

Input:

C : regularization parameter

tol : numerical tolerance

max_passes : max # of times to iterate over α 's without changing

$(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})$: training data

Output:

$\alpha \in \mathbb{R}^m$: Lagrange multipliers for solution

$b \in \mathbb{R}$: threshold for solution

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◦ Initialize $\alpha_i = 0, \forall i, \quad b = 0$.

◦ Initialize $passes = 0$.

◦ **for** $i = 1, \dots, m$,

◦ Calculate $E_i = f(x^{(i)}) - y^{(i)}$ using (2).

◦ **if** $((y^{(i)} E_i < -tol \quad \&\& \quad \alpha_i < C) \parallel (y^{(i)} E_i > tol \quad \&\& \quad \alpha_i > 0))$

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$$f(x) = \langle \omega, x \rangle + b$$

$$\omega = \sum_{i=1}^m \alpha_i y^{(i)} x^{(i)}$$

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- Select $j \neq i$ randomly.

- Calculate $E_j = f(x^{(j)}) - y^{(j)}$ using (2).

- Save old α 's: $\alpha_i^{(\text{old})} = \alpha_i, \alpha_j^{(\text{old})} = \alpha_j$.

- Compute L and H by (10) or (11).

- if** $(L == H)$

- continue** to next i .

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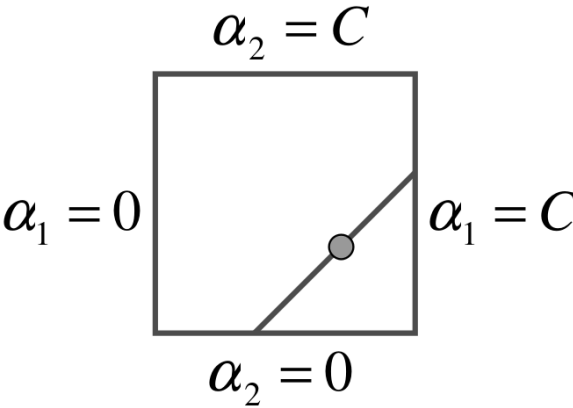
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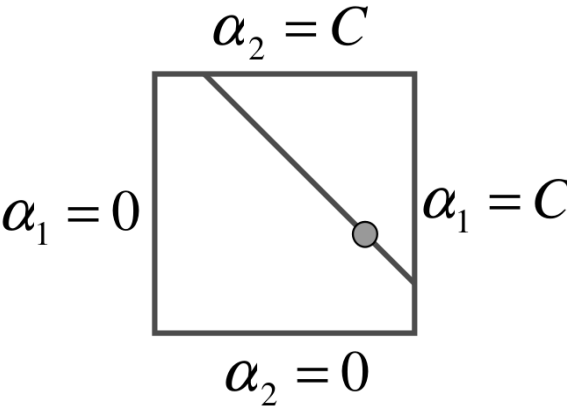
$$\omega = \sum_{i=1}^m \alpha_i y^{(i)} x^{(i)}$$

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$$\sum_{i=1}^m \alpha_i y^{(i)} = 0$$



$$y_1 \neq y_2 \Rightarrow \alpha_1 - \alpha_2 = \gamma$$



$$y_1 = y_2 \Rightarrow \alpha_1 + \alpha_2 = \gamma$$

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- Compute and clip new value for α_j

$$\alpha_j := \begin{cases} H & \text{if } \alpha_j > H \\ \alpha_j & \text{if } L \leq \alpha_j \leq H \\ L & \text{if } \alpha_j < L. \end{cases}$$

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- Compute and clip new value for α_j

- if** $(|\alpha_j - \alpha_j^{(\text{old})}| < 10^{-5})$

- continue** to next i .

- Determine value for α_i

$$\sum_{i=1}^m \alpha_i y^{(i)} = 0$$

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- Compute b

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- continue** to next i .

- Determine value for α_i

- Compute b

- $num_changed_alphas := num_changed_alphas + 1$.

- end if**

- end for**

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- Initialize $\alpha_i = 0, \forall i, \quad b = 0$.

- Initialize $passes = 0$.

- **while** ($passes < max_passes$)

- $num_changed_alphas = 0$.

- **for** $i = 1, \dots, m$,

- Calculate $E_i = f(x^{(i)}) - y^{(i)}$ using (2).

- **if** ($(y^{(i)} E_i < -tol \quad \&\& \quad \alpha_i < C) \parallel (y^{(i)} E_i > tol \quad \&\& \quad \alpha_i > 0)$)

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- Compute L and H by (10) or (11).

- **if** ($L == H$)

- continue** to next i .

- Compute and clip new value for α_j

- **if** ($|\alpha_j - \alpha_j^{(old)}| < 10^{-5}$)

- continue** to next i .

- Determine value for α_i

- Compute b

- $num_changed_alphas := num_changed_alphas + 1$.

- **end if**

- **end for**

- **if** ($num_changed_alphas == 0$)

- $passes := passes + 1$

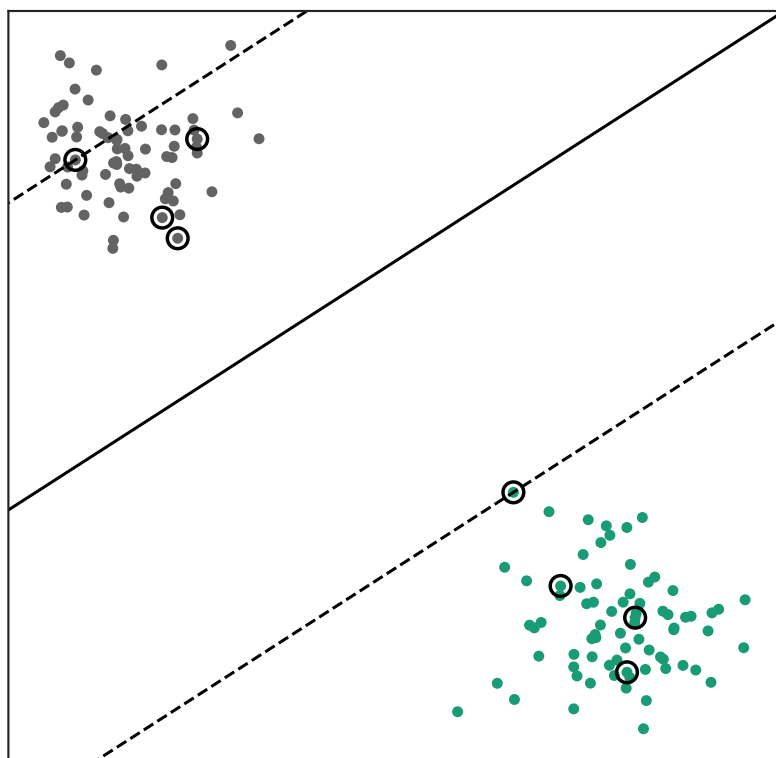
- **else**

- $passes := 0$

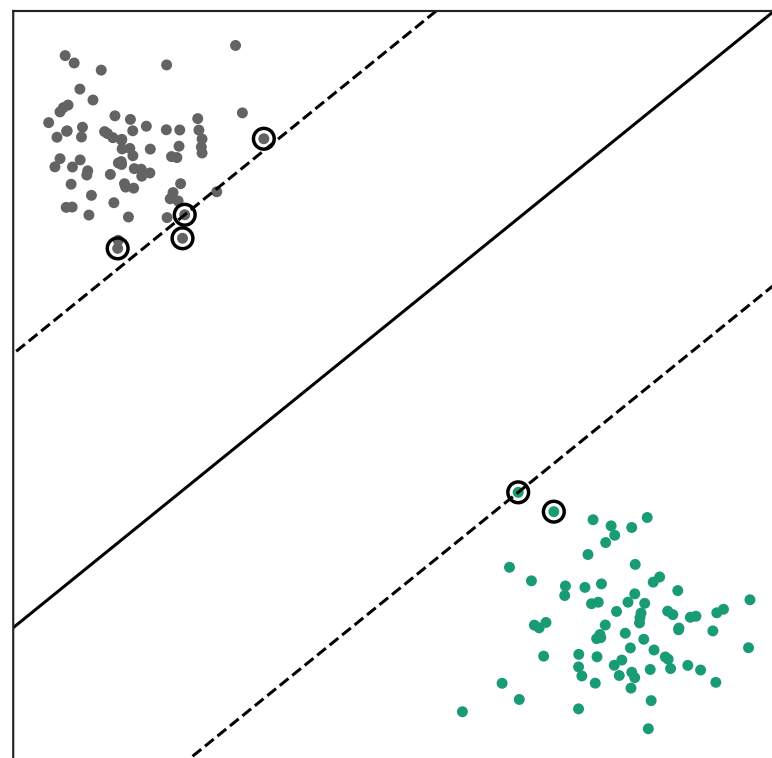
- **end while**

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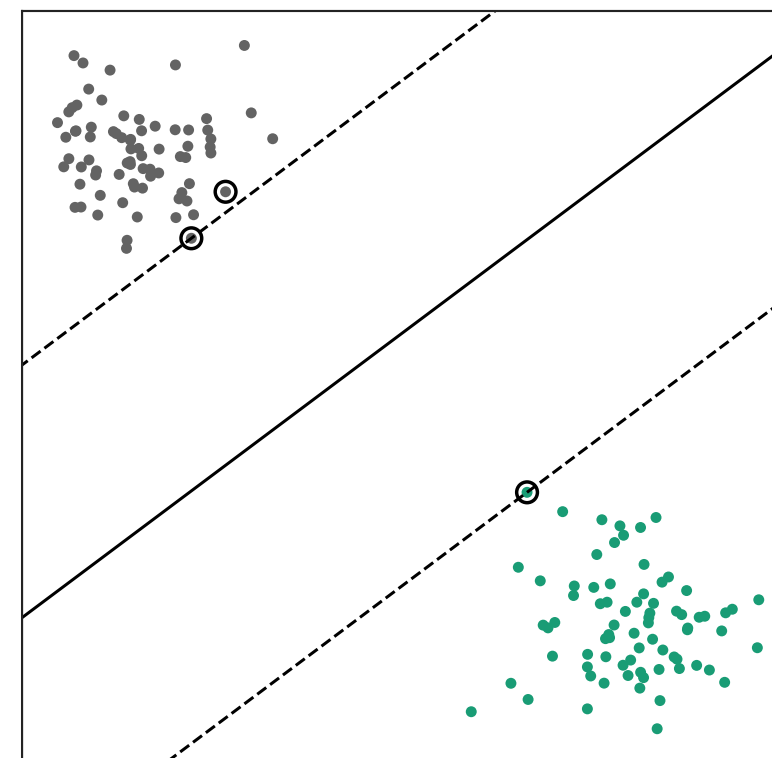
$$\omega = \sum_{i=1}^m \alpha_i y^{(i)} x^{(i)}$$



max_passes = 1



max_passes = 15



max_passes = 30