CSEN 1002

Task 8: LL(1) Parsing

Outline

- Example Grammar 1
 - Example 1
 - Example 2
 - Example 3
- 2 Example Grammar 2
 - Example 4
 - Example 5

Input

S;A;B# a;b;c;d# S/AaS,d;A/BbBaSc,e;B/e# S/ab,d;A/b,e;B/e# S/\$c;A/a;B/ab

$$\begin{array}{ccc} S & \rightarrow & AaS \mid d \\ A & \rightarrow & BbBaSc \mid \varepsilon \\ B & \rightarrow & \varepsilon \end{array}$$

Input

S;A;B# a;b;c;d# S/AaS,d;A/BbBaSc,e;B/e# S/ab,d;A/b,e;B/e# S/\$c;A/a;B/ab

$$\begin{array}{cccc} S & \rightarrow & AaS \mid d \\ A & \rightarrow & BbBaSc \mid \varepsilon \\ B & \rightarrow & \varepsilon \end{array}$$

LHS	RHS	First	Follow
S	AaS	a,b	\$,c
3	d	d	J,C
Α	BbBaSc	b	а
	е	е	а
В	е	е	a,b

LHS	RHS	First	Follow
S	AaS	a,b	\$,c
	d	d	J,C
Α	BbBaSc	b	2
	е	е	а
В	е	е	a,b

	а	b	С	d	\$
S					
Α					
В					

LHS	RHS	First	Follow
S	AaS	a,b	\$,c
	d	d	J,C
Α	BbBaSc	b	2
	е	е	а
В	е	е	a,b

	а	Ь	С	d	\$
S	AaS	AaS			
Α					
В					

LHS	RHS	First	Follow
S	AaS	a,b	\$,c
	d	d	J,C
Α	BbBaSc	b	2
	е	е	а
В	е	е	a,b

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α					
В					

LHS	RHS	First	Follow
S	AaS	a,b	\$,c
	d	d	J,C
Α	BbBaSc	b	а
4	е	е	а
В	е	е	a,b

	а	b	С	d	\$
S	AaS	AaS		d	
Α		BbBaSc			
В					

LHS	RHS	First	Follow
S	AaS	a,b	\$,c
	d	d	J,C
Α	BbBaSc	b	2
	е	е	а
В	е	е	a,b

	а	b	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В					

LHS	RHS	First	Follow
S	AaS	a,b	\$,c
	d	d	J,C
Α	BbBaSc	b	2
	е	е	а
В	е	е	a,b

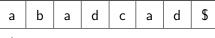
	а	b	С	d	\$
S	AaS	AaS		d	
Α	e	BbBaSc			
В	e	е			

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	e	BbBaSc			
В	e	e			

Derivation:

S

Initialized



	а	Ь	С	d	\$
S	AaS	AaS		d	
A	е	BbBaSc			
В	е	е			

Derivation:

S; AaS

M(S, a) = AaS. The stack content is updated and a new step in the derivation is added.

а	b	а	d	С	а	d	\$
							

A a

a S

\$

	а	Ь	С	d	\$
S	AaS	AaS		d	
A	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS

M(A, a) = e. The stack content is updated and a new step in the derivation is added.

а	b	а	d	С	а	d	\$
							

a S

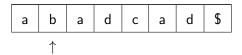
\$

	а	Ь	С	d	\$
S	AaS	AaS		d	
A	e	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS

Matching the top-of-the-stack terminal with input symbol



<u>\$</u>

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	e	е			

Derivation:

S; AaS; aS; aAaS

M(S,b) = AaS. The stack content is updated and a new step in the derivation is added.

а	b	а	d	С	а	d	\$
							

Α

	а	Ь	С	d	\$
S	AaS	AaS		d	
A	e	BbBaSc			
В	е	е			

Derivation:

M(A, b) = BbBaSc. The stack content is updated and a new step in the derivation is added.

а	b	а	d	С	а	d	\$
	↑						



L		,	
r	_	1	

В

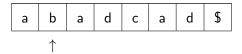


	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS; aBbBaScaS; abBaScaS

M(B,b) = e. The stack content is updated and a new step in the derivation is added.



B





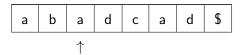


	а	Ь	С	d	\$
S	AaS	AaS		d	
A	e	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS; aBbBaScaS; abBaScaS

Matching the top-of-the-stack terminal with input symbol



а S









	а	Ь	С	d	\$
S	AaS	AaS		d	
A	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; aSaS; aBbBaScaS; abBaScaS; abaScaS

M(B, a) = e. The stack content is updated and a new step in the derivation is added.

а	b	а	d	С	а	d	\$
		↑					

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; aAaS; aBbBaScaS; abBaScaS; abaScaS

Matching the top-of-the-stack terminal with input symbol

а	b	а	d	С	а	d	\$
			\uparrow				

C

	а	Ь	С	d	\$
S	AaS	AaS		d	
A	e	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS; aAaS; aBbBaScaS; abBaScaS; abaScaS; abadcaS

M(S,d) = d. The stack content is updated and a new step in the derivation is added.

а	b	а	d	С	а	d	\$
			↑				

C

	а	Ь	С	d	\$
S	AaS	AaS		d	
A	e	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS; aAaS; aBbBaScaS; abBaScaS; abaScaS; abadcaS

Matching the top-of-the-stack terminal with input symbol

а	b	а	d	С	а	d	\$
				\uparrow			

С

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS; aAaS; aBbBaScaS; abBaScaS; abaScaS; abadcaS

Matching the top-of-the-stack terminal with input symbol

а	b	а	d	С	а	d	\$
					\uparrow		

	а	Ь	С	d	\$
S	AaS	AaS		d	
A	e	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS; aAaS; aBbBaScaS; abBaScaS; abaScaS; abadcaS

Matching the top-of-the-stack terminal with input symbol

а	b	а	d	С	а	d	\$
						↑	

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS; aAaS; aBbBaScaS; abBaScaS; abadcaS; abadcad

M(S,d) = d. The stack content is updated and a new step in the derivation is added.

a b a d c a	d	\$
-------------	---	----

	а	b	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; aSaS; aBbBaScaS; abaScaS; abaScaS; abadcaS; abadcad

Matching the top-of-the-stack terminal with input symbol

a b a d c a d \$

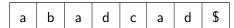
\$

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	e	е			

Derivation:

S; AaS; aSaS; aBbBaScaS; abBaScaS; abaScaS; abadcaS; abadcad

Parsed

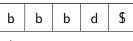


	а	Ь	С	d	\$
S	AaS	AaS		d	
A	е	BbBaSc			
В	е	е			

Derivation:

S

Initialized



	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	е	е			

Derivation:

S; AaS

M(S,b) = AaS. The stack content is updated and a new step in the derivation is added.

b	b	b	d	\$

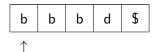
Α

a b c d \$ S AaS AaS d A e BbBaSc B B e e

Derivation:

S; AaS; BbBaScaS

M(A, b) = BbBaSc. The stack content is updated and a new step in the derivation is added.



В











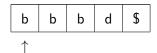


	а	Ь	С	d	\$
S	AaS	AaS		d	
A	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; BbBaScaS; bBaScaS

M(B,b) = e. The stack content is updated and a new step in the derivation is added.



B

S

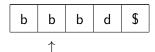
C

	а	Ь	С	d	\$
S	AaS	AaS		d	
A	e	BbBaSc			
В	е	е			

Derivation:

S; AaS; BbBaScaS; bBaScaS

Matching the top-of-the-stack terminal with input symbol



В

а

S

C

а

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; BbBaScaS; bBaScaS; baScaS

M(B,b) = e. The stack content is updated and a new step in the derivation is added.

b	b	b	d	\$
	↑			

a S c a S

	а	Ь	С	d	\$
S	AaS	AaS		d	
A	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; BbBaScaS; bBaScaS; baScaS; ERROR

ERROR as the top of the stack symbol doesn't match the next symbol on the tape

b	b	b	d	\$
	↑			

a S c a

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	е	е			

Derivation:

S

Initialized





<u>S</u>

	а	b	С	d	\$
S	AaS	AaS		d	
A	е	BbBaSc			
В	е	е			

Derivation:

S; AaS

M(S, a) = AaS. The stack content is updated and a new step in the derivation is added.

> b a C

Α

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS

M(A, a) = e. The stack content is updated and a new step in the derivation is added.

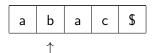
а	b	а	С	\$

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS

Matching the top-of-the-stack terminal with input symbol



<u>S</u>

	а	Ь	С	d	\$
S	AaS	AaS		d	
A	e	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS; aAaS

M(S,b) = AaS. The stack content is updated and a new step in the derivation is added.

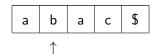
а	b	а	С	\$

Α

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	е	е			

Derivation:

M(A, b) = BbBaSc. The stack content is updated and a new step in the derivation is added.



В

S

C

_						
		a	Ь	С	d	\$
	S	AaS	AaS		d	
	Α	e	BbBaSc			
	В	e	e			

M(B,b) = e. The stack content is updated and a new step in the derivation is added.

а	b	а	С	\$
	↑			

S

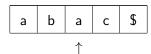
C

	а	Ь	С	d	\$
S	AaS	AaS		d	
A	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS; aAaS; aBbBaScaS; abBaScaS

Matching the top-of-the-stack terminal with input symbol



В

а S

C

а

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	е	е			

Derivation:

M(B, a) = e. The stack content is updated and a new step in the derivation is added.

а	b	а	С	\$

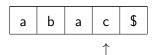
Cа

h d а C S AaS AaS d Α *BbBaSc* e В e е

Derivation:

S; AaS; aS; aAaS; aBbBaScaS; abBaScaS; abaScaS

Matching the top-of-the-stack terminal with input symbol



C

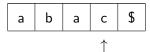
а S

	а	Ь	С	d	\$
S	AaS	AaS		d	
Α	е	BbBaSc			
В	е	е			

Derivation:

S; AaS; aS; aAaS; aBbBaScaS; abBaScaS; abaScaS; ERROR

ERROR as M(S, c) is \emptyset .



S C

Input

S;T# a;c;i# S/iST,e;T/cS,a# S/i,e;T/c,a# S/\$ac;T/\$ac

$$\begin{array}{ccc} \mathcal{S} & \rightarrow & \mathit{iST} \mid \varepsilon \\ \mathcal{T} & \rightarrow & \mathit{cS} \mid \mathit{a} \end{array}$$

Input

S;T# a;c;i# S/iST,e;T/cS,a# S/i,e;T/c,a# S/\$ac;T/\$ac

$$\begin{array}{ccc} S & \rightarrow & iST \mid \varepsilon \\ T & \rightarrow & cS \mid a \end{array}$$

LHS	RHS	First	Follow
S	iST	i	\$,c,a
3	е	е	Ψ,C,a
т	cS	С	\$,c,a
,	а	а	Ψ,C,a

LHS	RHS	First	Follow
S	iST	i	\$,c,a
3	е	е	IJ,C,a
7	cS	С	\$,c,a
'	а	а	Ψ,C,a

	а	С	i	\$
S				
T				

LHS	RHS	First	Follow
S	iST	i	\$,c,a
3	е	е	J,C,a
7	cS	С	\$,c,a
'	а	а	J,C,a

	а	С	i	\$
S			iST	
T				

LHS	RHS	First	Follow
S	iST	i	\$,c,a
3	е	е	J,C,a
7	cS	С	\$,c,a
,	a	а	Ψ,ς,α

	а	С	i	\$
S	e	e	iST	e
T				

LHS	RHS	First	Follow
S	iST	i	\$,c,a
	е	е	J,C,a
7	cS	С	\$,c,a
,	а	а	Ψ, C, a

	а	С	i	\$
S	e	e	iST	e
T		cS		

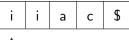
LHS	RHS	First	Follow
S	iST	i	\$,c,a
3	е	е	J,C,a
7	cS	С	\$,c,a
,	а	а	Ψ, C, a

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

S

Initialized





S

	а	С	i	\$
S	e	е	iST	e
T	а	cS		

S; iST

M(S,i) = iST. The stack content is updated and a new step in the derivation is added.

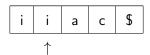
i	i	а	С	\$
				

i S T

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

S; iST

Matching the top-of-the-stack terminal with input symbol



	а	С	i	\$
S	e	е	iST	e
T	а	cS		

Derivation:

S; iST; iiSTT

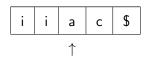
M(S,i) = iST. The stack content is updated and a new step in the derivation is added.

i	i	а	С	\$
	↑			

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

S; iST; iiSTT

Matching the top-of-the-stack terminal with input symbol



S T T

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

Derivation:

S; iST; iiSTT; iiTT

M(S,a) = e. The stack content is updated and a new step in the derivation is added.

i	i	а	С	\$
		\uparrow		

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

S; iST; iiSTT; iiTT; iiaT

M(T, a) = a. The stack content is updated and a new step in the derivation is added.

i	i	а	С	\$
		\uparrow		

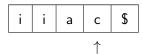
a T \$

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

Derivation:

S; iST; iiSTT; iiTT; iiaT

Matching the top-of-the-stack terminal with input symbol



	а	С	i	\$
S	e	e	iST	e
T	а	cS		

Derivation:

S; iST; iiSTT; iiTT; iiaT; iiacS

M(T,c)=cS. The stack content is updated and a new step in the derivation is added.

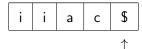
i	i	а	С	\$
			\uparrow	

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

Derivation:

S; iST; iiSTT; iiTT; iiaT; iiacS

Matching the top-of-the-stack terminal with input symbol



<u>S</u>

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

S; iST; iiSTT; iiTT; iiaT; iiacS; iiac

M(S,\$) = e. The stack content is updated and a new step in the derivation is added.

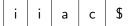
\$

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

Derivation:

S; iST; iiSTT; iiTT; iiaT; iiacS; iiac

Parsed



	а	С	i	\$
S	e	е	iST	e
T	а	cS		

Derivation:

S

Initialized





	а	С	i	\$
S	e	e	iST	e
T	а	cS		

S; iST

M(S,i) = iST. The stack content is updated and a new step in the derivation is added.

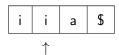
i	i	а	\$

i S T

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

S; iST

Matching the top-of-the-stack terminal with input symbol



S T

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

S; iST; iiSTT

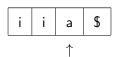
M(S,i) = iST. The stack content is updated and a new step in the derivation is added.

i	i	а	\$
	↑		

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

S; iST; iiSTT

Matching the top-of-the-stack terminal with input symbol



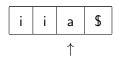
S T T

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

Derivation:

S; iST; iiSTT; iiTT

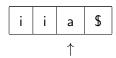
M(S,a) = e. The stack content is updated and a new step in the derivation is added.



	а	С	i	\$
S	e	e	iST	e
T	а	cS		

S; iST; iiSTT; iiTT; iiaT

M(T, a) = a. The stack content is updated and a new step in the derivation is added.



a T \$

	а	С	i	\$
S	e	e	iST	e
T	а	cS		

S; iST; iiSTT; iiTT; iiaT

Matching the top-of-the-stack terminal with input symbol



	а	С	i	\$
S	e	е	iST	e
T	а	cS		

Derivation:

ERROR as M(T,\$) is \varnothing .

T