

CSEN 1002

Task 8: LL(1) Parsing

Outline

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2 Example Grammar 2

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Example Grammar 1 - Parsing Table

Input

S;A;B# a;b;c;d# S/AaS,d;A/BbBaSc,e;B/e# S/ab,d;A/b,e;B/e#
S/\$c;A/a;B/ab

$$S \rightarrow AaS \mid d$$

$$A \rightarrow BbBaSc \mid \varepsilon$$

$$B \rightarrow \varepsilon$$

Example Grammar 1 - Parsing Table

Input

S;A;B# a;b;c;d# S/AaS,d;A/BbBaSc,e;B/e# S/ab,d;A/b,e;B/e#
S/\$c;A/a;B/ab

$$\begin{aligned} S &\rightarrow AaS \mid d \\ A &\rightarrow BbBaSc \mid \varepsilon \\ B &\rightarrow \varepsilon \end{aligned}$$

LHS	RHS	First	Follow
S	AaS	a,b	\$,c
	d	d	
A	BbBaSc	b	a
	e	e	
B	e	e	a,b

Example Grammar 1 - Parsing Table

LHS	RHS	First	Follow
S	AaS	a,b	$\$,c$
	d	d	
A	$BbBaSc$	b	a
	e	e	
B	e	e	a,b

	a	b	c	d	$\$$
S					
A					
B					

Example Grammar 1 - Parsing Table

LHS	RHS	First	Follow
S	AaS	a,b	$\$,c$
	d	d	
A	$BbBaSc$	b	a
	e	e	
B	e	e	a,b

	a	b	c	d	$\$$
S	AaS	AaS			
A					
B					

Example Grammar 1 - Parsing Table

LHS	RHS	First	Follow
S	AaS	a,b	$\$,c$
	d	d	
A	$BbBaSc$	b	a
	e	e	
B	e	e	a,b

	a	b	c	d	$\$$
S	AaS	AaS		d	
A					
B					

Example Grammar 1 - Parsing Table

LHS	RHS	First	Follow
S	AaS	a,b	$\$,c$
	d	d	
A	$BbBaSc$	b	a
	e	e	
B	e	e	a,b

	a	b	c	d	$\$$
S	AaS	AaS		d	
A		$BbBaSc$			
B					

Example Grammar 1 - Parsing Table

LHS	RHS	First	Follow
S	AaS	a,b	$\$,c$
	d	d	
A	$BbBaSc$	b	a
	e	e	
B	e	e	a,b

	a	b	c	d	$\$$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B					

Example Grammar 1 - Parsing Table

LHS	RHS	First	Follow
S	AaS	a,b	$\$,c$
	d	d	
A	$BbBaSc$	b	a
	e	e	
B	e	e	a,b

	a	b	c	d	$\$$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Example 1

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S

Initialized

a	b	a	d	c	a	d	\$
---	---	---	---	---	---	---	----

↑

S

\$

Example 1

	a	b	c	d	\$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

S; AaS

$M(S, a) = AaS$. The stack content is updated and a new step in the derivation is added.

a	b	a	d	c	a	d	\$
---	---	---	---	---	---	---	----



A
a
S
$\$$

Example 1

	a	b	c	d	$\$$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

S ; AaS ; aS

$M(A, a) = e$. The stack content is updated and a new step in the derivation is added.

a	b	a	d	c	a	d	$\$$
-----	-----	-----	-----	-----	-----	-----	------

↑

a
S
$\$$

Example 1

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; *AaS*; *aS*

Matching the top-of-the-stack terminal with input symbol

<i>a</i>	<i>b</i>	<i>a</i>	<i>d</i>	<i>c</i>	<i>a</i>	<i>d</i>	\$
----------	----------	----------	----------	----------	----------	----------	----



<i>S</i>
\$

Example 1

	a	b	c	d	$\$$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

S ; AaS ; aS ; $aAaS$

$M(S, b) = AaS$. The stack content is updated and a new step in the derivation is added.

a	b	a	d	c	a	d	$\$$
-----	-----	-----	-----	-----	-----	-----	------



A
a
S
$\$$

Example 1

	a	b	c	d	$\$$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

 $S; AaS; aS; aAaS; aBbBaScaS$

$M(A, b) = BbBaSc$. The stack content is updated and a new step in the derivation is added.

a	b	a	d	c	a	d	$\$$
-----	-----	-----	-----	-----	-----	-----	------



B
b
B
a
S
c
a
S
$\$$

Example 1

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

 $S; AaS; aS; aAaS; aBbBaScaS; abBaScaS$

$M(B, b) = e$. The stack content is updated and a new step in the derivation is added.

<i>a</i>	<i>b</i>	<i>a</i>	<i>d</i>	<i>c</i>	<i>a</i>	<i>d</i>	\$
----------	----------	----------	----------	----------	----------	----------	----



<i>b</i>
<i>B</i>
<i>a</i>
<i>S</i>
<i>c</i>
<i>a</i>
<i>S</i>
\$

Example 1

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; AaS; aS; aAaS; aBbBaScaS; abBaScaS

Matching the top-of-the-stack terminal with input symbol

a	b	a	d	c	a	d	\$
---	---	---	---	---	---	---	----



<i>B</i>
<i>a</i>
<i>S</i>
<i>c</i>
<i>a</i>
<i>S</i>
<i>\$</i>

Example 1

	a	b	c	d	$\$$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

S ; AaS ; aS ; $aAaS$; $aBbBaScaS$; $abBaScaS$; $abaScaS$

$M(B, a) = e$. The stack content is updated and a new step in the derivation is added.

a	b	a	d	c	a	d	$\$$
-----	-----	-----	-----	-----	-----	-----	------



a
S
c
a
S
$\$$

Example 1

	a	b	c	d	\$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

S; AaS; aS; aAaS; aBbBaScaS; abBaScaS; abaScaS

Matching the top-of-the-stack terminal with input symbol

a	b	a	d	c	a	d	\$
---	---	---	---	---	---	---	----



\$	S	c	a	S
----	-----	-----	-----	-----

Example 1

	a	b	c	d	$\$$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

S ; AaS ; aS ; a AaS ; a $BbBaScaS$; ab $BaScaS$; aba $ScaS$; $abadca$ S

$M(S, d) = d$. The stack content is updated and a new step in the derivation is added.

a	b	a	d	c	a	d	$\$$
-----	-----	-----	-----	-----	-----	-----	------



d
c
a
S
$\$$

Example 1

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; *AaS*; *aS*; *aAaS*; *aBbBaScaS*; *abBaScaS*; *abaScaS*; *abadcaS*

Matching the top-of-the-stack terminal with input symbol

<i>a</i>	<i>b</i>	<i>a</i>	<i>d</i>	<i>c</i>	<i>a</i>	<i>d</i>	\$
----------	----------	----------	----------	----------	----------	----------	----



<i>c</i>
<i>a</i>
<i>S</i>
\$

Example 1

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; *AaS*; *aS*; *aAaS*; *aBbBaScaS*; *abBaScaS*; *abaScaS*; *abadcaS*

Matching the top-of-the-stack terminal with input symbol

<i>a</i>	<i>b</i>	<i>a</i>	<i>d</i>	<i>c</i>	<i>a</i>	<i>d</i>	\$
----------	----------	----------	----------	----------	----------	----------	----



<i>a</i>
<i>S</i>
\$

Example 1

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; *AaS*; *aS*; *aAaS*; *aBbBaScaS*; *abBaScaS*; *abaScaS*; *abadcaS*

Matching the top-of-the-stack terminal with input symbol

<i>a</i>	<i>b</i>	<i>a</i>	<i>d</i>	<i>c</i>	<i>a</i>	<i>d</i>	\$
----------	----------	----------	----------	----------	----------	----------	----



<i>S</i>
\$

Example 1

	a	b	c	d	$\$$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

S ; AaS ; aS ; $aAaS$; $aBbBaScaS$; $abBaScaS$; $abaScaS$; $abad-$
 caS ; $abadcad$

$M(S, d) = d$. The stack content is updated and a new step in the derivation is added.

a	b	a	d	c	a	d	$\$$
-----	-----	-----	-----	-----	-----	-----	------



d
$\$$

Example 1

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; *AaS*; *aS*; *aAaS*; *aBbBaScaS*; *abBaScaS*; *abaScaS*; *abad-*
caS; *abadcad*

Matching the top-of-the-stack terminal with input symbol

<i>a</i>	<i>b</i>	<i>a</i>	<i>d</i>	<i>c</i>	<i>a</i>	<i>d</i>	\$
----------	----------	----------	----------	----------	----------	----------	----



\$

Example 1

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; *AaS*; *aS*; *aAaS*; *aBbBaScaS*; *abBaScaS*; *abaScaS*; *abad-*
caS; *abadcad*

Parsed

<i>a</i>	<i>b</i>	<i>a</i>	<i>d</i>	<i>c</i>	<i>a</i>	<i>d</i>	\$
----------	----------	----------	----------	----------	----------	----------	----

Example 2

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S

Initialized

b	b	b	d	\$
---	---	---	---	----



<i>S</i>
\$

Example 2

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; *AaS*

$M(S, b) = AaS$. The stack content is updated and a new step in the derivation is added.

<i>b</i>	<i>b</i>	<i>b</i>	<i>d</i>	\$
----------	----------	----------	----------	----



<i>A</i>
<i>a</i>
<i>S</i>
\$

Example 2

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; *AaS*; *BbBaScaS*

$M(A, b) = BbBaSc$. The stack content is updated and a new step in the derivation is added.

<i>b</i>	<i>b</i>	<i>b</i>	<i>d</i>	\$
----------	----------	----------	----------	----



<i>B</i>
<i>b</i>
<i>B</i>
<i>a</i>
<i>S</i>
<i>c</i>
<i>a</i>
<i>S</i>
\$

Example 2

	a	b	c	d	$\$$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

S ; AaS ; $BbBaSc$; $bBaSc$

$M(B, b) = e$. The stack content is updated and a new step in the derivation is added.

b	b	b	d	$\$$
-----	-----	-----	-----	------



b
B
a
S
c
a
S
$\$$

Example 2

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; *AaS*; *BbBaScaS*; *bBaScaS*

Matching the top-of-the-stack terminal with input symbol

<i>b</i>	<i>b</i>	<i>b</i>	<i>d</i>	\$
----------	----------	----------	----------	----



<i>B</i>
<i>a</i>
<i>S</i>
<i>c</i>
<i>a</i>
<i>S</i>
\$

Example 2

	a	b	c	d	$\$$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

 S ; AaS ; $BbBaScaS$; $bBaScaS$; $baScaS$

$M(B, b) = e$. The stack content is updated and a new step in the derivation is added.

b	b	b	d	$\$$
-----	-----	-----	-----	------



a
S
c
a
S
$\$$

Example 2

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; AaS; BbBaScaS; bBaScaS; baScaS; ERROR

ERROR as the top of the stack symbol doesn't match the next symbol on the tape

b	b	b	d	\$
---	---	---	---	----



<i>a</i>
<i>S</i>
<i>c</i>
<i>a</i>
<i>S</i>
<i>\$</i>

Example 3

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S

Initialized

a	b	a	c	\$
---	---	---	---	----



<i>S</i>
\$

Example 3

	a	b	c	d	\$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

S; AaS

$M(S, a) = AaS$. The stack content is updated and a new step in the derivation is added.

a	b	a	c	\$
---	---	---	---	----



A
a
S
$\$$

Example 3

	a	b	c	d	$\$$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

S ; AaS ; aS

$M(A, a) = e$. The stack content is updated and a new step in the derivation is added.

a	b	a	c	$\$$
-----	-----	-----	-----	------

↑

a
S
$\$$

Example 3

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; *AaS*; *aS*

Matching the top-of-the-stack terminal with input symbol

<i>a</i>	<i>b</i>	<i>a</i>	<i>c</i>	\$
----------	----------	----------	----------	----



<i>S</i>
\$

Example 3

	a	b	c	d	\$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

S; AaS; aS; aAaS

$M(S, b) = AaS$. The stack content is updated and a new step in the derivation is added.

a	b	a	c	\$
---	---	---	---	----



A
a
S
$\$$

Example 3

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; *AaS*; *aS*; *aAaS*; *aBbBaScaS*

$M(A, b) = BbBaSc$. The stack content is updated and a new step in the derivation is added.

<i>a</i>	<i>b</i>	<i>a</i>	<i>c</i>	\$
----------	----------	----------	----------	----



<i>B</i>
<i>b</i>
<i>B</i>
<i>a</i>
<i>S</i>
<i>c</i>
<i>a</i>
<i>S</i>
\$

Example 3

	a	b	c	d	$\$$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

 $S; AaS; aS; aAaS; aBbBaScaS; abBaScaS$

$M(B, b) = e$. The stack content is updated and a new step in the derivation is added.

a	b	a	c	$\$$
-----	-----	-----	-----	------



b
B
a
S
c
a
S
$\$$

Example 3

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; AaS; aS; aAaS; aBbBaScaS; abBaScaS

Matching the top-of-the-stack terminal with input symbol

a	b	a	c	\$
---	---	---	---	----



<i>B</i>
<i>a</i>
<i>S</i>
<i>c</i>
<i>a</i>
<i>S</i>
<i>\$</i>

Example 3

	a	b	c	d	$\$$
S	AaS	AaS		d	
A	e	$BbBaSc$			
B	e	e			

Derivation:

 $S; AaS; aS; aAaS; aBbBaScaS; abBaScaS; abaScaS$

$M(B, a) = e$. The stack content is updated and a new step in the derivation is added.

a	b	a	c	$\$$
-----	-----	-----	-----	------



a
S
c
a
S
$\$$

Example 3

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; AaS; aS; aAaS; aBbBaScaS; abBaScaS; abaScaS

Matching the top-of-the-stack terminal with input symbol

<i>a</i>	<i>b</i>	<i>a</i>	<i>c</i>	\$
----------	----------	----------	----------	----



<i>S</i>
<i>c</i>
<i>a</i>
<i>S</i>
\$

Example 3

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	\$
<i>S</i>	<i>AaS</i>	<i>AaS</i>		<i>d</i>	
<i>A</i>	<i>e</i>	<i>BbBaSc</i>			
<i>B</i>	<i>e</i>	<i>e</i>			

Derivation:

S; *AaS*; *aS*; *aAaS*; *aBbBaScaS*; *abBaScaS*; *abaScaS*; ERROR

ERROR as $M(S, c)$ is \emptyset .

<i>a</i>	<i>b</i>	<i>a</i>	<i>c</i>	\$
----------	----------	----------	----------	----



<i>S</i>
<i>c</i>
<i>a</i>
<i>S</i>
\$

Example Grammar 2 - Parsing Table

Input

$S;T\# a;c;i\# S/iST,e;T/cS,a\# S/i,e;T/c,a\# S/\$ac;T/\$ac$

$$\begin{array}{lcl} S & \rightarrow & iST \mid \varepsilon \\ T & \rightarrow & cS \mid a \end{array}$$

Example Grammar 2 - Parsing Table

Input

$S; T \# a; c; i \# S/iST, e; T/cS, a \# S/i, e; T/c, a \# S/\$ac; T/\$ac$

$$\begin{aligned} S &\rightarrow iST \mid \varepsilon \\ T &\rightarrow cS \mid a \end{aligned}$$

LHS	RHS	First	Follow
S	iST	i	$\$, c, a$
	e	e	
T	cS	c	$\$, c, a$
	a	a	

Example Grammar 2 - Parsing Table

LHS	RHS	First	Follow
S	iST	i	\$,c,a
	e	e	
T	cS	c	\$,c,a
	a	a	

	a	c	i	\$
S				
T				

Example Grammar 2 - Parsing Table

LHS	RHS	First	Follow
S	iST	i	$\$,c,a$
	e	e	
T	cS	c	$\$,c,a$
	a	a	

	a	c	i	$\$$
S			iST	
T				

Example Grammar 2 - Parsing Table

LHS	RHS	First	Follow
S	iST	i	$\$,c,a$
	e	e	
T	cS	c	$\$,c,a$
	a	a	

	a	c	i	$\$$
S	e	e	iST	e
T				

Example Grammar 2 - Parsing Table

LHS	RHS	First	Follow
S	iST	i	$\$,c,a$
	e	e	
T	cS	c	$\$,c,a$
	a	a	

	a	c	i	$\$$
S	e	e	iST	e
T		cS		

Example Grammar 2 - Parsing Table

LHS	RHS	First	Follow
S	iST	i	$\$,c,a$
	e	e	
T	cS	c	$\$,c,a$
	a	a	

	a	c	i	$\$$
S	e	e	iST	e
T	a	cS		

Example 4

	<i>a</i>	<i>c</i>	<i>i</i>	\$
<i>S</i>	<i>e</i>	<i>e</i>	<i>iST</i>	<i>e</i>
<i>T</i>	<i>a</i>	<i>cS</i>		

Derivation:

S

Initialized

<i>i</i>	<i>i</i>	<i>a</i>	<i>c</i>	\$
----------	----------	----------	----------	----

↑

S

\$

Example 4

	a	c	i	$\$$
S	e	e	iST	e
T	a	cS		

Derivation:

 $S; iST$

$M(S, i) = iST$. The stack content is updated and a new step in the derivation is added.

i	i	a	c	$\$$
-----	-----	-----	-----	------

↑

i
S
T
$\$$

Example 4

	a	c	i	$\$$
S	e	e	iST	e
T	a	cS		

Derivation:

$S; iST$

Matching the top-of-the-stack terminal with input symbol

i	i	a	c	$\$$
-----	-----	-----	-----	------



S
T
$\$$

Example 4

	<i>a</i>	<i>c</i>	<i>i</i>	\$
<i>S</i>	<i>e</i>	<i>e</i>	<i>iST</i>	<i>e</i>
<i>T</i>	<i>a</i>	<i>cS</i>		

Derivation:

S; *iST*; *iiSTT*

$M(S, i) = iST$. The stack content is updated and a new step in the derivation is added.

<i>i</i>	<i>i</i>	<i>a</i>	<i>c</i>	\$
----------	----------	----------	----------	----



<i>i</i>
<i>S</i>
<i>T</i>
<i>T</i>
\$

Example 4

	<i>a</i>	<i>c</i>	<i>i</i>	\$
<i>S</i>	<i>e</i>	<i>e</i>	<i>iST</i>	<i>e</i>
<i>T</i>	<i>a</i>	<i>cS</i>		

Derivation:

S; *iST*; *iiSTT*

Matching the top-of-the-stack terminal with input symbol

<i>i</i>	<i>i</i>	<i>a</i>	<i>c</i>	\$
----------	----------	----------	----------	----



<i>S</i>
<i>T</i>
<i>T</i>
\$

Example 4

	a	c	i	\$
S	e	e	iST	e
T	a	cS		

Derivation:

S; iST; iiSTT; iiTT

$M(S, a) = e$. The stack content is updated and a new step in the derivation is added.

i	i	a	c	\$
---	---	---	---	----



T
T
\$

Example 4

	a	c	i	$\$$
S	e	e	iST	e
T	a	cS		

Derivation:

S ; iST ; $iiSTT$; $iiTT$; $iiat$

$M(T, a) = a$. The stack content is updated and a new step in the derivation is added.

i	i	a	c	$\$$
-----	-----	-----	-----	------



a
T
$\$$

Example 4

	a	c	i	$\$$
S	e	e	iST	e
T	a	cS		

Derivation:

 $S; iST; iiSTT; iiTT; iiaT$

Matching the top-of-the-stack terminal with input symbol

i	i	a	c	$\$$
-----	-----	-----	-----	------



T
$\$$

Example 4

	<i>a</i>	<i>c</i>	<i>i</i>	\$
<i>S</i>	<i>e</i>	<i>e</i>	<i>iST</i>	<i>e</i>
<i>T</i>	<i>a</i>	<i>cS</i>		

Derivation:

S; *iST*; *iiSTT*; *iiTT*; *iiAT*; *iiacS*

$M(T, c) = cS$. The stack content is updated and a new step in the derivation is added.

<i>i</i>	<i>i</i>	<i>a</i>	<i>c</i>	\$
----------	----------	----------	----------	----



<i>c</i>
<i>S</i>
\$

Example 4

	<i>a</i>	<i>c</i>	<i>i</i>	\$
<i>S</i>	<i>e</i>	<i>e</i>	<i>iST</i>	<i>e</i>
<i>T</i>	<i>a</i>	<i>cS</i>		

Derivation:

S; iST; iiSTT; iiTT; iiaT; iiaacS

Matching the top-of-the-stack terminal with input symbol

i	i	a	c	\$
---	---	---	---	----



<i>S</i>
\$

Example 4

	<i>a</i>	<i>c</i>	<i>i</i>	\$
<i>S</i>	<i>e</i>	<i>e</i>	<i>iST</i>	<i>e</i>
<i>T</i>	<i>a</i>	<i>cS</i>		

Derivation:

S ; iST ; $iiSTT$; $iiTT$; $iiAT$; $iiacS$; $iiac$

$M(S, \$) = e$. The stack content is updated and a new step in the derivation is added.

<i>i</i>	<i>i</i>	<i>a</i>	<i>c</i>	\$
----------	----------	----------	----------	----



\$

Example 4

	<i>a</i>	<i>c</i>	<i>i</i>	\$
<i>S</i>	<i>e</i>	<i>e</i>	<i>iST</i>	<i>e</i>
<i>T</i>	<i>a</i>	<i>cS</i>		

Derivation:

S; iST; iiSTT; iiTT; iiaT; iiaacS; iiaac

Parsed

i	i	a	c	\$
---	---	---	---	----

Example 5

	<i>a</i>	<i>c</i>	<i>i</i>	\$
<i>S</i>	<i>e</i>	<i>e</i>	<i>iST</i>	<i>e</i>
<i>T</i>	<i>a</i>	<i>cS</i>		

Derivation:

S

Initialized

<i>i</i>	<i>i</i>	<i>a</i>	\$
----------	----------	----------	----

↑

S

\$

Example 5

	a	c	i	$\$$
S	e	e	iST	e
T	a	cS		

Derivation:

 $S; iST$

$M(S, i) = iST$. The stack content is updated and a new step in the derivation is added.

i	i	a	$\$$
-----	-----	-----	------

↑

i
S
T
$\$$

Example 5

	<i>a</i>	<i>c</i>	<i>i</i>	\$
<i>S</i>	<i>e</i>	<i>e</i>	<i>iST</i>	<i>e</i>
<i>T</i>	<i>a</i>	<i>cS</i>		

Derivation:

S; *iST*

Matching the top-of-the-stack terminal with input symbol

<i>i</i>	<i>i</i>	<i>a</i>	\$
----------	----------	----------	----



<i>S</i>
<i>T</i>
\$

Example 5

	a	c	i	$\$$
S	e	e	iST	e
T	a	cS		

Derivation:

 $S; iST; iiSTT$

$M(S, i) = iST$. The stack content is updated and a new step in the derivation is added.

i	i	a	$\$$
-----	-----	-----	------

↑

i
S
T
T
$\$$

Example 5

	<i>a</i>	<i>c</i>	<i>i</i>	\$
<i>S</i>	<i>e</i>	<i>e</i>	<i>iST</i>	<i>e</i>
<i>T</i>	<i>a</i>	<i>cS</i>		

Derivation:

S; *iST*; *iiSTT*

Matching the top-of-the-stack terminal with input symbol

<i>i</i>	<i>i</i>	<i>a</i>	\$
----------	----------	----------	----



<i>S</i>
<i>T</i>
<i>T</i>
\$

Example 5

	a	c	i	\$
S	e	e	iST	e
T	a	cS		

Derivation:

S; iST; iiSTT; iiTT

$M(S, a) = e$. The stack content is updated and a new step in the derivation is added.

i	i	a	\$
---	---	---	----



T
T
\$

Example 5

	a	c	i	$\$$
S	e	e	iST	e
T	a	cS		

Derivation:

 $S; iST; iiSTT; iiTT; iiaT$

$M(T, a) = a$. The stack content is updated and a new step in the derivation is added.

i	i	a	$\$$
-----	-----	-----	------



a
T
$\$$

Example 5

	<i>a</i>	<i>c</i>	<i>i</i>	\$
<i>S</i>	<i>e</i>	<i>e</i>	<i>iST</i>	<i>e</i>
<i>T</i>	<i>a</i>	<i>cS</i>		

Derivation:

S; *iST*; *iiSTT*; *iiTT*; *iaaT*

Matching the top-of-the-stack terminal with input symbol

<i>i</i>	<i>i</i>	<i>a</i>	\$
----------	----------	----------	----



<i>T</i>
\$

Example 5

	a	c	i	$\$$
S	e	e	iST	e
T	a	cS		

Derivation:

S; iST; iiSTT; iiTT; iiaT; ERROR

ERROR as $M(T, \$)$ is \emptyset .

i	i	a	$\$$
-----	-----	-----	------



T
$\$$