

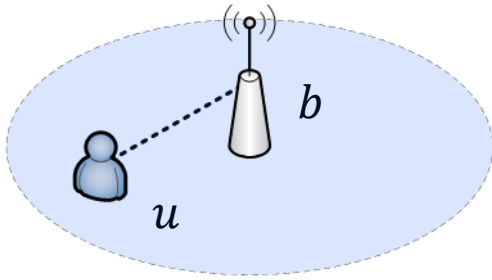
# HR- $k$ ESP: A Heuristic Algorithm for Robustness-Oriented $k$ Edge Server Placement

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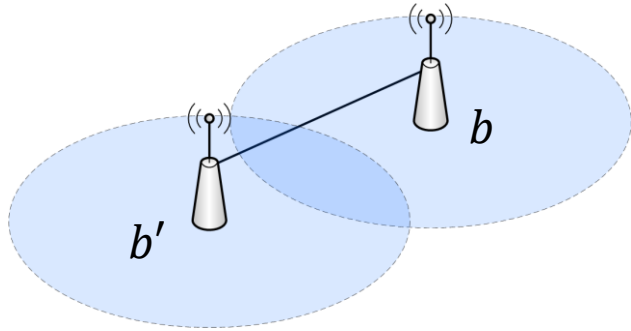
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The  $k$  Edge server placement ( **$k$ ESP**) problem is to select  $k$  suitable base stations as the server deployment locations in a given mobile network.

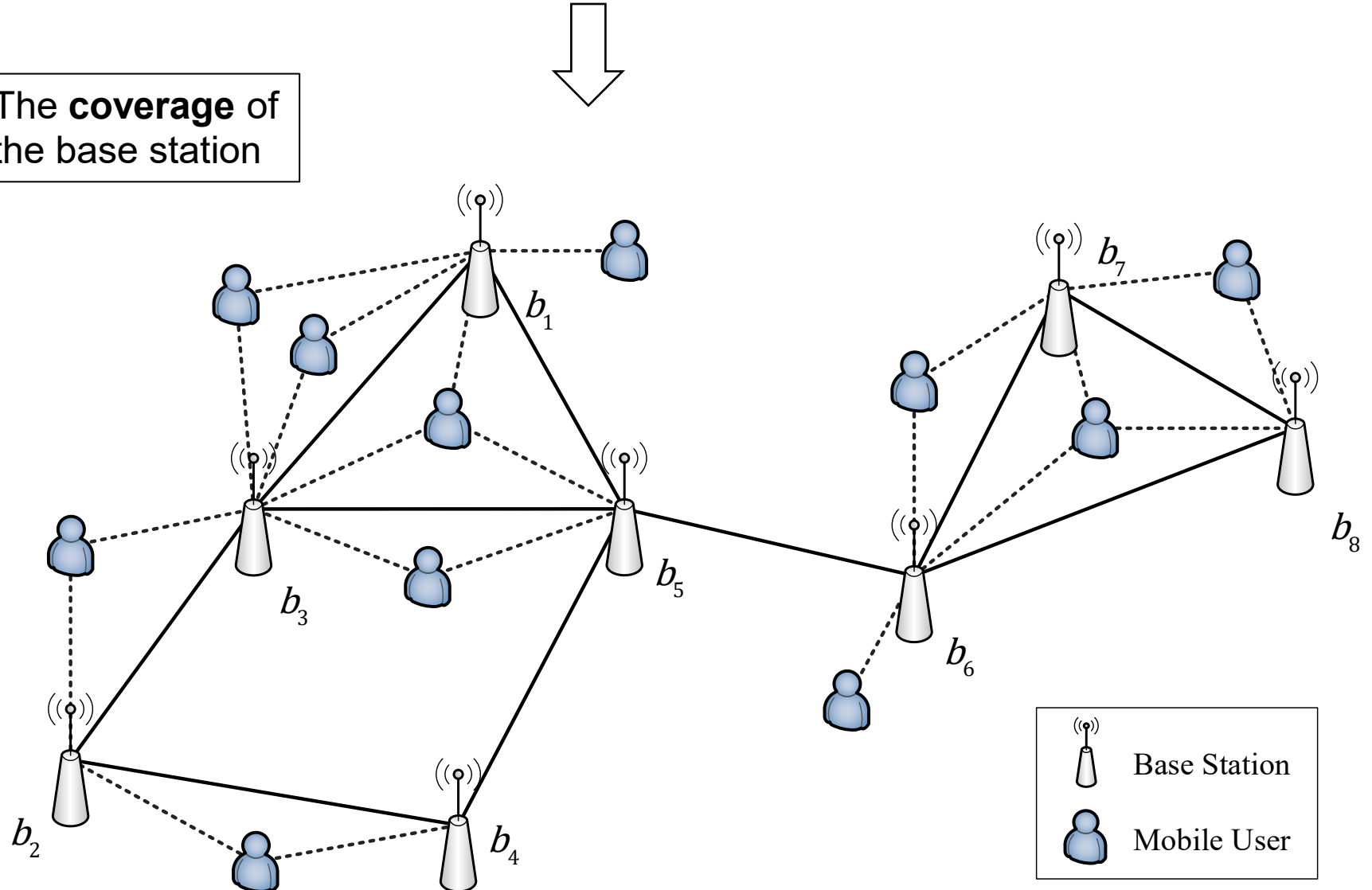


The **coverage** of the base station

The accessing relationship between a **user** and a **base station**.



The accessing relationship between **two base station**.



The **Robustness-Oriented**  $k$  ESP is to construct a edge server network to achieve the following two objective:

- More **user coverage**
- Higher anti-failure capability of network (network **robustness**)

**Network robustness** can be defined as the capability of the server network to **maintain the original quality of service (Qos)** in the face of sudden failures.

- The server network can operate steadily at **close to the theoretical best performance**
- Avoid high economic losses and network maintenance costs

There is a robustness-oriented  $k$ ESP solution (server deployment scheme  $\mathbf{p}$ ).

Server budget:  $k = 4$

User coverage: **10**

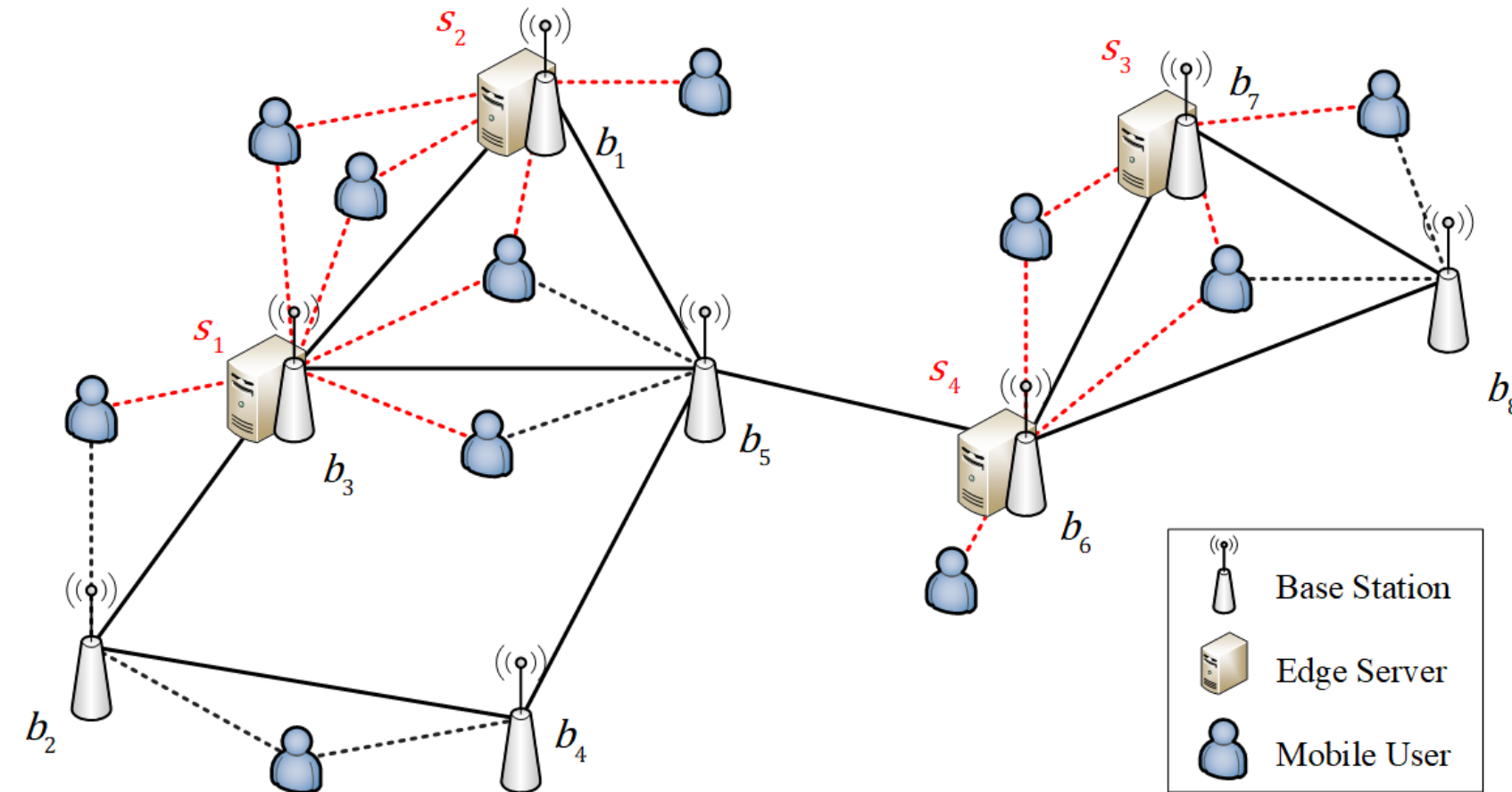
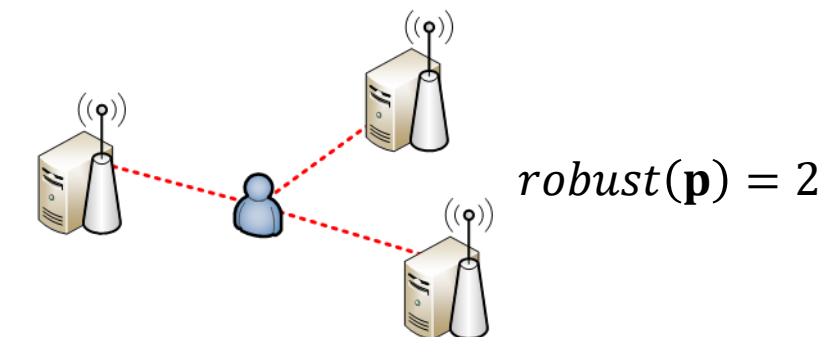
Deployment scheme:  $\{b_1, b_3, b_6, b_7\}$

Network robustness: **5**

**User Coverage**  $\text{coverage}(\mathbf{p})$  is the number of users served by edge servers



**Network Robustness**  $\text{robust}(\mathbf{p})$  is the number of times which the users are repeatedly served by edge servers.



For the  $k$ ESP solution  $\mathbf{p} = \{p_1, p_2, \dots, p_m\}$  ( $m$  is the number of base station). The **robustness-oriented**  $k$  edge server placement problem can be formulated as follows:

$$\text{maximize } CR(\mathbf{p}) = \sqrt{\omega_c \cdot (\text{coverage}(\mathbf{p}))^2 + \omega_r \cdot (\text{robust}(\mathbf{p}))^2}$$

while satisfying the following constraints:

$$\omega_c = \omega_r = 0.5$$

$$p_i \in \{0,1\}$$

Each base station has two states whether it deploys servers ( $p_i = 1$ ) or not ( $p_i = 0$ ).

$$\sum_{i=1}^m p_i = k$$

And the number of servers is equal to the server budget  $k$ .

## The Main Contributions:

- A **Heuristic** algorithm for **Robustness-oriented  $k$  Edge Server Placement** named **HR- $k$ ESP** is proposed to effectively solve the  $k$ ESP considering user coverage and network robustness
- A **simulation-based evaluation method** for the **network robustness** is proposed. After simulating the failure randomly, the network robustness is evaluated by the variation of the network performance (User Survival Rate).
- Intensive experiments are conducted on the widely-used EUA dataset<sup>1</sup> by considering various application scenarios, and the results indicate that HR- $k$ ESP **outperforms other representative algorithms in most cases.**

1. Lai, P., He, Q., Abdelrazek, M., et al.: Optimal edge user allocation in edge computing with variable sized vector bin packing. In: Proceedings of the 16th International Conference on Service-Oriented Computing (ICSOC 2018), pp. 230-245. (2018)

# The main thought of HR- $k$ ESP

The distribution of **service requirements** is **very similar** to the distribution of **users** and **base stations**

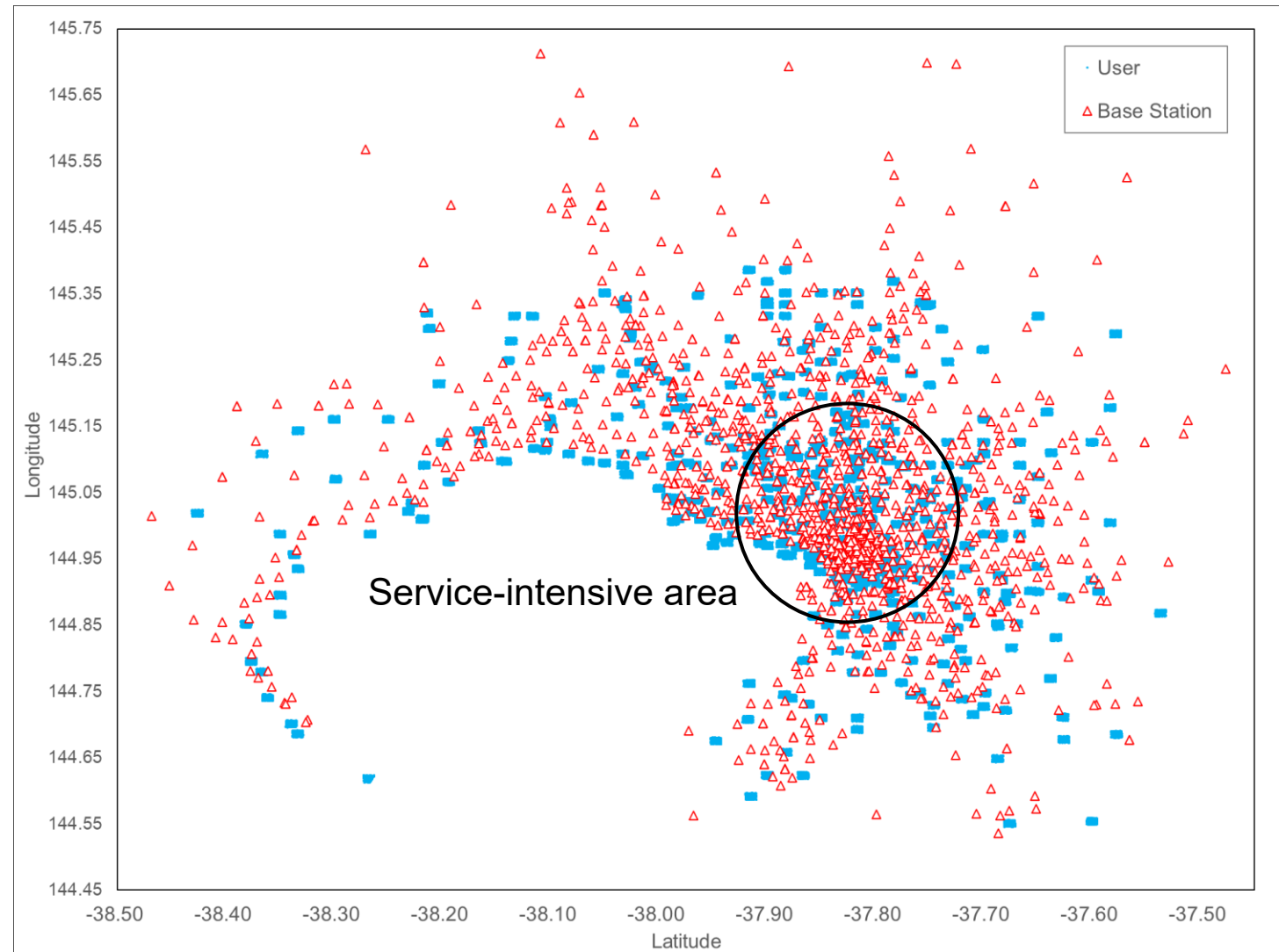
## The basic idea:

The server deployment scheme is **expanded gradually** from the **service-intensive area** to the **service-dispersive area**.

## The step of the HR- $k$ ESP<sub>0</sub> (basic version):

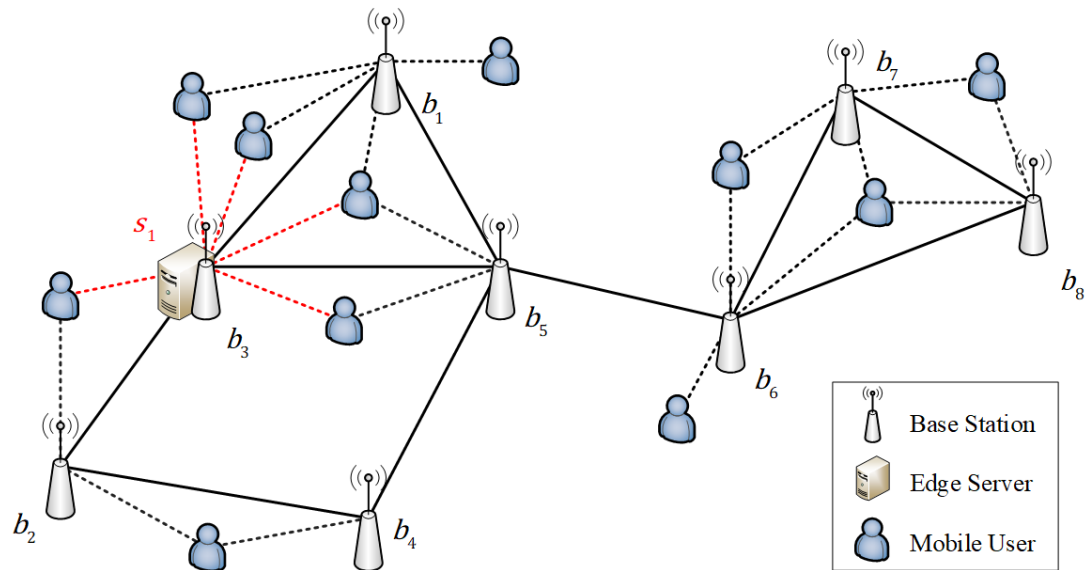
1. Select the **most service-intensive** base station as the starting point of the server deployment scheme.
2. Evaluate the neighbors of selected base station, and the one with the **largest robustness increment** is selected to expand the server deployment scheme.
3. Repeat step 2 until the number of servers reaches the budget.

Heuristic Information: **Robustness Increment**

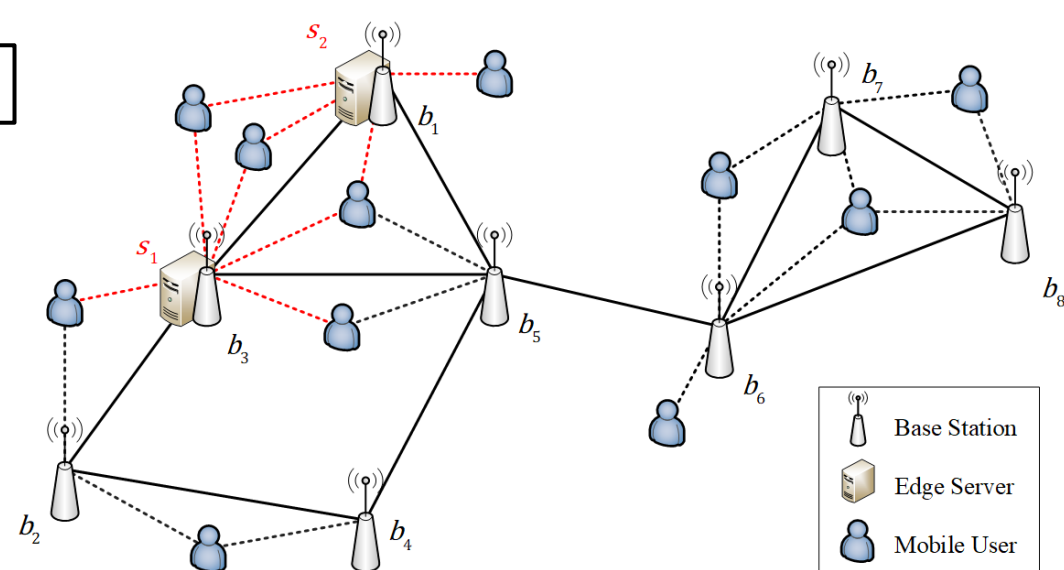


The distribution of users and base stations on the EUA dataset

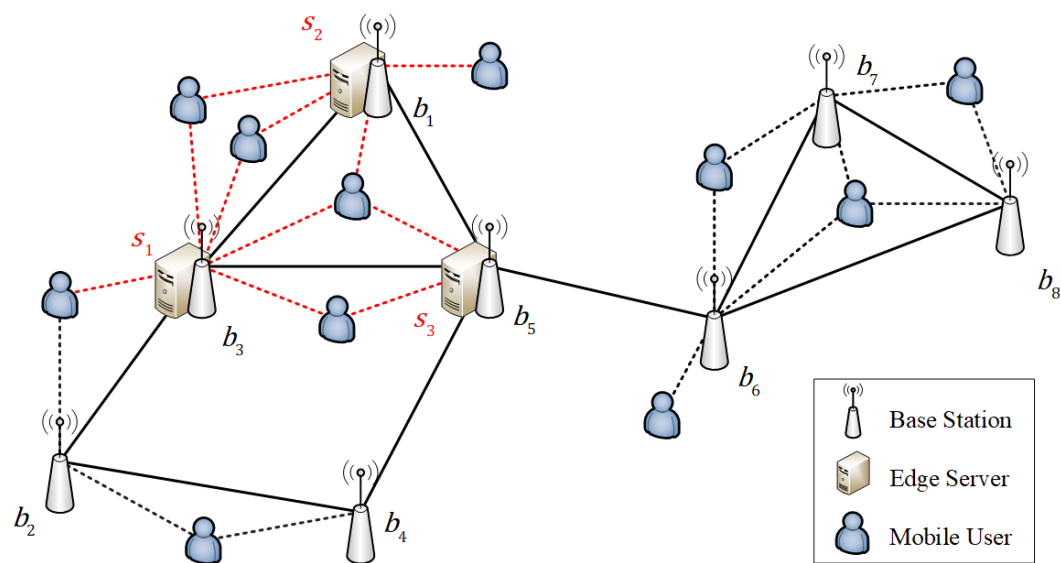
$k = 4$



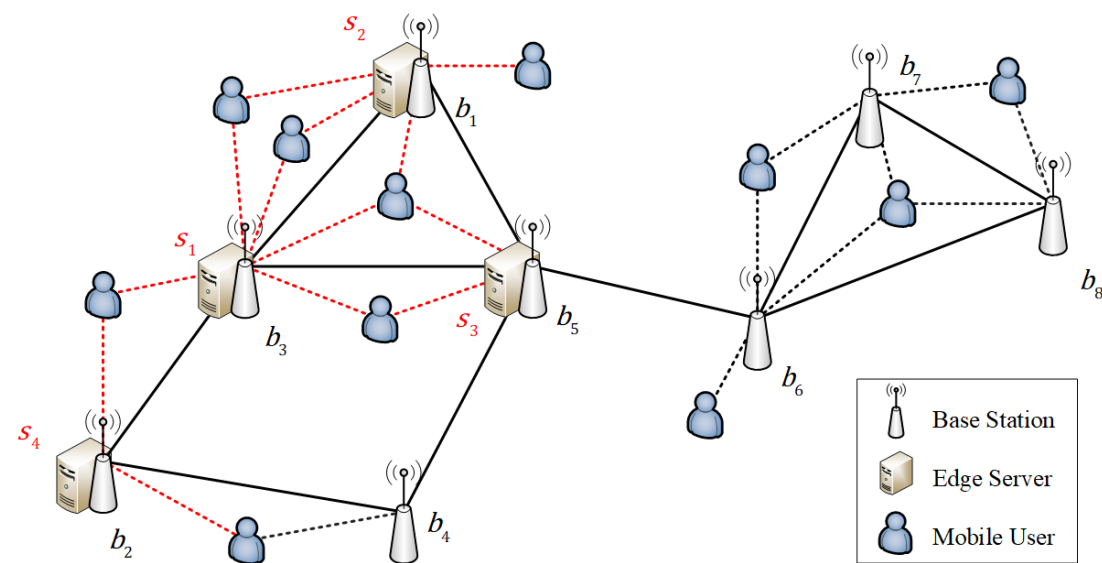
(a) Start with  $b_3$ , which is the most serviced intensive.



(b)  $b_1$  has the most robustness increment, among  $b_3$ 's neighbors  $\{b_1, b_2, b_5\}$



(c)  $b_5$  has the most robustness increment, among  $\{b_1, b_3\}$ 's neighbors  $\{b_2, b_4, b_5\}$




(d)  $b_2$  has the most robustness increment, among  $\{b_1, b_3, b_5\}$ 's neighbors  $\{b_2, b_4, b_6\}$



# The shortage of HR- $k$ ESP<sub>0</sub>

- It is suitable for the case that there is **only one service-intensive area**. In the actual scenario, there may be **more than one** service-intensive area.
- With the expansion of the server deployment scheme to the service-dispersive area, the **robustness increment** of candidate base station will **decrease gradually**.

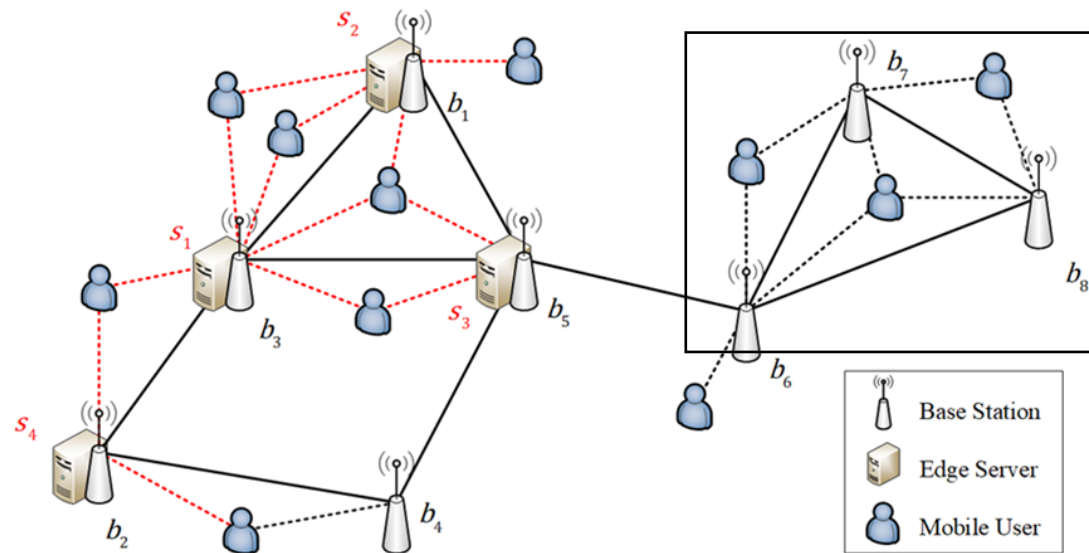
Instead of just expanding the server deployment scheme, it is also important to find new service-intensive area.

HR- $k$ ESP<sub>0</sub>  HR- $k$ ESP

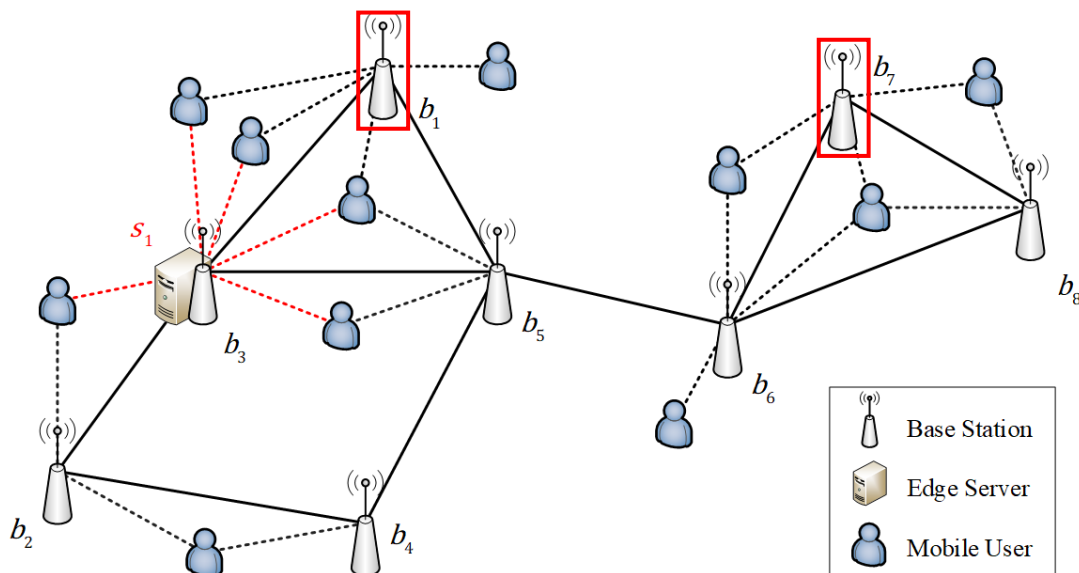
## The step of the HR- $k$ ESP (improved version):

1. Select the most service-intensive base station as the starting point of the server deployment scheme.
2. Evaluate the **neighbors** of selected base station, and the one with the largest robustness increment as  $b_{\text{near}}$ .
3. Evaluate the **others** (unselected base stations except for the neighbors mentioned), and the one with the largest potential robustness increment as  $b_{\text{far}}$ .
4. **Select the best one between  $b_{\text{near}}$  and  $b_{\text{far}}$  to extend the server deployment scheme.**
5. Repeat steps 2-4 until the number of servers reaches the budget.

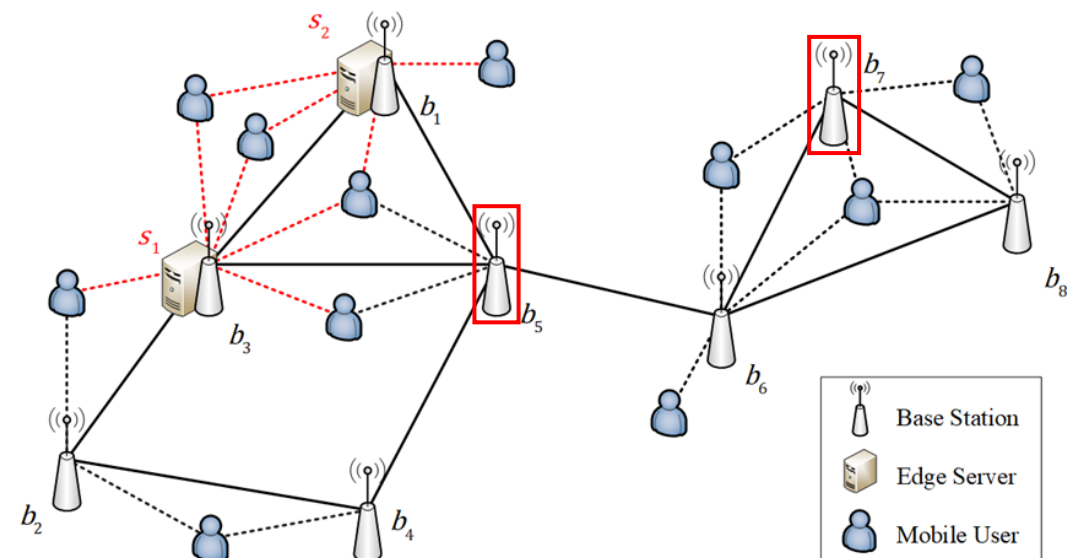
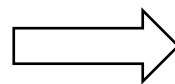
# The missed service-intensive area



(a) The previous solution of HR- $k\text{ESP}_0$  misses another service-intensive area.



(b)



(c)

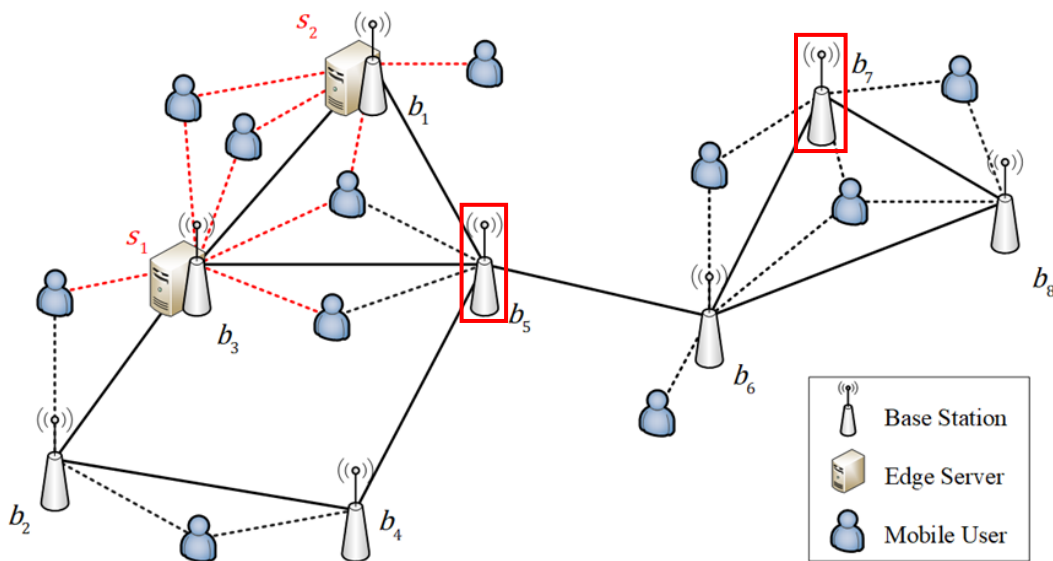
1. The starting base station is still  $b_3$ . Its neighbors is  $N_{\text{near}} = \{b_1, b_2, b_4, b_5\}$ , and others is  $N_{\text{far}} = \{b_6, b_7, b_8\}$ .
2. Evaluate the base stations of  $N_{\text{near}}$  and  $N_{\text{far}}$ , then find the  $b_{\text{near}}$  which is  $b_1$  and the  $b_{\text{far}}$  which is  $b_7$ .
3. Select the best ( $b_1$ ) of them to expand the solution.
4. Update the  $N_{\text{near}}$ ,  $N_{\text{far}}$  and selected  $b_{\text{near}}$ .

$$N_{\text{near}} = \{b_2, b_4, b_5\}$$

$$b_{\text{near}} = b_5$$

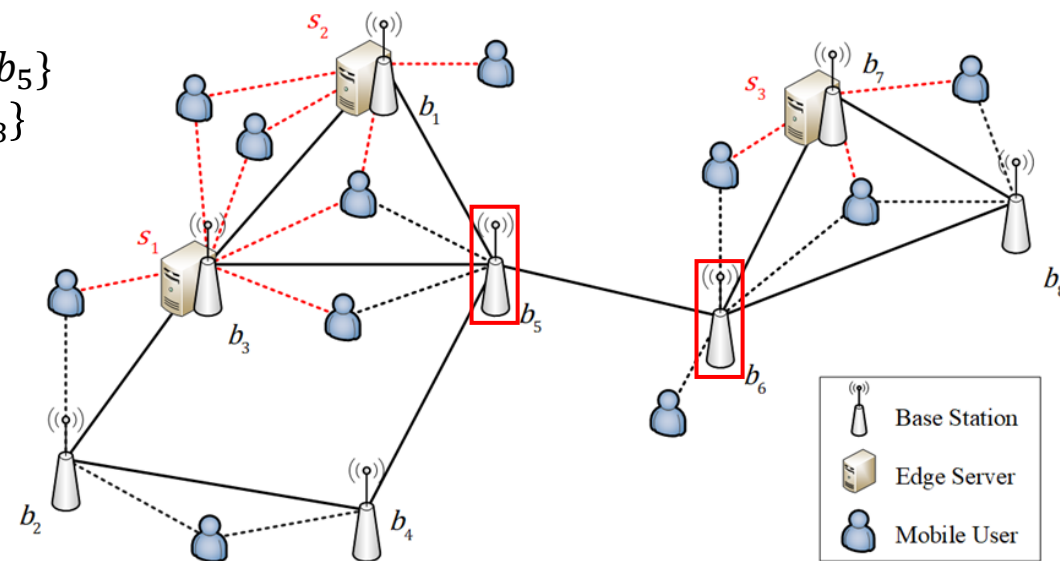
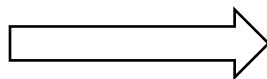
$$N_{\text{far}} = \{b_6, b_7, b_8\}$$

$$b_{\text{far}} = b_7$$



(a)

$$\begin{aligned}
 N_{\text{near}} &= \{b_2, b_4, b_5\} \\
 N_{\text{far}} &= \{b_6, b_7, b_8\} \\
 b_{\text{near}} &= b_5 \\
 b_{\text{far}} &= b_7
 \end{aligned}$$

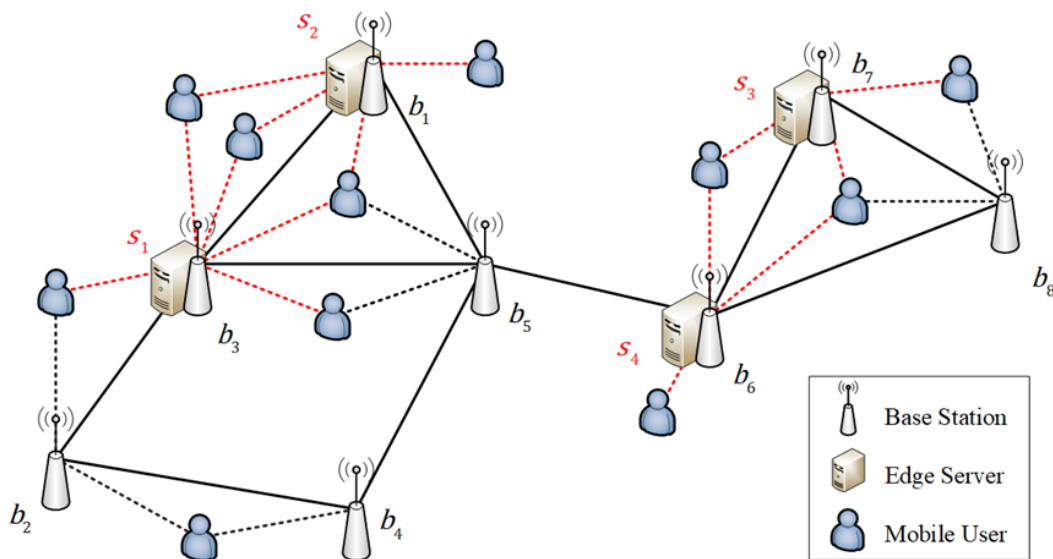


(b)

Since  $b_7$  is better than  $b_5$ , there is an opportunity to deploy the third server in **another service-intensive area**.

According to the same steps, the final selected base station is  $b_6$ .

The solution of HR- $k$ ESP is  $\{b_1, b_3, b_6, b_7\}$ .



(c)

# Experimental Evaluation

The EUA dataset<sup>1</sup> contains the locations of 1465 real-world base stations within metropolitan Melbourne in Australia.

## Benchmark algorithm

- *Random*, randomly select  $k$  base stations;
- *Greedy*, select the top- $k$  base stations according to the metric  $CR(\mathbf{p})$ ;
- *ESP-A<sup>2</sup>*, an approximate solution for kESP problem;
- *HR-kESP<sub>0</sub>*, the basic version of HR-kESP.

1. <https://github.com/swinedge/eua-dataset>

2. Cui, G., He, Q., Chen, F., et al.: Trading off between user coverage and network robustness for edge server placement. IEEE Transactions on Cloud Computing, 10(3), 2178-2189 (2022).

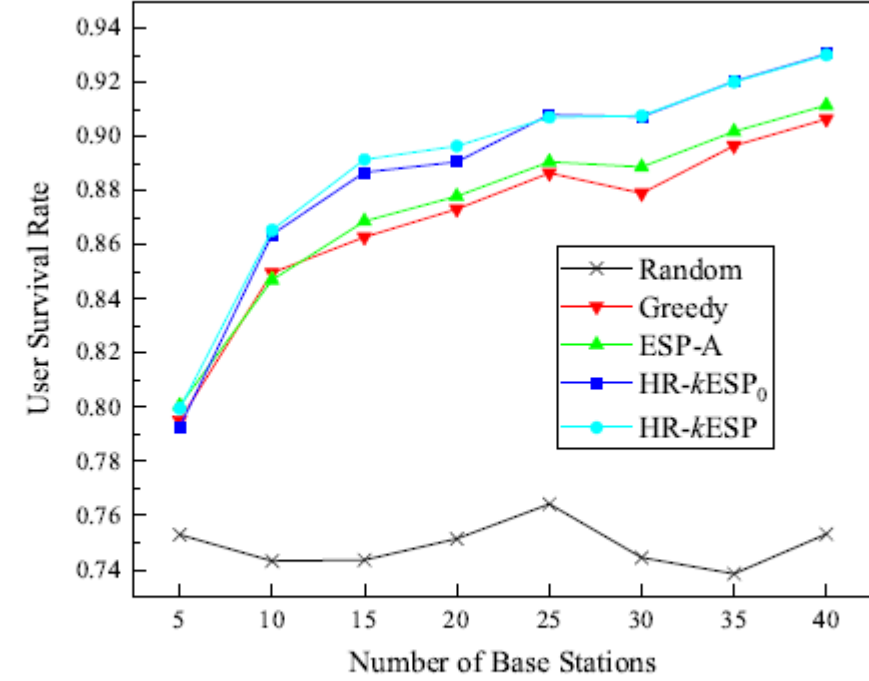
## The network robustness evaluation method

- Some servers are randomly shut down to simulate the sudden failures.
- The default proportion of failed servers is 50%.
- **User Survival Rate** is the measure of network robustness, which is the ratio of the number of the covered users after some server failures to its numbers before.

**Table 1.** Experimental Parameter Settings.

Parameters	$m$	$k$	$n$
Group 1	5, 10, ..., 35	4	80
Group 2	20	1, 2, ..., 8	80
Group 3	20	4	20, 40, ..., 160

- $m$ , the number of base stations
- $k$ , the servers budgets
- $n$ , the number of users



**Fig. 3.** User Survival Rate after Failures with Different Numbers of Base Stations.

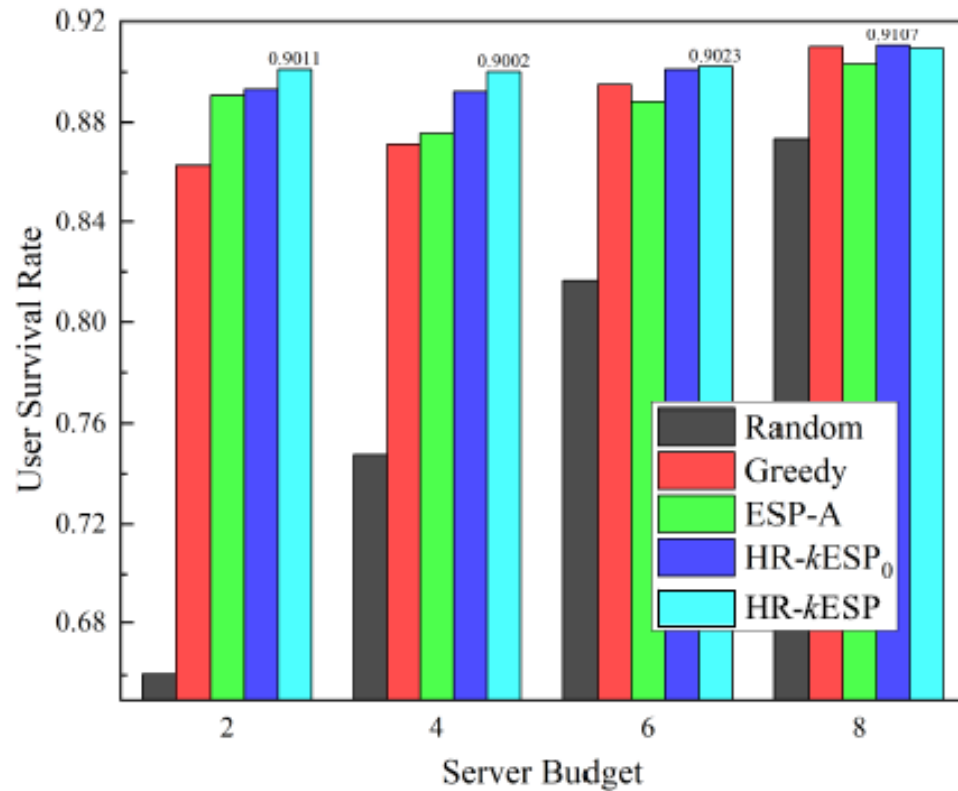
**Table 2.** The Performance ( $CR(p)$ ) of Algorithm with Different Numbers of Base Stations.

Algorithm\ $m$	5	10	15	20	25	30	35	40
Random	185.86	174.18	178.29	180.18	198.11	180.05	168.11	184.35
Greedy	239.02	350.36	393.46	429.27	472.57	466.55	495.26	514.79
ESP-A	228.72	345.92	398.10	436.62	478.43	476.33	506.70	522.41
HR- $k$ ESP <sub>0</sub>	233.34	350.42	400.68	436.08	<b>493.53</b>	489.34	518.96	<b>531.86</b>
HR- $k$ ESP	<b>235.38</b>	<b>353.79</b>	<b>404.71</b>	<b>441.10</b>	491.34	<b>490.65</b>	<b>520.93</b>	530.33

**The Result of Group 1**

**Table 3.** The Performance ( $CR(p)$ ) of Algorithm with Different Server Budgets.

Algorithm\k	1	2	3	4	5	6	7	8
Random	31.68	62.32	112.29	186.74	287.55	426.51	569.98	763.73
Greedy	52.02	105.01	237.88	433.37	693.00	929.68	1244.87	1597.61
ESP-A	<b>53.00</b>	<b>106.20</b>	246.50	441.28	704.48	933.31	1248.36	1570.70
HR- $k$ ESP <sub>0</sub>	<b>53.00</b>	105.62	<b>251.01</b>	449.66	716.03	967.16	1272.51	1603.55
HR- $k$ ESP	51.91	105.49	250.49	<b>455.72</b>	<b>720.87</b>	<b>982.07</b>	<b>1286.63</b>	<b>1621.23</b>

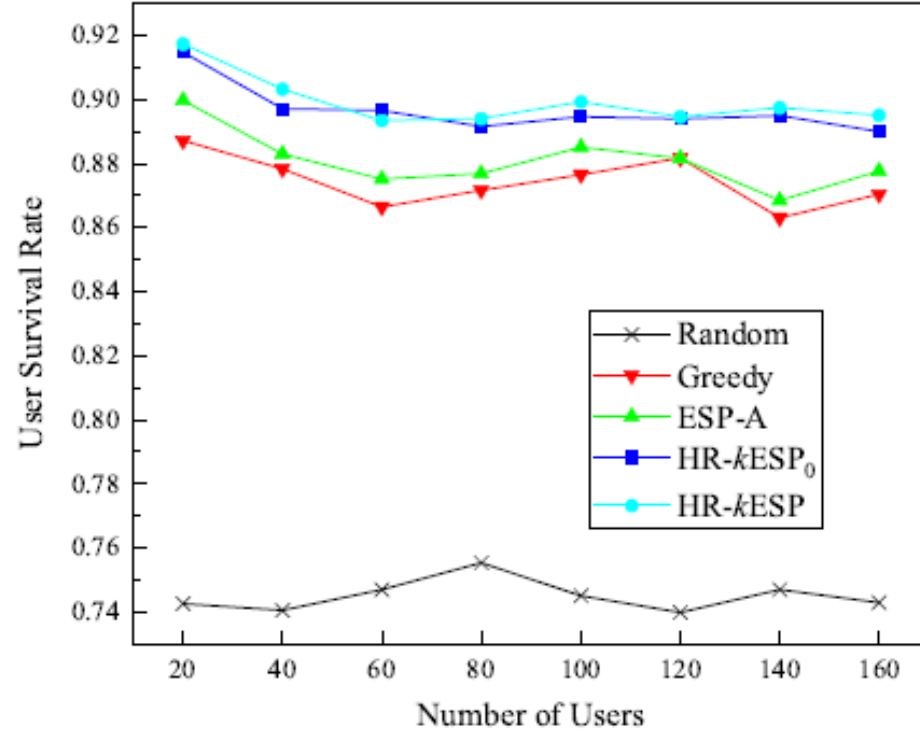


**The Result of Group 2**

**Fig. 4.** User Survival Rate after Failures with Different Server Budgets.

**Table 4.** The Performance ( $CR(p)$ ) of Algorithm with Different Numbers of Users.

Algorithm\ $n$	20	40	60	80	100	120	140	160
Random	43.65	91.16	141.12	188.31	219.96	253.56	309.23	350.02
Greedy	118.34	221.56	323.57	434.84	533.93	652.92	737.79	849.94
ESP-A	119.94	226.03	329.31	440.27	546.91	666.93	751.18	868.78
HR- $k$ ESP <sub>0</sub>	<b>123.61</b>	231.40	335.98	446.82	554.25	671.64	<b>776.13</b>	880.68
HR- $k$ ESP	122.76	<b>234.73</b>	<b>337.69</b>	<b>447.61</b>	<b>558.88</b>	<b>675.64</b>	771.60	<b>890.16</b>



## The Result of Group 3

**Fig. 5.** User Survival Rate after Failures with Different Numbers of Users.

# Conclusion

- For the **Robustness-oriented  $k$ ESP** problem, a heuristic algorithm named **HR- $k$ ESP** is proposed.

According to the **distribution** of the base stations and the users, from the **service-intensive area** to the **service-dispersive area**, the server deployment scheme is expanded gradually by one of **two candidates** which are respectively selected from two subsets (**adjacent** or **non-adjacent** base stations).

- A **evaluation method** for the **Network Robustness** is designed.

A metric named **User Survival Rate** is used to measure the network robustness. Assume the original number of covered users is  $n_{before}$ . After some server failures, the number of covered users is  $n_{after}$ .

$$User\ Survival\ Rate = \frac{n_{after}}{n_{before}}$$

- The experiments are conducted on the **public EUA dataset**, and the results indicate that **HR- $k$ ESP outperforms other benchmark algorithms in most cases**.



**Thank you for your listening!**