

Read in the following dictionary:

x_9	-2.0	-3.00 x_1	-2.00 x_2	-9.00 x_3	-5.00 x_4	+7.00 x_5	+1.00 x_6	-9.00 x_7	-3.00 x_8
x_{10}	3.0	+4.00 x_1	+3.00 x_2	-6.00 x_3	-6.00 x_4	-6.00 x_5	+3.00 x_6	+8.00 x_7	-2.00 x_8
x_{11}	3.0	-8.00 x_1	+5.00 x_2	-8.00 x_3	+2.00 x_4	-8.00 x_5			+2.00 x_8
x_{12}	-3.0	-10.00 x_1	-10.00 x_2		-10.00 x_4	+10.00 x_5	+4.00 x_6	-2.00 x_7	-3.00 x_8
x_{13}	3.0	-3.00 x_1	+9.00 x_2	+6.00 x_3	+1.00 x_4	-7.00 x_5	-3.00 x_6	+6.00 x_7	-5.00 x_8
x_{14}	-3.0	-7.00 x_1	+6.00 x_2	+2.00 x_3	+8.00 x_4	-5.00 x_5	+8.00 x_6		-5.00 x_8
x_{15}	-3.0	-1.00 x_1	-9.00 x_2	-8.00 x_3	-8.00 x_4	+6.00 x_5	+3.00 x_6	-7.00 x_7	-9.00 x_8
x_{16}	2.0	-2.00 x_1	+6.00 x_2	+5.00 x_3	+5.00 x_4	-8.00 x_5		+3.00 x_7	+3.00 x_8
z	0.0	-1.00 x_1	+4.00 x_2	+2.00 x_3	+5.00 x_4	+5.00 x_5	-2.00 x_6	-3.00 x_7	-3.00 x_8

0.1 Initialization Phase: Dual Problem Solving

New Objective in primal was changed to :

$$\max \sum_{j=1}^8 -x_j$$

Primal variable x_j corresponds to dual variable y_j for $j = 1, \dots, 16$ Dual Dictionary (with objective changed is):

y_1	1.0	+3.00 y_9	-4.00 y_{10}	+8.00 y_{11}	+10.00 y_{12}	+3.00 y_{13}	+7.00 y_{14}	+1.00 y_{15}	+2.00 y_{16}
y_2	1.0	+2.00 y_9	-3.00 y_{10}	-5.00 y_{11}	+10.00 y_{12}	-9.00 y_{13}	-6.00 y_{14}	+9.00 y_{15}	-6.00 y_{16}
y_3	1.0	+9.00 y_9	+6.00 y_{10}	+8.00 y_{11}		-6.00 y_{13}	-2.00 y_{14}	+8.00 y_{15}	-5.00 y_{16}
y_4	1.0	+5.00 y_9	+6.00 y_{10}	-2.00 y_{11}	+10.00 y_{12}	-1.00 y_{13}	-8.00 y_{14}	+8.00 y_{15}	-5.00 y_{16}
y_5	1.0	-7.00 y_9	+6.00 y_{10}	+8.00 y_{11}	-10.00 y_{12}	+7.00 y_{13}	+5.00 y_{14}	-6.00 y_{15}	+8.00 y_{16}
y_6	1.0	-1.00 y_9	-3.00 y_{10}		-4.00 y_{12}	+3.00 y_{13}	-8.00 y_{14}	-3.00 y_{15}	
y_7	1.0	+9.00 y_9	-8.00 y_{10}		+2.00 y_{12}	-6.00 y_{13}		+7.00 y_{15}	-3.00 y_{16}
y_8	1.0	+3.00 y_9	+2.00 y_{10}	-2.00 y_{11}	+3.00 y_{12}	+5.00 y_{13}	+5.00 y_{14}	+9.00 y_{15}	-3.00 y_{16}
z	-0	+2.00 y_9	-3.00 y_{10}	-3.00 y_{11}	+3.00 y_{12}	-3.00 y_{13}	+3.00 y_{14}	+3.00 y_{15}	-2.00 y_{16}

Initialization succeeded in finding final dual dictionary with 7 pivots

y_1	96.0	+4.00 y_5	-325.00 y_{10}	-137.33 y_{11}	-28.67 y_{12}	-22.67 y_2	-76.33 y_6	-759.67 y_{14}	-166.00 y_{16}
y_{13}	21.0	+1.00 y_5	-72.00 y_{10}	-33.00 y_{11}	-8.00 y_{12}	-5.00 y_2	-17.00 y_6	-171.00 y_{14}	-38.00 y_{16}
y_3	71.0	+2.00 y_5	-222.00 y_{10}	-89.67 y_{11}	-39.33 y_{12}	-16.33 y_2	-55.67 y_6	-555.33 y_{14}	-119.00 y_{16}
y_4	160.0	+7.00 y_5	-534.00 y_{10}	-244.67 y_{11}	-61.33 y_{12}	-37.33 y_2	-128.67 y_6	-1296.33 y_{14}	-285.00 y_{16}
y_9	4.0	-0.00 y_5	-12.00 y_{10}	-5.00 y_{11}	-2.00 y_{12}	-1.00 y_2	-3.00 y_6	-30.00 y_{14}	-6.00 y_{16}
y_{15}	20.0	+1.00 y_5	-69.00 y_{10}	-31.33 y_{11}	-8.67 y_{12}	-4.67 y_2	-16.33 y_6	-163.67 y_{14}	-36.00 y_{16}
y_7	51.0	+1.00 y_5	-167.00 y_{10}	-66.33 y_{11}	-28.67 y_{12}	-11.67 y_2	-39.33 y_6	-389.67 y_{14}	-81.00 y_{16}
y_8	298.0	+14.00 y_5	-1015.00 y_{10}	-464.00 y_{11}	-121.00 y_{12}	-70.00 y_2	-241.00 y_6	-2413.00 y_{14}	-535.00 y_{16}
z	5.0	-0.00 y_5	-18.00 y_{10}	-8.00 y_{11}	-3.00 y_{12}	-1.00 y_2	-4.00 y_6	-35.00 y_{14}	-8.00 y_{16}

Primal Dictionary is:

x_5	$1.16573417586e - 15$	$-4.00x_1$	$-1.00x_{13}$	$-2.00x_3$	$-7.00x_4$	$+0.00x_9$	$-1.00x_{15}$	$-1.00x_7$
x_{10}	18.0	$+325.00x_1$	$+72.00x_{13}$	$+222.00x_3$	$+534.00x_4$	$+12.00x_9$	$+69.00x_{15}$	$+167.00x_7$
x_{11}	8.0	$+137.33x_1$	$+33.00x_{13}$	$+89.67x_3$	$+244.67x_4$	$+5.00x_9$	$+31.33x_{15}$	$+66.33x_7$
x_{12}	3.0	$+28.67x_1$	$+8.00x_{13}$	$+39.33x_3$	$+61.33x_4$	$+2.00x_9$	$+8.67x_{15}$	$+28.67x_7$
x_2	1.0	$+22.67x_1$	$+5.00x_{13}$	$+16.33x_3$	$+37.33x_4$	$+1.00x_9$	$+4.67x_{15}$	$+11.67x_7$
x_6	4.0	$+76.33x_1$	$+17.00x_{13}$	$+55.67x_3$	$+128.67x_4$	$+3.00x_9$	$+16.33x_{15}$	$+39.33x_7$
x_{14}	35.0	$+759.67x_1$	$+171.00x_{13}$	$+555.33x_3$	$+1296.33x_4$	$+30.00x_9$	$+163.67x_{15}$	$+389.67x_7$
x_{16}	8.0	$+166.00x_1$	$+38.00x_{13}$	$+119.00x_3$	$+285.00x_4$	$+6.00x_9$	$+36.00x_{15}$	$+81.00x_7$
z	-5.0	$-96.00x_1$	$-21.00x_{13}$	$-71.00x_3$	$-160.00x_4$	$-4.00x_9$	$-20.00x_{15}$	$-51.00x_7$

Primal Dictionary with original objective is:

x_5	$1.16573417586e - 15$	$-4.00x_1$	$-1.00x_{13}$	$-2.00x_3$	$-7.00x_4$	$+0.00x_9$	$-1.00x_{15}$	$-1.00x_7$
x_{10}	18.0	$+325.00x_1$	$+72.00x_{13}$	$+222.00x_3$	$+534.00x_4$	$+12.00x_9$	$+69.00x_{15}$	$+167.00x_7$
x_{11}	8.0	$+137.33x_1$	$+33.00x_{13}$	$+89.67x_3$	$+244.67x_4$	$+5.00x_9$	$+31.33x_{15}$	$+66.33x_7$
x_{12}	3.0	$+28.67x_1$	$+8.00x_{13}$	$+39.33x_3$	$+61.33x_4$	$+2.00x_9$	$+8.67x_{15}$	$+28.67x_7$
x_2	1.0	$+22.67x_1$	$+5.00x_{13}$	$+16.33x_3$	$+37.33x_4$	$+1.00x_9$	$+4.67x_{15}$	$+11.67x_7$
x_6	4.0	$+76.33x_1$	$+17.00x_{13}$	$+55.67x_3$	$+128.67x_4$	$+3.00x_9$	$+16.33x_{15}$	$+39.33x_7$
x_{14}	35.0	$+759.67x_1$	$+171.00x_{13}$	$+555.33x_3$	$+1296.33x_4$	$+30.00x_9$	$+163.67x_{15}$	$+389.67x_7$
x_{16}	8.0	$+166.00x_1$	$+38.00x_{13}$	$+119.00x_3$	$+285.00x_4$	$+6.00x_9$	$+36.00x_{15}$	$+81.00x_7$
z	-4.0	$-83.00x_1$	$-19.00x_{13}$	$-54.00x_3$	$-138.00x_4$	$-2.00x_9$	$-19.00x_{15}$	$-40.00x_7$

1 Optimization Phase Simplex

Starting Dictionary is:

x_5	$1.16573417586e - 15$	$-4.00x_1$	$-1.00x_{13}$	$-2.00x_3$	$-7.00x_4$	$+0.00x_9$	$-1.00x_{15}$	$-1.00x_7$
x_{10}	18.0	$+325.00x_1$	$+72.00x_{13}$	$+222.00x_3$	$+534.00x_4$	$+12.00x_9$	$+69.00x_{15}$	$+167.00x_7$
x_{11}	8.0	$+137.33x_1$	$+33.00x_{13}$	$+89.67x_3$	$+244.67x_4$	$+5.00x_9$	$+31.33x_{15}$	$+66.33x_7$
x_{12}	3.0	$+28.67x_1$	$+8.00x_{13}$	$+39.33x_3$	$+61.33x_4$	$+2.00x_9$	$+8.67x_{15}$	$+28.67x_7$
x_2	1.0	$+22.67x_1$	$+5.00x_{13}$	$+16.33x_3$	$+37.33x_4$	$+1.00x_9$	$+4.67x_{15}$	$+11.67x_7$
x_6	4.0	$+76.33x_1$	$+17.00x_{13}$	$+55.67x_3$	$+128.67x_4$	$+3.00x_9$	$+16.33x_{15}$	$+39.33x_7$
x_{14}	35.0	$+759.67x_1$	$+171.00x_{13}$	$+555.33x_3$	$+1296.33x_4$	$+30.00x_9$	$+163.67x_{15}$	$+389.67x_7$
x_{16}	8.0	$+166.00x_1$	$+38.00x_{13}$	$+119.00x_3$	$+285.00x_4$	$+6.00x_9$	$+36.00x_{15}$	$+81.00x_7$
z	-4.0	$-83.00x_1$	$-19.00x_{13}$	$-54.00x_3$	$-138.00x_4$	$-2.00x_9$	$-19.00x_{15}$	$-40.00x_7$

Final Dictionary Solution: -4.0 Num Pivots: 1