Read in the following dictionary:

```
x_{10}
             -4.00x_1 +8.00x_2 +5.00x_3 -5.00x_4 -7.00x_5 -9.00x_6 -5.00x_7 +3.00x_8 -6.00x_9
      34.0
             +6.00x_1 -10.00x_2 -5.00x_3 -10.00x_4 -2.00x_5 +7.00x_6 -10.00x_7 -3.00x_8 +2.00x_9
x_{11}
                                          -5.00x_4 +7.00x_5 +2.00x_6 +8.00x_7 +6.00x_8 -1.00x_9
      25.0
            -10.00x_1 -3.00x_2
x_{12}
x_{13}
      51.0
            -10.00x_1 +5.00x_2 +1.00x_3 -8.00x_4 +3.00x_5 +8.00x_6 +9.00x_7 -1.00x_8 -9.00x_9
      9.0
             +6.00x_1 +2.00x_2 +6.00x_3 -8.00x_4 +2.00x_5 +4.00x_6 +8.00x_7 -8.00x_8 -8.00x_9
x_{14}
      0.0
             -3.00x_1 +1.00x_2 -5.00x_3 +3.00x_4
                                                             -4.00x_6 -4.00x_7 -1.00x_8 -3.00x_9
 z
```

No initialization required –; Proceed to Optimize.

1 Optimization Phase Simplex

Starting Dictionary is:

```
19.0
             -4.00x_1 +8.00x_2 +5.00x_3 -5.00x_4 -7.00x_5 -9.00x_6 -5.00x_7 +3.00x_8 -6.00x_9
x_{10}
      34.0
             +6.00x_1 -10.00x_2 -5.00x_3 -10.00x_4 -2.00x_5 +7.00x_6 -10.00x_7 -3.00x_8 +2.00x_9
x_{11}
x_{12}
      25.0
             -10.00x_1 -3.00x_2
                                           -5.00x_4 + 7.00x_5 + 2.00x_6 + 8.00x_7 + 6.00x_8 - 1.00x_9
      51.0
             -10.00x_1 + 5.00x_2 + 1.00x_3 - 8.00x_4 + 3.00x_5 + 8.00x_6 + 9.00x_7 - 1.00x_8 - 9.00x_9
x_{13}
             +6.00x_1 +2.00x_2 +6.00x_3 -8.00x_4 +2.00x_5 +4.00x_6 +8.00x_7 -8.00x_8 -8.00x_9
      9.0
x_{14}
             -3.00x_1 +1.00x_2 -5.00x_3 +3.00x_4
                                                              -4.00x_6 -4.00x_7 -1.00x_8 -3.00x_9
      0.0
```

 x_2 enters and x_{11} leaves

```
+0.80x_1 -0.80x_{11} +1.00x_3 -13.00x_4 -8.60x_5 -3.40x_6 -13.00x_7 +0.60x_8 -4.40x_9
x_{10}
                          46.2
                                                           +0.60x_1 -0.10x_{11} -0.50x_3 -1.00x_4 -0.20x_5 +0.70x_6 -1.00x_7 -0.30x_8 +0.20x_9
                             3.4
 x_2
x_{12}
                          14.8
                                                         -11.80x_1 + 0.30x_{11} + 1.50x_3 - 2.00x_4 + 7.60x_5 - 0.10x_6 + 11.00x_7 + 6.90x_8 - 1.60x_9
                                                           -7.00x_1 \ -0.50x_{11} -1.50x_3 -13.00x_4 +2.00x_5 +11.50x_6 \ +4.00x_7 \ -2.50x_8 -8.00x_9 +10.00x_7 +1
                          68.0
x_{13}
                                                           +7.20x_1 -0.20x_{11} +5.00x_3 -10.00x_4 +1.60x_5 +5.40x_6 +6.00x_7 -8.60x_8 -7.60x_9
                          15.8
x_{14}
                                                           -2.40x_1 -0.10x_{11} -5.50x_3 +2.00x_4 -0.20x_5 -3.30x_6 -5.00x_7 -1.30x_8 -2.80x_9
    z
                             3.4
```

 x_4 enters and x_{14} leaves

```
25.66
                                                              -8.56x_1 -0.54x_{11} -5.50x_3 +1.30x_{14} -10.68x_5 -10.42x_6 -20.80x_7 +11.78x_8 +5.48x_9
x_{10}
                            1.82
                                                               -0.12x_1 -0.08x_{11} -1.00x_3 +0.10x_{14} -0.36x_5 +0.16x_6 -1.60x_7 +0.56x_8 +0.96x_9
 x_2
                                                            -13.24x_1 + 0.34x_{11} + 0.50x_3 + 0.20x_{14} + 7.28x_5 -1.18x_6 + 9.80x_7 + 8.62x_8 -0.08x_9 + 1.00x_{14} + 1.00x_{15} 
x_{12}
                          11.64
                                                            -16.36x_1 - 0.24x_{11} - 8.00x_3 + 1.30x_{14} - 0.08x_5 + 4.48x_6 - 3.80x_7 + 8.68x_8 + 1.88x_9
                          47.46
x_{13}
                                                                +0.72x_1 -0.02x_{11} +0.50x_3 -0.10x_{14} +0.16x_5 +0.54x_6 +0.60x_7 -0.86x_8 -0.76x_9
                            1.58
  x_4
                            6.56
                                                                -0.96x_1 -0.14x_{11} -4.50x_3 -0.20x_{14} +0.12x_5 -2.22x_6 -3.80x_7 -3.02x_8 -4.32x_9
    z
```

 x_5 enters and x_{10} leaves

```
2.40262172285
                                                                                                                                                                                                                                                                      -0.80x_1 -0.05x_{11} -0.51x_3 +0.12x_{14} -0.09x_{10} -0.98x_6 -1.95x_7 +1.10x_8 +0.51x
   x_5
                                                            0.955056179775
                                                                                                                                                                                                                                                                      +0.17x_1 -0.06x_{11} -0.81x_3 +0.06x_{14} +0.03x_{10} +0.51x_6 -0.90x_7 +0.16x_8 +0.78x_1 +0.06x_{11} +0.06x_{12} +0.06x_{13} +0.06x_{14} +0.00x_{14} +0.00x_{15} +0.00x_{15
 x_2
                                                                  29.1310861423
                                                                                                                                                                                                                                                                  -19.07x_1 - 0.03x_{11} - 3.25x_3 + 1.09x_{14} - 0.68x_{10} - 8.28x_6 - 4.38x_7 + 16.65x_8 + 3.66x_8 + 3.
x_{12}
                                                                  47.2677902622
                                                                                                                                                                                                                                                                  -16.30x_1 - 0.24x_{11} - 7.96x_3 + 1.29x_{14} + 0.01x_{10} + 4.56x_6 - 3.64x_7 + 8.59x_8 + 1.84x_{10} + 1.8
x_{13}
                                                                  1.96441947566
                                                                                                                                                                                                                                                                      +0.59x_1 -0.03x_{11} + 0.42x_3 - 0.08x_{14} - 0.01x_{10} + 0.38x_6 + 0.29x_7 - 0.68x_8 - 0.68x
   x_4
                                                                  6.84831460674
                                                                                                                                                                                                                                                                        -1.06x_1 -0.15x_{11} -4.56x_3 -0.19x_{14} -0.01x_{10} -2.34x_6 -4.03x_7 -2.89x_8 -4.26x_8
```

Final Dictionary Solution: $6.84831460674~\mathrm{Num}$ Pivots: 4