\frac{\sqrt{l_x^2 + l_y^2}}{4\rho} \right)$$

$$l_x = O_1^x + (r_t + \rho) \cos \theta_1 - O_2^x - (r_t + \rho) \cos \theta_2$$

$$l_y = O_1^y + (r_t + \rho) \sin \theta_1 - O_2^y - (r_t + \rho) \sin \theta_2$$

$$\frac{\partial \alpha}{\partial \theta_1} = -\frac{1}{\sin \alpha} \frac{1}{4\rho} \frac{1}{2\sqrt{l_x^2 + l_y^2}} \left(-2 l_x (r_t + \rho) \sin \theta_1 \right. \\ \left. + 2 l_y (r_t + \rho) \cos \theta_1 \right)$$

$$= -\frac{(r_t + p)}{4p \sin \alpha} \left(-\frac{dx}{\sqrt{l_x^2 + l_y^2}} \sin \theta_1 + \frac{l_y}{\sqrt{l_x^2 + l_y^2}} \cos \theta_1 \right)$$

$$= -\frac{r_t + p}{4p \sin \alpha} \left(-\sin \theta_1 \cos \beta + \sin \beta \cos \theta_1 \right)$$

$$= -\frac{r_t + p}{4p \sin \alpha} \sin(\beta - \theta_1)$$

$$\frac{\partial L_{LR}}{\partial \theta_1} = -\frac{(r_t + p) \sin(\beta - \theta_1)}{\sin \alpha} + p$$

This derivative is zero when
line connecting inflexion points is
collinear with center of arc.