



**EXAMINATION PAPER: ACADEMIC SESSION 2020/2021**

Campus	Maritime Greenwich
Faculty	Liberal Arts and Sciences
School	Computing and Mathematical Sciences
Level	4
MODULE TITLE	Algorithms and Data Structures
MODULE CODE	COMP1819
Date and Time	May 2021 - 90 minutes

Answer **ALL** questions

This is a multi-choice, open-book examination. You may access the internet but you may not communicate in any way with another person (including by electronic means).

To give your answers, you must:

- **Submit your answers on Moodle.**
- Also, make sure to mark your choices on the answer sheet (on the last page). If there is a problem with Moodle submission, please send this answer sheet to [FLAS-exams@greenwich.ac.uk](mailto:FLAS-exams@greenwich.ac.uk) by the deadline.

**Failure to follow any of these instructions may result in you failing the exam.**

**Answer all questions with the best answer(s):**

1. Which of the following are operations in data structures (choose 3)?

- A. Traversal
- B. Subtraction
- C. Sorting
- D. Merging
- E. Travelling
- F. Debugging

[4 marks]

2. Which of the following can be used explain what an algorithm is (choose 2)?

- A. A sequence of computational steps that transform input into the output.
- B. A method calls itself.
- C. A logical and mathematical model of a particular organisation of data.
- D. A loosely written code to make final code.
- E. A step-by-step procedure to solve a problem.

[4 marks]

3. What is the Big-O performance of the following code (choose 1)?

```
7  def minmax(sequence):
8      size = len(sequence)
9      if (size == 0):
10         return (0,0)
11     min = max = sequence[0]
12     for val in sequence:
13         if (val > max):
14             max = val
15         if (val < min):
16             min = val
17     return (min,max)
```

- A.  $O(\min)$
- B.  $O(\text{size})$
- C.  $O(\max)$
- D.  $O(\min + \max)$
- E.  $O(\text{val})$

[4 marks]

4. ... is very helpful in the situation when data items are stored and then retrieved in reverse order (choose 1 to fill in ...)?

- A. Set
- B. Map
- C. Stack
- D. Queue
- E. None of the above

[4 marks]

5. What is the Big-O performance of the following code (choose 1)?

```
1. def question(m, n):
2.     k = 0
3.     for i in range(m):
4.         for j in range(n):
5.             k += i * j
6.     return k
```

- A.  $O(k)$
- B.  $O(m*k)$
- C.  $O(n*k)$
- D.  $O(m*n)$
- E.  $O(i*j)$

[4 marks]

6. Consider the following code, what would be the output from lines 37, 39 and 40 (choose 1)?

```
1. class ArrayStack:
2.
3.     def __init__(self):
4.         self.__stack = []
5.
6.     def len(self):
7.         return len(self.__stack)
8.
9.     def isEmpty(self):
10.        return self.len()==0
11.
12.    def push(self, value):
13.        self.__stack.append(value)
14.
15.    def view(self):
16.        return str(self.__stack)
17.
18.    def pop(self):
19.        if self.isEmpty():
20.            raise StackError('stack empty')
21.        else:
22.            return self.__stack.pop()
23.
24.    def peek(self, p = 0):
25.        if p>0 or (1 - p)>len(self.__stack):
26.            raise StackError('location beyond stack bottom')
27.        return self.__stack[p - 1]
28.
29.    def top(self):
30.        return self.peek()
31.
32.
33. if __name__ == '__main__':
34.     S = ArrayStack()
35.     S.push(5)
36.     S.push(3)
37.     print(S.pop())
38.     S.push(7)
39.     print(S.pop())
40.     print(S.pop())
```

- A. 7  
3  
5
- B. 3  
5  
7
- C. 5  
3  
7
- D. 3  
7  
5
- E. The code will compile but there will be an exception raised.

[4 marks]

7. After adding 1, 3 and 7 into an empty queue, and then deleting one element at a time, in which order will they be deleted? (Choose 1)

- A. 731
- B. 137
- C. 713
- D. 317
- E. None of the above

[4 marks]

8. When would it be ideal to use linear searching? (Choose 2)

- A. When the list is linearly independent
- B. When the list is sorted
- C. When the list has only a few elements
- D. When performing a few searches in an unordered list
- E. When performing a search for duplicated values
- F. Can be used all the time.

[4 marks]

9. What is the complexity order for the best case for a linear search of n items? (Choose 1)

- A.  $O(1)$
- B.  $O(\log n)$
- C.  $O(n)$
- D.  $O(n \log n)$
- E.  $O(n^2)$

[4 marks]

10. Which of the following would be a drawback when using linear search of n items? (Choose 1)

- A. Requires more memory.
- B. It is complex to understand.
- C. Running time is more compared to other searching algorithms.
- D. It requires looping implementation.
- E. It cannot be programmed with recursion.

[4 marks]

11. Which of the following data structure CANNOT be stored in a linear type (Choose 1)

- A. Stack
- B. Queue
- C. Binary Tree
- D. List
- E. None of the above

[4 marks]

12. Consider the following code for Bubble Sort, what would be the THIRD line of the output (from line 8)? (Choose 1)

```
1. def bubbleSort(arr):
2.     n = len(arr)
3.
4.     # Traverse through all array elements
5.     for i in range(n):
6.
7.         # Last i elements are already in place
8.         print(arr)
9.
10.        for j in range(0, n-i-1):
11.
12.            # traverse the array from 0 to n-i-1
13.            # Swap if the element found is greater
14.            # than the next element
15.            if arr[j] > arr[j+1] :
16.                arr[j], arr[j+1] = arr[j+1], arr[j]
17.
18. # Driver code to test above
19. arr = [64, 34, 25, 12, 22, 11, 90]
20.
21. bubbleSort(arr)
22.
23. print (arr)
```

- A. [11, 12, 22, 25, 34, 64, 90]
- B. [64, 34, 25, 12, 22, 11, 90]
- C. [34, 25, 12, 22, 11, 64, 90]
- D. [25, 12, 22, 11, 34, 64, 90]
- E. There is an error with the code.

[4 marks]

13. What is the Big O performance of the worst case with an insertion sort of n items? (Choose 1)

- A.  $O(n/2)$
- B.  $O(\log n)$
- C.  $O(n)$
- D.  $O(n \log n)$
- E.  $O(n^2)$

[4 marks]

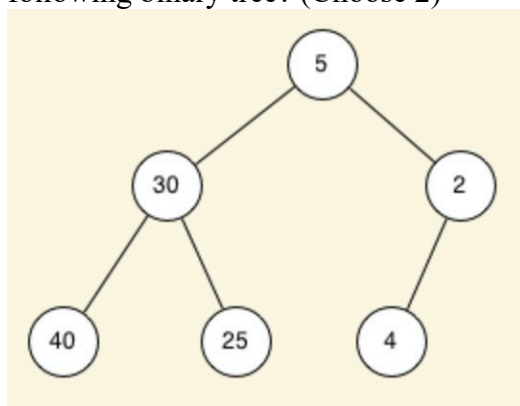
14. Consider the following code for Selection Sort, what would be the SECOND line of the output from line 16? (Choose 1)

```
1. A = [64, 25, 12, 22, 11]
2.
3. # Traverse through all array elements
4. for i in range(len(A)):
5.
6.     # Find the minimum element in remaining
7.     # unsorted array
8.     min_idx = i
9.     for j in range(i+1, len(A)):
10.         if A[min_idx] > A[j]:
11.             min_idx = j
12.
13.     # Swap the found minimum element with
14.     # the first element
15.     A[i], A[min_idx] = A[min_idx], A[i]
16.     print(A)
```

- A. [11, 12, 25, 22, 64]
- B. [11, 12, 22, 25, 64]
- C. [11, 25, 12, 22, 64]
- D. [64, 25, 12, 22, 11]
- E. There is an error with the code.

[4 marks]

15. What would be the pre-order traversal and post-order traversal of the following binary tree? (Choose 2)



- A. 40, 25, 4, 30, 2, 5
- B. 40, 25, 30, 4, 2, 5
- C. 5, 30, 40, 25, 2, 4

- D. 40, 30, 25, 5, 4, 2
- E. 5, 30, 2, 40, 25, 4

[4 marks]

16. Consider the following code using Maps, what would be the output from line 2? (Choose 1)

```
1. m = {'a':1, 'b':2, 'd':3, 'c':3}
2. print(m['d'])
```

- A. 0
- B. 3
- C. 4
- D. None
- E. There is an error with the code.

[4 marks]

17. Consider the following code using Maps, what would be the output at line 14? (Choose 1)

```
1. freq = {}
2. for char in "comp 1819 algorithms and data structure":
3.     w = ''.join(c for c in char if c.isalpha())
4.     if w:                                     # require at least one alphabetic character
5.         freq[w] = 1 + freq.get(w, 0)
6.
7. max_w = ''
8. max_c = 0
9. for (w,c) in freq.items():                   # (key, value) tuples represent (w, c)
10.    if c > max_c:
11.        max_w = w
12.        max_c = c
13.
14. print(max_w, max_c)
```

- A. a 4
- B. t 4
- C. comp 1
- D. comp 4
- E. There is an error with the given code.

[4 marks]

18. Consider the following code using Sets, what is the output at line 21? (Choose 1)

```
1. set1 = set([1, 2, 3, 4, 5, 6,
2.             7, 8, 9, 10])
3. print("Initial Set: ")
4. print(set1)
5.
6. # Removing elements from Set
7. set1.remove(1)
8. print(set1)
9.
10. # Discard elements from Set
11. set1.discard(3)
12. print(set1)
```

```
13.  
14. # Removing elements from Set  
15. for i in range(5, 10):  
16.     set1.remove(i)  
17. print(set1)  
18.  
19. set2 = set([2, 6])  
20.  
21. print(set1.union(set2))
```

- A. {2, 4, 6, 8, 10}
- B. {2, 4, 6}
- C. {2, 10, 4, 6}
- D. {2, 4, 10}
- E. There is an error with the code.

[4 marks]

19. Identify the correct statements about a recursive method (choose 2)?

- A. A method of solving a problem where the solution depends on solutions of smaller instances.
- B. It can be an illegal call.
- C. An object-oriented piece of code to execute an object.
- D. A repeatedly executed block of code until a given condition is satisfied.
- E. A method calls itself from its own code.

[4 marks]

20. What is the output of the following code (choose 1)?

```
7  def fibonacci(n):  
8      """Return the nth Fibonacci number."""  
9      if n <= 1:  
10         return 3  
11     else:  
12         return fibonacci(n-2) + fibonacci(n-1)  
13  
14     print(fibonacci(3))
```

- A. 1
- B. 3
- C. 5
- D. 9
- E. 11

[4 marks]

21. How many times are the method drawSpiral being called in the following code (choose 1)?



```
7 import turtle
8
9 myTurtle = turtle.Turtle()
10 myWin = turtle.Screen()
11
12 def drawSpiral(myTurtle, lineLen):
13     if lineLen > 0:
14         myTurtle.forward(lineLen)
15         myTurtle.right(90)
16         drawSpiral(myTurtle, lineLen-10)
17
18 drawSpiral(myTurtle, 35)
19 myWin.exitonclick()
20
```

- A. 1
- B. 4
- C. 2
- D. 5
- E. None of the above.

[4 marks]

22. What is the Big-O performance for merging two sorted lists of size p and q (choose 1)?

- A.  $O(p|q)$
- B.  $O(p+q)$
- C.  $O(p \cdot \log q)$
- D.  $O(q \cdot \log p)$
- E.  $O(p \cdot q)$

[4 marks]

23. Given an already-sorted array, identify which sorting algorithms would have the best running time? (Choose 2)

- A. Bubble Sort with a swap flag
- B. Insertion Sort
- C. Selection Sort
- D. Quick Sort
- E. Merge Sort

[4 marks]

24. What is the output of the following code (choose 1)?

```
7 def inplace_quick_sort(S, a, b):
8     """Sort the list from S[a] to S[b] inclusive using the quick-sort algorithm."""
9     if a >= b: return # range is trivially sorted
10    pivot = S[b] # last element of range is pivot
11    left = a # will scan rightward
12    right = b-1 # will scan leftward
13    while left <= right:
14        # scan until reaching value equal or larger than pivot (or right marker)
15        while left <= right and S[left] < pivot:
16            left += 1
17        # scan until reaching value equal or smaller than pivot (or left marker)
18        while left <= right and pivot < S[right]:
19            right -= 1
20        if left <= right: # scans did not strictly cross
21            S[left], S[right] = S[right], S[left] # swap values
22            left, right = left + 1, right - 1 # shrink range
23
24    # put pivot into its final place (currently marked by left index)
25    S[left], S[b] = S[b], S[left]
26    # make recursive calls
27    inplace_quick_sort(S, a, left - 1)
28    inplace_quick_sort(S, left + 1, b)
29
30 S = [85, 24, 63, 45, 17, 31, 96, 50]
31 inplace_quick_sort(S, 0, 6)
32 print(S)
```

- A. [85, 17, 24, 31, 45, 50, 63, 96]
- B. [85, 17, 24, 31, 45, 63, 96, 50]
- C. [17, 24, 31, 45, 63, 85, 96, 50]
- D. [17, 24, 31, 45, 85, 63, 96, 50]
- E. [17, 24, 31, 45, 50, 63, 85, 96]

[4 marks]

25. How many times are the method `merge_sort` being called in the following code (choose 1)?

```
7 def merge(S1, S2, S):
8     """Merge two sorted Python lists S1 and S2 into properly sized list S."""
9     i = j = 0
10    while i + j < len(S):
11        if j == len(S2) or (i < len(S1) and S1[i] < S2[j]):
12            S[i+j] = S1[i]      # copy ith element of S1 as next item of S
13            i += 1
14        else:
15            S[i+j] = S2[j]      # copy jth element of S2 as next item of S
16            j += 1
17
18    def merge_sort(S):
19        """Sort the elements of Python list S using the merge-sort algorithm."""
20        n = len(S)
21        if n < 2:
22            return              # list is already sorted
23        # divide
24        mid = n // 2
25        S1 = S[0:mid]           # copy of first half
26        S2 = S[mid:n]           # copy of second half
27        # conquer (with recursion)
28        merge_sort(S1)          # sort copy of first half
29        merge_sort(S2)          # sort copy of second half
30        # merge results
31        merge(S1, S2, S)        # merge sorted halves back into S
32
33    S = [85, 24, 63, 45, 17, 31, 96, 50]
34
35    merge_sort(S)
36
37    print(S)
```

- A. 15
- B. 7
- C. 3
- D. 1
- E. None of the above.

[4 marks]

## **Answer Sheet**

TITLE OF PAPER   Algorithms and Data Structures

COURSE CODE   COMP1819

Your Student ID (e.g 000123456):   00 \_\_\_\_\_

Please circle all correct answers

- |     |   |   |   |   |   |   |
|-----|---|---|---|---|---|---|
| 1.  | A | B | C | D | E | F |
| 2.  | A | B | C | D | E |   |
| 3.  | A | B | C | D | E |   |
| 4.  | A | B | C | D | E |   |
| 5.  | A | B | C | D | E |   |
| 6.  | A | B | C | D | E |   |
| 7.  | A | B | C | D | E |   |
| 8.  | A | B | C | D | E | F |
| 9.  | A | B | C | D | E |   |
| 10. | A | B | C | D | E |   |
| 11. | A | B | C | D | E |   |
| 12. | A | B | C | D | E |   |
| 13. | A | B | C | D | E |   |
| 14. | A | B | C | D | E |   |
| 15. | A | B | C | D | E |   |
| 16. | A | B | C | D | E |   |
| 17. | A | B | C | D | E |   |
| 18. | A | B | C | D | E |   |
| 19. | A | B | C | D | E |   |
| 20. | A | B | C | D | E |   |
| 21. | A | B | C | D | E |   |
| 22. | A | B | C | D | E |   |
| 23. | A | B | C | D | E |   |
| 24. | A | B | C | D | E |   |
| 25. | A | B | C | D | E |   |