

# Machine Learning - Module 04 Regularization

Summary: Today you will fight overfitting! You will discover the concepts of regularization and how to implement it into the algorithms you already saw until now.

# Notions and ressources

## Notions of the module

Regularization, overfitting. Regularized loss function, regularized gradient descent. Regularized linear regression. Regularized logistic regression.

#### Useful Ressources

You are strongly advise to use the following resource: Machine Learning MOOC - Stanford Here are the sections of the MOOC that are relevant for today's exercises:

#### Week 3

#### Classification and Representation

- Classification (Video + Reading)
- Hypothesis Representation (Video + Reading)
- Decision Boundary (Video + Reading)

#### Logistic Regression Model

- Cost Function (Video + Reading)
- Simplified Cost Function and Gradient Descent (Video + Reading)

#### **Multiclass Classification**

- Mutliclass Classification: One-vs-all (Video + Reading)
- Review (Reading + Quiz)

# Common Instructions

- The version of Python recommended to use is 3.7, you can check the version of Python with the following command: python -V
- The norm: during this piscine, it is recommended to follow the PEP 8 standards, though it is not mandatory. You can install pycodestyle which is a tool to check your Python code.
- The function eval is never allowed.
- The exercises are ordered from the easiest to the hardest.
- Your exercises are going to be evaluated by someone else, so make sure that your variable names and function names are appropriate and civil.
- Your manual is the internet.
- You can also ask questions in the #bootcamps channel in the 42AI or 42born2code.
- If you find any issue or mistakes in the subject please create an issue on 42AI repository on Github.
- We encourage you to create test programs for your project even though this work won't have to be submitted and won't be graded. It will give you a chance to easily test your work and your peers' work. You will find those tests especially useful during your defence. Indeed, during defence, you are free to use your tests and/or the tests of the peer you are evaluating.
- Submit your work to your assigned git repository. Only the work in the git repository will be graded. If Deepthought is assigned to grade your work, it will be run after your peer-evaluations. If an error happens in any section of your work during Deepthought's grading, the evaluation will stop.

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# Chapter I

# Exercise 00

A WHERE BHITTEN	Exercise: 00		
	Polynomial models II		
Turn-in directory: $ex00/$			
Files to turn in : polynomial_model_extended.py			
Forbide	Forbidden functions: sklearn		

# Objective

Create a function that takes a matrix X of dimensions  $(m \times n)$  and an integer p as input, and returns a matrix of dimension  $(m \times (np))$ . For each column  $x_j$  of the matrix X, the new matrix contains  $x_j$  raised to the power of k, for k = 1, 2, ..., p:

$$x_1 \mid \ldots \mid x_n \mid x_1^2 \mid \ldots \mid x_n^2 \mid \ldots \mid x_1^p \mid \ldots \mid x_n^p$$

#### Instructions

In the polynomial\_model\_extended.py file, write the following function as per the instructions given below:

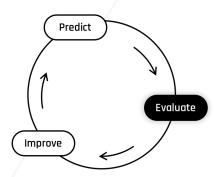
# Examples

# Chapter II

# Exercise 01

#### Interlude

Fighting Overfitting... With Regularization



In the **module07**, we talked about the problem of **overfitting** and the necessity of splitting the dataset into a **training set** and a **test set** in order to spot it. However, being able to detect overfitting does not mean being able to avoid it. To address this important issue, it is time to introduce you to a new technique: **regularization**. If you remember well, overfitting happens because the model takes advantage of irrelevant signals in the training data. The basic idea behind regularization is to **penalize the model for putting too much weight on certain** (usually heavy polynomial) **features**. We do this by adding an extra term in the loss function:

regularized loss function = loss function + 
$$\frac{\lambda}{2m} \sum_{j=1}^{n} \theta_j^2$$

By doing so, we are encouraging the model to keep its  $\theta$  values as small as **possible**. Indeed, the values of  $\theta$  themselves are now taken into account when calculating the loss.

 $\lambda$  (called lambda) is the parameter through which you can modulate how reglarization should impact the model's construction.

- If  $\lambda = 0$ , there is no regularization (as we did until now).
- If  $\lambda$  is very large, it will drive all the  $\theta$  parameters to 0.



In the regularization term, the sum starts at j=1 because we do NOT want to penalize the value of  $\theta_0$  (the y-intercept, which doesn't depend on a feature).

#### Be carefull!

Machine Learning was essentially developed by computer scientists (not mathematicians). This can cause problems when we try to represent things mathematically. For example: using the  $\theta_0$  notation to represent the y-intercept makes things easy when we apply the linear algebra trick, **but** it completly messes up the overall matrix notation! According to that notation, the X' matrix has the following properties:

- its rows,  $x'^{(i)}$ , follow the mathematical indexing: starting at 1.
- its columns,  $x_{i}^{'}$ , follow the computer science indexing: starting at 0.

$$X' = \underbrace{\begin{bmatrix} 1 & x_1^{(1)} & \dots & x_n^{(1)} \\ \vdots & \vdots & \ddots & \vdots \\ 1 & x_1^{(m)} & \dots & x_n^{(m)} \end{bmatrix}}_{i = 0, \dots, n} = \begin{bmatrix} x_0^{(1)} & x_1^{(1)} & \dots & x_n^{(1)} \\ \vdots & \vdots & \ddots & \vdots \\ x_0^{(m)} & x_1^{(m)} & \dots & x_n^{(m)} \end{bmatrix} }_{i = 1, \dots, m}$$

It's precisely for this reason that you keep seeing that X' is of dimension  $(m \times (n+1))$ .

#### Terminology

The regularization technique we are introducing here is named  $L_2$  regularization, because it adds the squared  $L_2$  norm of the  $\theta$  vector to the loss function. The  $L_2$  norm of a given vector x, written

$$L_2(x) = ||x||_2 = \sqrt{\sum_i x_i^2} L_2(x)^2 = ||x||_2^2 = \sum_i x_i^2$$

is its **euclidean norm** (i.e. the sum of the components squared).

There is an infinite variety of norms that could be used as regularization terms, depending on the desired regularization effect. Here, we will only use  $L_2$ , the most common one.



The notation  $\sum_i$  means: "the sum for all i" There is no need to give explicitly the start and the end of the summation index if we want to sum over all the values of i. However, it is better to do it anyway because it forces us to be sure of what we are doing. And in our case, we do not want to sum over  $\theta_0$  ...

#### Our old friend vectorization ...

It is not a surprise, we can use vectorization to calculate  $\sum_{j=1}^{n} \theta_{j}^{2}$  more efficiently. It could be a good exercise for you to try to figure it out by yourself. We suggest you give it a try and then check the answer on the next page.

## Answers to the Vectorization Problem

So, how do you vectorize the following?

$$\sum_{i=j}^{n} \theta_j^2$$

It's very similar to a **dot product** of  $\theta$  with itself. The only problem here is to find a way to not take  $\theta_0$  into account.

Let's construct a vector  $\theta'$  with the following rules :

$$\theta'_0 = 0$$
 $\theta'_j = \theta_j \text{ for } j = 1, \dots, n$ 

In other words:

$$\theta' = \begin{bmatrix} 0 \\ \theta_1 \\ \vdots \\ \theta_n \end{bmatrix}$$

This way, we can perform the dot product without having  $\theta_0$  interfering in our calculations:

$$\theta' \cdot \theta' = \begin{bmatrix} 0 \\ \theta_1 \\ \vdots \\ \theta_n \end{bmatrix} \cdot \begin{bmatrix} 0 \\ \theta_1 \\ \vdots \\ \theta_n \end{bmatrix}$$

$$= 0 \cdot 0 + \theta_1 \cdot \theta_1 + \dots + \theta_n \cdot \theta_n$$

$$= \sum_{j=1}^n \theta_j^2$$

Q MITCH BILLIAND	Exercise: 01	
	L2 Regularization	
Turn-in	$a  ext{ directory}: ex01/$	
Files to	o turn in: 12_reg.py	
Forbide	den functions : sklearn	

# Objective

You must implement the following formulas as functions:

#### Iterative

$$L_2(\theta)^2 = \sum_{j=1}^n \theta_j^2$$

Where:

•  $\theta$  is a vector of dimension (n+1).

#### Vectorized

$$L_2(\theta)^2 = \theta' \cdot \theta'$$

Where:

•  $\theta'$  is a vector of dimension (n+1), constructed using the following rules:

$$\theta'_0 = 0$$
 $\theta'_j = \theta_j \quad \text{for } j = 1, \dots, n$ 

# Instructions

In the  $12\_reg.py$  file, write the following function as per the instructions given below:

## Examples

```
x = np.array([2, 14, -13, 5, 12, 4, -19]).reshape((-1, 1))
# Example 1:
iterative_l2(x)
# Output:
911.0

# Example 2:
12(x)
# Output:
911.0

y = np.array([3,0.5,-6]).reshape((-1, 1))
# Example 3:
iterative_l2(y)
# Output:
36.25

# Example 4:
12(y)
# Output:
36.25
```

# Chapter III

# Exercise 02

2. WHERE WILLIAMS	Exercise: 02		
	Regularized Linear Loss Function		
Turn-in directory: $ex02/$			
Files to turn in : linear_loss_reg.py			
Forbide	Forbidden functions: sklearn		

# Objective

You must implement the following formula as a function:

$$J(\theta) = \frac{1}{2m} [(\hat{y} - y) \cdot (\hat{y} - y) + \lambda(\theta' \cdot \theta')]$$

Where:

- y is a vector of dimension m, the expected values,
- $\hat{y}$  is a vector of dimension m, the predicted values,
- $\lambda$  is a constant, the regularization hyperparameter,
- $\theta'$  is a vector of dimension n, constructed using the following rules:

$$\theta'_0 = 0$$
 $\theta'_j = \theta_j \quad \text{for } j = 1, \dots, n$ 

## Instructions

In the linear\_loss\_reg.py file, write the following function as per the instructions given below:



such situation is a good use case for decorators...

## Examples

```
y = np.array([2, 14, -13, 5, 12, 4, -19]).reshape((-1, 1))
y_hat = np.array([3, 13, -11.5, 5, 11, 5, -20]).reshape((-1, 1))
theta = np.array([1, 2.5, 1.5, -0.9]).reshape((-1, 1))

# Example :
reg_loss_(y, y_hat, theta, .5)
# Output:
0.8503571428571429

# Example :
reg_loss_(y, y_hat, theta, .05)
# Output:
0.5511071428571429

# Example :
reg_loss_(y, y_hat, theta, .9)
# Output:
1.116357142857143
```

# Chapter IV

# Exercise 03

S WASCAN BATTREESE	Exercise: 03	
	Regularized Logistic Loss Function	
Turn-in directory: $ex03/$		
Files to turn in : logistic_loss_reg.py		
Forbidden functions: sklearn		

## Objective

You must implement the following formula as a function:

$$J(\theta) = -\frac{1}{m} [y \cdot \log(\hat{y}) + (\vec{1} - y) \cdot \log(\vec{1} - \hat{y})] + \frac{\lambda}{2m} (\theta' \cdot \theta')$$

Where:

- $\hat{y}$  is a vector of dimension m, the vector of predicted values,
- $\bullet$  y is a vector of dimension m, the vector of expected values,
- $\vec{1}$  is a vector of dimension m, a vector full of ones,
- $\bullet~\lambda$  is a constant, the regularization hyperparameter,
- $\theta'$  is a vector of dimension n, constructed using the following rules:

$$\theta'_0 = 0$$
 $\theta'_j = \theta_j \text{ for } j = 1, \dots, n$ 

## Instructions

In the logistic\_loss\_reg.py file, write the following function as per the instructions given below:



this is a good use case for decorators...

## Examples

```
y = np.array([1, 1, 0, 0, 1, 1, 0]).reshape((-1, 1))
y_hat = np.array([.9, .79, .12, .04, .89, .93, .01]).reshape((-1, 1))
theta = np.array([1, 2.5, 1.5, -0.9]).reshape((-1, 1))

# Example :
reg_log_loss_(y, y_hat, theta, .5)
# Output:
0.43377043716475955

# Example :
reg_log_loss_(y, y_hat, theta, .05)
# Output:
0.13452043716475953

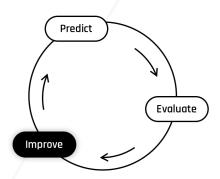
# Example :
reg_log_loss_(y, y_hat, theta, .9)
# Output:
0.6997704371647596
```

# Chapter V

# Exercise 04

#### Interlude

#### Regularized Gradient



To derive the gradient of the regularized loss function,  $\nabla(J)$  you have to change a bit the formula of the unregularized gradient. Given the fact that we are not penalizing  $\theta_0$ , the formula will remain the same as before for this parameter. For the other parameters  $(\theta_1, \ldots, \theta_n)$ , we must add the partial derivative of the regularization term:  $\lambda \theta_j$ .

Therefore, we get:

$$\nabla(J)_0 = \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})$$

$$\nabla(J)_{j} = \frac{1}{m} \left( \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)}) x_{j}^{(i)} + \lambda \theta_{j} \right) \text{ for } j = 1, ..., n$$

Where:

- $\nabla(J)_j$  is the j<sup>th</sup> component of the gradient vector  $\nabla(J)$ ,
- *m* is the number of training examples used,
- $h_{\theta}(x^{(i)})$  is the model's prediction for the i<sup>th</sup> training example,
- $x^{(i)}$  is the feature vector of the i<sup>th</sup> training example,
- $y^{(i)}$  is the expected target value for the i<sup>th</sup> example,
- $\lambda$  is a constant, the regularization hyperparameter,

•  $\theta_j$  is the j<sup>th</sup> parameter of the  $\theta$  vector.

Which can be vectorized as:

$$\nabla(J) = \frac{1}{m} [X'^{T}(h_{\theta}(X) - y) + \lambda \theta']$$

Where:

- $\nabla(J)$  is a vector of dimension (n+1) the gradient vector,
- $\bullet$  m is the number of training examples used,
- X is a matrix of dimension  $(m \times n)$ , the design matrix,
- X' is a matrix of dimension  $(m \times (n+1))$ , the design matrix onto which a column of ones is added as a first column,
- y is a vector of dimension m, the vector of expected values,
- $h_{\theta}(X)$  is a vector of dimension m, the vector of predicted values,
- $\lambda$  is a constant,
- $\theta$  is a vector of dimension (n+1), the parameter vector,
- $\theta'$  is a vector of dimension (n+1), constructed using the following rules:

$$\theta'_0 = 0$$
 $\theta'_j = \theta_j \text{ for } j = 1, \dots, n$ 

## Linear Gradient vs Logistic Gradient

As before, we draw your attention on the only difference between linear regression and logistic regression's gradient equations: the hypothesis function  $h_{\theta}(X)$ .

- In the linear regression:  $h_{\theta}(X) = X'\theta$ ,
- In the logistic regression:  $h_{\theta}(X) = \operatorname{sigmoid}(X'\theta)$ .

A MITTERS BETWEENER	Exercise: 04		
	Regularized Linear Gradient		
Turn-in directory : $ex04/$			
Files to turn in : reg_linear_grad.py			
Forbide	Forbidden functions: sklearn		

## Objective

You must implement the following formulas as a functions for the **linear regression hypothesis**:

#### Iterative

$$\nabla(J)_0 = \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$

$$\nabla(J)_j = \frac{1}{m} \left( \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)} + \lambda \theta_j \right) \text{ for } j = 1, \dots, n$$

Where:

- $\nabla(J)_j$  is the j<sup>th</sup> component of  $\nabla(J)$ ,
- $\nabla(J)$  is a vector of dimension (n+1), the gradient vector,
- ullet m is a constant, the number of training examples used,
- $h_{\theta}(x^{(i)})$  is the model's prediction for the i<sup>th</sup> training example,
- $x^{(i)}$  is the feature vector (of dimension n) of the i<sup>th</sup> training example, found in the i<sup>th</sup> row of the X matrix,
- X is a matrix of dimensions  $(m \times n)$ , the design matrix,
- $y^{(i)}$  is the i<sup>th</sup> component of the y vector,
- ullet y is a vector of dimension m, the vector of expected values,
- $\bullet~\lambda$  is a constant, the regularization hyperparameter,
- $\theta_j$  is the j<sup>th</sup> parameter of the  $\theta$  vector,
- $\theta$  is a vector of dimension (n+1), the parameter vector.

#### Vectorized

$$\nabla(J) = \frac{1}{m} [X'^{T}(h_{\theta}(X) - y) + \lambda \theta']$$

Where:

- $\nabla(J)$  is a vector of dimension (n+1), the gradient vector,
- *m* is a constant, the number of training examples used,
- X is a matrix of dimensions  $(m \times n)$ , the design matrix,
- X' is a matrix of dimensions  $(m \times (n+1))$ , the design matrix onto which a column of ones is added as a first column,
- $X^{T}$  is the transpose of the matrix, with dimensions  $((n+1) \times m)$ ,
- $h_{\theta}(X)$  is a vector of dimension m, the vector of predicted values,
- y is a vector of dimension m, the vector of expected values,
- $\lambda$  is a constant, the regularization hyperparameter,
- $\theta$  is a vector of dimension (n+1), the parameter vector,
- $\theta'$  is a vector of dimension (n+1), constructed using the following rules:

$$\theta'_0 = 0 
\theta'_j = \theta_j \text{ for } j = 1, \dots, n$$

## Instructions

In the reg\_linear\_grad.py file, write the following functions as per the instructions given below:

```
reg_linear_grad(y, x, theta, lambda_):
"""Computes the regularized linear gradient of three non-empty numpy.ndarray,
   with two for-loop. The three arrays must have compatible shapes.
         y: has to be a numpy.ndarray, a vector of shape m * 1.
        x: has to be a numpy.ndarray, a matrix of dimesion m * n.
theta: has to be a numpy.ndarray, a vector of shape (n + 1) * 1.
lambda_: has to be a float.
        A numpy.ndarray, a vector of shape (n + 1) * 1, containing the results of the formula for all j. None if y, x, or theta are empty numpy.ndarray. None if y, x or theta does not share compatibles shapes.
         None if y, x or theta or lambda_ is not of the expected type.
        This function should not raise any Exception.
      ... Your code ...
def vec_reg_linear_grad(y, x, theta, lambda_):
      """Computes the regularized linear gradient of three non-empty numpy.ndarray, without any for-loop. The three arrays must have compatible shapes.
      Args
        y: has to be a numpy.ndarray, a vector of shape m * 1. x: has to be a numpy.ndarray, a matrix of dimesion m * n.
         theta: has to be a numpy.ndarray, a vector of shape (n + 1) * 1.
      Return:
         A numpy.ndarray, a vector of shape (n + 1) * 1, containing the results of the formula for all j.
        None if y, x, or theta are empty numpy.ndarray.

None if y, x or theta does not share compatibles shapes.

None if y, x or theta or lambda_ is not of the expected type.
      Raises:
```



this is a good use case for decorators...

## Examples

```
x = np.array([
[ 1, -5, 11],

[ 9, -11, 8]])

y = np.array([[2], [14], [-13], [5], [12], [4], [-19]])

theta = np.array([[7.01], [3], [10.5], [-6]])
reg_linear_grad(y, x, theta, 1)
array([[ -60.99
vec_reg_linear_grad(y, x, theta, 1)
array([[ -60.99
reg_linear_grad(y, x, theta, 0.5)
array([[ -60.99
vec_reg_linear_grad(y, x, theta, 0.5)
array([[ -60.99
reg_linear_grad(y, x, theta, 0.0)
array([[ -60.99
                   [-643.66428571]])
vec_reg_linear_grad(y, x, theta, 0.0)
array([[ -60.99
                   [-643.66428571]])
```

# Chapter VI

# Exercise 05

22. MINESS. BILLIONS	Exercise: 05		
	Regularized Logistic Gradient		
Turn-in	directory: $ex05/$		
Files to turn in : reg_logistic_grad.py			
Forbido	Forbidden functions: sklearn		

# Objective

You must implement the following formulas as a functions for the **logistic regression hypothesis**:

#### Iterative

$$\nabla(J)_0 = \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$

$$\nabla(J)_j = \frac{1}{m} \left( \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)} + \lambda \theta_j \right) \text{ for } j = 1, \dots, n$$

Where:

- $\nabla(J)_j$  is the j<sup>th</sup> component of  $\nabla(J)$ ,
- $\nabla(J)$  is a vector of dimension (n+1), the gradient vector,
- m is a constant, the number of training examples used,
- $h_{\theta}(x^{(i)})$  is the model's prediction for the i<sup>th</sup> training example,
- $x^{(i)}$  is the feature vector of dimension n) of the i<sup>th</sup> training example, found in the i<sup>th</sup> row of the X matrix,
- X is a matrix of dimensions  $(m \times n)$ , the design matrix,

- $y^{(i)}$  is the i<sup>th</sup> component of the y vector,
- y is a vector of dimension m, the vector of expected values,
- $\lambda$  is a constant, the regularization hyperparameter,
- $\theta_i$  is the j<sup>th</sup> parameter of the  $\theta$  vector,
- $\theta$  is a vector of dimension (n+1), the parameter vector.

#### Vectorized

$$\nabla(J) = \frac{1}{m} [X'^{T}(h_{\theta}(X) - y) + \lambda \theta']$$

Where:

- $\nabla(J)$  is a vector of dimension (n+1), the gradient vector,
- $\bullet$  m is a constant, the number of training examples used,
- X is a matrix of dimensions  $(m \times n)$ , the design matrix,
- X' is a matrix of dimensions  $(m \times (n+1))$ , the design matrix onto which a column of ones is added as a first column,
- $X^{T}$  is the transpose of the matrix, with dimensions  $((n+1) \times m)$ ,
- $h_{\theta}(X)$  is a vector of dimension m, the vector of predicted values,
- $\bullet$  y is a vector of dimension m, the vector of expected values,
- $\lambda$  is a constant, the regularization hyperparameter,
- $\theta$  is a vector of dimension (n+1), the parameter vector,
- $\theta'$  is a vector of dimension (n+1), constructed using the following rules:

$$\theta'_0 = 0 
\theta'_j = \theta_j \text{ for } j = 1, \dots, n$$

#### Instructions

In the reg\_logistic\_grad.py file, create the following function as per the instructions given below:



this is a good use case for decorators...

## Examples

```
x = np.array([[0, 2, 3, 4],
y = np.array([[0], [1], [1]])
theta = np.array([[-2.4], [-1.5], [0.3], [-1.4], [0.7]])
# Example 1.1:
reg_logistic_grad(y, x, theta, 1)
vec_reg_logistic_grad(y, x, theta, 1)
# Output
array([[-0.55711039],
reg_logistic_grad(y, x, theta, 0.5)
# Output:
array([[-0.55711039],
                 [-2.33404624],
vec_reg_logistic_grad(y, x, theta, 0.5)
array([[-0.55711039],
reg_logistic_grad(y, x, theta, 0.0)
# Output:
array([[-0.55711039],
[-0.90334809],
vec_reg_logistic_grad(y, x, theta, 0.0)
array([[-0.55711039],
[-0.90334809],
```

# Chapter VII

# Exercise 06

#### Interlude

#### Linear Regression to the Next Level: Ridge Regression

Until now we only talked about  $L_2$  regularization and its implication on the calculation of the loss function and gradient for both linear and logistic regression.

Now it's time to use proper terminology: When we apply  $L_2$  regularization on a linear regression model, the new model is called a **Ridge Regression** model. Besides that brand-new name, Ridge regression is nothing more than linear regression regularized with  $L_2$ .

We suggest you watch this nice explanation very nice explanation of Ridge Regularization. By the way, this Youtube channel, StatQuest, is very good to help you understand the gist of a lot of machine learning concepts. You will not waste your time watching its statistics and machine learning playlists!

S wisen summer	Exercise: 06	
	Ridge Regression	
Turn-in	directory: $ex06/$	
Files to turn in : ridge.py		
Forbido	den functions : sklearn	

## Objective

Now it's time to implement your MyRidge class, similar to the class of the same name in sklearn.linear model.

#### Instructions

In the ridge.py file, create the following class as per the instructions given below: Your MyRidge class will have at least the following methods:

- \_\_init\_\_, special method, similar to the one you wrote in MyLinearRegression (module06),
- get\_params\_, which get the parameters of the estimator,
- set\_params\_, which set the parameters of the estimator,
- loss\_, which return the loss between 2 vectors (numpy arrays),
- loss\_elem\_, which return a vector corresponding to the squared diffrence between 2 vectors (numpy arrays),
- predict\_, which generates predictions using a linear model,
- gradient\_, which calculates the vectorized regularized gradient,
- fit\_, which fits Ridge regression model to a training dataset.



You should consider inheritance from MyLinearRegression.

If MyRidge inheritates from MyLinearRegression, you may not need to reimplement predict\_ method.

The difference between loss\_elem\_, loss\_, gradient\_ and fit\_ methods implementation MyRidge's and MyLinearRegression (implemented in module 02) is the use of a regularization term.



again, this is a good use case for decorators...

# Chapter VIII

# Exercise 07

CS. WEREIN BELLINOSE	Exercise: 07	
	Practicing Ridge Regression	
Turn-in	directory: $ex07/$	
Files to turn in: space_avocado.py, benchmark_train.py,		
models.[csv/yml/pickle]		
Forbidden functions: sklearn		

## Objective

It's training time! Let's practice our brand new Ridge Regression with a polynomial model.

#### Introduction

You have already used the dataset space\_avocado.csv. The dataset is constituted of 5 columns:

- index: not relevant,
- weight: the avocado weight order (in ton),
- prod\_distance: distance from where the avocado ordered is produced (in Mkm),
- time\_delivery: time between the order and the receipt (in days),
- target: price of the order (in trantorian unit).

It contains the data of all the avocado purchase made by Trantor administration (guacamole is a serious business there).

#### Instructions

You have to explore different models and select the best you find. To do this:

- Split your space\_avocado.csv dataset into a training, a cross-validation and a test sets.
- Use your polynomial\_features method on your training set.
- Consider several Linear Regression models with polynomial hypotheses with a maximum degree of 4.
- For each hypothesis consider a regularized factor ranging from 0 to 1 with a step of 0.2.
- Evaluate your models on the cross-validation set.
- Evaluate the best model on the test set.

According to your model evaluations, what is the best hypothesis you can get?

- Plot the evaluation curve which help you to select the best model (evaluation metrics vs models  $+ \lambda$  factor).
- Plot the true price and the predicted price obtain via your best model with the different  $\lambda$  values (meaning the dataset + the 5 predicted curves).

The training of all your models can take a long time. Thus you need to train only the best one during the correction. But, you should return in benchmark\_train.py the program which perform the training of all the models and save the parameters of the different models into a file. In models.[csv/yml/pickle] one must find the parameters of all the models you have explored and trained. In space\_avocado.py train the model based on the best hypothesis you find and load the other models from models.[csv/yml/pickle]. Then evaluate the best model on the right set and plot the different graphics as asked before.

# Chapter IX

# Exercise 08

## Interlude

#### Regularized Logistic Regression is still Logistic Regression

As opposed to linear regression, **regularized logistic regression is still called logistic regression**.

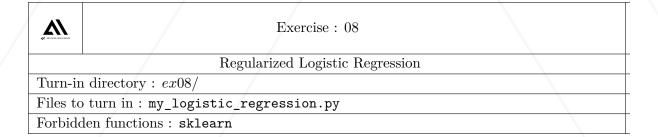
Working without regularization parameters can be considered simply as a special case where  $\lambda=0$ .

if  $\lambda = 0$ :

$$\nabla(J) = \frac{1}{m} [X'^T (h_{\theta}(X) - y) + \lambda \theta']$$

$$= \frac{1}{m} [X'^T (h_{\theta}(X) - y) + 0 \cdot \theta']$$

$$= \frac{1}{m} [X'^T (h_{\theta}(X) - y)]$$



## Objective

In the last exercise, you implemented of a regularized version of the linear regression algorithm, called Ridge regression. Now it's time to update your logistic regression classifier as well! In the scikit-learn library, the logistic regression implementation offers a few regularization techniques, which can be selected using the parameter penalty (L<sub>2</sub> is default). The goal of this exercise is to update your old MyLogisticRegression class to take that into account.

#### Instructions

In the my\_logistic\_regression.py file, update your MyLogisticRegression class according to the following:

• add a penalty parameter which can take the following values: '12', 'none' (default value is '12').

- update the fit\_(self, x, y) method:
  - o if penalty == '12': use a regularized version of the gradient descent.
  - if penalty = 'none': use the unregularized version of the gradient descent from module03.

# Examples

```
from my_logistic_regression import MyLogisticRegression as mylogr
theta = np.array([[-2.4], [-1.5], [0.3], [-1.4], [0.7]])

# Example 1:
model1 = mylogr(theta, lambda_=5.0)

model1.penality
# Output
'12'

model1.lambda_
# Output
5.0

# Example 2:
model2 = mylogr(theta, penality=None)

model2.penality
# Output
None

model2.lambda_
# Output
0.0

# Example 3:
model3 = mylogr(theta, penality=None, lambda_=2.0)

model3.penality
# Output
None

model3.lambda_
# Output
None
```



this is also a great use case for decorators...

# Chapter X

# Exercise 09

S WINCH BUILDINGS	Exercise: 09	
	Practicing Regularized Logistic Regression	
Turn-in	$a  ext{ directory}: ex09/$	
Files to turn in: solar_system_census.py, benchmark_train.py,		
models.[csv/yml/pickle]		
Forbidden functions: sklearn		

## Objective

It's training time! Let's practice our updated Logistic Regression with polynomial models.

#### Introduction

You have already used the dataset solar\_system\_census.csv and solar\_system\_census\_planets.cs

- The dataset is divided in two files which can be found in the resources folder: solar\_system\_census.csv and solar\_system\_census\_planets.csv.
- The first file contains biometric information such as the height, weight, and bone density of several Solar System citizens.
- The second file contains the homeland of each citizen, indicated by its Space Zipcode representation (i.e. one number for each planet... :)).

As you should know, Solar citizens come from four registered areas (zipcodes):

- The flying cities of Venus (0),
- United Nations of Earth (1),
- Mars Republic (2),
- The Asteroids' Belt colonies (3).

#### Instructions

#### Split the Data

Take your solar\_system\_census.csv dataset and split it in a training set, a cross-validation set and a test set.

#### Training and benchmark

One part of your submission will be find in benchmark\_train.py and models.[csv/yml/pickle] files. You have to:

- Train different regularized logistic regression models with a polynomial hypothesis of **degree 3**. The models will be trained with different  $\lambda$  values, ranging from 0 to 1. Use one-vs-all method.
- Evaluate the f1 score of each of the models on the cross-validation set. You can use the f1\_score\_function that you wrote in the ex11 of module08.
- Save the different models into a models. [csv/yml/pickle].

#### Solar system census program

The second and last part of your submission is in solar\_system\_census.py. You have to:

- Loads the differents models from models. [csv/yml/pickle] and train from scratch only the best one on a training set.
- Visualize the performance of the different models with a bar plot showing the score of the models given their  $\lambda$  value.
- Print the **f1 score** of all the models calculated on the test set.
- Visualize the target values and the predicted values of the best model on the same scatterplot. Make some effort to have a readable figure.



For the second script solar\_system\_census.py, only a train and test set are necessary as one is simply looking to the performance.

# Chapter XI

# Conclusion - What you have learnt

The excercises serie is finished, well done! Based on all the knowledges tackled today, you should be able to discuss and answer the following questions:

- 1. Why do we use logistic hypothesis for a classification problem rather than a linear hypothesis?
- 2. What is the decision boundary?
- 3. In the case we decide to use a linear hypothesis to tackle a classification problem, why the classification of some data points can be modified by considering more examples (for example, extra data points with extrem ordinate)?
- 4. In a one versus all classification approach, how many logisitic regressor do we need to distinguish between N classes?
- 5. Can you explain the difference between accuracy and precision? What is the type I and type II errors?
- 6. What is the interest of the F1-score?

#### Contact

You can contact 42AI association by email: contact@42ai.fr You can join the association on 42AI slack and/or posutale to one of the association teams.

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