

Decalendar and Declock

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1 Summary

Decalendar is a [decimal](#) calendar system and Declock is a decimal timekeeping system. The goal of Decalendar and Declock is to replace all calendar and timekeeping systems that are based on non-decimal [numeral systems](#). Instead of months, weeks, hours, minutes, and seconds, Decalendar and Declock use a single decimal number called the **day-of-the-year** (**doty**).

1.1 Demonstrations

1.1.1 Timestamps

Page load

The Decalendar timestamp below shows the year and **doty** at the time this webpage was loaded. This timestamp is slightly more **precise** and much more **concise** than a timestamp with hours, minutes, and seconds.

Now

A timestamp that doesn't move isn't much fun, so here's one that increments every one ten thousandth (10^{-5}) of a day (**centimilliday**), which in Decalendar is called a **beat**. It's like a heart beat! Or if you prefer, a musical beat!

Diff

If we subtract the first timestamp from the second, we can see how long this webpage has been open. You don't have to read it all in one sitting, it's not a speed-reading competition, so please feel free to take breaks .

1.1.2 Date conversion

Enter a [Gregorian calendar](#) date below to see the equivalent Decalendar date in **doty** date format (**year+day**) and decimal year format (**year.yyy**). Try special dates like birthdays and anniversaries.

1.1.3 Timestamp arithmetic

Doty numbers make working with dates and times a breeze . Use the inputs below to add numbers to the current year and **doty**. Add a positive number to see a future date or add a negative number to get a past date. You can use decimal **doty** numbers for times and even decimal years for dates! For example, the decimal year date 1969.84 ($1969 + 306/365$) is equivalent to the **doty** date 1969+306.

1.2 Day of the year

Figure 1 shows the components of the **doty** number that corresponds to midnight on January 1st in the Gregorian calendar. The first two **digits** (hundreds and tens) of the **doty** are the **dek** number (30 in Figure 1). **Deks** are groups of 10 days that fulfill the role of both months and weeks in **Decalendar**. The next digit (ones) of the **doty** number is the day-of-the-dek (**dotd**) number (6 in Figure 1), which serves as both the day-of-the-month (**dotm**) and the day-of-the-week (**dotw**) in **Decalendar**. Gregorian calendar dates require us to look up the day of the week, while the **doty** contains all of the analogous information for **Decalendar** in its first 3 digits (hundreds, tens, and ones).

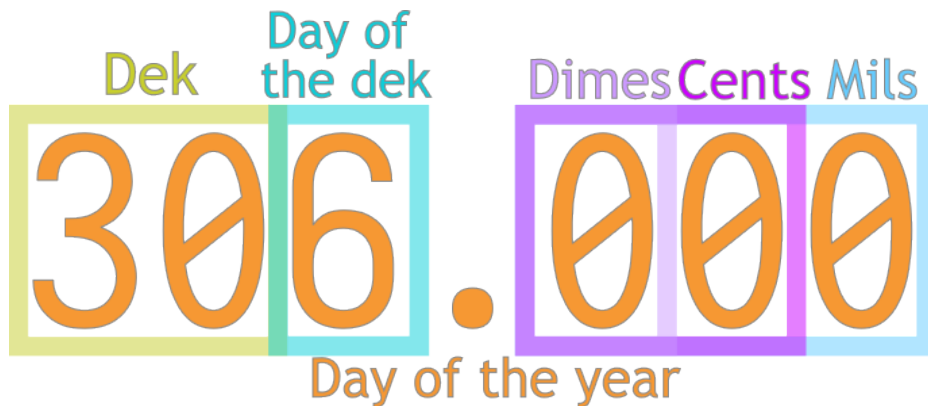


Figure 1: The components of a day-of-the-year (**doty**)

1.3 Deks

As mentioned in Section 1.2, **deks** function as both months and weeks in **Decalendar**. A **dek** consists of 2 groups of 5 days called **pents**. Each **pent** can follow a sequence of workdays and restdays called a **pently** schedule. The code in Example 1.1 generates Figure 2 which compares the typical weekly schedule and the **Schedule 3 pently** schedule. Like other **pently** schedules, **Schedule 3** is named after the number of workdays it contains. The 3 workdays in **Schedule 3** are followed by a 2-day **pentend**, the **Decalender** equivalent of a weekend.

Unlike **Schedule 3** and the other **pently** schedules, the weekly schedule is asymmetric and divides up workdays into proportions that are easier to express as fractions: $3/8$ (.375), $1/3$ (.3), and $7/24$ (0.2916). In contrast, the proportions of the day in **pently** schedules are never **repeating decimal** numbers. Each **Schedule 3** workday is split up symmetrically into proportions so that workday starts at .3 (7.2 hours), lasts .4 (9.6 hours), and ends at .7 (16.8 hours). Section 5.4.3 provides more information on **Schedule 3** and the other **pently** schedules.

Example 1.1.

```
import pandas as pd

ax = (
    pd.DataFrame(
        {
            "Days": ["Mon", "Tue", "Wed", "Thur", "Fri", "Sat", "Sun"],
            "Evening rest": [7 / 24] * 5 + [0] * 2,
            "Work": [1 / 3] * 5 + [0] * 2,
            "Morning rest": [3 / 8] * 5 + [1] * 2,
        }
    )
    .set_index("Days")
    .plot.bar(
        stacked=True,
        color=["blue", "crimson", "blue"],
        title="Weekly schedule",
        fontsize=15,
        legend=False,
        xlabel="Days of the week",
        ylabel="Proportion of the day",
        rot=0,
        width=0.8,
    )
)
ax.invert_yaxis()
ax.legend(["Rest", "Work"], loc="upper right")
ax.patch.set_alpha(0)

for c in ax.containers:
    labels = [round(v.get_height(), 3) if v.get_height() > 0 else "" for v in c]
    labels = [str(l)[1:] for l in labels if l != 1]
    ax.bar_label(c, labels=labels, label_type="center", color="white", fontsize=15)
```

```

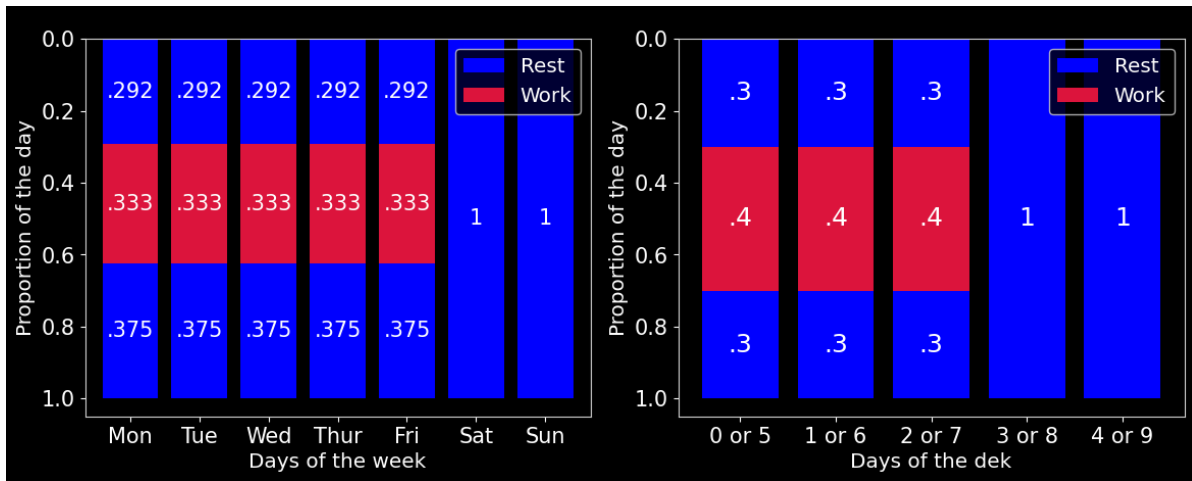
ax = (
    pd.DataFrame(
        {
            "Days": ["0 or 5", "1 or 6", "2 or 7", "3 or 8", "4 or 9"],
            "Evening rest": [0.3] * 3 + [0] * 2,
            "Work": [0.4] * 3 + [0] * 2,
            "Morning rest": [0.3] * 3 + [1] * 2,
        }
    )
    .set_index("Days")
    .plot.bar(
        stacked=True,
        color=["blue", "crimson", "blue"],
        title="Pently schedule",
        fontsize=15,
        legend=False,
        xlabel="Days of the dek",
        ylabel="Proportion of the day",
        rot=0,
        width=0.8,
    )
)
ax.invert_yaxis()
ax.legend(["Rest", "Work"], loc="upper right")
ax.patch.set_alpha(0)

for c in ax.containers:
    labels = [round(v.get_height(), 1) if v.get_height() > 0 else "" for v in c]
    labels = [str(l)[1:] for l in labels if l != 1]
    ax.bar_label(c, labels=labels, label_type="center", color="white", fontsize=18)

```

1.4 Declock time

The digits after the decimal in the `doty` are **Declock** units. Of these units, **mils** are notable because they provide the right level of precision for displaying time on clocks and watches. **Dimes** are also noteworthy because they are used for time zone offsets. Figure 3 shows how a Declock **fractional day** time can be combined with a time zone offset. The `+0` at the end of the time in Figure 3 indicates that the time is in the **Zone 0** time zone, which is equivalent to the **UTC+00:00** time zone of **Coordinated Universal Time (UTC)**.



(a) Proportion of the day spent working and resting every day of the week (b) Proportion of the day spent working and resting every day of the pent

Figure 2: Weekly and pently schedule comparison

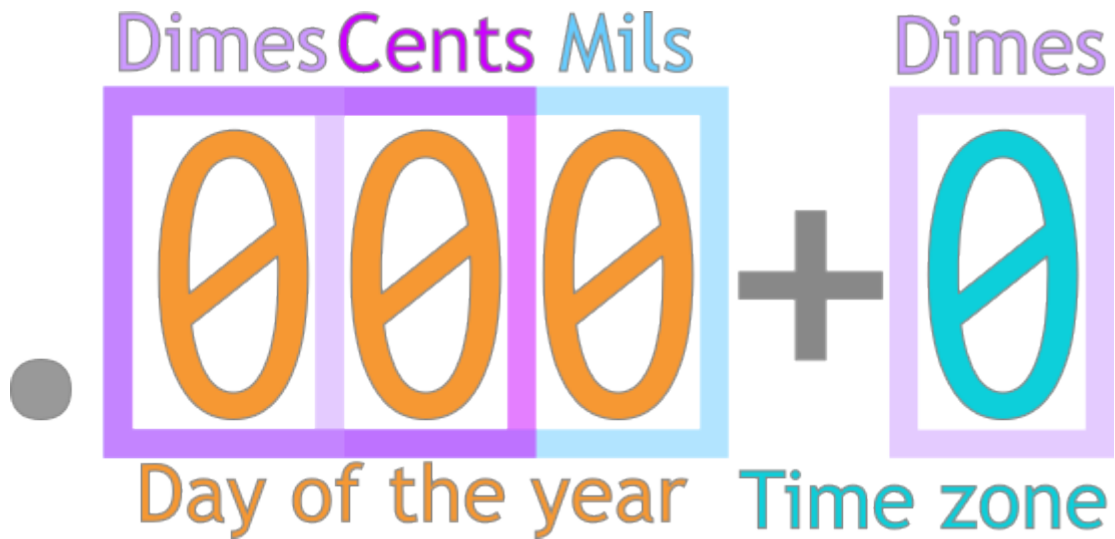


Figure 3: The components of a Declock time

1.5 Decalendar ordinal date

In addition to being combined with a time zone offset as in Figure 3, a **doty** can be combined with a year to form a **Decalendar** ordinal (**deco**) date. Figure 4 shows a **deco** date that is equivalent to January 1st, 1969 in the Gregorian calendar. The **Declock** time in Figure 3 and the **deco** date in Figure 4 both use a plus sign (+) as a delimiter. If we combined the **deco** date from Figure 4 and the **Declock** time from Figure 3, we would obtain a **deco stamp**: 1960+306.000+0. Table 1 compares **doty** and **deco** dates in its first column and **doty** and **deco stamps** in its second column.



Figure 4: The components of a **Decalendar** ordinal (**deco**) date

Table 1

Click to toggle table expansion

Table 1: Comparison of **doty** and **deco** dates and **stamps**

| | date | stamp |
|------|----------|----------------|
| doty | 306 | 306.000+0 |
| deco | 1969+306 | 1969+306.000+0 |

2 Basic concepts

2.1 Fractions analogy

In the simplest terms, **Decalendar** counts fractions of a year, while **Declock** counts fractions of a day. The denominator for **Decalendar** is the number of days in the year, and the **Declock** denominator is 10^x , where x is the number of digits in the numerator. In both systems, only the numerator, not the denominator, is provided. In the context of **Decalendar**, the numerator is the days that have passed in the year, while in the context of **Declock**, the numerator is the parts of the day that have passed in the day.

To avoid any confusion between the two, we can say “Day 5” to mean the date when 5 days have passed this year or **Day 0** to mean the first day-of-the-year (**doty**). This is like the use of the term “day zero” in other contexts, such as epidemiology. The analogous term for times is **Dot**. The word **Dot** conveys that at its core **Declock** is a system built on [fractional days](#) expressed as decimal numbers. The 5 in **Dot 5** can be thought of as a number after a decimal (0.5) or a numerator (/), either way it means noon, the time when half the day has passed.

2.2 Implied tolerance and duration

The analogy to decimals or fractions is important, because it explains why adding a zero at the end of a time does not change the time, only the implied tolerance of time points or the implied duration of time intervals. If **Dot 5** is a time point, it has an implied tolerance of 5% of the day ($.5 \pm .05$), because any time after **Dot 45** and before **Dot 55** ($[.45, .55)$) would round to **Dot 5**. On the other hand, if **Dot 5** is the start time for a time interval, that interval is implied to start at **Dot 5** and end before **Dot 6** ($[.5, .6)$) and thus have a duration of 10% of the day (**Dot 6**-**Dot 5**). Every additional digit we add decreases the implied tolerance and the implied duration 10-fold.

If we really want to insist on punctuality, we could include up to 5 digits in a time. Specifying times with more than 5 digits is possible, and may be useful for scientific or technical purposes, but it is analogous to providing [extremely long GPS coordinates](#); at some point the level of precision stops having relevance to daily life. If we want to strive for the highest level of precision possible, we can add the word “sharp” or the # symbol to the time. Saying “5 Sharp” or writing **5#** means as close as possible to noon. Times that include # cannot have an implied duration. We can only add # to a time, so there is no need say “Dot 5 Sharp” or write **.5#**.

2.3 Context clues

Not saying “Day” or “Dot” in general is acceptable, because it is convenient and often the numbers make perfect sense in context. If someone says “let’s have lunch at 5”, it is clear that they are referring to noon (**Dot 5**) and not the sixth **doty** (**Day 5**). Also, the number itself

may provide a clue. Numbers greater than 365 could still be a **doty**, but it would represent a day in an upcoming year, not the current year. The meaning of such dates depends on whether the current year is a common year ($n=365$) or a leap year ($n=366$). Saying “500” could mean Day 134 (if $n=366$) or Day 135 (if $n=365$) of the subsequent year, but it would most likely mean noon (Dot 500).

2.4 Stamps

If a **Decalender** date and a **Declock** time are combined, they form a time **stamp**. The date always goes before the time in any **stamp**. When said together, the numbers “0” and “5” mean the first **doty** (Day 0) at noon (Dot 5). In written form, this would be 000.5. This format is called **.y**, which is read the same way as **doty**, but emphasizes that the **.** is used in a floating point decimal **doty**. In other words, **doty** can be used instead of “day of the year” in a sentence, whereas **.y** indicates a **stamp**, such as 000.5. Ideally, a **stamp** will include all of the information needed to identify a singular point in time, and thus should include a year and time zone.

2.5 Specific dates and times

The **stamp** in Section 2.4 assumes that the year and time zone are known. A date without a year is like a time without a time zone, both depend on the context. Most likely, we are talking about the current year and the local time zone, but it may be unclear. Including a year allows us to pinpoint a specific day, instead of a day that could happen any year. Similarly, a time with a time zone occurs once every day, rather than once in every time zone per day. The Day 306 of 1969, would be written 1969+306 and said “Year 1969 Day 306” or simply “1969 306”, while midnight in Zone 0 would be written .000+0 and said “Dot 0 Zone 0”, “0 Zone 0”, or “0 0”. Combined together, this date and time form the **stamp** 1969+306.000+0.

2.6 Negative numbers

Every component of **Decalender** dates and **Declock** times can be negative. A negative year is before 1 BCE (Before Common Era) and a negative time zone is West of Zone 0. The year is usually provided without a sign, because most people rarely discuss years before 1 BCE, but numeric time zone offset must have a sign. Negative **doty** numbers work like [zero-based indexes](#) in [computer programming](#) in that they label the days of the year from $-N$ to -1 , where N is the number of the days in the current year. The first **doty** is indexed by both 0 and $-N$, while the last **doty** is indexed by both -1 and N .

In general, negative numbers show the number of parts that are left in the whole. A negative **doty** shows how many days remain in the year and a negative time [counts down](#) to the end of the day. To extend the fractions analogy in Section 2.1 to negative numbers, the negative

number added to the whole gives us the numerator of the positive fraction ($pos = N + neg$). Positive and negative numbers arrive at the same answer from opposite directions.

In certain contexts, the choice of using a negative number over a positive number may mean that we want to emphasize how much time is left instead of how much has passed. Even though `Dot -1` and `Dot 9` are synonymous `Declock` times, the former could highlight that there is only 1 tenth (or .1) of the day remaining before midnight. `Dot 5` and `Dot -5` both mean noon, like saying that a glass is half-empty or half-full.

The negative equivalent of `1969+306`, the `deco` date in Figure 4 and Table 1, is `1970-059`. This negative `deco` date literally subtracts 59 days from the beginning of year 1970 to arrive at `Day 306` of 1969. The year in negative `deco` dates is always 1 greater than the year in the equivalent positive `deco` date. Both `1969+306` and `1970-059` translate to January 1, 1970 in the Gregorian calendar. `Decalendar` years are shifted by two months in relation to the Gregorian calendar years because `Decalendar` years start on March 1.

This shift causes the Gregorian calendar year to be 1 greater than the year in the positive `deco` dates during January and February and 1 less than the year in negative `deco` dates during every other month. For example, the `Deco` dates `1969+000` and `1970-365` are March 1, 1969 in the Gregorian calendar. Immediately after midnight on this date, the negative `doty` will change from -365 to -364, while the positive `doty` will remain at 0. At noon, the positive `deco` date will be `1969+306.500` and the negative `deco` date will be `1970-058.500`.

2.7 Units

`Declock` times often have three digits because this is the best level of precision for displaying time on clocks and watches. While 3 digits are often best, `Declock` times can have any number of digits, depending on the desired precision level. `Declock` provides names for extremely precise time units, but the most relevant units are within a few orders of magnitude from a day, which is the base unit of both `Declock` and `Decalendar`. Listing the units of each, as in Table 2, highlights the relationship between the two:

Table 2

Click to toggle table expansion

Table 2: The units of `Decalendar` and `Declock`

| Quantity | Name | Symbol | Formal Name |
|----------|-------------------|--------|------------------------------|
| 100 | <code>hekt</code> | | <code>hectoday</code> |
| 91 | <code>delt</code> | | <code>deltakeraiayear</code> |

| | | | |
|--------------------|--------|------|-------------------|
| 90 | qop | | qoppaday |
| 80 | pi | | piday |
| 73 | ep | | epsilonkeraiayear |
| 70 | om | | omicronday |
| 61 | wau | | waukeraiayear |
| 60 | xi | | xiday |
| 50 | nu | | nuday |
| 40 | mu | M | muday |
| 30 | lam | | lamday |
| 20 | kap | | kappaday |
| 10 | dek | , | decaday |
| 1 | day | d, | day |
| 10^{-1} | dime | , | deciday |
| 10^{-2} | cent | ¢, % | centiday |
| 10^{-3} | mil | m, % | milliday |
| 2×10^{-4} | period | . | didecimilliday |
| 10^{-4} | phrase | , | decimilliday |
| 2×10^{-5} | bar | | dicentimilliday |
| 10^{-5} | beat | | centimilliday |
| 10^{-6} | mic | | microday |
| 10^{-7} | liph | ̄m | decimicroday |
| 10^{-8} | lib | ̄m | centimicroday |
| 10^{-9} | nan | n | nanoday |
| 10^{-10} | roph | ˘ | decinanoday |
| 10^{-11} | rob | ̈j | centinanoday |
| 10^{-12} | pic | p | picoday |
| 10^{-13} | noph | ̄n | decipicoday |
| 10^{-14} | nob | ̄n | centipicoday |
| 10^{-15} | femt | f | femtoday |
| 10^{-16} | coph | ̄p | decifemtoday |
| 10^{-17} | cob | ̄p | centifemtoday |
| 10^{-18} | att | a | attoday |
| 10^{-19} | foph | f | deciattoday |
| 10^{-20} | fob | f | centiattoday |
| 10^{-21} | zept | z | zeptoday |
| 10^{-22} | toph | ̄a | decizeptoday |
| 10^{-23} | tob | ̄a | centizeptoday |
| 10^{-24} | yokt | y | yoctoday |
| 10^{-25} | zoph | ̄z | deciyoctoday |
| 10^{-26} | zob | ̄z | centiyoctoday |
| 10^{-27} | ront | r | rontoday |

| | | | |
|------------|------|---|---------------|
| 10^{-28} | yoph | ȳ | decirontoday |
| 10^{-29} | yob | ÿ | centirontoday |
| 10^{-30} | quek | q | quectoday |

In Table 2, the units with positive exponents are used for **Decalendar**, while the ones with negative exponents are used for **Declock**. **Cents** (¢) can serve as a useful point of comparison to understand the scale of some of the units in Table 2 above, because each **cent** is 1 percent of the day, which is about a quarter hour ($1\% = 14.4$ minutes). In comparison to **cents**, **mils** are ten times smaller ($.1\% = 1.4$ minutes), **dimes** () are ten times larger ($10\% = 144$ minutes), and **deks** () are 1000 times larger ($1000\% = 14400$ minutes). To be clear, 1 **dek** contains 10 whole days while the other units are fractions of days.

Declock units smaller than **mils** are not easy to think of as percents of a day. For **phrases** () and **beats** (), music serves as a much more useful analogy. In fact, **phrases** and **beats** are musical terms. The duration of a musical beat depends on the tempo, but a **Declock beat** is always precisely 0.864 seconds long. This translates to a tempo of 69.4 ($69 /$ or $625/9$) beats per minute, which is coincidentally also within the normal range of a resting heart rate. **Declock beats** are organized into groups of 2 called **bars** or **measures**, groups of 10 called **phrases**, and groups of 20 called **periods**. A real example of music that follows this exact pattern is Haydn's [Feldpartita](#).

Declock units smaller than **beats** are too small for typical daily use. For example, a **mic** (**microday**,) is faster than a blink of an eye. Each frame in a video playing at 60 frames per second will be shown for about 1.93 **liphs** (**milliphrases**, \bar{m}). A **lib** (**millibeat**, \bar{m}) is not enough time for a neuron in a human brain to fire and return to rest. Sound can travel from a person's ear to their other ear in about 7 **nans** (**nanodays**). Noticing that a sound reaches one ear before the other can help humans to localize the source of the sound, but a **roph** (**microphrase**, $\bar{~}$) difference might be too fast to notice. In a **rob** (**microbeat**, \ddot{p}), a USB 3.0 cable transferring 5 gigabytes per second can send 4.32 kilobytes, the equivalent of a text file with 4320 characters.

3 Time zones

Of the units discussed above, **dimes** are notable, because they are the units of **Declock** time zones. The times in **Zone 1** are one **dime** earlier than **Zone 0** and two **dimes** earlier than **Zone -1**. Time zones are important, because different time zones could have very different times and even different dates. Mexico City is in **Zone -3** and Tokyo is in **Zone 4**, meaning for the majority of the day (**Dot 7** to be exact) Tokyo is one day ahead of Mexico City. If it is noon on the last day of the year 1999 in Mexico City, it will be **Dot 200** on the first day of the year 2000 in Tokyo. This date and time in Mexico City can be written 2000+000.200+4 or 2001-364.800+4, while the equivalent date and time for Tokyo is 1999+365.500-3 or

2000-000.500-3. If we removed the time zone from the end, we would not know that all of these **stamps** describe the same moment in time.

Declock groups together the 26 **Coordinated Universal Time (UTC) offsets** (-12:00 to +14:00) into 11 time zones (**Zone -5** to **Zone 6**) by converting hours into **dimes** ($dimes = hours \div 2.4$) and rounding to the nearest whole number ($dimes = \lfloor hours \div 2.4 \rfloor$). This time zone system is simple and facilitates conversion, but locations on the edges of the main time zones may experience a significant difference between **Dot 5** and **solar noon**, the point when the sun reaches its highest position in the sky.

If we decide to prioritize the amount of sunlight at **Dot 5** over simplicity and ease of conversion, we could convert degrees of longitude into **cents** or **mils**, instead of converting hours into **dimes**. For example, we could say that Mexico City is in **Zone -275** instead of **Zone -3**, because the longitude of Mexico City is 99 degrees West, which translates to an offset of -275 **mils** ($mils = degrees \div .36$). Essentially, we could create as many additional **Declock** time zones as are desired simply by adding digits to the end of each time zone. Adding one digit yields 110 double-digit **cent** time zones, adding two digits creates 1100 triple-digit **mil** time zones, and so on.

4 Related systems

4.1 French Republican calendar

4.1.1 French Republican calendar *décades*

The **French Republican calendar** and **Decalendar** both organize days in groups of 10. A group of 10 days in the French Republican calendar is called a *décade*, while a group of 10 days in **Decalendar** is called a **dek**. The names of the days in a **dek** are derived from their **zero-based** cardinal numbers (zero, one, two...), whereas the days of the *décade* are named after their ordinal numbers (first, second, third...). In both cases, the names are based on Roman and Greek **numeral prefixes**. Table 3 provides the cardinal numbers, one-letter codes, names, and types of the days of the **dek** as well as the names of their French Republican calendar equivalents.

Table 3

Click to toggle table expansion

Table 3: The days of the **dek** and their French Republican calendar equivalents

| # | Code | Name | Type | French |
|---|------|--------|------|-----------------|
| 0 | N | Nulday | work | <i>primidi</i> |
| 1 | U | Unoday | work | <i>duodi</i> |
| 2 | D | Duoday | work | <i>tridi</i> |
| 3 | T | Triday | rest | <i>quartidi</i> |
| 4 | Q | Quaday | rest | <i>quintidi</i> |
| 5 | P | Penday | work | <i>sextidi</i> |
| 6 | H | Hexday | work | <i>septidi</i> |
| 7 | S | Sepday | work | <i>octidi</i> |
| 8 | O | Octday | rest | <i>nonidi</i> |
| 9 | E | Ennday | rest | <i>décadi</i> |

4.1.2 French Republican calendar time

The French Republican calendar and **Declock** both break the day down into decimal portions. In **Declock**, a **dime** is a tenth ($\frac{1}{10}$) of a day, a **cent** is a hundredth (10^{-2}) of a day, a **mil** is a thousandth (10^{-3}) of a day, and a **beat** is a hundred thousandth (10^{-5}) of a day, whereas the French Republican calendar calls these units decimal hours, decimal minutes, *décimes*, and decimal seconds, respectively. Table 4 shows the start times of each **dime** ($\frac{1}{10}$) in a day and its equivalent in 24-hour and 12-hour standard time.

Table 4

Click to toggle table expansion

Table 4: The **dimes** in a day and their standard time equivalents

| | 24-hour | 12-hour |
|---|---------|---------|
| 0 | 00:00 | 12:00AM |
| 1 | 02:24 | 2:24AM |
| 2 | 04:48 | 4:48AM |
| 3 | 07:12 | 7:12AM |
| 4 | 09:36 | 9:36AM |

| | | |
|---|-------|---------|
| 5 | 12:00 | 12:00PM |
| 6 | 14:24 | 2:24PM |
| 7 | 16:48 | 4:48PM |
| 8 | 19:12 | 7:12PM |
| 9 | 21:36 | 9:36PM |

4.2 Swatch Internet Time

[Swatch Internet Time](#) uses the term “.beats” to describe a thousandth of day (10^{-3}). In **Declock**, a **beat** is a hundred thousandth of a day (10^{-4}), because this is the approximate duration of a heartbeat or a beat of music. Another difference is that Swatch Internet Time has only 1 time zone, **UTC+1**, limiting its utility outside of Central Europe or West Africa. **Declock** has 11 main single-digit time zones, but can support as many time zones as needed by adding additional digits. More information on **Declock** time zones can be found in [Section 3](#).

4.3 Gregorian calendar

4.3.1 Coordinate analogy

In the Gregorian calendar, dates are like a set of coordinates, where the month and the day-of-the-month (**dotm**) are like longitude and latitude in the [geographic coordinate system](#) or x and y in the [Cartesian coordinate system](#). The **Decalendar** ordinal (**deco**) date format provides two coordinates in one number: the day-of-the-year (**doty**). [Table 5](#) shows the **doty** number of all Gregorian calendar dates.

To locate a specific date in [Table 5](#), first find the month among the columns (think of the month as an x-axis value) and then move down through the rows to the **dotm** (which is like a y-axis value). To convert a **doty** number to a Gregorian calendar date, we first find the **dek** number (the first two digits of the **doty**) among the rows in [Table 6](#) and then move to the right to the **dotd** (the last digit of the **doty**). The dates in [Table 6](#) are shown in **mm-dd** format.

Table 5

Click to toggle table expansion

Table 5: Gregorian calendar date to `doty` conversion

| Day | Mar | Apr | May | Jun | Jul | Aug | Sep | Oct | Nov | Dec | Jan | Feb |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 1 | 0 | 31 | 61 | 92 | 122 | 153 | 184 | 214 | 245 | 275 | 306 | 337 |
| 2 | 1 | 32 | 62 | 93 | 123 | 154 | 185 | 215 | 246 | 276 | 307 | 338 |
| 3 | 2 | 33 | 63 | 94 | 124 | 155 | 186 | 216 | 247 | 277 | 308 | 339 |
| 4 | 3 | 34 | 64 | 95 | 125 | 156 | 187 | 217 | 248 | 278 | 309 | 340 |
| 5 | 4 | 35 | 65 | 96 | 126 | 157 | 188 | 218 | 249 | 279 | 310 | 341 |
| 6 | 5 | 36 | 66 | 97 | 127 | 158 | 189 | 219 | 250 | 280 | 311 | 342 |
| 7 | 6 | 37 | 67 | 98 | 128 | 159 | 190 | 220 | 251 | 281 | 312 | 343 |
| 8 | 7 | 38 | 68 | 99 | 129 | 160 | 191 | 221 | 252 | 282 | 313 | 344 |
| 9 | 8 | 39 | 69 | 100 | 130 | 161 | 192 | 222 | 253 | 283 | 314 | 345 |
| 10 | 9 | 40 | 70 | 101 | 131 | 162 | 193 | 223 | 254 | 284 | 315 | 346 |
| 11 | 10 | 41 | 71 | 102 | 132 | 163 | 194 | 224 | 255 | 285 | 316 | 347 |
| 12 | 11 | 42 | 72 | 103 | 133 | 164 | 195 | 225 | 256 | 286 | 317 | 348 |
| 13 | 12 | 43 | 73 | 104 | 134 | 165 | 196 | 226 | 257 | 287 | 318 | 349 |
| 14 | 13 | 44 | 74 | 105 | 135 | 166 | 197 | 227 | 258 | 288 | 319 | 350 |
| 15 | 14 | 45 | 75 | 106 | 136 | 167 | 198 | 228 | 259 | 289 | 320 | 351 |
| 16 | 15 | 46 | 76 | 107 | 137 | 168 | 199 | 229 | 260 | 290 | 321 | 352 |
| 17 | 16 | 47 | 77 | 108 | 138 | 169 | 200 | 230 | 261 | 291 | 322 | 353 |
| 18 | 17 | 48 | 78 | 109 | 139 | 170 | 201 | 231 | 262 | 292 | 323 | 354 |
| 19 | 18 | 49 | 79 | 110 | 140 | 171 | 202 | 232 | 263 | 293 | 324 | 355 |
| 20 | 19 | 50 | 80 | 111 | 141 | 172 | 203 | 233 | 264 | 294 | 325 | 356 |
| 21 | 20 | 51 | 81 | 112 | 142 | 173 | 204 | 234 | 265 | 295 | 326 | 357 |
| 22 | 21 | 52 | 82 | 113 | 143 | 174 | 205 | 235 | 266 | 296 | 327 | 358 |
| 23 | 22 | 53 | 83 | 114 | 144 | 175 | 206 | 236 | 267 | 297 | 328 | 359 |
| 24 | 23 | 54 | 84 | 115 | 145 | 176 | 207 | 237 | 268 | 298 | 329 | 360 |
| 25 | 24 | 55 | 85 | 116 | 146 | 177 | 208 | 238 | 269 | 299 | 330 | 361 |
| 26 | 25 | 56 | 86 | 117 | 147 | 178 | 209 | 239 | 270 | 300 | 331 | 362 |
| 27 | 26 | 57 | 87 | 118 | 148 | 179 | 210 | 240 | 271 | 301 | 332 | 363 |
| 28 | 27 | 58 | 88 | 119 | 149 | 180 | 211 | 241 | 272 | 302 | 333 | 364 |
| 29 | 28 | 59 | 89 | 120 | 150 | 181 | 212 | 242 | 273 | 303 | 334 | 365 |
| 30 | 29 | 60 | 90 | 121 | 151 | 182 | 213 | 243 | 274 | 304 | 335 | |
| 31 | 30 | | 91 | | 152 | 183 | | 244 | | 305 | 336 | |

Table 6

Click to toggle table expansion

Table 6: Doty number to Gregorian calendar date conversion

| Dek | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|-----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 0 | 03-01 | 03-02 | 03-03 | 03-04 | 03-05 | 03-06 | 03-07 | 03-08 | 03-09 | 03-10 |
| 1 | 03-11 | 03-12 | 03-13 | 03-14 | 03-15 | 03-16 | 03-17 | 03-18 | 03-19 | 03-20 |
| 2 | 03-21 | 03-22 | 03-23 | 03-24 | 03-25 | 03-26 | 03-27 | 03-28 | 03-29 | 03-30 |
| 3 | 03-31 | 04-01 | 04-02 | 04-03 | 04-04 | 04-05 | 04-06 | 04-07 | 04-08 | 04-09 |
| 4 | 04-10 | 04-11 | 04-12 | 04-13 | 04-14 | 04-15 | 04-16 | 04-17 | 04-18 | 04-19 |
| 5 | 04-20 | 04-21 | 04-22 | 04-23 | 04-24 | 04-25 | 04-26 | 04-27 | 04-28 | 04-29 |
| 6 | 04-30 | 05-01 | 05-02 | 05-03 | 05-04 | 05-05 | 05-06 | 05-07 | 05-08 | 05-09 |
| 7 | 05-10 | 05-11 | 05-12 | 05-13 | 05-14 | 05-15 | 05-16 | 05-17 | 05-18 | 05-19 |
| 8 | 05-20 | 05-21 | 05-22 | 05-23 | 05-24 | 05-25 | 05-26 | 05-27 | 05-28 | 05-29 |
| 9 | 05-30 | 05-31 | 06-01 | 06-02 | 06-03 | 06-04 | 06-05 | 06-06 | 06-07 | 06-08 |
| 10 | 06-09 | 06-10 | 06-11 | 06-12 | 06-13 | 06-14 | 06-15 | 06-16 | 06-17 | 06-18 |
| 11 | 06-19 | 06-20 | 06-21 | 06-22 | 06-23 | 06-24 | 06-25 | 06-26 | 06-27 | 06-28 |
| 12 | 06-29 | 06-30 | 07-01 | 07-02 | 07-03 | 07-04 | 07-05 | 07-06 | 07-07 | 07-08 |
| 13 | 07-09 | 07-10 | 07-11 | 07-12 | 07-13 | 07-14 | 07-15 | 07-16 | 07-17 | 07-18 |
| 14 | 07-19 | 07-20 | 07-21 | 07-22 | 07-23 | 07-24 | 07-25 | 07-26 | 07-27 | 07-28 |
| 15 | 07-29 | 07-30 | 07-31 | 08-01 | 08-02 | 08-03 | 08-04 | 08-05 | 08-06 | 08-07 |
| 16 | 08-08 | 08-09 | 08-10 | 08-11 | 08-12 | 08-13 | 08-14 | 08-15 | 08-16 | 08-17 |
| 17 | 08-18 | 08-19 | 08-20 | 08-21 | 08-22 | 08-23 | 08-24 | 08-25 | 08-26 | 08-27 |
| 18 | 08-28 | 08-29 | 08-30 | 08-31 | 09-01 | 09-02 | 09-03 | 09-04 | 09-05 | 09-06 |
| 19 | 09-07 | 09-08 | 09-09 | 09-10 | 09-11 | 09-12 | 09-13 | 09-14 | 09-15 | 09-16 |
| 20 | 09-17 | 09-18 | 09-19 | 09-20 | 09-21 | 09-22 | 09-23 | 09-24 | 09-25 | 09-26 |
| 21 | 09-27 | 09-28 | 09-29 | 09-30 | 10-01 | 10-02 | 10-03 | 10-04 | 10-05 | 10-06 |
| 22 | 10-07 | 10-08 | 10-09 | 10-10 | 10-11 | 10-12 | 10-13 | 10-14 | 10-15 | 10-16 |
| 23 | 10-17 | 10-18 | 10-19 | 10-20 | 10-21 | 10-22 | 10-23 | 10-24 | 10-25 | 10-26 |
| 24 | 10-27 | 10-28 | 10-29 | 10-30 | 10-31 | 11-01 | 11-02 | 11-03 | 11-04 | 11-05 |
| 25 | 11-06 | 11-07 | 11-08 | 11-09 | 11-10 | 11-11 | 11-12 | 11-13 | 11-14 | 11-15 |
| 26 | 11-16 | 11-17 | 11-18 | 11-19 | 11-20 | 11-21 | 11-22 | 11-23 | 11-24 | 11-25 |
| 27 | 11-26 | 11-27 | 11-28 | 11-29 | 11-30 | 12-01 | 12-02 | 12-03 | 12-04 | 12-05 |
| 28 | 12-06 | 12-07 | 12-08 | 12-09 | 12-10 | 12-11 | 12-12 | 12-13 | 12-14 | 12-15 |
| 29 | 12-16 | 12-17 | 12-18 | 12-19 | 12-20 | 12-21 | 12-22 | 12-23 | 12-24 | 12-25 |
| 30 | 12-26 | 12-27 | 12-28 | 12-29 | 12-30 | 12-31 | 01-01 | 01-02 | 01-03 | 01-04 |
| 31 | 01-05 | 01-06 | 01-07 | 01-08 | 01-09 | 01-10 | 01-11 | 01-12 | 01-13 | 01-14 |
| 32 | 01-15 | 01-16 | 01-17 | 01-18 | 01-19 | 01-20 | 01-21 | 01-22 | 01-23 | 01-24 |
| 33 | 01-25 | 01-26 | 01-27 | 01-28 | 01-29 | 01-30 | 01-31 | 02-01 | 02-02 | 02-03 |
| 34 | 02-04 | 02-05 | 02-06 | 02-07 | 02-08 | 02-09 | 02-10 | 02-11 | 02-12 | 02-13 |
| 35 | 02-14 | 02-15 | 02-16 | 02-17 | 02-18 | 02-19 | 02-20 | 02-21 | 02-22 | 02-23 |
| 36 | 02-24 | 02-25 | 02-26 | 02-27 | 02-28 | 02-29 | | | | |

4.3.2 Gregorian calendar date conversion

In addition to using a conversion table like Table 5, we can convert between Gregorian calendar dates and Decalendar `doty` dates programmatically. The code in Example 4.1 is derived from the `days_from_civil` and `civil_from_days` algorithms described by Howard Hinnant in *chrono-Compatible Low-Level Date Algorithms* (2014). The output of the `greg2doty` function is a `doty` number, while its inverse function, `doty2greg`, returns an array containing a month and a `dotm` number.

Example 4.1.

JavaScript

`greg2doty`

```
function greg2doty(month = 1, day = 1) {  
  return Math.floor(  
    (153 * (month > 2 ? month - 3 : month + 9) + 2) / 5 + day - 1  
  )  
}
```

`greg2doty()`

306

`doty2greg`

```
function doty2greg(doty = 306) {  
  const m = Math.floor((5 * doty + 2) / 153);  
  return [Math.floor(m < 10 ? m + 3 : m - 9), Math.floor(doty - (153 * m + 2) / 5 + 2)];  
}
```

`doty2greg()`

[1, 1]

Julia

`greg2doty`

```

function greg2doty(month=1, day=1)
  Int(floor((153 * (month > 2 ? month - 3 : month + 9) + 2) / 5 + day - 1))
end

greg2doty()

```

306

doty2greg

```

function doty2greg(doty = 306)
  m = floor((5 * doty + 2) / 153);
  return Int(m < 10 ? m + 3 : m - 9), Int(floor(doty - (153 * m + 2) / 5 + 2))
end

doty2greg()

```

(1, 1)

Python

greg2doty

```

def greg2doty(month=1, day=1):
    return (153 * (month - 3 if month > 2 else month + 9) + 2) // 5 + day - 1

greg2doty()

```

306

doty2greg

```

def doty2greg(doty=306):
    m = (5 * doty + 2) // 153
    return m + 3 if m < 10 else m - 9, doty - (153 * m + 2) // 5 + 1

doty2greg()

```

(1, 1)

R

greg2doty

```
greg2doty <- function(month = 1, day = 1) {  
  floor((153 * (ifelse(month > 2, month - 3, month + 9)) + 2) / 5 + day - 1)  
}  
  
greg2doty()
```

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doty2greg

```
doty2greg <- function(doty = 306) {  
  m <- floor((5 * doty + 2) / 153)  
  c(ifelse(m < 10, m + 3, m - 9), floor(doty - (153 * m + 2) / 5 + 2))  
}  
  
doty2greg()
```

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4.3.3 Gregorian calendar months and years

Decalendar only uses months for converting to and from Gregorian calendar dates. Nevertheless, discussing months can help to explain how **Decalendar** works. The **Decalendar** year ends with January and February, as shown in Table 7. During these two months, the **Decalendar** year is 1 less than the Gregorian calendar year. To obtain a **Decalendar** year (dy) from a Gregorian calendar year (gy) and month number (gm), we subtract 1 from gy if gm is less than 3 ($dy = gy - [gm < 3]$). To obtain a Gregorian calendar year (gy) from a **Decalendar** year (dy) and $doty$, we add 1 to dy if $doty$ is greater than 305 ($gy = dy + [dm > 305]$). Code to convert between **Decalendar** and Gregorian calendar years is provided in Example 4.2.

Table 7

Click to toggle table expansion

Table 7: The numeric values of months in **Decalendar** and the Gregorian calendar

| dm | gm | Month |
|----|----|-----------|
| 0 | 3 | March |
| 1 | 4 | April |
| 2 | 5 | May |
| 3 | 6 | June |
| 4 | 7 | July |
| 5 | 8 | August |
| 6 | 9 | September |
| 7 | 10 | October |
| 8 | 11 | November |
| 9 | 12 | December |
| 10 | 1 | January |
| 11 | 2 | February |

Example 4.2.

JavaScript

greg2year

```
function greg2year(year = 1970, month = 1) { return year - (month < 3) }  
  
console.log(greg2year());
```

1969

doty2year

```
function doty2year(year = 1969, doty = 306) { return year + (doty > 305) }  
  
console.log(doty2year());
```

1970

Julia

greg2year

```
function greg2year(year=1970, month=1)
    year - (month < 3)
end

greg2year()
```

1969

doty2year

```
function doty2year(year=1969, doty=306)
    year + (doty > 305)
end

doty2year()
```

1970

Python

greg2year

```
def greg2year(year=1970, month=1):
    return year - (month < 3)

greg2year()
```

1969

doty2year

```
def doty2year(year=1969, doty=306):
    return year + (doty > 305)
```



```
doty2year()
```

1970

R

greg2year

```
greg2year <- function(year = 1970, month = 1) {  
  year - (month < 3)  
}  
  
greg2year()
```

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doty2year

```
doty2year <- function(year = 1969, doty = 306) {  
  year + (doty > 305)  
}  
  
doty2year()
```

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4.3.4 Leap years

A leap year has 366 days in both **Decalendar** and the Gregorian calendar. Day 365 is Leap Day in **Decalendar** and is synonymous with February 29, the Gregorian calendar leap day. **Decalendar** positions Leap Day, Day 365, at the end of the year, which requires an adjustment of the Gregorian calendar definition of a leap year. To check if a **Decalendar** year is a leap, we must first add 1 to the year before plugging it into Equation 1 or the **year2bool** function in Example 4.3.

Interestingly, years from negative **deco** dates do not need any adjustment. The first day of Year 1999 is 1999+000 or 2000-366, while the last day is 1999+365 or 2000-001. Year

1999 is a leap year from the perspective of the positive **deco** dates, 1999+000 and 1999+365, because it goes from Day 0 to Day 365. In the context of the negative **deco** dates, 2000-366 and 2000-001, Year 2000 is a leap year because it goes from Day -366 to Day -1.

$$y \bmod 4 = 0 \wedge year \bmod 100 \neq 0 \vee year \bmod 400 = 0 \quad (1)$$

Example 4.3.

JavaScript

leap

```
function year2bool(year = 1970) {
  return year % 4 == 0 && year % 100 != 0 || year % 400 == 0;
}

year2bool()
```

false

Julia

leap

```
function year2bool(year=1970)
  year % 4 == 0 && year % 100 != 0 || year % 400 == 0
end

year2bool()
```

false

Python

leap

```
def year2bool(year=1970):
    return year % 4 == 0 and year % 100 != 0 or year % 400 == 0

year2bool()
```

False

R

leap

```
year2bool <- function(year = 1970) {
  year %% 4 == 0 & year %% 100 != 0 | year %% 400 == 0
}

year2bool()
```

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4.4 ISO 8601

4.4.1 Years

Both Decalendar and [ISO 8601](#) dates show [years](#) as 4-digit numbers. Unlike ISO 8601, Decalendar does not require years to be included in dates. As shown in [Table 1](#), Decalendar deco dates include years while doty dates do not. Year 0 in both Decalendar and ISO 8601 is 1 BCE (Before Common Era) in the Gregorian calendar. The first day of Year 0 in Decalendar, 0000+000, is called the Decalendar epoch and translates to March 1, 1 BCE in the Gregorian calendar. The first day of Year 0 according to ISO 8601 is -0001+306 in Decalendar and January 1, 1 BCE in the Gregorian calendar.

4.4.2 Ordinal dates

Deco dates (year+day) are very similar to [ISO 8601 ordinal \(isoo\) dates](#) (year-day). Like Decalendar doty numbers, isoo dates count the number of days since the start of the year. Unlike ordinal dates, doty numbers are [zero-based](#) and do not differ across common and leap years. The deco date can be easily obtained from the isoo date using the calculations shown

in Equation 2, Equation 3, and Example 4.4. These calculation shift the `isoo` date by 60 or 61 days to account for the 2-month difference between `Decalendar` and the Gregorian calendar.

In Example 4.4, the `isoo2doty` and `doty2isoo` functions convert between ISO 8601 ordinal day numbers and `doty` numbers. We use the `year2bool` function from Example 4.3 in Example 4.4 to correct for the fact that Leap Day shifts ISO 8601 ordinal day numbers by 1 day in leap years. To be clear, we only have to take Leap Day into account when dealing with `isoo` dates. `Decalendar` `doty` numbers are the same in common and leap years, because Leap Day is at the end of the `Decalendar` year.

$$(isoordinal + 305 - year2bool(year)) \mod 365 \quad (2)$$

$$(doty + 60 + year2bool(year + 1)) \mod 365 \quad (3)$$

Example 4.4.

JavaScript

`isoo2doty`

```
function isoo2doty(yd = "1970-001") {
  const [year, day] = yd.includes("-") ? yd.split("-") : yd.split(/(?=\d{4})/);
  return [parseInt(year) - (parseInt(day) < (60 + year2bool(year - 1))),
    (parseInt(day) + 305 - year2bool(year)) % 365]
}

console.log(isoo2doty())
```

[1969, 306]

`isoo2deco`

```
function isoo2deco(yd = "1970-001") {
  const [year, doty] = isoo2doty(yd).map(i => i.toString())
  return `${year.padStart(4, "0")}${doty.padStart(3, "0")}`
}

console.log(isoo2deco())
```

1969+306

doty2isoo

```
function doty2isoo(year = 1969, doty = 306) {  
  return `${doty2year(year, doty).toString().padStart(4, "0")}-${  
    ((doty + 60 + year2bool(year + 1)) % 365).toString().padStart(3, "0")}`  
}  
  
console.log(doty2isoo());
```

1970-001

Julia

isoo2year

```
function isoo2year(year=1970, day=1)  
  year - (day < (60 + year2bool(year - 1)))  
end  
  
isoo2year()
```

1969

isoo2doty

```
function isoo2year(year=1970, day=1)  
  year - (day < (60 + year2bool(year - 1)))  
end  
  
isoo2year()
```

1969

doty2isoo

```

function doty2isoo(year=1970, doty=0)
    (doty + 60 + year2bool(year + 1)) % 365
end

"${lpad(doty2year(), 4, '0'))+$(lpad(doty2isoo(), 3, '0'))"

```

"1970+060"

Python

isoo2year

```

def isoo2year(year=1970, day=1):
    return year - (day < (60 + year2bool(year - 1)))

isoo2year()

```

1969

isoo2doty

```

def isoo2doty(year=1970, day=1):
    return (day + 305 - year2bool(year)) % 365

f"{isoo2year():>04}+{isoo2doty():>03}"

```

'1969+306'

doty2isoo

```

def doty2isoo(year=1970, doty=0):
    return (doty + 60 + year2bool(year + 1)) % 365

f"{doty2year():>04}+{doty2isoo():>03}"

```

'1970+060'

R

isoo2year

```
isoo2year <- function(year = 1970, day = 1) {  
  year - (day < (60 + year2bool(year - 1)))  
}  
  
isoo2year()
```

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isoo2doty

```
isoo2doty <- function(year = 1970, day = 1) {  
  (day + 305 - year2bool(year)) %% 365  
}  
  
paste0(sprintf("%04d", isoo2year()), "+", sprintf("%03d", isoo2doty()))
```

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doty2isoo

```
doty2isoo <- function(year = 1970, doty = 0) {  
  (doty + 60 + year2bool(year + 1)) %% 365  
}  
  
paste0(sprintf("%04d", doty2year()), "+", sprintf("%03d", doty2isoo()))
```

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4.4.3 Calendar dates

ISO 8601 [calendar dates \(isoc\)](#) consist of a four-digit year, a two-digit month, and a two-digit dotm separated by hyphens (`year-mm-dd`). This format is the current widely accepted standard for displaying Gregorian calendar dates. We can combine code from [Example 4.1](#) and [Example 4.2](#) to convert between `deco` dates and `isoc` dates, as shown in [Example 4.5](#).

The code in Example 4.5 formats the output of the `greg2year` and `greg2doty` functions into `deco` dates and the output of the `doty2year` and `doty2greg` functions into `isoc` dates.

As mentioned in Section 4.3.1, `Decalendar` uses `doty` numbers as dates instead of month and day-of-the-month (`dotm`) numbers, but if required, Gregorian calendar dates can be provided in the `Decalendar` calendar (`decc`, pronounced “deck-see”) format (`year+m+dd`), which is very similar to the `isoc` date format. The `decc` format is described in Section 5.1. Examples of the `decc` format are provided in Section 5.3. To be clear, the `decc` format is only used to display Gregorian calendar dates and otherwise does not play any role in `Decalendar`.

Example 4.5.

JavaScript

`greg2deco`

```
function greg2deco(year = 1970, month = 1, day = 1) {
  return `${greg2year(year, month).toString().padStart(4, "0")}${
    greg2doty(month, day).toString().padStart(3, "0")}`;
}
```

`doty2isoc`

```
function doty2isoc(year = 1969, doty = 306) {
  return `${doty2year().toString().padStart(4, "0")}-${
    doty2greg().map(
      i => i.toString().padStart(2, "0")
    ).join("-")}`;
}
```

`greg2isoc`

```
function greg2isoc(year = 1970, month = 1, day = 1) {
  return `${year.toString().padStart(4, "0")}-${
    month.toString().padStart(2, "0")}-${
    day.toString().padStart(2, "0")}`;
}
```

Julia

deco date

```
"$(lpad(greg2year(), 4, '0'))+$(lpad(greg2doty(), 3, '0'))"
```

"1969+306"

ISO 8601 date

```
"$(lpad(doty2year(), 4, '0'))-$(join(map((x) -> lpad(x, 2, '0'), doty2greg()), '-'))"
```

"1970-01-01"

Python

deco date

```
f"{greg2year():>04}+{greg2doty():<3}"
```

'1969+306'

ISO 8601 date

```
f"{doty2year():>04}-{ '-' .join(map(lambda i: str(i).rjust(2, '0'), doty2greg()))}"
```

'1970-01-01'

R

deco date

```
paste0(  
  sprintf("%04d", greg2year()), "+",  
  sprintf("%03d", greg2doty())  
)
```

Unable to display output for mime type(s): text/html

ISO 8601 date

```
paste0(sprintf("%04d", doty2year()), "-",
        paste(sprintf("%02d", doty2greg()), collapse = '-'))
)
```

Unable to display output for mime type(s): text/html

4.4.4 Time zones

Isoc dates can be combined with the [ISO 8601 time \(isot\) format](#) (hh:mm:ss) to form isoc timestamps. Likewise, deco dates can be combined with Declock times to form deco timestamps. Both deco (year+day.dddddZ) and isoc (year-mm-ddThh:mm:ssZ) timestamps can end in a Z. This Z is a [military time zone code](#) that represents the [UTC+00:00](#) time zone, which is the basis of [Coordinated Universal Time \(UTC\)](#).

Deco timestamps that are synchronized with UTC can either end in Z (year+day.dddddZ) or +0 (year+day.ddddd+0). Noon UTC can be written .5Z or .5+0 in Declock and 12:00:00Z, 120000Z, 12:00:00+00, or 120000+00 as per ISO 8601. The code in [Example 4.6](#) converts between UTC offsets and military time zone codes. [Section 3](#) provides more information on Declock time zones.

Example 4.6.

JavaScript

hour2zone

```
function hour2zone(hour = 0) {
    return hour == 0 ? "Z"
        : hour > 0 && hour < 10 ? String.fromCharCode(hour + 64)
        : hour > 9 && hour < 13 ? String.fromCharCode(hour + 65)
        : hour < 0 && hour > -13 ? String.fromCharCode(Math.abs(hour) + 77)
        : "J";
}

console.log(hour2zone(-new Date().getTimezoneOffset() / 60))
```

Q

zone2hour

```
function zone2hour(zone = "Z") {  
  return (zone = zone.toUpperCase()) == "Z" ? 0  
    : zone > "@" && zone < "J" ? zone.charCodeAt() - 64  
    : zone > "J" && zone < "N" ? zone.charCodeAt() - 65  
    : zone < "Z" && zone > "M" ? -(zone.charCodeAt() - 77)  
    : zone;  
}  
  
console.log(zone2hour(hour2zone(-new Date().getTimezoneOffset() / 60)))
```

-4

Julia

hour2zone

```
# import Pkg; Pkg.add("TimeZones")  
# using TimeZones  
# localzone()  
function hour2zone(hour=0)  
  (  
    hour == 0 ? "Z" :  
    hour > 0 && hour < 10 ? Char(hour + 64) :  
    hour > 9 && hour < 13 ? Char(hour + 65) :  
    hour < 0 && hour > -13 ? Char(abs(hour) + 77) : "J";  
  )  
end  
  
hour2zone()
```

"Z"

zone2hour

```
function zone2hour(zone="Z")  
  (  
    (zone = uppercase(string(zone))) == "Z" ? 0 :
```

```

zone > "@" && zone < "J" ? Int(codepoint(only(zone))) - 64 :
zone > "J" && zone < "N" ? Int(codepoint(only(zone))) - 65 :
zone < "Z" && zone > "M" ? -(Int(codepoint(only(zone))) - 77) : zone;
)
end

zone2hour()

```

0

Python

hour2zone

```

# import time
# print(int(-time.timezone / 3600))
def hour2zone(hour=0):
    return (
        "Z" if hour == 0 else
        chr(hour + 64) if 0 < hour < 10 else
        chr(hour + 65) if 9 < hour < 13 else
        chr(abs(hour) + 77) if -13 < hour < 0 else "J"
    )

hour2zone()

```

'Z'

zone2hour

```

def zone2hour(zone="Z"):
    return (
        0 if (zone := zone.upper()) == "Z" else
        ord(zone) - 64 if "@" < zone < "J" else
        ord(zone) - 65 if "J" < zone < "N" else
        -(ord(zone) - 77) if "M" < zone < "Z" else zone
    )

zone2hour()

```

0

R

hour2zone

```
# Sys.timezone()
hour2zone <- function(hour = 0) {
  ifelse(hour == 0, "Z",
    ifelse(hour > 0 && hour < 10, intToUtf8(hour + 64),
      ifelse(hour > 9 && hour < 13, intToUtf8(hour + 65),
        ifelse(hour < 0 && hour > -13, intToUtf8(abs(hour) + 77), "J"))))
}

hour2zone()
```

Unable to display output for mime type(s): text/html

zone2hour

```
zone2hour <- function(zone = "Z") {
  ifelse((zone <- toupper(zone)) == "Z", 0,
    ifelse(zone > "@" && zone < "J", utf8ToInt(zone) - 64,
      ifelse(zone > "J" && zone < "N", utf8ToInt(zone) - 65,
        ifelse(zone < "Z" && zone > "M", -(utf8ToInt(zone) - 77), zone))))
}

zone2hour()
```

Unable to display output for mime type(s): text/html

4.4.5 Times

The formula for conversion of standard time to Declock time is shown in Equation 4. The value of x in Equation 4. can be modified to obtain different units, which are displayed in Table 8. To convert Declock time into standard time, we first convert into hours using Equation 5 and the appropriate x value from Table 8. Then, we convert hours into minutes with Equation 6 and minutes into seconds with Equation 7. The `hms02doty` and `doty2hms0`

functions in Example 4.7 uses these formulas to convert between standard time and Declock time.

$$declock = \frac{hour}{24} + \frac{minute}{1440} + \frac{second}{86400} \cdot 10^x \tag{4}$$

$$hour = declock \cdot 24 \cdot 10^x \tag{5}$$

$$minute = \frac{hour - \lfloor hour \rfloor}{60} \tag{6}$$

$$second = \frac{minute - \lfloor minute \rfloor}{60} \tag{7}$$

Table 8

Click to toggle table expansion

Table 8: The powers of ten of units based on days

| x | units |
|----|---------|
| -1 | deks |
| 0 | days |
| 1 | dimes |
| 2 | cents |
| 3 | mils |
| 4 | phrases |
| 5 | beats |
| 6 | mics |

Example 4.7.

JavaScript

hms02doty

```
function hmso2doty(hour = 1, minute = 0, second = 0) {
  return hour / 24 + minute / 1440 + second / 86400
}

console.log(hmso2doty())
```

0.041666666666666664

hmso2isot

```
function hmso2isot(hour = 1, minute = 0, second = 0) {
  return hour / 24 + minute / 1440 + second / 86400
}

console.log(hmso2isot())
```

0.041666666666666664

doty2hmso

```
function doty2hmso(doty = 1 / 24) {
  const hour = doty * 24,
    floorHour = Math.floor(hour),
    minute = (hour - floorHour) / 60,
    floorMinute = Math.floor(minute);
  return [floorHour, floorMinute, (minute - floorMinute) / 60]
}

console.log(doty2hmso())
```

[1, 0, 0]

Julia

time

hmso2doty

```
function hmso2doty(hour=1, minute=0, second=0)
    hour / 24 + minute / 1440 + second / 86400
end

hmso2doty()
```

0.041666666666666664

doty2hmso

```
function doty2hmso(doty=1/24)
    hour = doty * 24
    floorHour = floor(hour)
    minute = (hour - floorHour) / 60
    floorMinute = floor(minute)
    return floorHour, floorMinute, (minute - floorMinute) / 60
end

doty2hmso()
```

(1.0, 0.0, 0.0)

Python

hmso2doty

```
def hmso2doty(hour=1, minute=0, second=0):
    return hour / 24 + minute / 1440 + second / 86400

hmso2doty()
```

0.041666666666666664

doty2hmso

```
def doty2hmso(doty = 1/24):
    hour = doty * 24
```



```

    floorHour = hour.__floor__()
    minute = (hour - floorHour) / 60
    floorMinute = minute.__floor__()
    return floorHour, floorMinute, (minute - floorMinute) / 60

doty2hmso()

```

(1, 0, 0.0)

R

hmso2doty

```

hmso2doty <- function(hour = 1, minute = 0, second = 0) {
  hour / 24 + minute / 1440 + second / 86400
}

hmso2doty()

```

Unable to display output for mime type(s): text/html

doty2hmso

```

doty2hmso <- function(doty = 1 / 24) {
  hour <- doty * 24
  floorHour <- floor(hour)
  minute <- (hour - floorHour) / 60
  floorMinute <- floor(minute)
  c(floorHour, floorMinute, (minute - floorMinute) / 60)
}

doty2hmso()

```

Unable to display output for mime type(s): text/html

4.4.6 Timestamps

Decalendar seeks to make months and weeks obsolete. Similarly, **Declock** aims to deprecate hours, minutes, and seconds in favor of [fractional days](#) (`.day`). **Deco** timestamps, which combine **Decalendar** dates and **Declock** times, are more concise and easier to read than ISO 8601 timestamps. An **isoc** timestamp that includes seconds is 20 characters long (`year-mm-ddThh:mm:ssZ`), while a **deco** timestamp with slightly greater precision is only 15 characters long (`year+day.dddddZ`). ISO 8601 timestamps can omit delimiters except for the **T** which separates the date and the time (`yearmmddThhmmssZ`). Without delimiters, **isoc** timestamps become even more difficult to read and still cannot match the brevity of **Decalendar** timestamps.

Coincidentally, an ISO 8601 ordinal (**isoo**) timestamp (`year-dayThh:mm:ssZ`) without delimiters (`yeardayThhmmssZ`) is the same length as a **deco** timestamp (`year+day.dddddZ`). **Deco** timestamps cannot exist without delimiters, because removing the plus sign (+) from a **deco** timestamp turns it into a **doty** number (`ddddddd.dddd`). If we removed the + from the **deco** timestamp 1969+306.00000, we would obtain the **doty** number 1969306.00000 would represent midnight 1969306 days from the beginning of the current year. The rules for **deco** timestamp interpretation are summarized by the code in the `deco2doty` function in [Example 4.14](#).

To create a **deco** timestamp, we can use the `doty2deco` or the `greg2deco` functions as shown in [Example 4.8](#). Similarly, [Example 4.8](#) also shows how to create an **isoc** timestamp with the `doty2isoc` and `doty2isoc` functions. All of these timestamp creation functions assume that the provided times are in the UTC+00:00 time zone or **Zone 0** and need to be adjusted to the provided time zone by adding the appropriate time zone offset to the timestamp. [Section 4.6.4](#) and [Section 4.6.5](#) further discuss timestamps and provide functions for building, parsing, and converting timestamps.

Example 4.8.

JavaScript

`doty2deco`

```
function doty2deco(year = 1969, doty = 306, zone = 0) {
    return `${year.toString().padStart(4, "0")}${doty.toString().padStart(3, "0")}`;
}
```

`hms2doty`

```
function hms2doty(hour = 1, minute = 0, second = 0) {
  return hour / 24 + minute / 1440 + second / 86400
}

console.log(hms2doty())
```

0.041666666666666664

hms2deco

```
function hms2deco(hour = 0, minute = 0, second = 0) {
  return (Math.round(hms2doty(hour, minute, second)
    * 1e5) / 1e5).toString().padStart(5, '0')
}
```

doty2hms

```
function doty2hms(doty = 1 / 24) {
  const hour = doty * 24,
    floorHour = Math.floor(hour),
    minute = (hour - floorHour) / 60,
    floorMinute = Math.floor(minute);
  return [floorHour, floorMinute, (minute - floorMinute) / 60]
}

console.log(doty2hms())
```

[1, 0, 0]

Julia

time

hms2doty

```
function hms2doty(hour=1, minute=0, second=0)
  hour / 24 + minute / 1440 + second / 86400
```

```
end
```

```
hms2doty()
```

0.041666666666666664

doty2hms

```
function doty2hms(doty=1/24)
    hour = doty * 24
    floorHour = floor(hour)
    minute = (hour - floorHour) / 60
    floorMinute = floor(minute)
    return floorHour, floorMinute, (minute - floorMinute) / 60
end
```

```
doty2hms()
```

(1.0, 0.0, 0.0)

Python

hms2doty

```
def hms2doty(hour=1, minute=0, second=0):
    return hour / 24 + minute / 1440 + second / 86400

hms2doty()
```

0.041666666666666664

doty2hms

```
def doty2hms(doty = 1/24):
    hour = doty * 24
    floorHour = hour.__floor__()
    minute = (hour - floorHour) / 60
```

```

    floorMinute = minute.__floor__()
    return floorHour, floorMinute, (minute - floorMinute) / 60

doty2hmso()

```

(1, 0, 0.0)

R

hmso2doty

```

hmso2doty <- function(hour = 1, minute = 0, second = 0) {
  hour / 24 + minute / 1440 + second / 86400
}

hmso2doty()

```

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doty2hmso

```

doty2hmso <- function(doty = 1 / 24) {
  hour <- doty * 24
  floorHour <- floor(hour)
  minute <- (hour - floorHour) / 60
  floorMinute <- floor(minute)
  c(floorHour, floorMinute, (minute - floorMinute) / 60)
}

doty2hmso()

```

Unable to display output for mime type(s): text/html

4.4.7 Time intervals

ISO 8601 specifies three methods of unequivocally representing [time intervals](#), `start/stop`, `start/span`, and `span/stop`. The Decalendar equivalents of these three time interval representations are `start:stop`, `start>span`, and `stop<span`. Notably, the `start/stop` syntax is

used in Google Calendar “Add to Calendar” links (<https://calendar.google.com/calendar/render?action=>). Clicking on an “Add to Calendar” link opens a web browser interface for adding an event to an online calendar. The `greg2link` and `doty2link` functions in Example 4.9 create such links for Google, Outlook, Office 365, and Yahoo online calendars.

Example 4.9.

4.4.8 Repeating time intervals

ISO 8601 time intervals can be made to repeat with the `Rn/` prefix (`Rn/start/stop`, `Rn/start/span`, `Rn/span/stop`), where `n` is the number of repetitions. Such [repeating time intervals](#) are always consecutive and never overlap. The first three 6-hour intervals of 1970 could be written `R3/1970-01-01T00:00:00Z/T06` as per ISO 8601. This time interval in `Decalendar` could be written `1969+306>.75>.25>0`. Unlike ISO 8601, `Decalendar` allows for the creation of non-consecutive and overlapping recurring intervals. If we wanted to include 3-hour breaks in between the three 6-hour intervals, we could write `1969+306>1>.25>.125`. Similarly, the three 6-hour intervals could be made to overlap by 3 hours by writing `1969+306>.5>.25<.125`.

The `Decalendar` time interval representations above are called `spreads` and were inspired by the concept of [array slicing](#) from computer programming. `Decalendar` allows for the use of both `slices` (`start:stop:step`) and `spreads` (`start>span>split>space`) to create time intervals. [Slicing of dates and times](#) is fully implemented in the [Pandas Python library](#). The pandas code shown in Example 4.10 uses slicing to obtain the start times of the last three 6-hour intervals in Gregorian calendar year 1970, which is `1970+305>.75>.25>0` in `Decalendar` and `R3/1970-12-31T06:00:00Z/T06` as per ISO 8601.

Example 4.10.

```
import pandas as pd

pd.date_range("1970", "1971", freq="6H")[-4:-1]
```

```
DatetimeIndex(['1970-12-31 06:00:00', '1970-12-31 12:00:00',
               '1970-12-31 18:00:00'],
              dtype='datetime64[ns]', freq='6H')
```

4.5 Julian dates

A **Julian date** is the number of **fractional days** since $-4713+268.5$, which is noon on November 24, 4714 BC in the Gregorian calendar and January 1, 4713 BC in the Julian calendar. The analogous date format in **Decalendar** is the day-of-the-**era** (**dote**). Both Julian and **dote** dates count days from a starting point called an **epoch**. The **Decalendar** epoch is $0000+000.0$, which is midnight on March 1, 1 BC in the Gregorian calendar. To convert a Julian date into a **dote**, we simply subtract 1721120.5 days ($dote = julian - 1721120.5$).

Like Julian dates, **dote** dates are very useful for date and time calculations. Equation 8 shows how a year and a **doty** can be turned into a **dote**. The conversion of a **dote** into a year and **doty** requires calculations adapted from the “**civil_from_days**” algorithm from (Hinnant 2014). Briefly, the **dote** is used to obtain the **solar cycle** in Equation 9, which is then plugged into Equation 10 and Equation 11 to calculate the **day-of-the-cycle** (**dotc**) and the **year-of-the-cycle** (**yotc**) in Equation 11. Equation 12 takes the **yotc** and the solar cycle and yields the year, while Equation 13 generates the **doty** from the **yotc** and the **dotc**.

$$dote = doty + (365 \cdot year + \lfloor \frac{year}{4} \rfloor - \lfloor \frac{year}{100} \rfloor + \lfloor \frac{year}{400} \rfloor) \quad (8)$$

$$cycle = \lfloor \frac{\begin{cases} dote & \text{if } dote \geq 0; \\ dote - 146096 & \text{otherwise.} \end{cases}}{146097} \rfloor \quad (9)$$

$$dotc = days - cycle \cdot 146097 \quad (10)$$

$$yotc = \lfloor \frac{dotc - \lfloor \frac{dotc}{1460} \rfloor + \lfloor \frac{dotc}{36524} \rfloor - \lfloor \frac{dotc}{146096} \rfloor}{365} \rfloor \quad (11)$$

$$year = yotc + cycle * 400 \quad (12)$$

$$doty = \lfloor dotc - (365 \cdot yotc + \lfloor \frac{yotc}{4} \rfloor - \lfloor \frac{yotc}{100} \rfloor + \lfloor \frac{yotc}{400} \rfloor) \rfloor \quad (13)$$

The conversion between **doty** and **dote** is the most important calculation in **Decalendar** because it defines the behavior of positive and negative **deco** dates and stamps. The arithmetic

Example 4.11.

JavaScript

doty2dote

```
function doty2dote(year = 1969, doty = 306) {  
    return doty + Math.floor(year * 365 + Math.floor(year / 4) - Math.floor(year / 100) +  
}  
  
console.log(doty2dote());
```

719468

Julia

unix

doty2dote

```
function doty2dote(s=0, ms=0)  
    days = s / 86400 + ms / 86400000 + 719468  
    dote = days - (era = floor((days >= 0 ? days : days - 146096) / 146097)) * 146097  
    year = Int(floor((dote - dote / 1460 + dote / 36524 - dote / 146096) / 365) + era * 40  
    year, days - floor(year * 365 + year / 4 - year / 100 + year / 400)  
end  
  
y, d = doty2dote(time())  
day = Int(floor(d))  
"$ (lpad(y, 4, '0'))+$ (lpad(day, 3, '0')).$ (lpad(Int(round((d - day) * 1e5)), 5, '0'))+0"
```

"2023+221.59666+0"

Python

doty2dote

```
from time import time  
  
def doty2dote(s=0, ms=0):  
    days = s / 86400 + ms / 86400000 + 719468  
    dote = days - (era := (days if days >= 0 else days - 146096) // 146097) * 146097
```



```

    year = int((dote - dote / 1460 + dote / 36524 - dote / 146096) // 365 + era * 400)
    return year, days - (year * 365 + year / 4 - year / 100 + year / 400).__floor__()

y, d = doty2dote(time())
f"{y:>04}+{(day := d.__floor__()):>03}.{round((d - day) * 1e5):>05}+0"

```

```
'2023+221.59677+0'
```

R

doty2dote

```

doty2dote <- function(s = 0, ms = 0) {
  days = s / 86400 + ms / 86400000 + 719468
  dote = days - (era = floor(ifelse(days >= 0, days, days - 146096) / 146097)) * 146097
  year = floor((dote - dote / 1460 + dote / 36524 - dote / 146096) / 365) + era * 400
  c(year, days - floor(year * 365 + year / 4 - year / 100 + year / 400))
}

yd <- doty2dote(as.numeric(Sys.time()))

paste0(sprintf("%04d", yd[1]), "+",
        sprintf("%03d", (day = floor(yd[2]))), ".",
        sprintf("%05d", round((yd[2] - day) * 1e5)), "+0"
)

```

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4.6 UNIX time

4.6.1 Julian time conversion to UNIX time

Building on the conversion of Julian dates into `dote` and `doty` numbers, it may be easiest to obtain the official definition of `deco` dates and `Declock` times is based on UNIX time. UNIX time is the number of seconds since the UNIX Epoch, which is 1969+306.0 in `Decalendar` or midnight in the [UTC+0](#) time zone on January 1, 1970 in the Gregorian calendar. A day is exactly 86,400 seconds (100,000 `beats`) long in UNIX time, Julian dates, `deco` dates, and `Declock` times. To obtain UNIX time from a Julian Date, we subtract 2440587.5 from the Julian Date and multiply by 86400 as shown in Equation 14.

$$unix = (JD - 2440587.5) \cdot 86400 \quad (14)$$

4.6.2 UNIX time conversion to deco date

To calculate **deco** dates directly from UNIX time, we can use a calculation adapted the 2014 article entitled “[chrono-Compatible Low-Level Date Algorithms](#)” by [Howard Hinnant](#) (2014). Briefly, the seconds (or milliseconds) in UNIX time are first converted to **days** ($days = seconds \div 86400$). Then, the **days** are used to obtain the **era** (Equation 9), **day-of-the-era** (Equation 8), **year** (Equation 12), and **doty** (Equation 13).

4.6.3 UNIX time conversion to Decalendar timestamp

To obtain fractional days, we have to sum up all of the days in previous years and subtract this sum from **days** to obtain the current **Decalendar** ordinal (**deco**) timestamp as shown in Equation 15. The code in Example 4.12 converts UNIX time into a **deco** timestamp in the Zone 0 time zone by passing the current UNIX timestamp to the `unix2doty` function. If we call this function without arguments (`unix2doty()`) the result will be the year and **doty** of the UNIX Epoch: 1969 and 306. To see Example 4.12 in action, visit this [CodePen](#) which displays the current **deco** (`year+day.ddddd`) and **isoc** (`year-mm-ddThh:mm:ss`) timestamps.

$$time = year \cdot 365 + \sum_{n=1}^{year} \left[\begin{array}{ll} y & \text{mod } 4 = 0 \\ \wedge y & \text{mod } 100 \neq 0 \\ \vee y & \text{mod } 400 = 0 \end{array} \right] \quad (15)$$

Example 4.12.

JavaScript

`unix2doty`

```
function unix2doty(ms = 0) {
  const days = ms / 86400000 + 719468,
    dote = days - (era = Math.floor((days >= 0 ? days : days - 146096) / 146097)) * 146097,
    year = Math.floor((dote - dote / 1460 + dote / 36524 - dote / 146096) / 365) + era,
    return [year, days - Math.floor(year * 365 + year / 4 - year / 100 + year / 400)];
}

const [year, doty] = unix2doty(Date.now());
```

```

console.log(
  `${year.toString().padStart(4, "0")}.${$[
    (day = Math.floor(doty)).toString().padStart(3, "0")].$[
    (Math.round((doty - day) * 1e5)).toString().padStart(5, "0")]}+0`
);

```

2023+221.59651+0

Julia

unix

unix2doty

```

function unix2doty(s=0, ms=0)
    days = s / 86400 + ms / 86400000 + 719468
    dote = days - (era = floor((days >= 0 ? days : days - 146096) / 146097)) * 146097
    year = Int(floor((dote - dote / 1460 + dote / 36524 - dote / 146096) / 365) + era * 40)
    year, days - floor(year * 365 + year / 4 - year / 100 + year / 400)
end

y, d = unix2doty(time())
day = Int(floor(d))
"${lpad(y, 4, '0')}.${lpad(day, 3, '0')}.${lpad(Int(round((d - day) * 1e5)), 5, '0')}.+0"

```

"2023+221.59666+0"

Python

unix2doty

```

from time import time

def unix2doty(s=0, ms=0):
    days = s / 86400 + ms / 86400000 + 719468
    dote = days - (era := (days if days >= 0 else days - 146096) // 146097) * 146097
    year = int((dote - dote / 1460 + dote / 36524 - dote / 146096) // 365 + era * 400)
    return year, days - (year * 365 + year / 4 - year / 100 + year / 400).__floor__()

```

```
y, d = unix2doty(time())
f"{y:>04}+{(day := d.__floor__()):>03}.{round((d - day) * 1e5):>05}+0"
```

```
'2023+221.59677+0'
```

R

unix2doty

```
unix2doty <- function(s = 0, ms = 0) {
  days = s / 86400 + ms / 86400000 + 719468
  dote = days - (era = floor(ifelse(days >= 0, days, days - 146096) / 146097)) * 146097
  year = floor((dote - dote / 1460 + dote / 36524 - dote / 146096) / 365) + era * 400
  c(year, days - floor(year * 365 + year / 4 - year / 100 + year / 400))
}

yd <- unix2doty(as.numeric(Sys.time()))

paste0(sprintf("%04d", yd[1]), "+",
  sprintf("%03d", (day = floor(yd[2]))), ".",
  sprintf("%05d", round((yd[2] - day) * 1e5)), "+0"
)
```

Unable to display output for mime type(s): text/html

Lua

```
function unix2doty(ms)
  local days = ms / 86400000 + 719468
  local era = (days >= 0 and days or days - 146096) // 146097
  local dote = days - era * 146097
  local year = math.floor((dote - dote / 1460 + dote / 36524 - dote / 146096) / 365) + era
  return math.floor(year), days - math.floor(year * 365 + year / 4 - year / 100 + year / 400)
end

print(unix2doty(0))
```

CopyQ

4.6.4 Building timestamps

Example 4.13.

53

unix2deco

```
function unix2deco(ms = 0) {  
  const [year, doty] = unix2doty(ms);  
  return `${year.toString().padStart(4, "0")}+${  
    (day = Math.floor(doty)).toString().padStart(3, "0")}.${  
    (Math.round((doty - day) * 1e5)).toString().padStart(5, "0")}+0`  
};  
  
console.log(unix2deco())
```

1969+306.00000+0

Julia

unix

unix2deco

```
function unix2deco(s=0, ms=0)  
  y, d = unix2doty(time())  
  day = Int(floor(d))  
  "$(@lpad(y, 4, '0'))+$(@lpad(day, 3, '0')).$(@lpad(Int(round((d - day) * 1e5)), 5, '0'))+  
end  
  
unix2deco()
```

"2023+221.59666+0"

Python

unix2deco

```
from time import time  
  
def unix2deco(s=0, ms=0):  
  y, d = unix2doty(time())  
  return f"{y:>04}+{(day := d.__floor__():>03)}.{{round((d - day) * 1e5):>05}}+0"
```

```
unix2deco()
```

```
'2023+221.59677+0'
```

R

unix2deco

```
unix2deco <- function(s = 0, ms = 0) {  
  yd <- unix2deco(as.numeric(Sys.time()))  
  paste0(sprintf("%04d", yd[1]), "+",  
          sprintf("%03d", (day = floor(yd[2]))), ".",  
          sprintf("%05d", round((yd[2] - day) * 1e5)), "+0"  
  )  
}  
  
unix2deco()
```

4.6.5 Parsing timestamps

To extract the components of a `Decalendar` timestamp, we can use the `parse_dec` function in Example 4.8. Parsing timestamps is the first step before any later processes such as timestamp arithmetic or conversion between timestamp formats. The `parse_dec` function returns a year, a `doty`, and a fractional day time zone offset. The year and time zone offset can be omitted in the timestamp provided to `parse_dec`. If not specified in the timestamp, the year is the current year and the time zone offset is 0.

Example 4.14.

JavaScript

parse_dec

```
function parse_dec(timestamp = "1969+306.00000Z") {  
  const arr = timestamp.toString().split(/(?=[+-]| [a-zA-Z])/, 3);  
  switch (arr.length) {  
    case 1: return [unix2doty(Date.now())[0], parseFloat(arr[0]), 0];  
    case 2: return (/^[a-zA-Z]+$/).test(arr[1])
```

```

        ? [unix2doty(Date.now())[0], parseFloat(arr[0]), zone2hour(arr[1]) / 24]
        : [parseInt(arr[0]), parseFloat(arr[1]), 0];
    };
    return [parseInt(arr[0]), parseFloat(arr[1]), /^[a-zA-Z]+$/.test(arr[2])
        ? zone2hour(arr[2]) / 24
        : parseFloat(arr[2].replace(/([+-])/, "$1\."))];
}

console.log(parse_dec());

```

[1969, 306, 0]

5 Dot formats

The stamps shown above are in the decimal days of the year (.y) format, which is the main Decalendar format. In addition to the .y format, there are 2 other supplemental **datetime** formats, which are based on decimal days of the month (decc), and decimal days of the week (.w). Table 9 summarizes the three decimal day-of-the (dot or .) formats:

Table 9

Click to toggle table expansion

Table 9: The three dot formats

| Day of the | . | General Form | Specific Example |
|------------|---|-----------------|------------------|
| Year | y | year±day.day±z | 1999+365.500-3 |
| Month | m | year±m±dd.day±z | 1999+B+29.500-3 |
| Week | w | year±ww±d.day±z | 1999+52+5.500-3 |

In Table 9, day is the 3-digit day of the year (doty) number, dd is the 2-digit day of the month (dotm) number, d is the 1-digit day of the week (dotw) number, and .day is the time in mils.

5.1 The .m format

The `m` in the `.m` format is the 1-digit month number and is the double-digit `dotm`. To fit all of the months in a single digit, `m` is in [hexadecimal](#) form (Base16 encoded). This means that the first 10 months are represented by the numbers 0 through 9 ([zero-based numbering](#)) while the last two months of the year are represented by the letters “A” and “B” instead of numbers. The `.m` format is similar to the [ISO8601 calendar date](#) format (year-mm-dd).

The [ordinal numerals](#) of September, October, November, and December in `Decalendar` (Sep=7th, Oct=8th, Nov=9th, Dec=10th) match the [numeral prefixes](#) in their names (Sep=7, Oct=8, Nov=9, Dec=10). The `m` value of a month is based on its cardinal number in `Decalendar`, which is 1 less than its ordinal number (Sep=6, Oct=7, Nov=8, Dec=9).

To convert a double-digit Gregorian calendar month number (`mm`) into a single-digit `Decalendar` `m` value, we subtract 3 if `mm` is greater than 2, add 9 if not, as shown in Equation 16, and then encode into hexadecimal (Base16). To do the inverse (convert `m` to `mm`), we decode from hexadecimal, add 3 to `m` values less than 10 and subtract 9 from other `m` values, as shown in Equation 17. After hexadecimal encoding, January is represented by A and February is represented by B (mnemonic: `jAn`=January, `feB`=February).

$$m = \begin{cases} mm - 3 & \text{if } month > 2; \\ mm + 9 & \text{otherwise.} \end{cases} \quad (16)$$

$$m = \begin{cases} month + 3 & \text{if } month < 10; \\ month - 9 & \text{otherwise.} \end{cases} \quad (17)$$

5.2 The decw format

The week number in the `decw` format, `ww`, ranges from 0 to 53 or -54 to -1. Weeks in the `decw` format start from Sunday. Table 10 shows the possible `dotw` values, which range from 0 to 6 or -7 to -1.

Table 10

Click to toggle table expansion

Table 10: The weeks in the **decw** format

| Day | Pos | Neg |
|-----------|-----|-----|
| Sunday | 0 | -7 |
| Monday | 1 | -6 |
| Tuesday | 2 | -5 |
| Wednesday | 3 | -4 |
| Thursday | 4 | -3 |
| Friday | 5 | -2 |
| Saturday | 6 | -1 |

5.3 Dot format examples

Table 11 builds on the example from Section 3 to compare all three `.` formats. The 3 `.` formats differ only in their approach to the date, not the time. Therefore, the times below are all shown to 1-digit **dime** precision (same as time zones) instead of the typical 3-digit **mil** precision. In Mexico City, the time is **+5-3** or **-5-3**, while the time in London is **+8+0** or **-2+0** and time in Tokyo is **+2+4** or **-8+4**.

Table 11

Click to toggle table expansion

Table 11: The time in Mexico City, London, and Tokyo in all three dot formats

| Day of the | . | Mexico City | London | Tokyo |
|------------|---|---------------|---------------|---------------|
| Year | y | 1999+365.5-3 | 1999+365.8+0 | 2000+000.2+4 |
| Year | y | 2000-001.5-3 | 2000-001.2+0 | 2001-365.8+4 |
| Month | m | 1999+B+29.5-3 | 1999+B+29.8+0 | 2000+0+00.2+4 |
| Month | m | 2000-1-01.5-3 | 2000-1-01.2+0 | 2001-C-31.8+4 |
| Week | w | 1999+52+2.5-3 | 1999+52+2.8+0 | 2000+00+3.2+4 |
| Week | w | 2000-01-5.5-3 | 2000-01-5.2+0 | 2001-53-4.8+4 |

In Table 11, the `.m` format tells us that the month in Tokyo is January (**Month 0**) and the month in Mexico City and London is December (**Month B**). We could say the `.m` dates in

Mexico City and London as “Year 1999 Month B Day 29” or “Year 1999 Month -1 Day -1” and the Tokyo date as “Year 2000 Month 0 Day 0” or “Year 2000 Month -C Day -31”.

The **decw** format always starts the year with **Week 0**, but the year can start on any day of the week. Table 11 shows that the year 2000 starts on a Saturday (**Week 0 Day 6**). The **decw** dates in Mexico City and London could be said “Year 1999 Week 52 Day 2” or “Year 1999 Week -1 Day -5”, while the date in Tokyo could be pronounced “Year 2000 Week 0 Day 3” or “Year 2000 Week -52 Day -4” in Tokyo.

In contrast to the **.m** and the **decw** formats, the dates in the **.y** format are one character shorter and a little easier to say. The spoken form of the **.y** date in Mexico City and London is “Year 1999 Day 365” or “Year 1999 Day -1” and the spoken form of the Tokyo date is “Year 2000 Day 0” or “Year 2000 Day -365”.

5.4 Deks

Even though it provides formats for months and weeks, **Decalendar** envisions a world in which these units are replaced by **deks**. In terms of scale, **deks** are somewhere between a week and a month, precisely half a day less than a week and a half (1.5 weeks - 0.5 days) and approximately a third of month. **Deks** could provide the functionality of both weeks and months if we followed a **dekly** schedule instead of **weekly** and **monthly** schedules. The transition to a **dekly** schedule would be a massive undertaking, but could start with the creation of the digital infrastructure needed for the new system. Every desktop and mobile application that uses dates could be adapted to optionally use **deks** instead of weeks and months.

5.4.1 Days of the dek

A major difficulty with the Gregorian calendar is that the date is disconnected from the day of the week. In contrast, the day of the **dek** (**dotd**) is simply the last digit of the day number in the **.y** format. For example, the first day of the year (**Day 0**) is always a **Nulday**, the last day of common years (**Day 364**) is always an **Quaday**, and the last day of leap years (**Day 365**) is always a **Penday**. The day number allows us to distinguish workdays from restdays. **Decalendar** defines **Triday**, **Quaday**, **Octday**, and **Ennday** as restdays, which means that days with numbers that end in 3, 4, 8, or 9 are days off from work and school. Each **dek** consists of 2 **pents** (**pentadays**), each **pent** has 3 workdays called the **trep** (**trepalium**) and 2 restdays called the **pentend**. In total, there are 219 workdays and 146 restdays in a **Decalendar** year, not counting the only obligatory holiday, Leap Day (**Day 365**).

5.4.2 Workdays

The Gregorian calendar has many more workdays, 260 in common years and 261 in leap year. Despite having many fewer workdays and many more restdays, workers following **Decalendar**

would actually spent slightly more time at work overall, because the **Decalendar** workday goes from **Dot 3** to **Dot 7** and thus is 4 **dimes** (9.6 hours) long, 6.6 **cents** (96 minutes) longer than the typical 9-to-5 work schedule (**Dot 375** to **Dot 7083**). In other words, this work schedule starts 75 **mils** (1.8 hours) earlier than 9AM (**Dot 375**) and ends 8.3 **mils** (12 minutes) earlier than 5PM (**Dot 7083**). In a typical 40-hour workweek, workers spend 23.80952381 **cents** per day at work on average, which adds up to 8.6 **deks** ($260 \times 8 / 240$) per common year and 8.7 **deks** ($261 \times 8 \div 240$) per leap year. In contrast, workers following **Decalendar** spend 24 **cents** per day at work on average, which totals up to 87.6 **days** ($219 \times .4$) spent at work every year. The default approach of **Decalendar** is to compensate for having more restdays with longer workdays.

5.4.3 Schedules

Pently schedules

If necessary, the length of the workday and the number of workdays in the **dek** can be adjusted according to different schedules. As mentioned above, each half of the **dek** is called a **pent**. Each **pent** can have its own **pently** schedule. The expectation is that workers will work for 12 **dimes** per **pent**. It is possible to split those 12 **dimes** over the course of 5, 4, 3, or 2 days in each **pent**. Table 12 displays how the number of workdays and restdays in a **pent** affects the start time, end time, and duration of the workday. The different **pently** schedules are named after the number of workdays per **pent**. People can switch between **pently** schedules every **pent** as needed, but unless there is a compelling reason to follow a different **pently** schedule, everyone should follow the **Schedule 3** by default. **Schedule 3** has 3 workdays and 2 restdays in each **pent**. Each **Schedule 3** workday starts at **Dot 3**, ends at **Dot 7**, and lasts 4 **dimes**.

Table 12

| Click to toggle table expansion | | | | | |
|---|----------|----------|-------|-----|----------|
| Table 12: The characteristics of the pently schedules | | | | | |
| Schedule | Workdays | Restdays | Start | End | Duration |
| 2 | 2 | 3 | .2 | .8 | .6 |
| 3 | 3 | 2 | .3 | .7 | .4 |
| 4 | 4 | 1 | .35 | .65 | .3 |
| 5 | 5 | 0 | .38 | .62 | .24 |

Daily schedules

Decalendar recommends waking up at **Dot 2** and going to bed at **Dot 8**. This recommendation allots 4 **dimes** (9.6 hours) for falling asleep and sleeping. To keep daily schedules symmetrical, the time spent awake should be split evenly before and after work. People following **Schedule 3** would thus have 10 **cents** (2.4 hours) to prepare for work and another 10 **cents** to prepare for bed. Table 13 shows the recommended **Schedule 3** daily schedule. **Schedule 4** and **Schedule 5** allot even more time, 15 **cents** (3.6 hours) and 18 **cents** (4.32 hours), respectively, for before-work and after-work activities. The recommended sleep schedule does not fit well with **Schedule 2**, but this incompatibility does not have to result in a sleep deficit. If the **Schedule 2** workdays are not consecutive, people following **Schedule 2** can catch up on sleep on their days off by going to bed early before and sleeping in after every workday.

Table 13

| Click to toggle table expansion | | | |
|---------------------------------|-----|----------|------------------------------|
| Table 13: The workday schedule | | | |
| Start | End | Duration | Description |
| .2 | .3 | .1 | Wake up and prepare for work |
| .3 | .7 | .4 | Work |
| .7 | .8 | .1 | End work and prepare for bed |
| .8 | .2 | .4 | Go to bed and sleep |

5.5 Subyear units

In addition to serving as a part of the Gregorian date coordinate system described above, months can also indicate the current season or quarter. **Deks** can also serve as indicator of subyear units like seasons.

5.5.1 Seasons

We can use Table 5 to convert any Gregorian calendar date to a positive **doty** number. This is especially useful for variable dates that have to be converted every year. For example, the dates of the solstices, the longest and shortest days of the year, vary slightly every year. Instead of calculating the exact **doty** number of the solstices ourselves we could translate from existing Gregorian calendar dates. Solstices and equinoxes (the points in between the solstices) are the basis of the some holidays, such as **Nowruz**.

The dates of the solstices and the equinoxes can be used as definitions of the seasons. Each season has its opposite. The opposite of Spring is Fall and the opposite of Summer is Winter. These opposites are always occurring simultaneously, one opposing season in the Northern hemisphere and the other in the Southern hemisphere. Table 14 lists the opposing seasons in the North and South columns (which correspond to the Northern and Southern hemispheres) and the approximate dates of the solstices and the equinoxes that mark the start of each season.

Table 14

Click to toggle table expansion

Table 14: Solstice and equinox Gregorian calendar and **doty** dates

| Code | North | South | doty | dotm | Date | Event |
|------|--------|--------|-------------|-------------|--------------|--------------------|
| S0 | Spring | Fall | 19 | 0+19 | March 20 | Northward Equinox |
| S1 | Summer | Winter | 111 | 3+19 | June 20 | Northward Solstice |
| S2 | Fall | Spring | 205 | 6+21 | September 22 | Southward Equinox |
| S3 | Winter | Summer | 295 | 9+20 | December 21 | Southward Solstice |

Using the information in Table 14, we can group the **deks** and **pents** in a year according to the seasons in which they occur. We identify **deks** using the first 2 digits of the 3-digit day number of any day in that **dek**. The **pent** number is twice the **dek** number plus one if the **dotd** is greater than 4 ($dek \cdot 2 + dotd > 4$). For example, Day 19 is the last day in Dek 1 and Pent 3, while Day 111 is the second day in Dek 11 and Pent 22.

We can round up the start of the first season and round down the start of the second season to obtain the division of **pents** by season as summarized in Table 15. It is important to note that the last season starts in Pent 59 of one year and ends with Pent 3 of the subsequent year. In common years, each season in Table 15 has 18 **pents** (90 days), except for the season in the second row, which has 19 **pents** (95 days). In leap years, the season in the last row of Table 15 has 18.2 **pents** (91 days).

Table 15

Click to toggle table expansion

Table 15: The **pents** that begin and end each season

| Code | North | South | First | Last | Duration |
|------|--------|--------|-------|------|----------|
| S0 | Spring | Fall | 4 | 21 | 18 |
| S1 | Summer | Winter | 22 | 40 | 19 |
| S2 | Fall | Spring | 41 | 58 | 18 |
| S3 | Winter | Summer | 59 | 3 | 18 |

5.5.2 Qops, Delts, Eps and Waus

Qops

In contrast to the variable length of seasons, other **Decalendar** units are constant length. Of these constant length units, **qops** (**qoppas**,) are most like seasons. **Qops** divide the year into four parts, but unlike seasons, **qops** do not include **Pent 72**, the last **pent** of the year. **Pent 72** is not included in the last **qop** so that each **qop** is 9 **deks** and 90 days long. The omission of **Dek 36** also maintains the pattern of alternating even and odd numbers in each row. This omission leaves out only 5 or 6 days per year, because **Dek 36** overlaps with **Dek 0**. Table 16 shows the division of **deks** by **qop**.

Table 16

Click to toggle table expansion

Table 16: The **deks** that begin and end each **qop**

| Code | First | Last |
|------|-------|------|
| Q0 | 0 | 8 |
| Q1 | 9 | 17 |
| Q2 | 18 | 26 |
| Q3 | 27 | 35 |

Delts

In addition to **qops** shown above, **Decalendar** describes 3 other similar units called **delts** (**deltas**,), **eps** (**epsilons**,), and **waus** (). These units do not leave out as many days in

each year, because they split the year by day, rather than by **dek**. **Delts**, **eps**, and **wau** split the year into 4, 5, and 6 parts, respectively. **Delts** are 91 days long and leave out one day at the end of common years and two days at the end of leap years. Just as above, leaving out a small number of days at the end of the year preserves a pattern that can be useful for remembering the days on which **delts** start and end. Table 17 list the numbers of the days that begin and end each **delt**. In Table 16, not only do rows alternate between even and odd numbers, but the **delt** number is the last digit of both the start and the end day of the **delt**.

Table 17

Click to toggle table expansion

Table 17: The days that begin and end each **delt**

| Code | First | Last |
|------|-------|------|
| D0 | 0 | 90 |
| D1 | 91 | 181 |
| D2 | 182 | 272 |
| D3 | 273 | 363 |

Eps

Unlike **delts**, **eps** are 73 days long and do not leave out any days from common years. **Qops**, **delts**, and **eps** all leave out leap days in leap years. Table 18 list the numbers of the days that begin and end each **ep**.

Table 18

Click to toggle table expansion

Table 18: The days that begin and end each **ep**

| Code | First | Last |
|------|-------|------|
| E0 | 0 | 72 |
| E1 | 73 | 145 |
| E2 | 146 | 218 |
| E3 | 219 | 291 |

Waus

The only unit that can include the leap year is a **wau** (), which is 61 days long and follows a similar pattern as a **delt**, except the last **wau** in common years is 1 day short than all the others. Table 19 list the numbers of the days that begin and end each **wau**. As with **delts**, the **wau** number is the last digit of the numbers of its first and last day.

Table 19

Click to toggle table expansion

Table 19: The days that begin and end each **wau**

| Code | First | Last |
|------|-------|------|
| W0 | 0 | 60 |
| W1 | 61 | 121 |
| W2 | 122 | 182 |
| W3 | 183 | 243 |
| W4 | 244 | 304 |
| W5 | 305 | 365 |

All of the subyear unit codes can be preceded by a year and followed by a day number. The midpoint of common years is noon on the first day of **Delt 2**, **D2+00.5** or **+182.5**, and the midpoint of leap years is midnight of the first day of **Wau 3**, **W3+00.0** or **+183.0**. The first day of Spring in northern hemisphere and Fall in the southern hemisphere in the year 2000 is **2000S0+00** or **2000+020**, while the last day of this season is **2000S0+89** or **2000+109**. The subyear units are essentially date intervals, series of contiguous dates. **Decalendar** includes very powerful approaches to describing series of dates, times, and **stamps**.

6 Series

A single **doty** number, such as **Day 0**, implies a duration on 1 day. We can indicate a duration of multiple days by listing consecutive days in a **series**. A **series** consists of dates, times, or **stamps** separated by commas (,). The items in a **series** should all be of the same type. In other words, **series** should be homogeneous and not mix dates, times, and **stamps**. The first 3 days of the year in the form of a **series** would be written **0,1,2**, while the last three

days would be -3,-2,-1. The first half a day, from midnight to noon, could be written 0,.1,.2,.3,.4.

6.1 Slices

Instead of listing every single day in a **series**, we can “slice” from Day 0 up to but not including Day 3 by writing :3. Simple slices consist of a **start** and a **stop** separated by a colon (**start:stop**). When the **start** is omitted, slices begin at the first value, which in the context of a year is Day 0 and in the context of a day is midnight. Therefore, writing :3 is the same as writing 0:3, both represent the first 3 days of the year: 0,1,2. Using this approach, we can shorten the series 0,.1,.2,.3,.4 to :.5. If we omit the **stop**, instead of the **start**, we would “slice” up to and including the last value.

In the context of **doty** dates, omitting the **stop** value obtains all of the days in the year after the **start**, because the default **stop** is the number of days in the year (**n**). For example, the slice 3: has a **start** of Day 3 and a **stop** of **n**, and thus represents every day in the year except the first 3. The number of items we obtain from a slice is called a **span**. To calculate the **span**, we subtract the **start** from the **stop** ($stop - start$). In a common year, the **span** of 003: is $n - 3 = 362$, while in a leap year it would be $n - 3 = 363$. If both the **start** and the **stop** are omitted, every day is included ($span = n - 0$). Table 20 lists the seasons, **qops**, and **delt**s in the form of slices. The superscript plus sign () in Table 20 indicates a number that has to be incremented in leap years.

Table 20

Click to toggle table expansion

Table 20: The slices that represent the 4-part subyear units

| Index | Season | Qop | Delt |
|-------|---------|---------|---------|
| 0 | 20:110 | :90 | :91 |
| 1 | 110:205 | 90:180 | 91:182 |
| 2 | 205:354 | 180:270 | 182:273 |
| 3 | 295:385 | 270:360 | 273:364 |

6.2 Steps

The simple slices (**start:stop**) described above are a type of time **segment**, an unbroken time interval. To break up a simple slice into a non-consecutive **series**, we can add a **step**

value and create a **stepped slice** (**start:stop:step**). **Stepped slices** move in **step**-sized “steps” starting from **start**, skipping over *step* − 1 items with each “step”, keeping only items that are “stepped” on.

In other words, **stepped slices** keep items whose index (zero-based position) in the **slice** is evenly divisible by **step**. A **step** value of 1 keeps every item, because every index is divisible by 1, and a **step** of 2 keeps every other item, those with even-numbered indexes. **Day 0** and every other third day in the year thereafter (**Day 3**, **Day 6**, etc.) can be represented by the **slice ::3**.

To create a **series** of times on days throughout the year, we can use a **slice** with a **series** of **steps**. The **slice :365:1,1,3** represents all of the **Decalendar** workdays in a year. It is necessary to specify 365 as the **stop**, so that Leap Day (**Day 365**) is not included as a workday in leap years. Similarly, **3::1,4** is a **seq** that represents all of the regular restdays, not including the Leap Day holiday.

Stepped slices cannot be included in **series**, because both use commas (,) and it would not be possible to differentiate a **series** of **steps** from subsequent items in the **series**. The simple rule is that **slices** with more than 1 colon (:) cannot be part of a **series**. For example, **:365:1,1,3** is a **stepped slice** with a **series** of 3 **steps** rather than a **series** consisting of a **slice** and two numbers.

6.3 Spreads

To create **series** of consecutive items with breaks in between, it may be better to use a **spread** than a **slice**. Simple **spreads** consist of either a **start** and a **span** (**start>span**) separated by a greater-than sign (>) or a **stop** and a **span** (**stop<span**) separated by a less-than (<) sign. The default **start** and **stop** values are the same for both **slices** and **spreads**. We can **spread** forward from the default **start** to capture the first **span** days in a year. For example, the first 3 days in a year can be represented by the **spread >3**, which is synonymous with the **slice :3**. In this example, the **start** is 0, while the **stop** and the **span** are both 3. In addition to default **start** and **stop** values, **spreads** also have default **span** values. A **spread** that only uses default values (> or <) will include every day in the year (*span* = *n*). [Table 21](#) lists the seasons, **qops**, and **delts** in the form of **spreads**.

Table 21

Click to toggle table expansion

Table 21: The spreads that represent the 4-part subyear units

| Index | Season | Qop | Delt |
|-------|--------|--------|--------|
| 0 | 20>90 | >90 | >91 |
| 1 | 110>95 | 90>90 | 91>91 |
| 2 | 205>90 | 180>90 | 182>91 |
| 3 | 295>90 | 270>90 | 273>91 |

If we “spread” forward from a positive **start**, the default **span** is $n - \text{start}$. If we spread backward from a positive **stop**, the default **span** is **stop**. We can spread backward from the default **stop** to capture the last **span** days in a year. For example, <3 represents the last 3 days of any year. We could also use a negative **start** of -3, the third to last day of any year, to create the slice -3: and the spread -3>, both of which are synonymous with <3. One advantage of **spreads** over **slices** is the ability to access days from the end of a year without negative numbers. A **span** value of zero does not return any items. Negative **span** values reverse the direction of the first sign, turning **start** into **stop** and vice versa.

6.4 Splits

As with **stepped slices**, we can create non-consecutive **series** by “splitting” a **simple spread** (**start>span** or **stop<span**) into **split spread** (e.g. **start>span>split**) with a **split** value that works like the opposite of a **step**. While **steps** keep items that are “stepped” on, **splits** exclude items that are used to create the boundaries of the **splits**. The default **split** value is **span**, meaning that the entire **span** is included in one **split**.

A **split spread** with a **split** value of 1 (**start>span>1**) is the same as a **stepped slice** with a **step** value of 2 (**start:stop:2**). Split values greater than 1 but less than **span** will yield a **series** of **segments**. If **split** is zero (**start>span>0**), the **split spread** will not return any items. A negative **split** value reverses the direction of the second greater-than sign (**start>span>-2** and **start>span<2** are synonymous). This can be useful when providing a series of **split** values. Negative **split** values reverse the direction of a **split** and a **split** value of zero skips a **split**. Just like **stepped slices**, **split spreads** cannot be included in a **series**, because every **split** can have a **series** of values.

The direction of the second sign in **split spreads** determines whether we begin creating splits from the **start** (>) or the **stop** (<) of the **span**. If the first two values (**start** and **span** or **stop** and **span**) are blank, the direction of the first sign does not matter and the first two signs can be combined into a “much greater-than sign” (>>), a “much less-than sign” (<<), a diamond (<>), or simply an x. The split spreads <>4 and <>4 are synonymous; both skip every 5th day to create

groups of 4 days throughout the year starting with the first 4 days of the year >4 . Notably, 4 and 4 will always end with a **segment** containing the last 4 days of common years, $360:364$, $360>4$, or $364<4$, even in leap years, because partial **splits** are not allowed.

6.5 Spaces

The patterns described above require that **splits** are separated by the default **space** value of 1. We can specify a different **space** value in the form **start>span>split>space**. The **split spreads** $3>2$ and $3>2$ create 3-day **splits** separated by 2-day **spaces**. This is the pattern of workdays in the Decalendar system. The first **segment** of $3>2$ and $3>2$ can be written as $:3$, >3 , or $3<$, while the last **segment** is $360:363$, $360>3$, or $363<3$. The workdays in the first dek of $3>2$ and $3>2$ can be written as the following **series** of **segments**: $:4,5:8$, $>3,5>3$, or $3<,8<3$. Unlike **stepped slices** and **split spreads**, **simple slices** and **simple spreads** can be used in **series**.

A **space** value of 0 may also be useful. For example, **delt**s, **qop**s, **eps**, and **waus** can be summarized as **split spreads** as shown in Table 22. When **space** is zero, the direction of the third sign does not matter. The **split spreads** $61>0$, $61>0$, $61<0$, and $61<0$ all represents the **waus** in a year. **Waus** divide leap years evenly and **eps** divide common years evenly. Therefore, $x61>0$ and $x61<0$ can represent all of the **waus** in leap years, just like $x73>0$ and $x73<0$ can represent all of the **eps** in common years. The seasons can be described by a **spread** with a **series** of **splits** and a **space** of 0: $\gg90,95,90,90>0$.

Table 22

Click to toggle table expansion

Table 22: The spreads that represent the constant length subyear units

| Unit | Spread |
|------|--------|
| Delt | $91>0$ |
| Qop | $90>0$ |
| Ep | $73>0$ |
| Wau | $61>0$ |

If **space** is greater than zero and the second and third sign are pointing in opposite directions, the resulting time **segments** will overlap. The **split spreads** $>1>.4<.2$ and $<1<.4>.2$ both result in the same 4 overlapping time **segments**: $:.4$, $.2:.6$, $.4:.8$, $.6:1$. Negative values can be used in a **series** of **spaces** to temporarily reverse the direction and intersperse overlapping

and non-overlapping segments. The `split spread >1>.4<.2,-.1` yields two segments that overlap and one segment that does not overlap: `:.4`, `.2:.6`, `.6:1`.

Overlapping segments could be used to plan work shifts that require a hand-off between teams. The segments created by `>1>.4<.2` are shifted by two dimes in relation to each other and overlap by 2 dimes. If these segments are in Zone 0 time, they represent the normal workday (`.3:.7`) for Zone 3 (`:.4`), Zone 1 (`.2:.6`), Zone -1 (`.4:.8`), and Zone -3 (`.6:1`). Each of these 4 segments could represent a team working during the normal workday in their respective time zone. All but the last team would have two dimes of overlap with the subsequent team.

6.6 Sequential spreads and slices

Split spreads can be combined with other spreads into sequences called `seq spreads` (sequential spreads). The intuition behind `seq spreads` and is that each item in the first (outer) spread serves as a starting point for the second (inner) spread. The main use of `seq spreads` is to first “spread” across days and then “spread” across times in those days. We can combine `3>2`, a split spread that represents the Decalendar workdays, with `.3>.4`, a simple spread that provides the start and span of the Decalendar workday, to obtain `3>2>.3>.4`, a `seq spread` that represents the time spent at work in a Decalendar year.

In this `seq spread`, the `split` is the number of workdays (3), the space is the number of restdays (2), the second-to-last number is the start of the workday (`.3`) and the last number is the workday span (`.4`). The spread `3>2>.3>.4` first starts at midnight of each workday, then moves forward 3 dimes to the new start of Dot 3, and then “spreads” forward by a span of 4 dimes to the new stop of Dot 7. We could replace the start of the workday in `3>2>.3>.4` with the end of workday if we reverse the last sign: `3>2>.7<.4`, because `.3>.4` and `.7<.4` are synonymous.

We combine the two spreads with `>` because we want to move forward from the beginning of each workday, instead of backward to the previous day. If we combined `3>2` and `.3>.4` with `<`, the resulting spread `3>2<.3>.4` would move backward from midnight of each workday to Dot 7 of each previous day and then “spread” forward to Dot 1 of each workday. We may want to use such a mixed direction `seq spreads` when dealing with time zones. If we lived in Zone -3 and wanted to know how the workdays in Zone 4 translated into our time zone, we could take the spread `3>2>.3>.4` and move its start to 7 dimes earlier: `3>2<.4>.4`. `Seq spreads` enable such time zone conversions without the use of negative numbers.

The `seq slice` equivalent of `3>2>.3>.4` is `:365:1,1,3:.3:.7`. `Seq spreads` will always be a more succinct way for creating long consecutive sequences with breaks than `slices`. For example, to include a lunch break in the middle of work, we could simply add a `split` and a space to the `seq spread` above: `3>2>.3>.4>.18>.04`. To do the same with a `seq slice`, we have to create 17 steps of 0.01 and a step of .04: `:365:1,1,3:.3:.7:17*1%,4%`. Here, we are using the replication operator (`*`) to avoid writing 0.01 17 times and the percent operator (`%`) to

save a few characters, but even so the `seq slice` is not as concise as the `seq spread`. Table 23 shows each part of this schedule in the form of `simple slices` and `simple spreads`.

Table 23

Click to toggle table expansion

Table 23: A workday schedule with a lunch break

| slice | spread | spread | label |
|---------|---------|---------|-------|
| .30:.48 | .30>.18 | .48<.18 | work0 |
| .48:.52 | .48>.04 | .52<.04 | lunch |
| .52:.70 | .52>.18 | .70<.18 | work1 |

6.7 Pomodoro

Another real-life application of `spreads` can be to intersperse breaks in between periods of work as in the [Pomodoro technique](#). The times spent working and resting can vary, but a reasonable translation of the original Pomodoro into the `Declock` units would be to have each pomodoro consist of 17 mils of work and 3 mils of rest, with a 17 mil break after every 4 pomodoros. To repeat 16 pomodoros throughout the `Decalendar` workday, we could use the following `seq spread`: `.3>.7>.08>.02 .017>.003`. Here, we use the “very much greater-then sign” (`>`) instead of a combination of a “much greater-than sign” (`>`) and a greater-than sign (`>`). The pomodoro pattern is difficult to capture with a `slice` because we have to use `*` for the steps of the inner and the outer `slice`: `.3:.7:8*.01,.02::17*.001,.003`.

6.7.1 Replication operator

The replication operator (`*`) is very useful for replacing repetitive values. For example, to divide any year into six parts we could use the `spread 5*61,60 >0` to create 5 “splits” that are all 61 days long and one last “split” that is 60 days (60 days in a common year or 61 days in a leap year) long. The `*` helps us avoid the repetitiveness of writing `61,61,61,61,61,60 >0`. In addition to being used in the `split` and `space` of a `split spread` or the `step` of a `stepped slice`, the `*` can also be used in the `span` of a `split spread` or the `stop` of a `stepped slice` to indicate how many cycles of `splits` or `steps` we want to complete. For example, `>4*>5*61,60 >0` indicates that we want 4 years (the current year and the 3 subsequent years) “split” into 6 parts for a total of 24 parts. In other words, `4*` means that we want to stop cycling after completing four yearly cycles. We can read `4*` out loud as “four times” because it means we intend to go through the yearly cycle “four times”.

6.7.2 Percent, permil, and permyr operators

We can make the `seq spread` above even shorter by using the `per` operators: `%`, `‰`, and `‱`. Most of the values in `.3>2*>.08>.02 .017>.003` are either percents (`.01` or `1/100`) or permils (`.001` or `1/1000`) of a day, we can therefore rewrite this `seq spread` as `.3>2*>8%>2% 17‰>3‰`. It may be difficult to write the permil (`‰`) operator (hex: 2030, html: `‰`, vim: `%0`, compose: `%o`), because it does not appear on a typical keyboard, so it is also possible to write `.3>2*>8%>2% 17‰>3‰` as `.3>2*>8%>2% 17m>3m`, with the letter `m`, which stands for mil, replacing `‰`. In addition to the percent (`%`) and permil (`‰`) operators, there is also the permyr (`‱`) operator, which is short for permyriad and represents Declock phrases (10¹⁰).

6.7.3 Pently schedules as seq spreads, splices, and sleds

We can use `seq spreads` to describe the [pentlyschedules](#). Schedule 5 is particularly interesting because it includes all of the days of the year. `Spreads` that include every item can be written as `>` or `<`, but `seq spreads` must have at least 5 values. The Schedule 5 `seq spread` `.38>.24` has 4 blank values, which represent the default `start`, `span`, `split`, and `space`. Similarly, the Schedule 4 `seq spread` `4 .35>.3` has 3 blank values, which represent the default `start`, `span`, and `space`. The Schedule 2 and Schedule 3 `seq spreads`, `2>3>.2>.6` and `3>2>.3>.4`, respectively, only have 2 blank values, the `start` and the `span`. As an alternative to `seq spreads` and `seq slices`, we can use `slice-spread` hybrids called `sleds` or `spread-slice` hybrids called `splices`. `Sleds` put the `slice` elements first (`start:stop:step:start>span>split>space`), while `splices` start with the `spread` elements (`start>span>split>space>start:stop:step`). The `pentlyschedules` are easiest to write as `seq spreads` and `splices`, as shown in Table 24.

Table 24

| Click to toggle table expansion | | | | |
|---|------------|-----------|-------------------|--------------------|
| Table 24: The seq spreads, splices, and sleds that represent the 4 pently schedules | | | | |
| Schedule | seq spread | splice | sled | seq slice |
| 2 | 2>3>.2>.6 | 2>3>.2:.8 | :365:1,4:.2>.6 | :365:1,4:.2:.8 |
| 3 | 3>2>.3>.4 | 3>2>.3:.7 | :365:1,1,3:.3>.4 | :365:1,1,3:.3:.7 |
| 4 | 4 .35>.3 | 4 .35:.65 | :365:3*1,2:.35>.3 | :365:3*1,2:.35:.65 |
| 5 | .38>.24 | .38:.62 | :365:..38>.24 | :365:..38:.62 |

6.8 Yearly transition

6.8.1 Common years

The **pently** schedules are important for the transition between years. In common years, the last **dek** of the year (**Dek 36**) contains the last **pent** of the current year (**Pent 72**), and the first **pent** of the subsequent year (**Pent 0**). If these two **pents** follow the default **pently** schedule, **Schedule 3**, the natural rhythm of 3 workdays followed by 2 rest days continues uninterrupted. Table 25 shows the positive and negative **doty** numbers, names, and types (work or rest) of the days in **Dek 36** in common years. Notably, while the positive **doty** numbers continue counting past the end of the year, the negative **doty** numbers of the current year turn into the positive **doty** numbers of the subsequent year. The negative **doty** numbers in **Dek 36** can thus serve as the bridge from the one year to the next.

Table 25

Click to toggle table expansion

Table 25: The days in Dek 36 in common years

| Pos | Neg | Name | Type |
|-----|-----|--------|------|
| 360 | -5 | Nulday | work |
| 361 | -4 | Unoday | work |
| 362 | -3 | Duoday | work |
| 363 | -2 | Triday | rest |
| 364 | -1 | Quaday | rest |
| 365 | 0 | Nulday | work |
| 366 | 1 | Unoday | work |
| 367 | 2 | Duoday | work |
| 368 | 3 | Triday | rest |
| 369 | 4 | Quaday | rest |

6.8.2 Leap years

In leap years, **Dek 36** contains the last 6 days of the current year and the first 4 days of the subsequent year. Interestingly, **Dek 36** always contain 6 workdays and 4 restdays, just like every other **dek**, but in leaps years these days do not follow the typical order of **Schedule 3**. Leap years end in 3 restdays instead of 2, because Leap Day (**Day 365**) is always a holiday. Leap day is always a **Penday** and always followed by a **Nulday**. After Leap Day, the normal

rhythm of **Schedule 3** resumes. Table 26 shows the positive and negative **doty** numbers of the days in Dek 36 in leap years, as well as their names and their types (work or rest).

Table 26

Click to toggle table expansion

Table 26: The days in Dek 36 in leap years

| Pos | Neg | Name | Type |
|-----|-----|--------|------|
| 360 | -6 | Nulday | work |
| 361 | -5 | Unoday | work |
| 362 | -4 | Duoday | work |
| 363 | -3 | Triday | rest |
| 364 | -2 | Quaday | rest |
| 365 | -1 | Penday | rest |
| 366 | 0 | Nulday | work |
| 367 | 1 | Unoday | work |
| 368 | 2 | Duoday | work |
| 369 | 3 | Triday | rest |

6.9 Holidays

Leap Day is a important holiday because it occurs only once every four years except for years that start centuries not divisible by 400 and it results in the only time when there are 3 consecutive restdays in **Decalendar**. Another **Decalendar** holiday that only occurs in leap years is Dyad Day. At noon on Dyad Day, the positive and negative **.y** format **stamps** are the same (+183.5 and -183.5), meaning that 183.5 days have passed in the year and 183.5 days remain in the year. Unlike Leap Day, Dyad Day is naturally a day off. Many Gregorian calendar holidays just so happen to also fall on the first day of a **pent** (Nulday or Quaday). Table 27 lists 8 such holidays and their **doty**, **dotm**, and Gregorian calendar dates.

Table 27

Click to toggle table expansion

Table 27: Gregorian calendar holidays that happen to fall on **Decalendar** restdays

| Name | doty | dotm | date |
|------------------|------|------|-------------|
| Cinco de Mayo | 65 | 2+04 | May 5 |
| Flag Day | 105 | 3+13 | June 14 |
| Juneteenth Day | 110 | 3+18 | June 19 |
| Independence Day | 125 | 4+03 | July 4 |
| All Saints' Day | 245 | 8+00 | November 1 |
| Veterans' Day | 255 | 8+10 | November 11 |
| Boxing Day | 300 | 9+25 | December 26 |
| New Year's Eve | 305 | 9+31 | December 31 |

Any holiday with a fixed (rather than floating) date in the Gregorian calendar can easily be added to **Decalendar**. Holidays with floating dates do not follow easily recognizable patterns. **Decalendar** recommends redefining such dates to always be on the same **doty** every year. For example, November 25 (**Day** 269) is a sensible fixed date for Thanksgiving, because it is exactly 30 days before Christmas (December 25, **Day** 299) and falls on a **Decalendar** restday. When assigning fixed dates to floating date holidays, we should choose **Decalendar** restdays to avoid disrupting the normal rhythm of the **pently** schedules. Instead of gaining days off because of holidays, workers should gain additional time off from their employers. In the United States, the 11 federal holidays (88 hours = 3.6 dimes) would translate to 9 **Schedule** 3 days offs (3.6 dimes).

7 References

Hinnant, Howard. 2014. "Chrono-Compatible Low-Level Date Algorithms." http://howardhinnant.github.io/date_algorithms.html.