

第二次作业

第一题

```
template <class ElemType>
void CyQueue<ElemType>::EnQueue(CyQueue &Q, ElemType x) {
    if (flag && rear == front)
        cout << "Queue Full!!" << endl;
    Q.queue[rear] = x;
    rear = (rear + 1) % MaxSize;
    if (!flag)
        flag = 1;
}
template <class ElemType> ElemType CyQueue<ElemType>::OutQueue(CyQueue &Q) {
    if (!flag)
        cout << "Queue Empty!!" << endl;
    ElemType e = array[front];
    front = (front + 1) % Q.MaxSize;
    if (front == rear)
        flag = 0;
    return e;
}
```

第二题

(1)

```
For(int i = 0; i < halfSize; i++) Push(s, Deque(q));
```

```
While(!isEmptyStack(s)) {
    EnQueue(q, Pop(s));
    EnQueue(q, DeQue(q));
}
```

(2)

第三题

Diagram illustrating the recursive step of the Longest Common Subsequence (LCS) algorithm. The main sequence is "a b a a b a b a b a b a c a". Three vertical red dashed lines indicate the recursive calls. The subproblems are shown as sequences of "a" and "b" characters, each with a length of 6:

- Subproblem 1: "a b a b a c" (aligned under the first two 'a's)
- Subproblem 2: "a b a b a c" (aligned under the first two 'b's)
- Subproblem 3: "a b a b a c" (aligned under the last two 'a's)

第四题

$$n = \sum_{i=1}^h k^{i-1} = \frac{k^h - 1}{k - 1}$$

$$\text{叶子节点数为 } k^h = n(k - 1) + 1$$

第五题

(1)

$$2^{h-1} - 1 < 500$$

$$2^h - 1 \geq 500$$

$$\Rightarrow h = 9$$

(2)

$$500 - (2^{h-1} - 1) = 245 \text{ 个}$$

(3)

$$2^{h-1} - 1 - (2^{h-1} - 245) = 244 \text{ 个}$$

第六题

```
int BinaryTree::FindMax(TNODE *root) {
    int root_val, left, right, max = INT_MIN;
    if (root != NULL) {
        root_val = root->value;
        left = FindMax(root->left);
        right = FindMax(root->right);
        max = max(left, right, root_val);
    }
    return max;
}
```

时间复杂度： $O(n)$ 空间复杂度： $O(n)$

第七题

```

int BinaryTree::FindLevelwithMaxSum(BinaryTree *root) {
    TNode *temp;
    int level = 0, maxLevel = 0;
    struct Queue Q;
    int currentSum = 0, maxSum = 0;
    if (!root)
        return 0;
    InitQueue(Q);
    EnQueue(Q, root);
    while (!Q.isEmpty()) {
        int size = Q.size();
        while (size-- > 0) {
            temp = DeQueue(Q);
            currentSum += temp.value;

            if (temp.left)
                EnQueue(Q, temp.left);
            if (temp.right)
                EnQueue(Q, temp.right);
        }
        if (maxSum < currentSum)
            maxSum = currentSum;
        currentSum = 0;
    }
    return maxSum;
}

```

时间复杂度: $O(n)$ 空间复杂度: $O(n)$

第八题

上界: 当 E 条边全部集中在一个连通分支时连通分量最大, 当该分支为完全图时有最少个点

$$E = \frac{n(n-1)}{2} \Rightarrow n \geq \left\lceil \frac{1 + \sqrt{1 + 8E}}{2} \right\rceil$$

因此连通分量为 $V - \left\lceil \frac{1 + \sqrt{1 + 8E}}{2} \right\rceil + 1$

下界:

$$\begin{cases} \text{当 } E \geq V - 1 \text{ 时, 下界为 } 1 \\ \text{当 } E < V - 1 \text{ 时, 下界为 } V - E \end{cases}$$

第九题

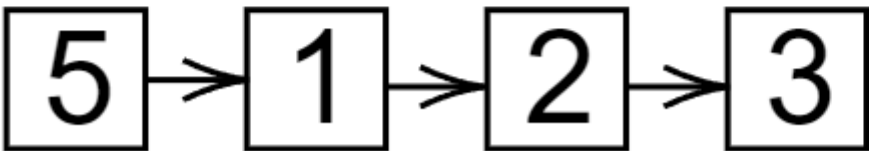
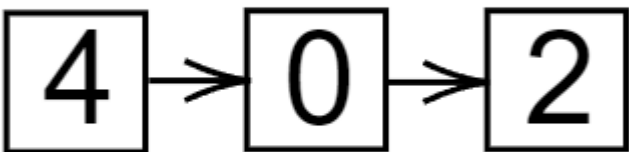
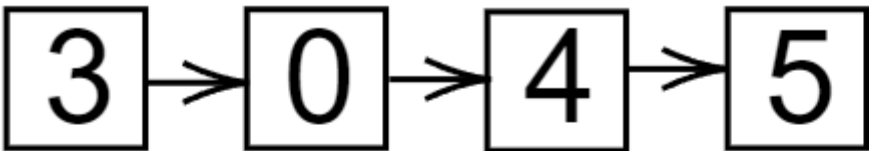
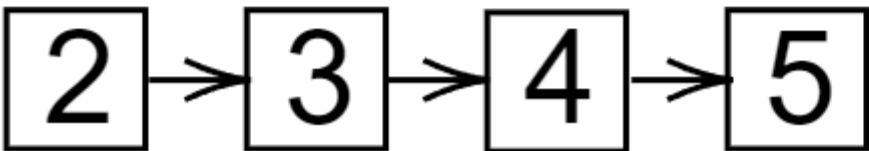
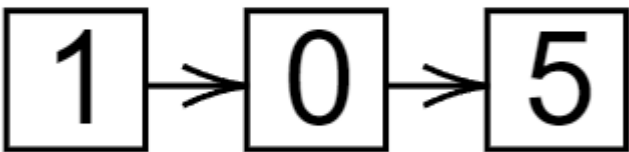
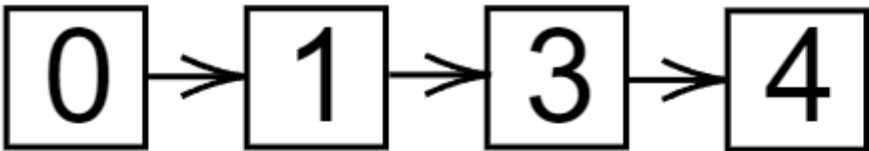
入度: $\sum_{k=0}^{n-1} A[k][i]$

出度: $\sum_{k=0}^{n-1} A[i][k]$

度: $\sum_{k=0}^{n-1} (A[k][i] + A[i][k])$

第十题

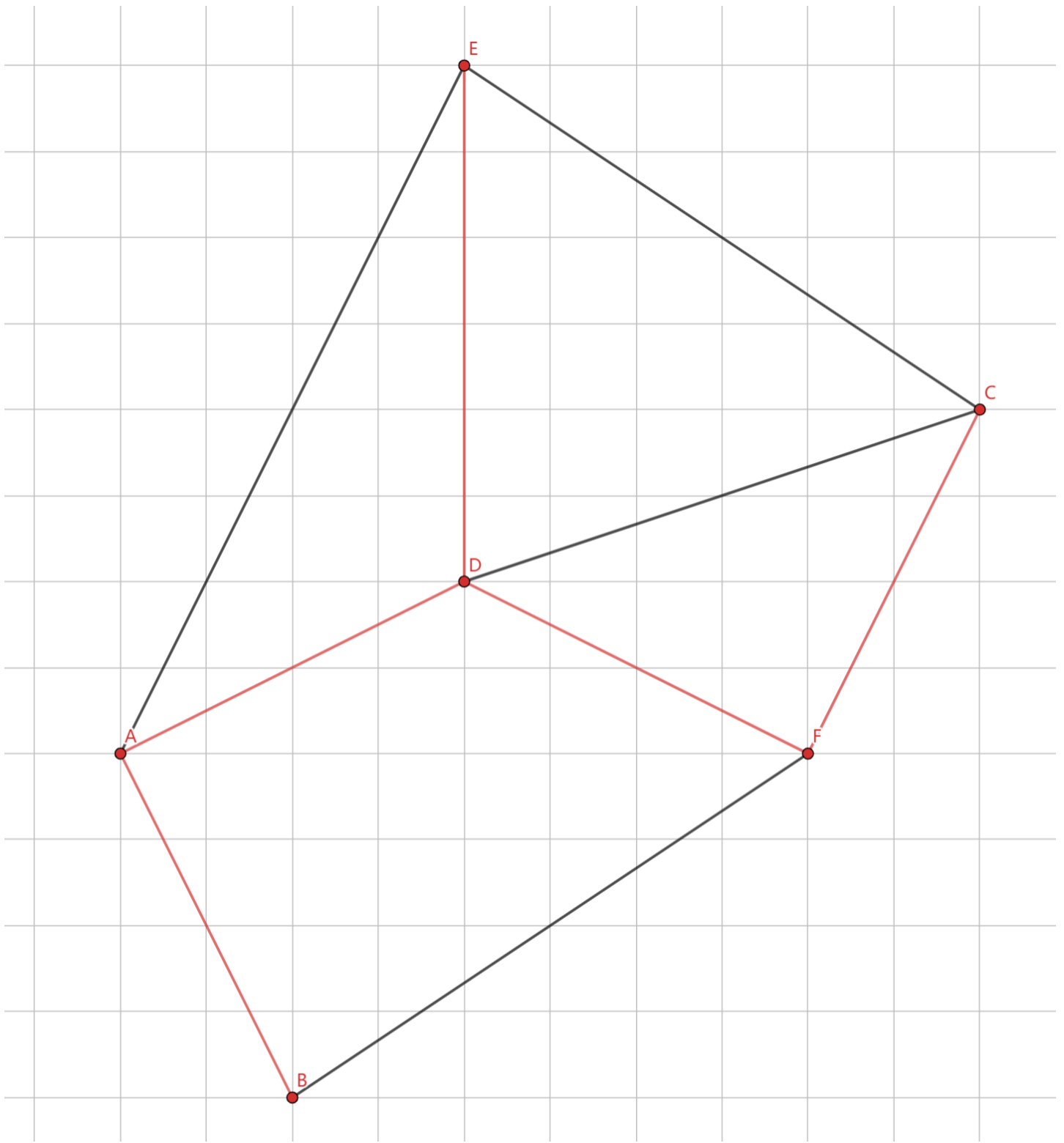
(1)



(2)

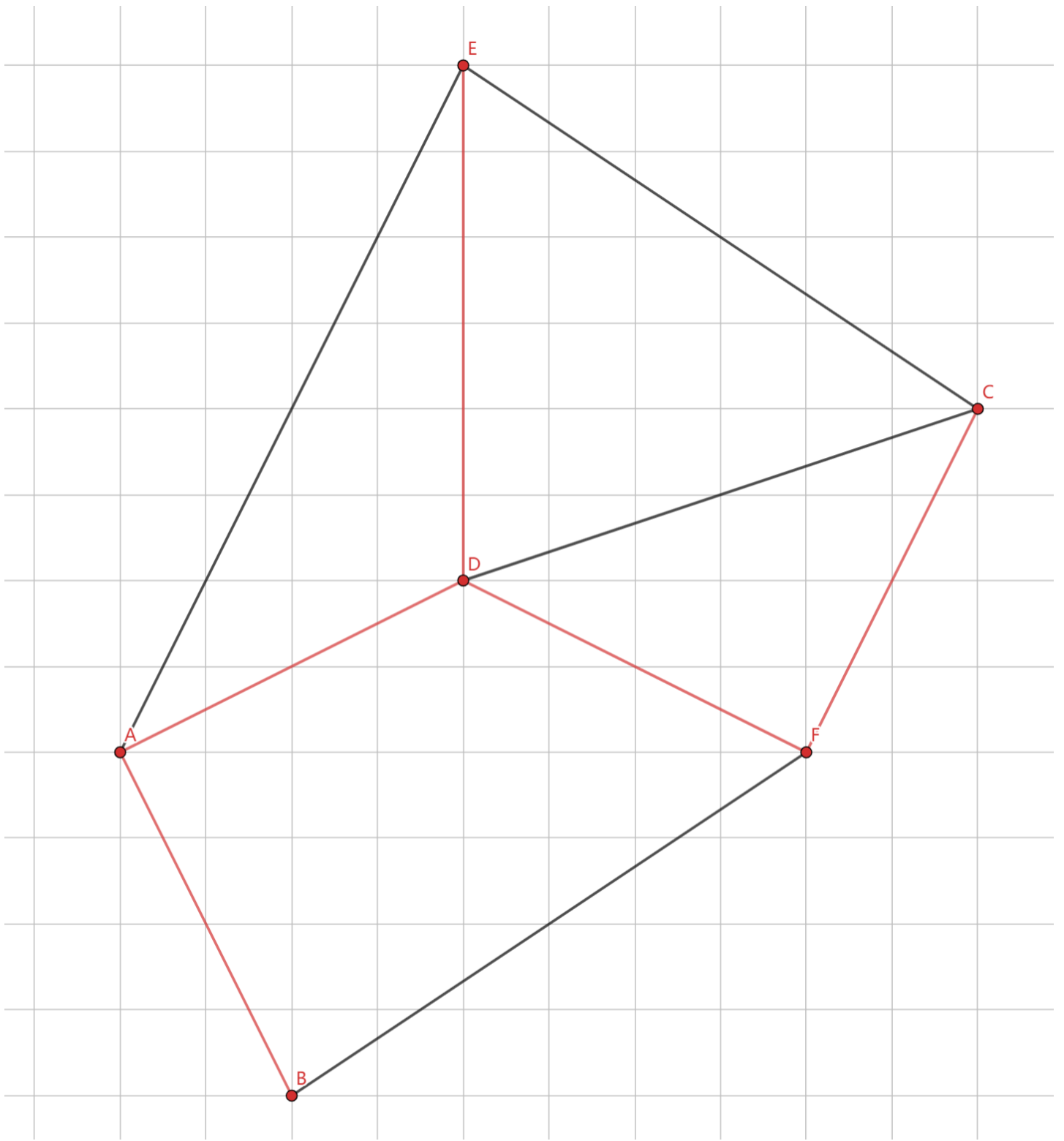
Prim

顺序: 3-5,0-3,0-1,2-5,3-4



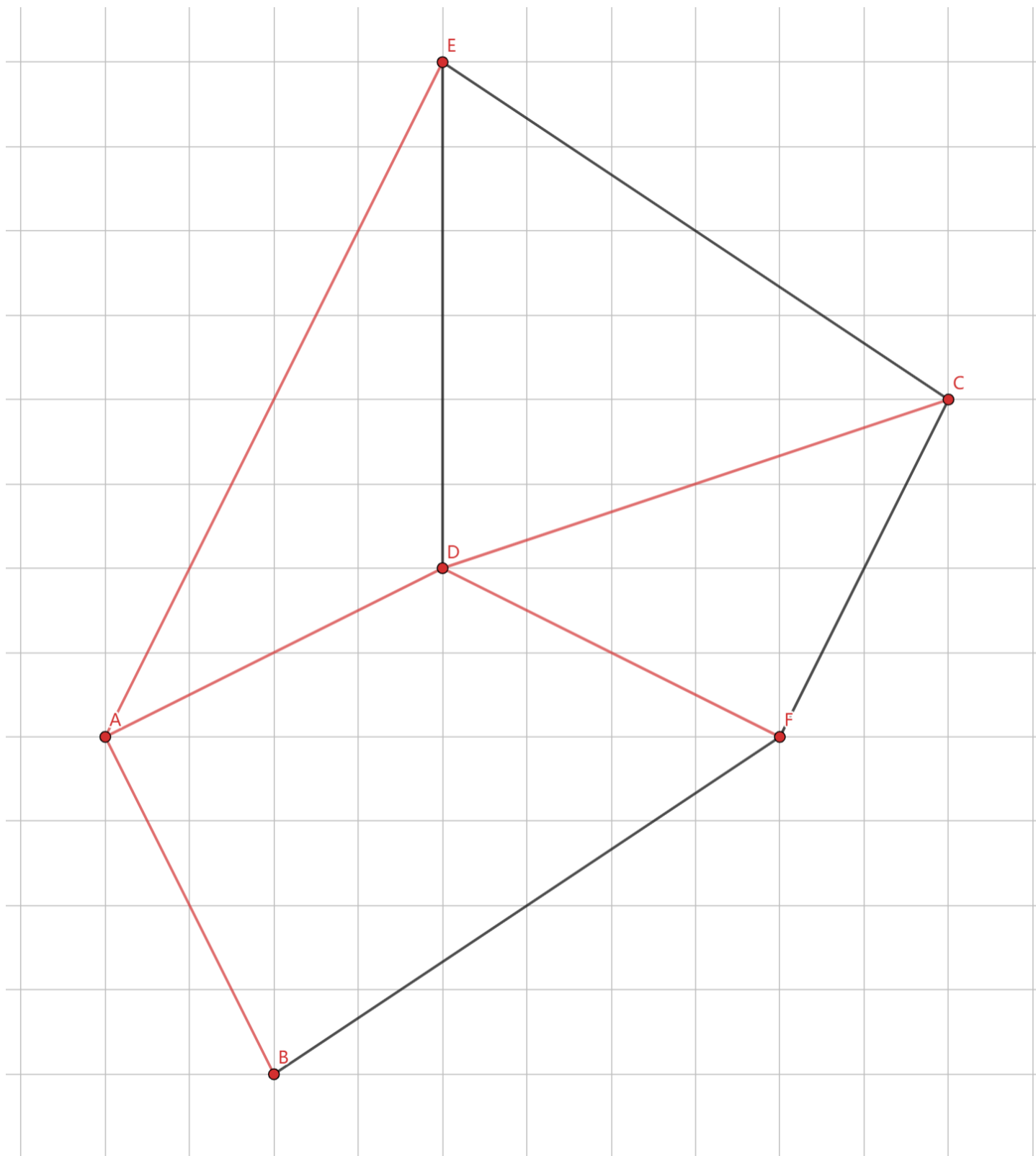
Kruskal

顺序: 3-5,0-3,0-1,2-5,3-4



(3)

以A点作为源点



第十一题


```
Graph *ReverseTheDirectedGraph(Graph *G) {  
    Graph *Gr;  
    if (G == NULL) {  
        Gr = NULL;  
        return NULL;  
    }  
    Initialize(Gr, Vcnt(G), NULL);  
    int n = Vcnt(G);  
    for (int i = 0; i < n; i++) {  
        for (int j = 0; j < n; j++) {  
            if (G->edge(i, j))  
                Gr->insert(j, i);  
        }  
    }  
}
```