Read in the following dictionary:

```
+6.00x_1 -2.00x_2 +2.00x_3 -6.00x_4 -5.00x_5 -9.00x_6 +10.00x_7 -10.00x_8
x_9
x_{10}
      -3.0
              +3.00x_1 -1.00x_2 +8.00x_3 -7.00x_4 -5.00x_5 -8.00x_6 +5.00x_7 -4.00x_8
       8.0
              +2.00x_1 +10.00x_2 -1.00x_3
                                                    -10.00x_5 -6.00x_6 +8.00x_7
x_{11}
      -14.0
              +6.00x_1 +8.00x_2 +2.00x_3 +4.00x_4 +7.00x_5 +4.00x_6 -2.00x_7 +1.00x_8
x_{12}
      25.0
              +1.00x_1 -9.00x_2 -10.00x_3 +1.00x_4 +4.00x_5 +2.00x_6 -4.00x_7
x_{13}
                                           -1.00x_4 -1.00x_5 -3.00x_6 -3.00x_7
       0.0
              +1.00x_1 +1.00x_2
 z
```

0.1 Initialization Phase: Dual Problem Solving

New Objective in primal was changed to:

$$\max \sum_{j=1}^{8} -x_j$$

Primal variable x_j corresponds to dual variable y_j for j = 1, ..., 13 Dual Dictionary (with objective changed is):

```
1.0
            -6.00y_9 -3.00y_{10} -2.00y_{11} -6.00y_{12} -1.00y_{13}
y_1
            +2.00y_9 +1.00y_{10} -10.00y_{11} -8.00y_{12} +9.00y_{13}
     1.0
y_2
     1.0
            -2.00y_9 -8.00y_{10} +1.00y_{11} -2.00y_{12} +10.00y_{13}
y_3
                                                -4.00y_{12} -1.00y_{13}
     1.0
            +6.00y_9 +7.00y_{10}
y_4
            +5.00y_9 +5.00y_{10} +10.00y_{11} -7.00y_{12} -4.00y_{13}
y_5
     1.0
     1.0
            +9.00y_9 +8.00y_{10} +6.00y_{11} -4.00y_{12} -2.00y_{13}
y_6
     1.0
           -10.00y_9 - 5.00y_{10} - 8.00y_{11} + 2.00y_{12} + 4.00y_{13}
y_7
           +10.00y_9 + 4.00y_{10} + 2.00y_{11} -1.00y_{12}
           -11.00y_9 + 3.00y_{10} - 8.00y_{11} + 14.00y_{12} - 25.00y_{13}
```

Initialization succeeded in finding final dual dictionary with 4 pivots

```
0.13333333333333
                                      -0.10y_2 -1.07y_{11} -0.03y_1 +0.87y_{13}
y_{12}
                           +14.00y_9 - 1.40y_2 - 8.60y_{11} + 2.20y_1 + 24.80y_{13}
             0.2
y_3
      0.0666666666667
                            -2.00y_9 +0.20y_2 +1.47y_{11} -0.27y_1 -2.07y_{13}
y_{10}
      0.933333333333
                            -8.00y_9 +1.80y_2 +14.53y_{11} -1.73y_1 -18.93y_{13}
y_4
             0.4
                            -5.00y_9 +1.70y_2 +24.80y_{11} -1.10y_1 -20.40y_{13}
y_5
                            -7.00y_9 +2.00y_2 +22.00y_{11} -2.00y_1 -22.00y_{13}
             1.0
y_6
                                      -1.20y_2 -17.47y_{11} +1.27y_1 +16.07y_{13}
y_7
      0.933333333333
       1.13333333333
                            +2.00y_9 +0.90y_2 +8.93y_{11} -1.03y_1 -9.13y_{13}
y_8
       2.0666666667
                            -17.00y_9 -0.80y_2 -18.53y_{11} -1.27y_1 -19.07y_{13}
z
```

Primal Dictionary is:

```
-14.00x_3 + 2.00x_{10} + 8.00x_4 + 5.00x_5 + 7.00x_6
            17.0
                                                                                                   -2.00x_8
x_9
x_2
                          +0.10x_{12} +1.40x_3 -0.20x_{10} -1.80x_4 -1.70x_5 -2.00x_6 +1.20x_7 -0.90x_8
             0.8
       18.53333333333
                         +1.07x_{12} +8.60x_3 -1.47x_{10} -14.53x_4 -24.80x_5 -22.00x_6 +17.47x_7 -8.93x_8
x_{11}
       1.26666666667
                          +0.03x_{12} -2.20x_3 +0.27x_{10} +1.73x_4 +1.10x_5 +2.00x_6 -1.27x_7 +1.03x_8
x_1
       19.0666666667
                          -0.87x_{12} - 24.80x_3 + 2.07x_{10} + 18.93x_4 + 20.40x_5 + 22.00x_6 - 16.07x_7 + 9.13x_8
x_{13}
      -2.06666666667
                         -0.13x_{12} -0.20x_3 -0.07x_{10} -0.93x_4 -0.40x_5 -1.00x_6 -0.93x_7 -1.13x_8
```

Primal Dictionary with original objective is:

```
17.0
                                  -14.00x_3 + 2.00x_{10} + 8.00x_4 + 5.00x_5 + 7.00x_6
                                                                                                 -2.00x_{8}
            0.8
                        +0.10x_{12} +1.40x_3 -0.20x_{10} -1.80x_4 -1.70x_5 -2.00x_6 +1.20x_7 -0.90x_8
x_2
      18.5333333333
                       +1.07x_{12} +8.60x_3 -1.47x_{10} -14.53x_4 -24.80x_5 -22.00x_6 +17.47x_7 -8.93x_8
x_{11}
                       +0.03x_{12} -2.20x_3 +0.27x_{10} +1.73x_4 +1.10x_5 +2.00x_6 -1.27x_7 +1.03x_8
      1.26666666667
x_1
                        -0.87x_{12} - 24.80x_3 + 2.07x_{10} + 18.93x_4 + 20.40x_5 + 22.00x_6 - 16.07x_7 + 9.13x_8
x_{13}
      19.0666666667
      2.06666666667
                       +0.13x_{12} -0.80x_3 +0.07x_{10} -1.07x_4 -1.60x_5 -3.00x_6 -3.07x_7 +0.13x_8
 z
```

1 Optimization Phase Simplex

Starting Dictionary is:

```
17.0
                                  -14.00x_3 + 2.00x_{10} + 8.00x_4 + 5.00x_5 + 7.00x_6
x_9
            0.8
                        +0.10x_{12} +1.40x_3 -0.20x_{10} -1.80x_4 -1.70x_5 -2.00x_6 +1.20x_7 -0.90x_8
x_2
      18.53333333333
x_{11}
                        +1.07x_{12} +8.60x_3 -1.47x_{10} -14.53x_4 -24.80x_5 -22.00x_6 +17.47x_7 -8.93x_8
      1.26666666667
                        +0.03x_{12} -2.20x_3 +0.27x_{10} +1.73x_4 +1.10x_5 +2.00x_6 -1.27x_7 +1.03x_8
      19.066666667
                        -0.87x_{12} - 24.80x_3 + 2.07x_{10} + 18.93x_4 + 20.40x_5 + 22.00x_6 - 16.07x_7 + 9.13x_8
x_{13}
                       +0.13x_{12} -0.80x_3 +0.07x_{10} -1.07x_4 -1.60x_5 -3.00x_6 -3.07x_7 +0.13x_8
      2.06666666667
```

 x_8 enters and x_2 leaves

```
15.222222222
                         -0.22x_{12} - 17.11x_3 + 2.44x_{10} + 12.00x_4 + 8.78x_5 + 11.44x_6 - 2.67x_7 + 2.22x_2
x_9
     0.88888888889
                         +0.11x_{12} +1.56x_3 -0.22x_{10} -2.00x_4 -1.89x_5 -2.22x_6 +1.33x_7 -1.11x_2
x_8
      10.5925925926
                         +0.07x_{12} -5.30x_3 +0.52x_{10} +3.33x_4 -7.93x_5 -2.15x_6 +5.56x_7 +9.93x_2
x_{11}
      2.18518518519
                         +0.15x_{12} -0.59x_3 +0.04x_{10} -0.33x_4 -0.85x_5 -0.30x_6 +0.11x_7 -1.15x_2
x_1
      27.1851851852
                         +0.15x_{12} - 10.59x_3 + 0.04x_{10} + 0.67x_4 + 3.15x_5 + 1.70x_6 - 3.89x_7 - 10.15x_2
x_{13}
                         +0.15x_{12} -0.59x_3 +0.04x_{10} -1.33x_4 -1.85x_5 -3.30x_6 -2.89x_7 -0.15x_2
      2.18518518519
```

 x_{10} enters and x_8 leaves

```
+1.00x_{12} +0.00x_3 -11.00x_8 -10.00x_4 -12.00x_5 -13.00x_6 +12.00x_7 -10.00x_2
          25.0
x_9
           4.0
                      +0.50x_{12} +7.00x_3 -4.50x_8 -9.00x_4 -8.50x_5 -10.00x_6 +6.00x_7 -5.00x_2
x_{10}
x_{11}
     12.6666666667
                      +0.33x_{12} -1.67x_3 -2.33x_8 -1.33x_4 -12.33x_5 -7.33x_6 +8.67x_7 +7.33x_2
     2.33333333333
                      +0.17x_{12} -0.33x_3 -0.17x_8 -0.67x_4 -1.17x_5 -0.67x_6 +0.33x_7 -1.33x_2
x_1
                       +0.17x_{12} - 10.33x_3 - 0.17x_8 + 0.33x_4 + 2.83x_5 + 1.33x_6 - 3.67x_7 - 10.33x_2
     27.3333333333
x_{13}
                      +0.17x_{12} -0.33x_3 -0.17x_8 -1.67x_4 -2.17x_5 -3.67x_6 -2.67x_7 -0.33x_2
     2.33333333333
```

 x_{12} enters and Unbounded Dictionary! x_{12} enters and Unbounded Dictionary!