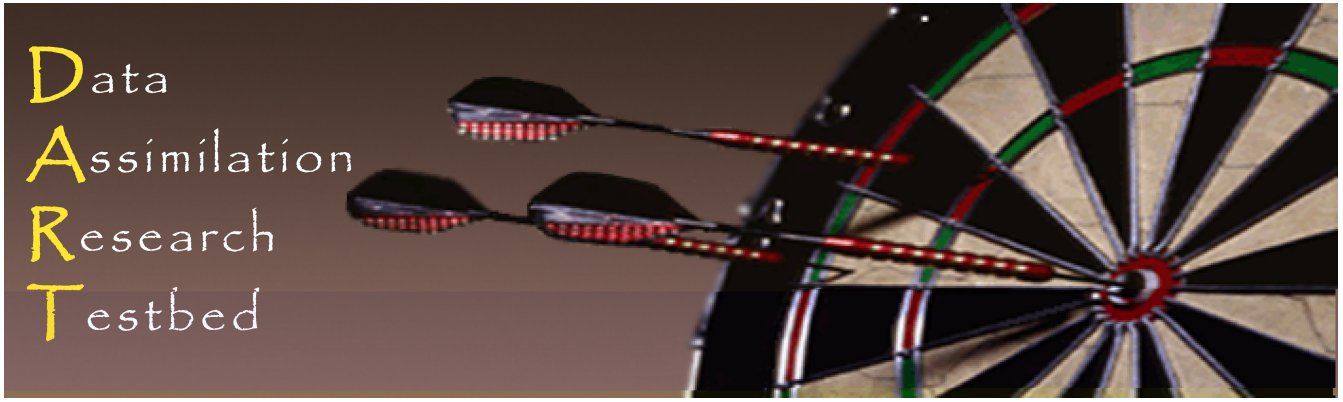
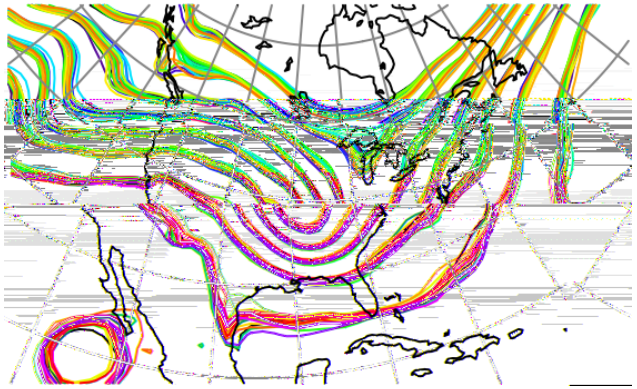


DART Tutorial Section 4:
How should observations impact an unobserved state variable? Multivariate assimilation.



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Single observed variable, single unobserved variable.

So far, have known observation likelihood for single variable.

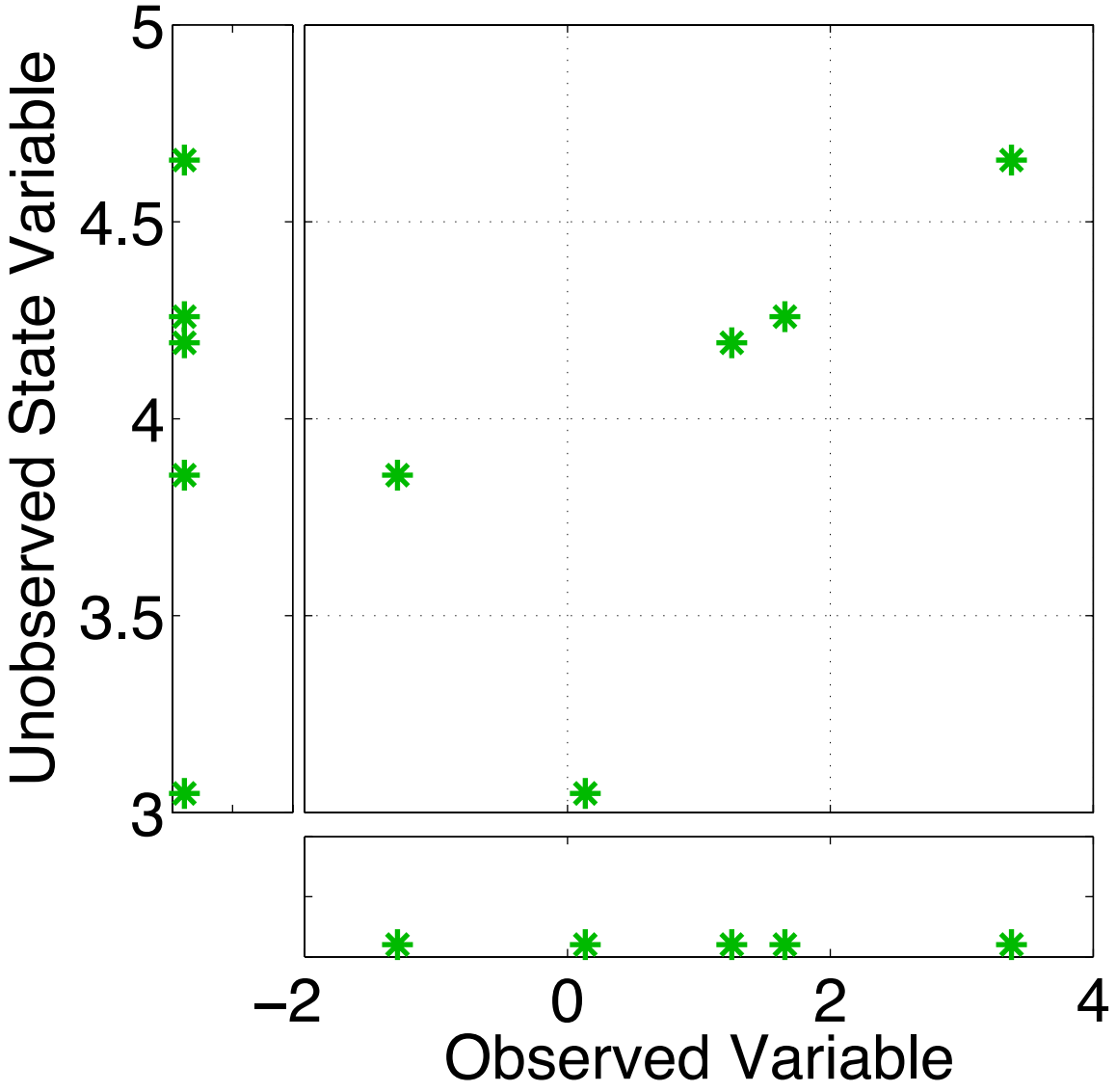
Now, suppose prior has an additional variable.

Will examine how ensemble methods update additional variable.

Basic method generalizes to any number of additional variables.

Methods related to Kalman filter in some sense, but not done here.

Ensemble filters: Updating additional prior state variables

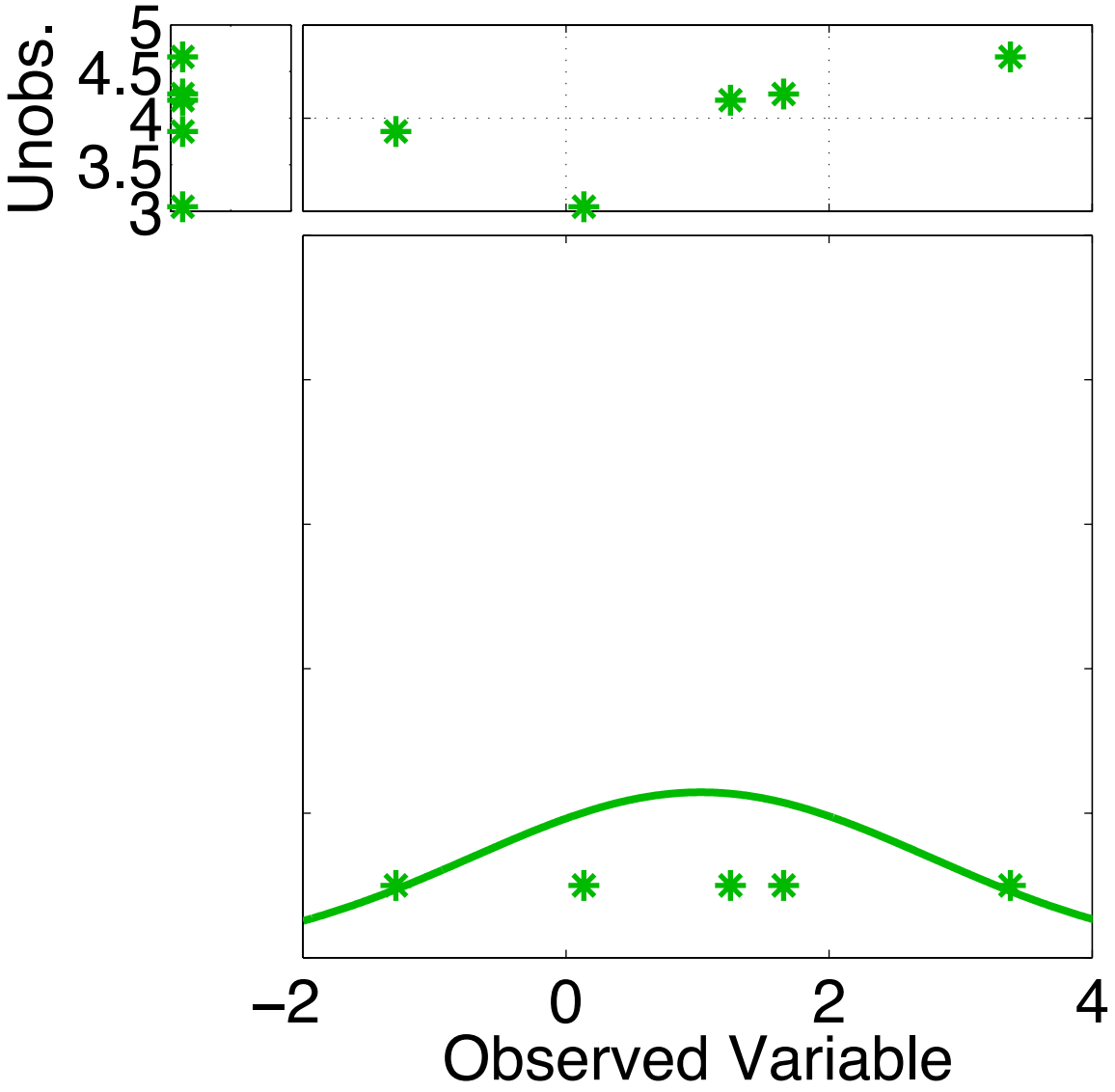


Assume that all we know is the prior joint distribution.

One variable is observed.

What should happen to the unobserved variable?

Ensemble filters: Updating additional prior state variables

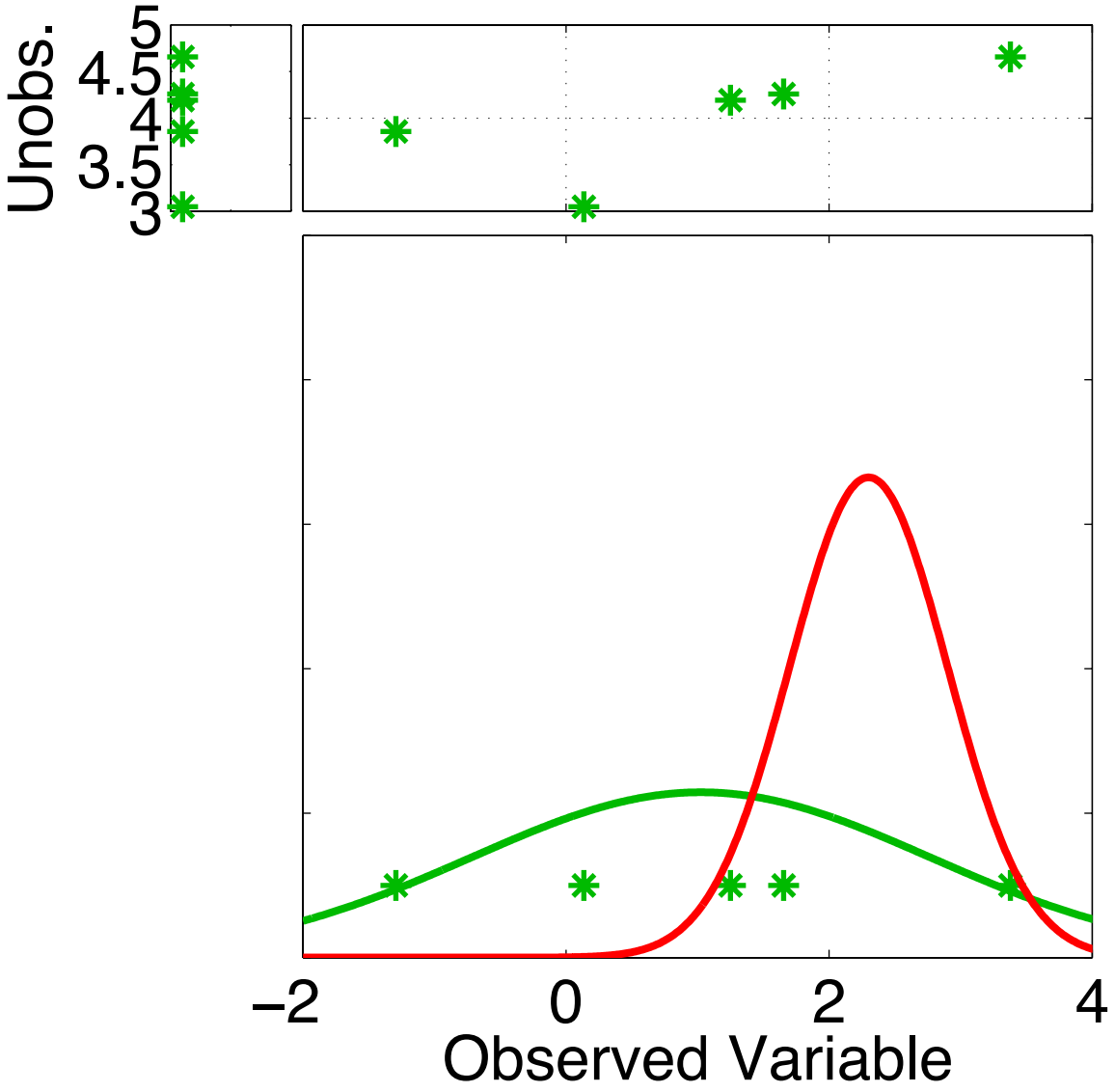


Assume that all we know is the prior joint distribution.

One variable is observed.

Update observed variable with one of the previous methods.

Ensemble filters: Updating additional prior state variables



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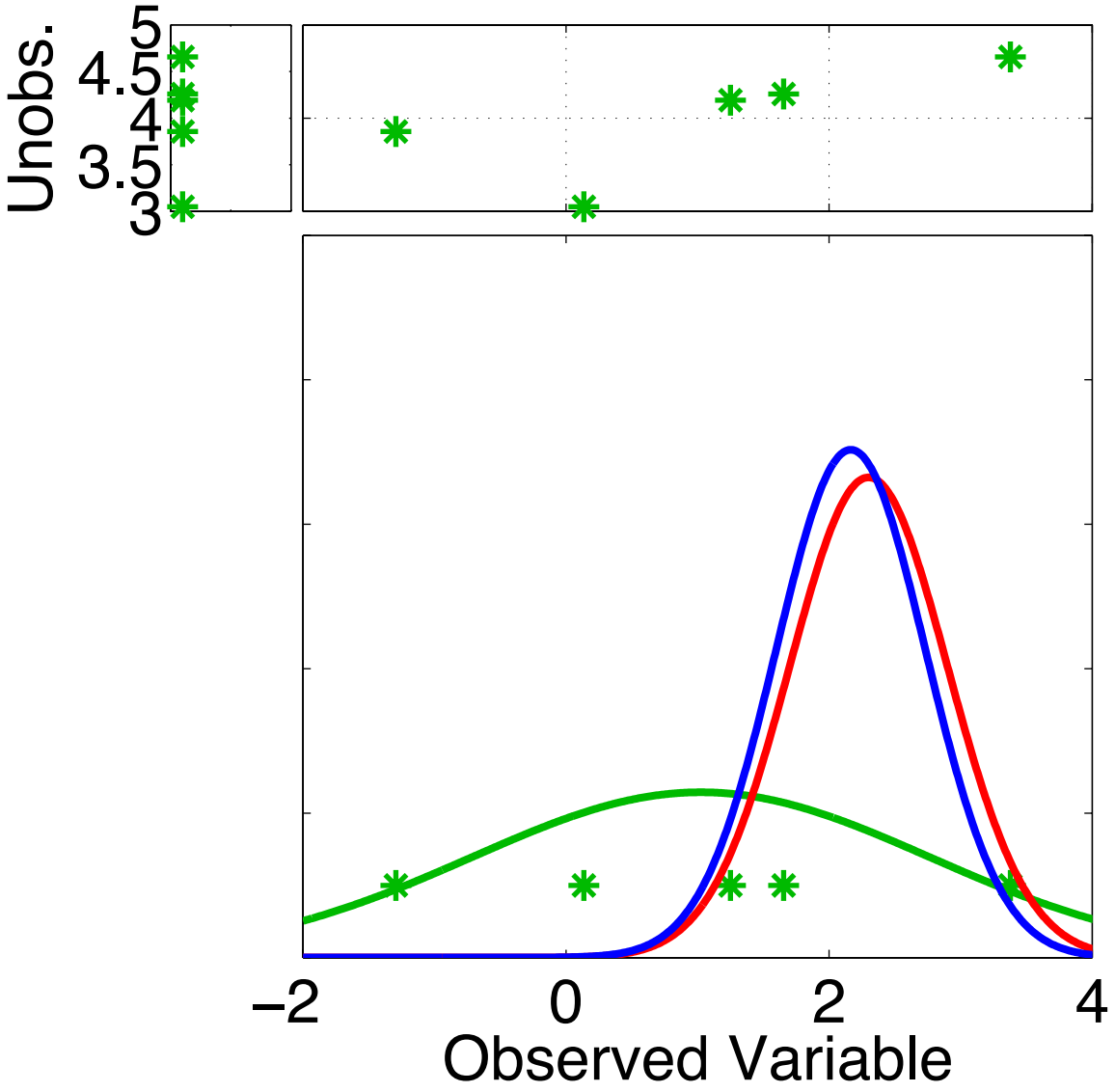
Ensemble filters: Updating additional prior state variables



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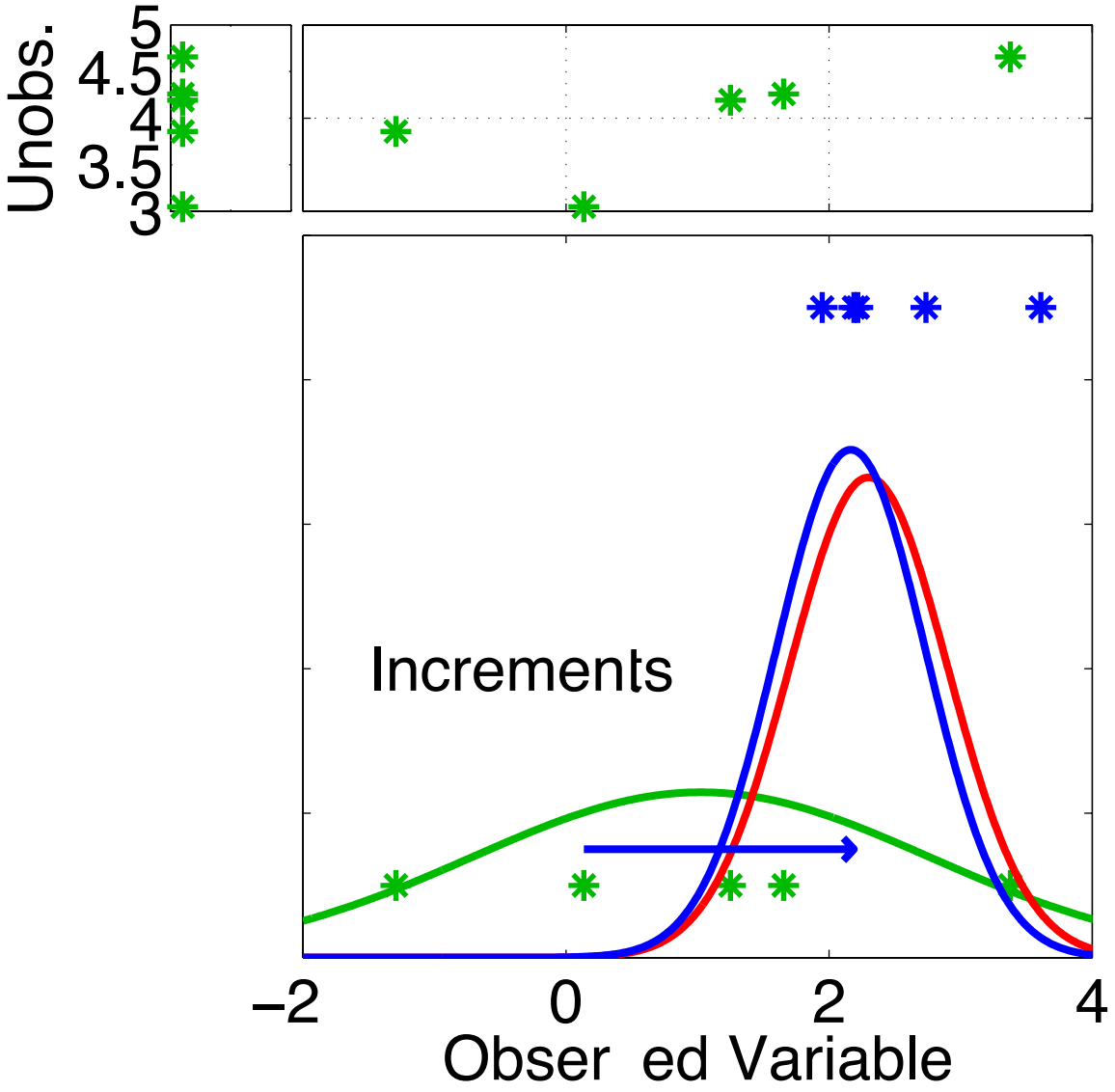
Update observed variable with one of the previous methods.

Ensemble filters: Updating additional prior state variables

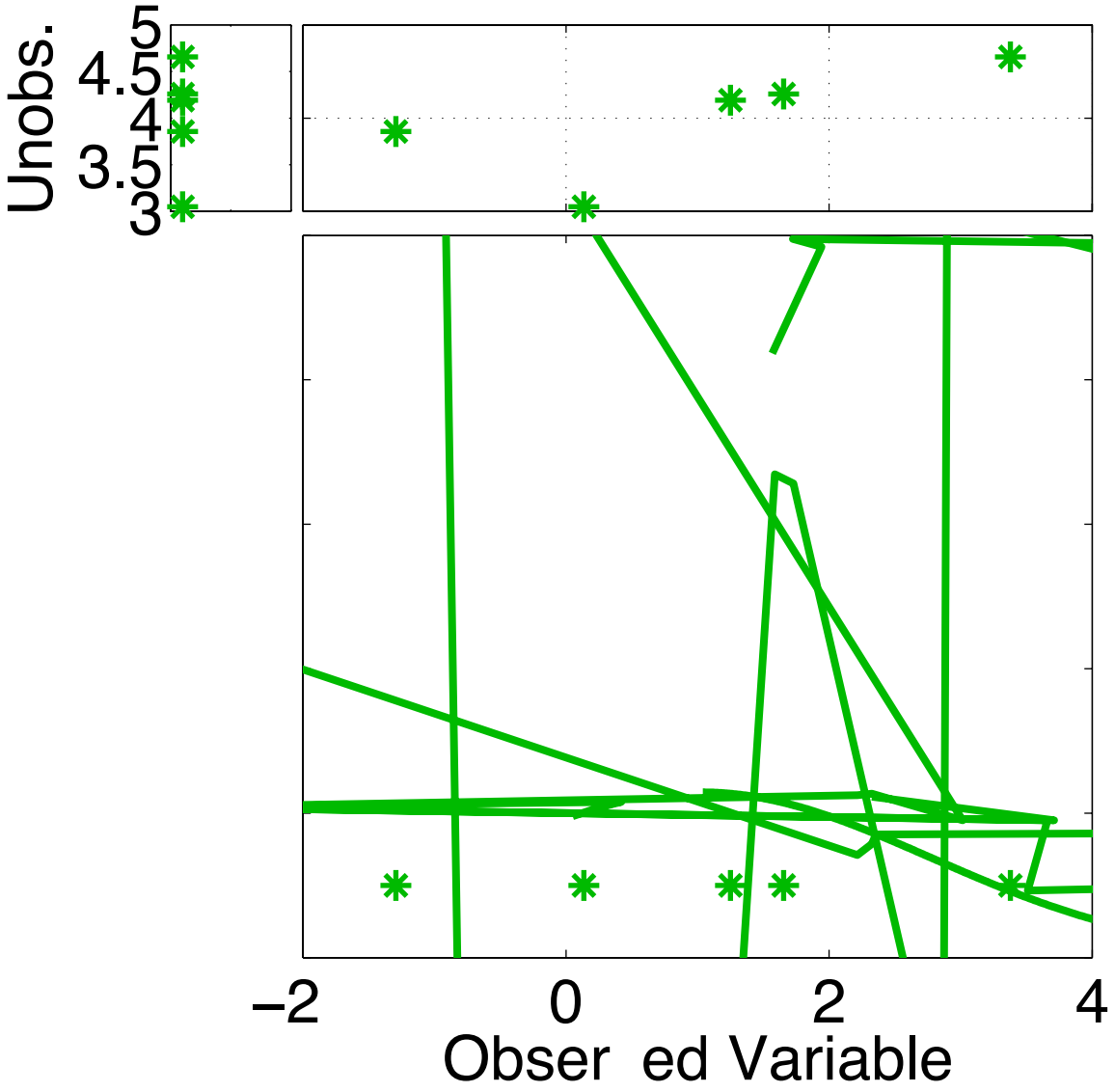


Assume that all we know is the prior joint distribution.

One variable is observed.

Compute increments for prior ensemble members of observed variable.

Ensemble filters: Updating additional prior state variables



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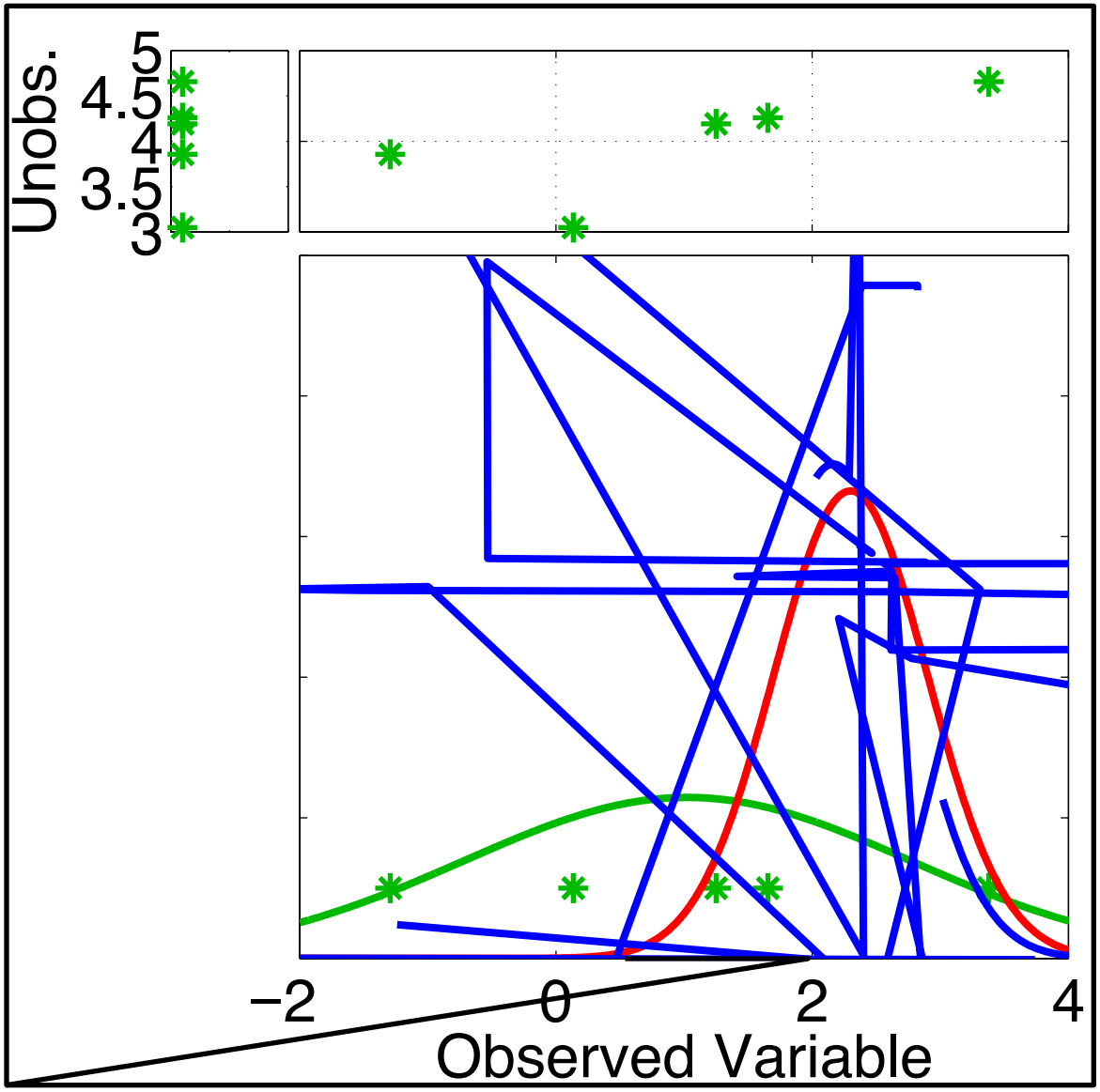

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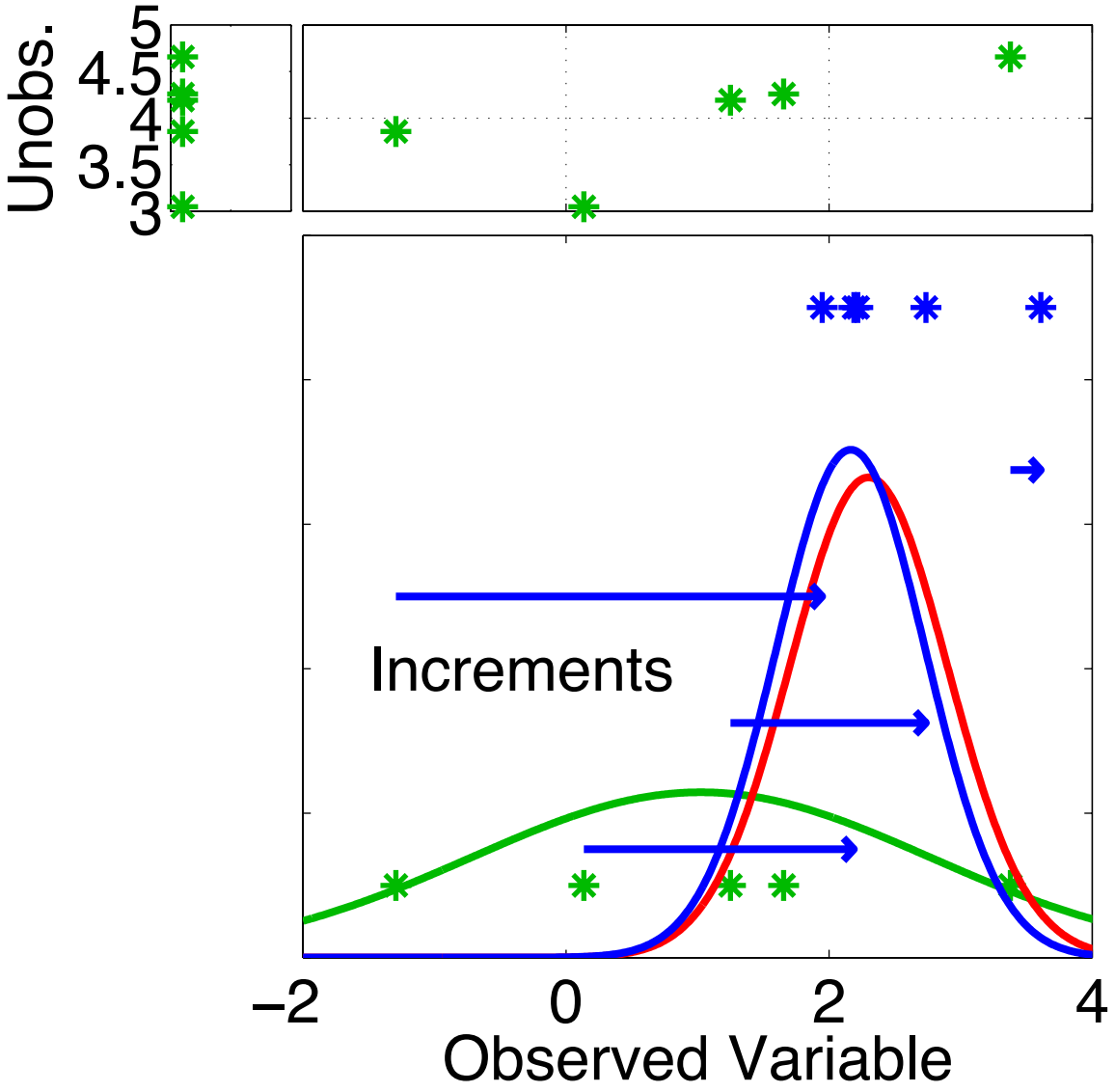

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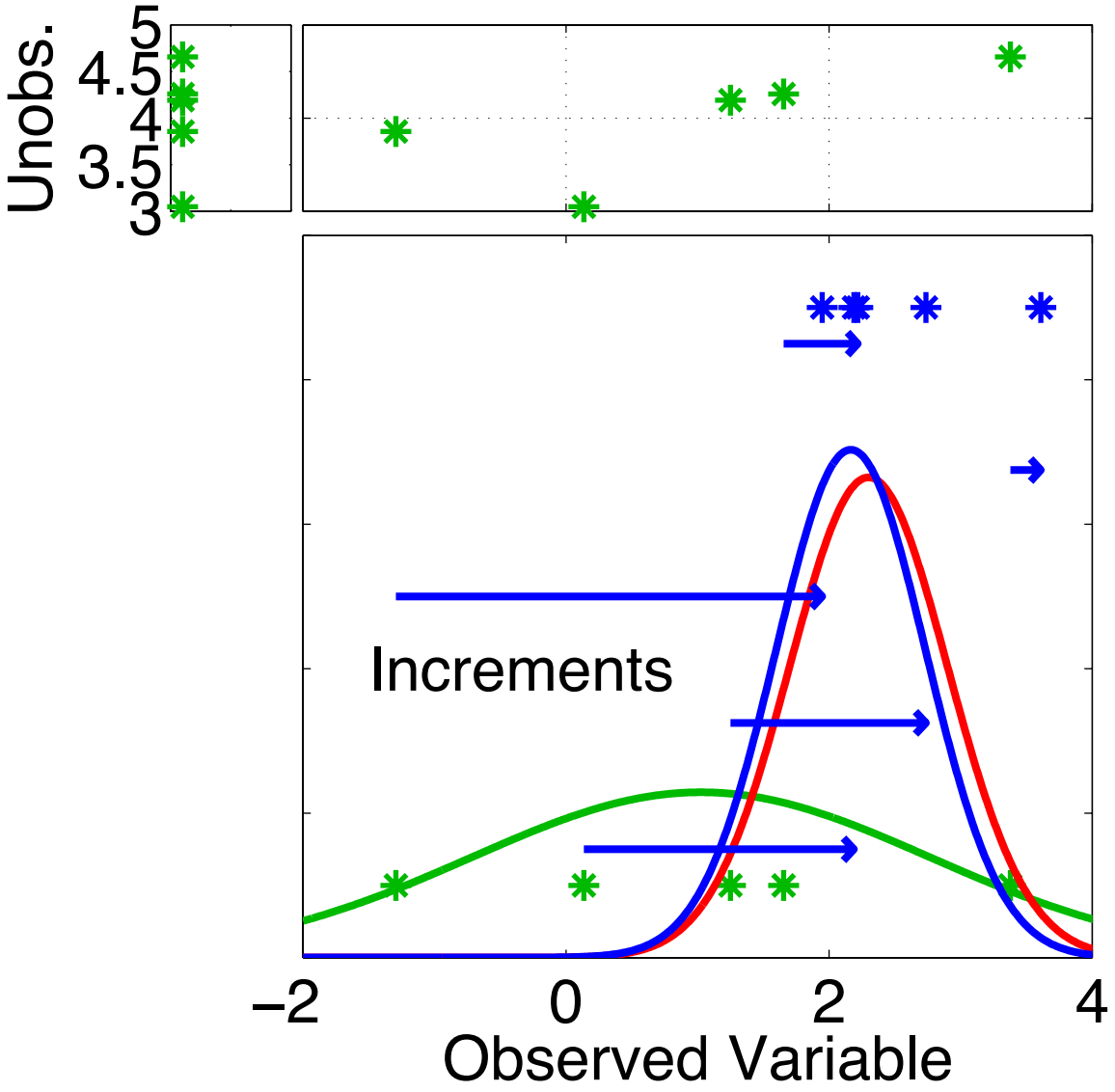

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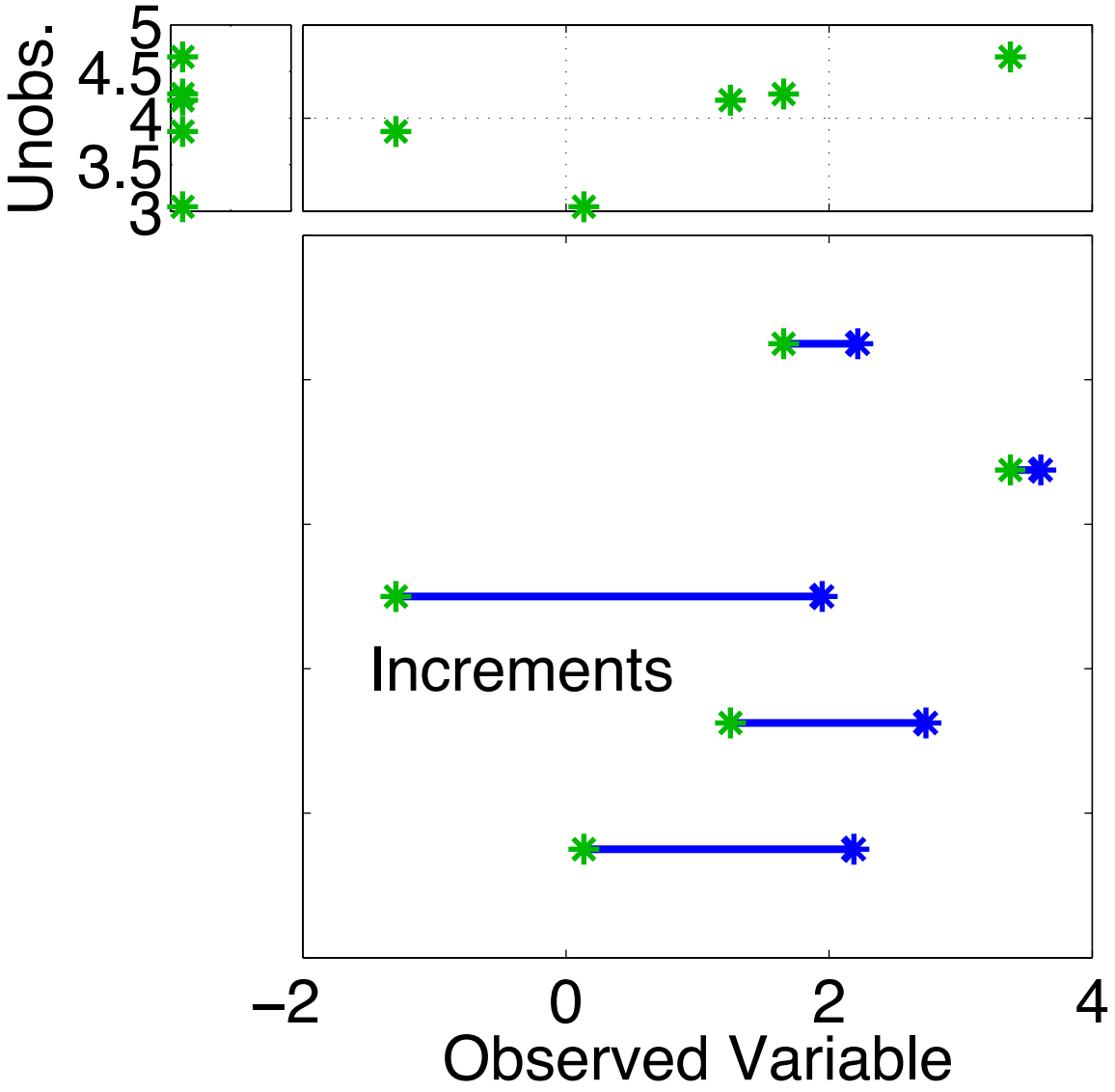
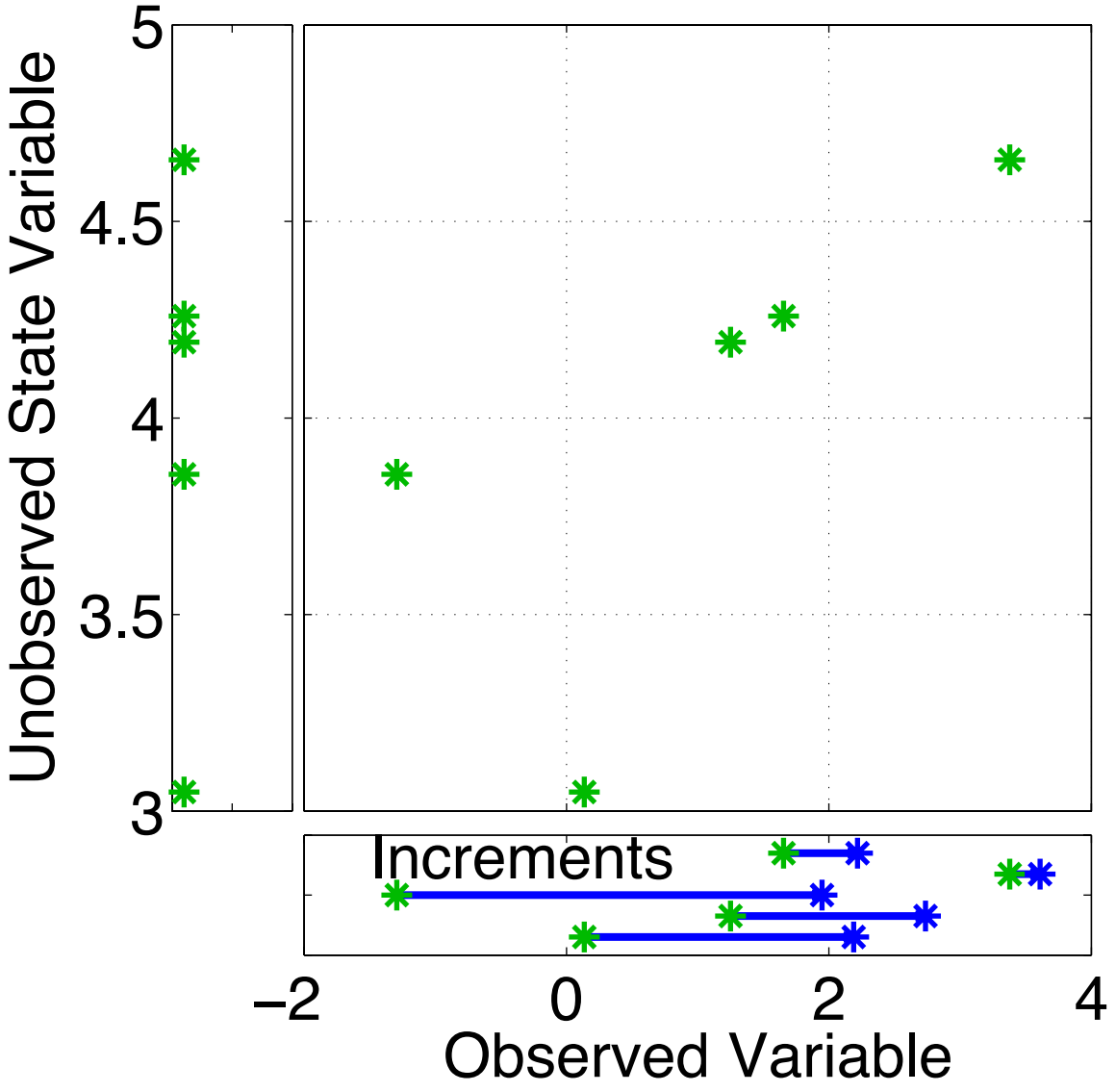
Ensemble filters: Updating additional prior state variables



Using only increments guarantees that if observation had no impact on observed variable, the unobserved variable is unchanged.

Highly desirable!

Ensemble filters: Updating additional prior state variables



Assume that all we know is the prior joint distribution.

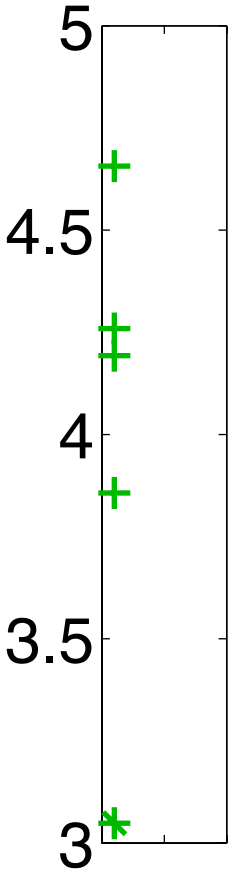
How should the unobserved variable be impacted?

1st choice: least squares

Equivalent to linear regression.

Same as assuming binormal prior.

Ensemble filters: Updating additional prior state variables



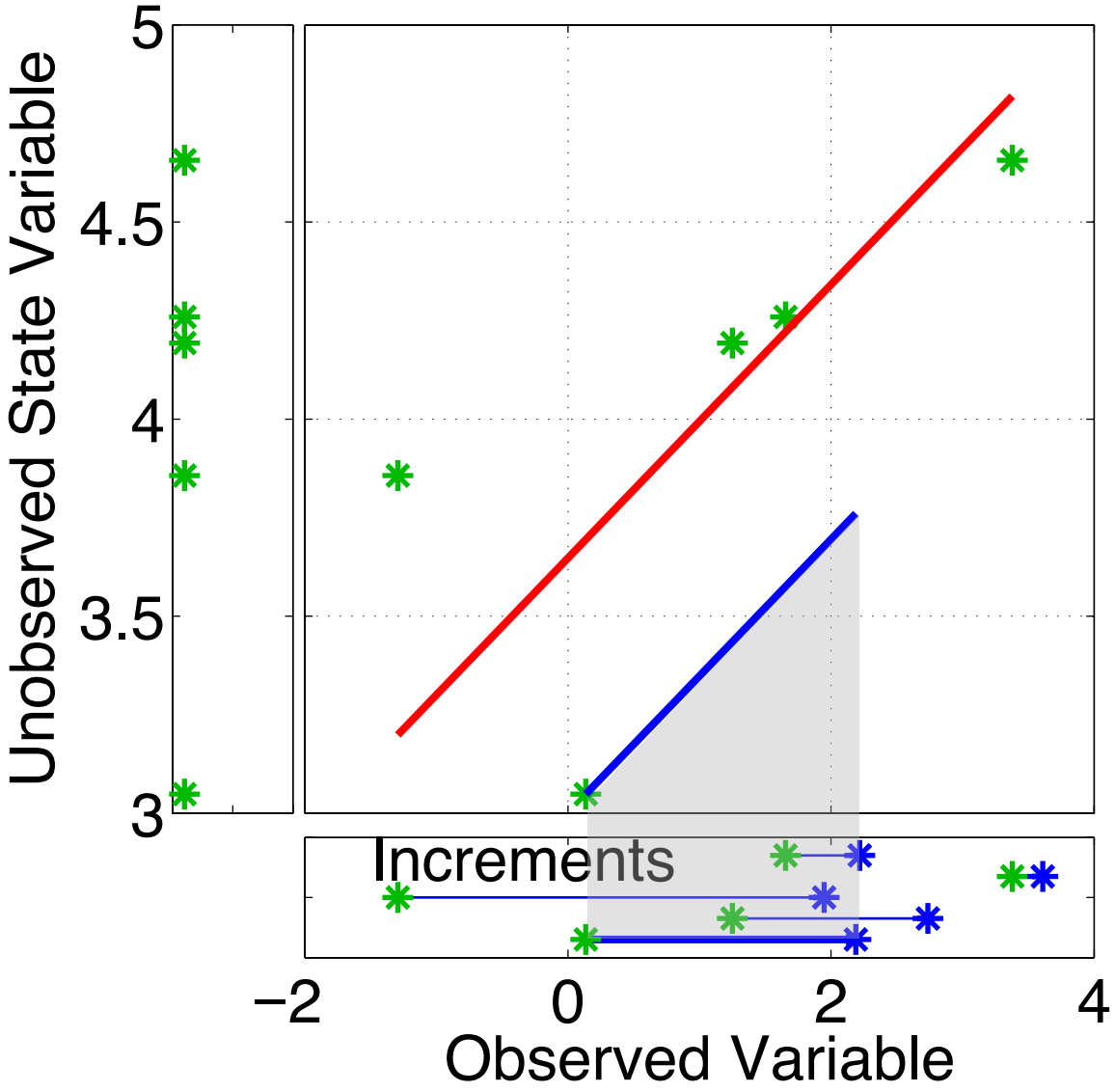
Have joint prior distribution of two variables.

How should the unobserved variable be impacted?

1st choice: least squares

Begin by finding least squares fit.

Ensemble filters: Updating additional prior state variables

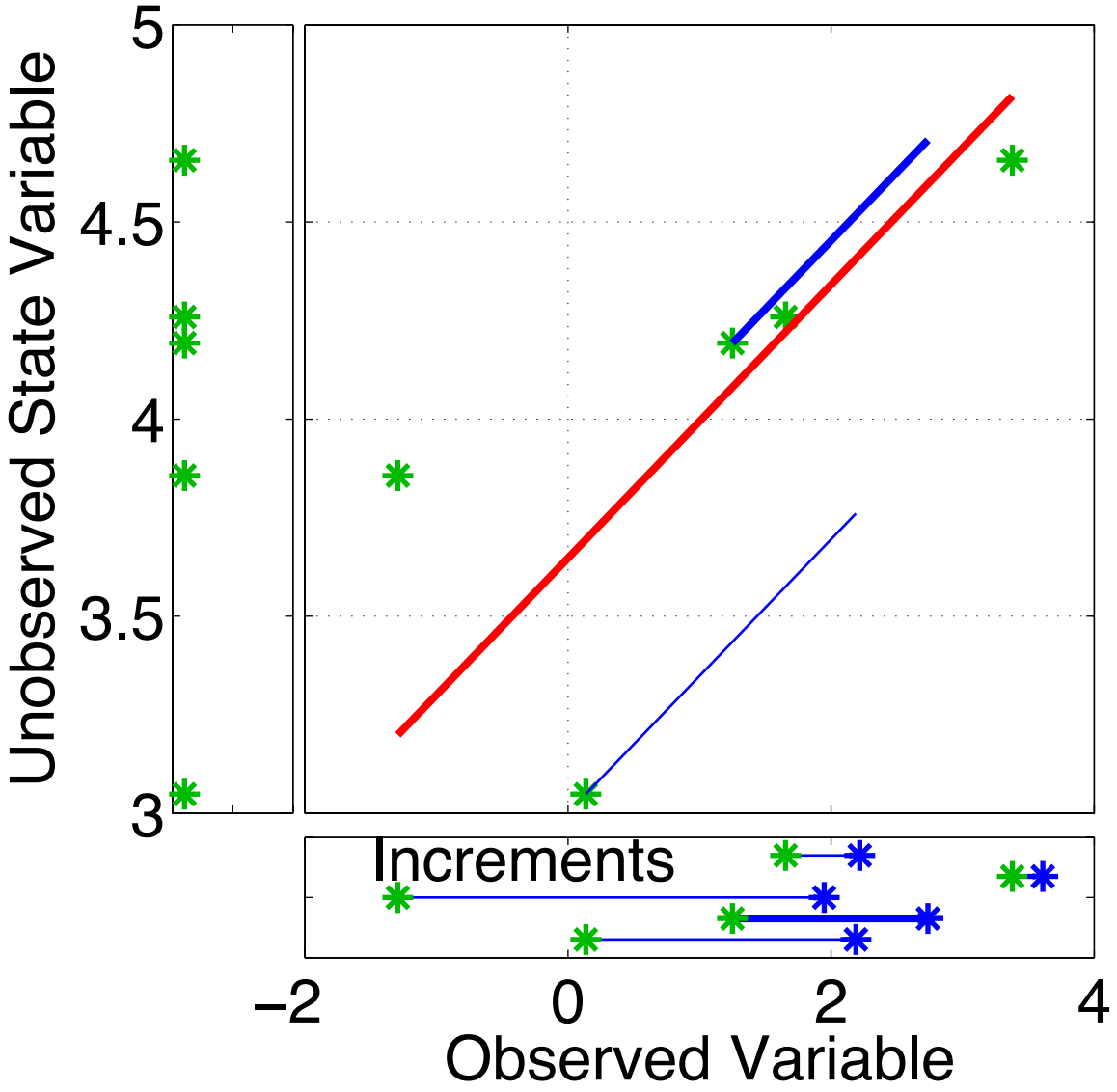


Have joint prior distribution of two variables.

Next, regress the observed variable increments onto increments for the unobserved variable.

Equivalent to first finding image of increment in joint space.

Ensemble filters: Updating additional prior state variables



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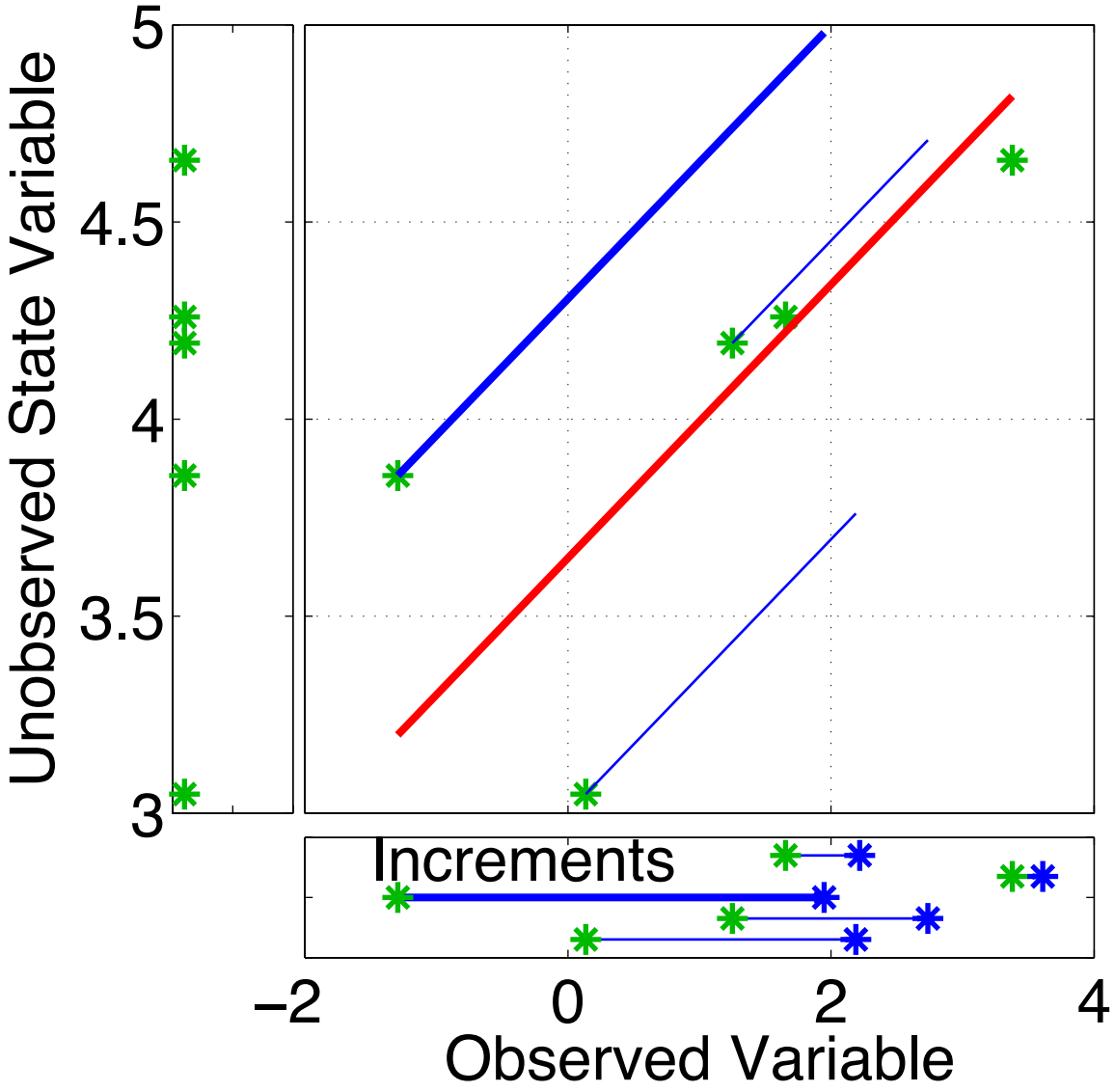

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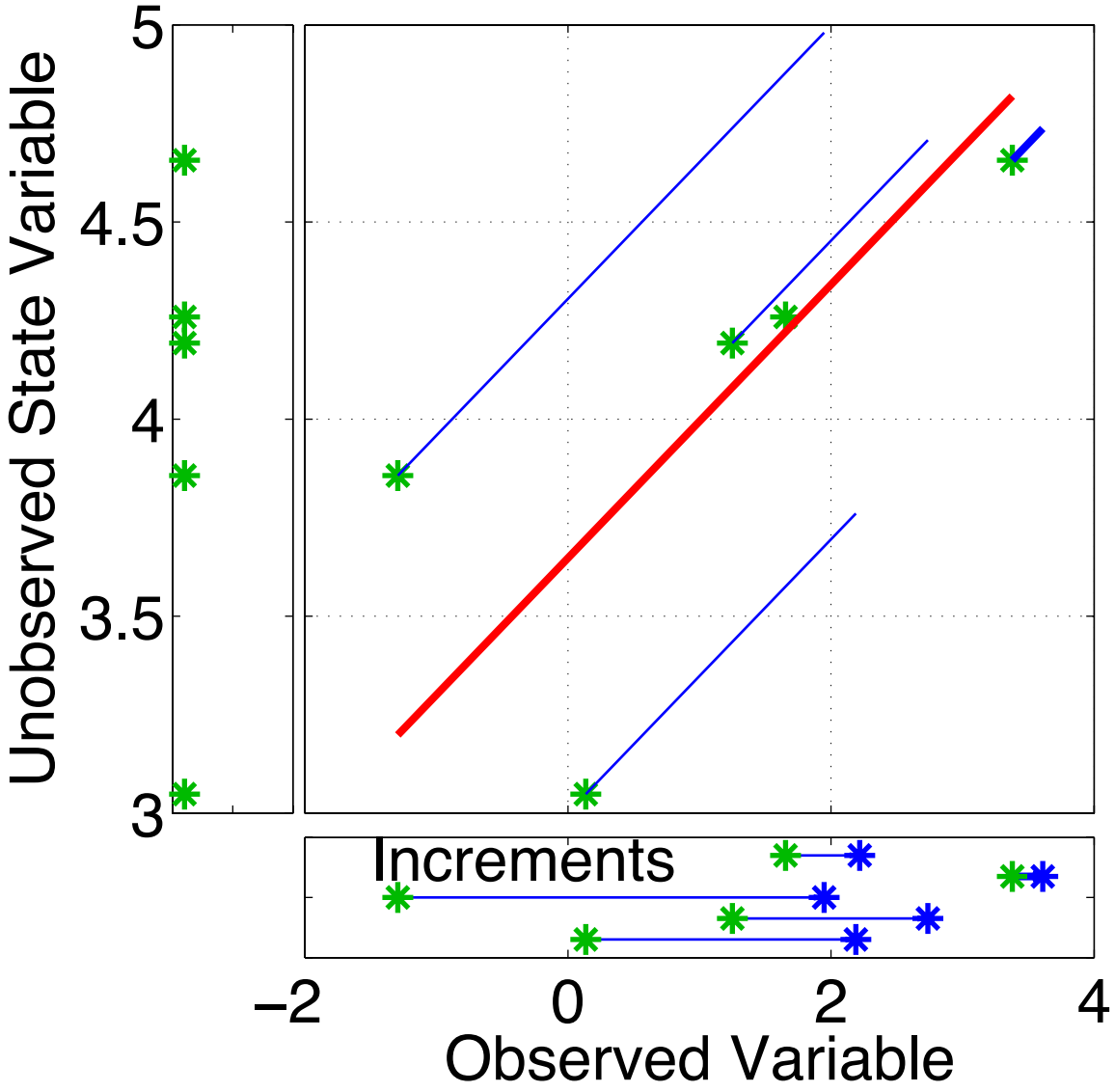

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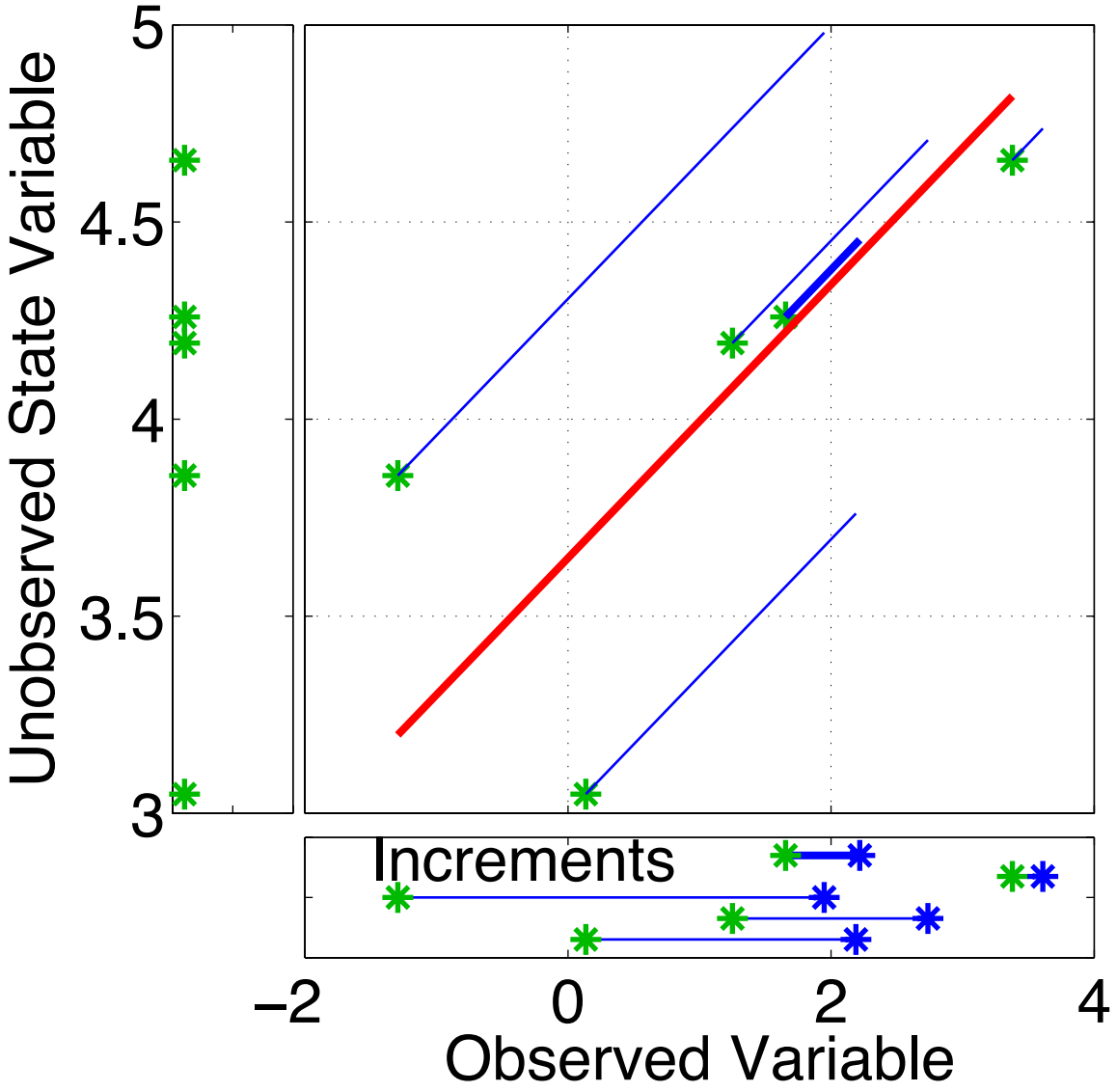

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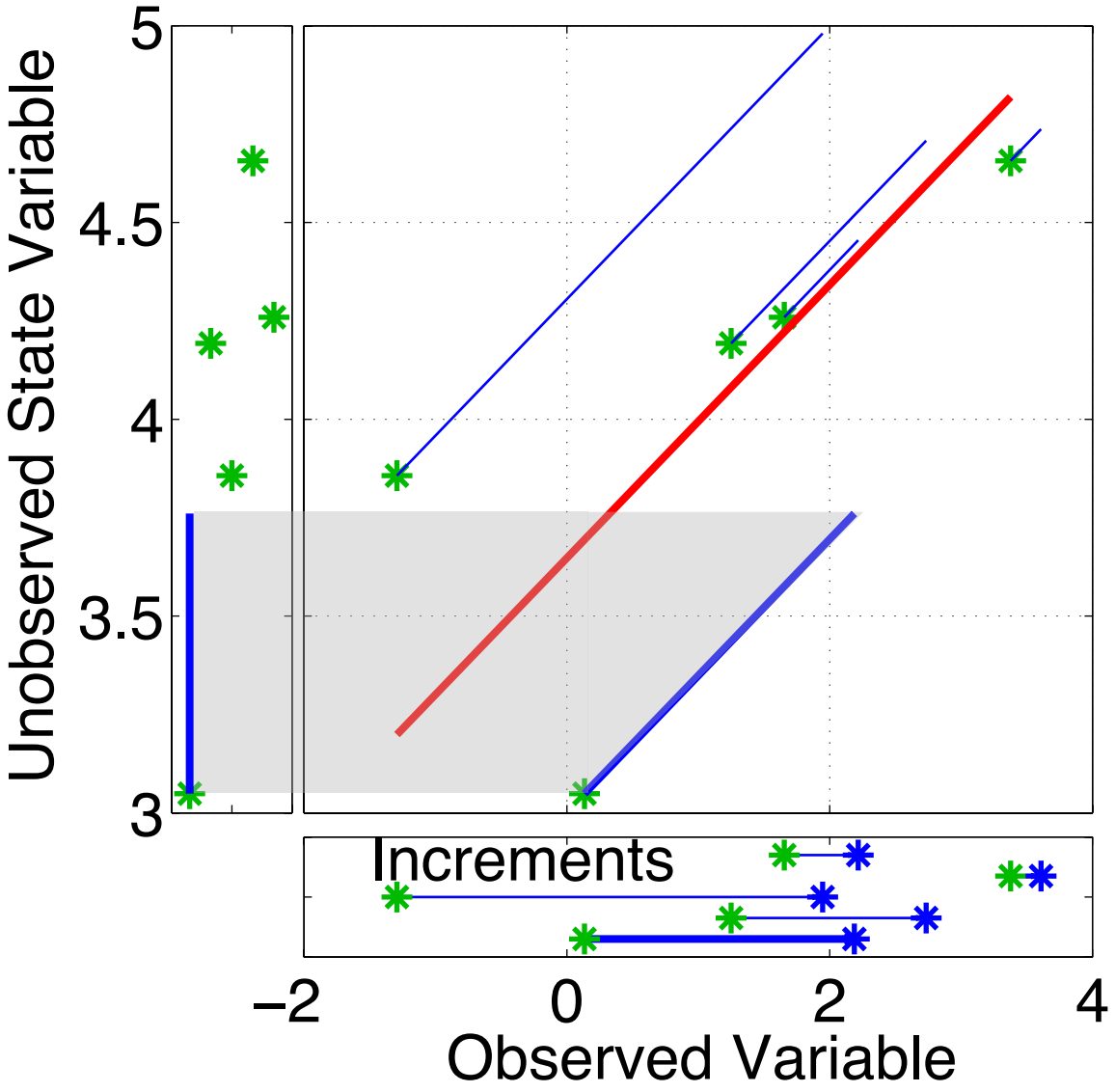
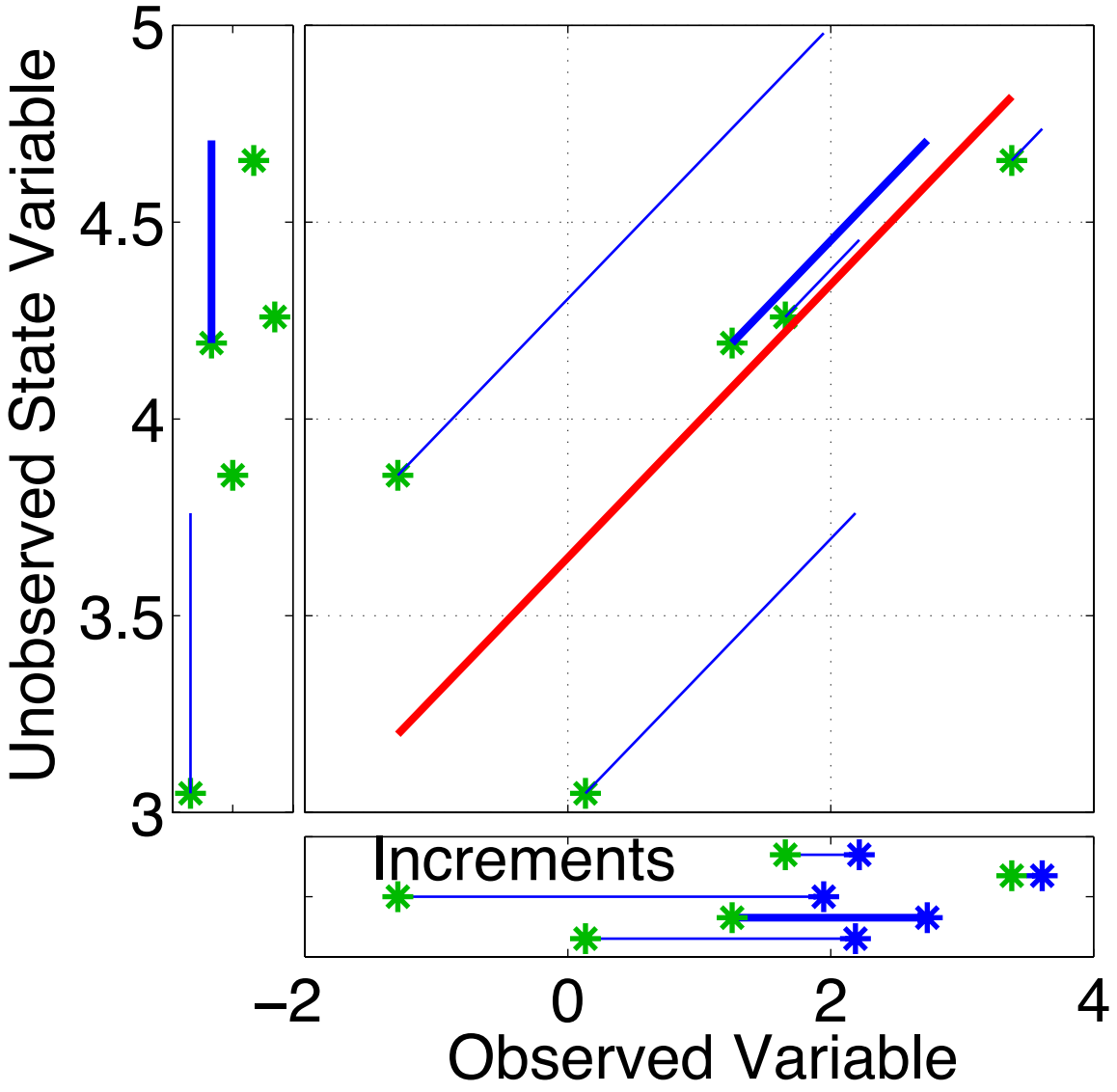


Have joint prior distribution of two variables.

Regression: Equivalent to first finding image of increment in joint space.

Then projecting from joint space onto unobserved priors.

Ensemble filters: Updating additional prior state variables



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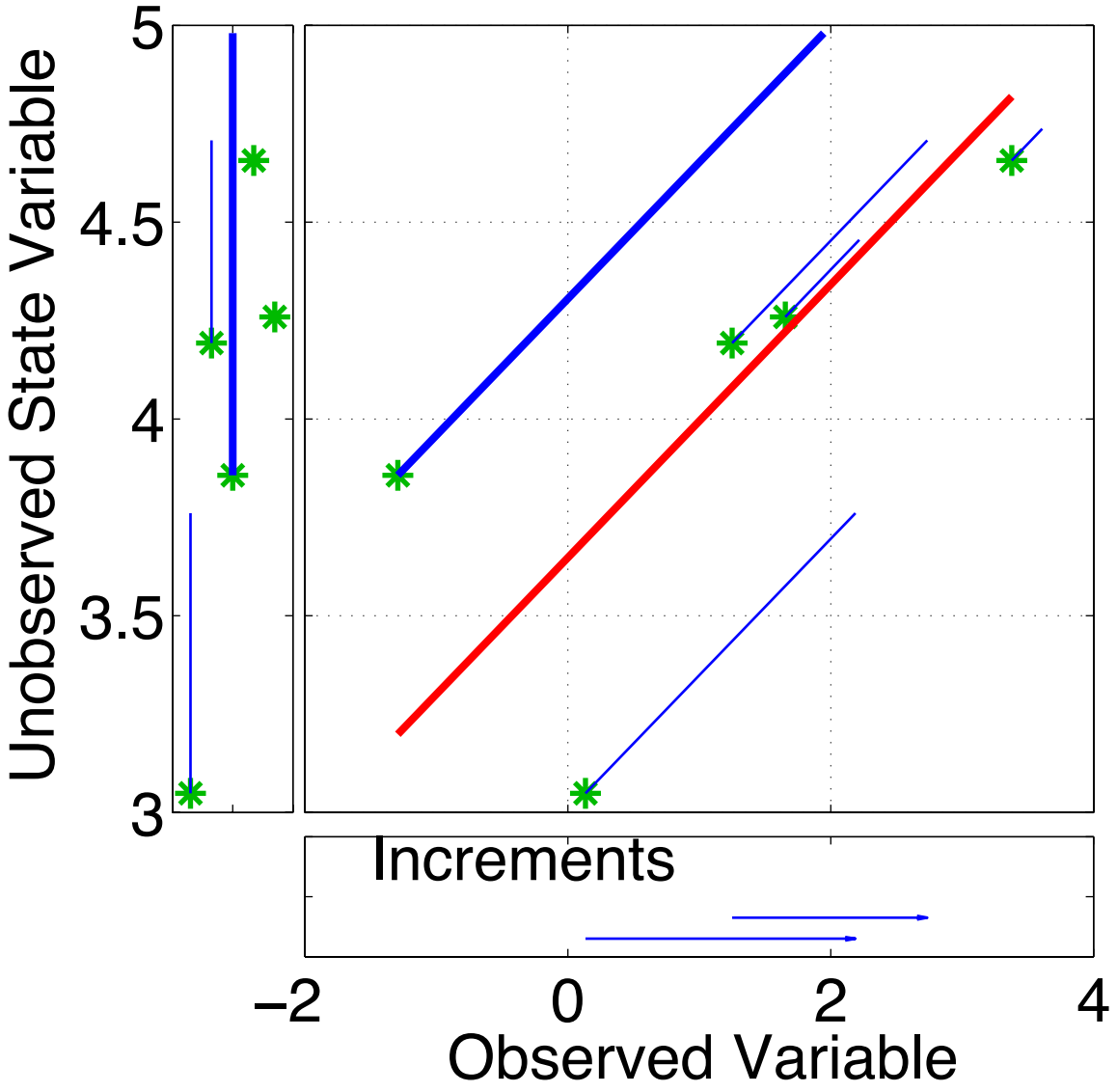

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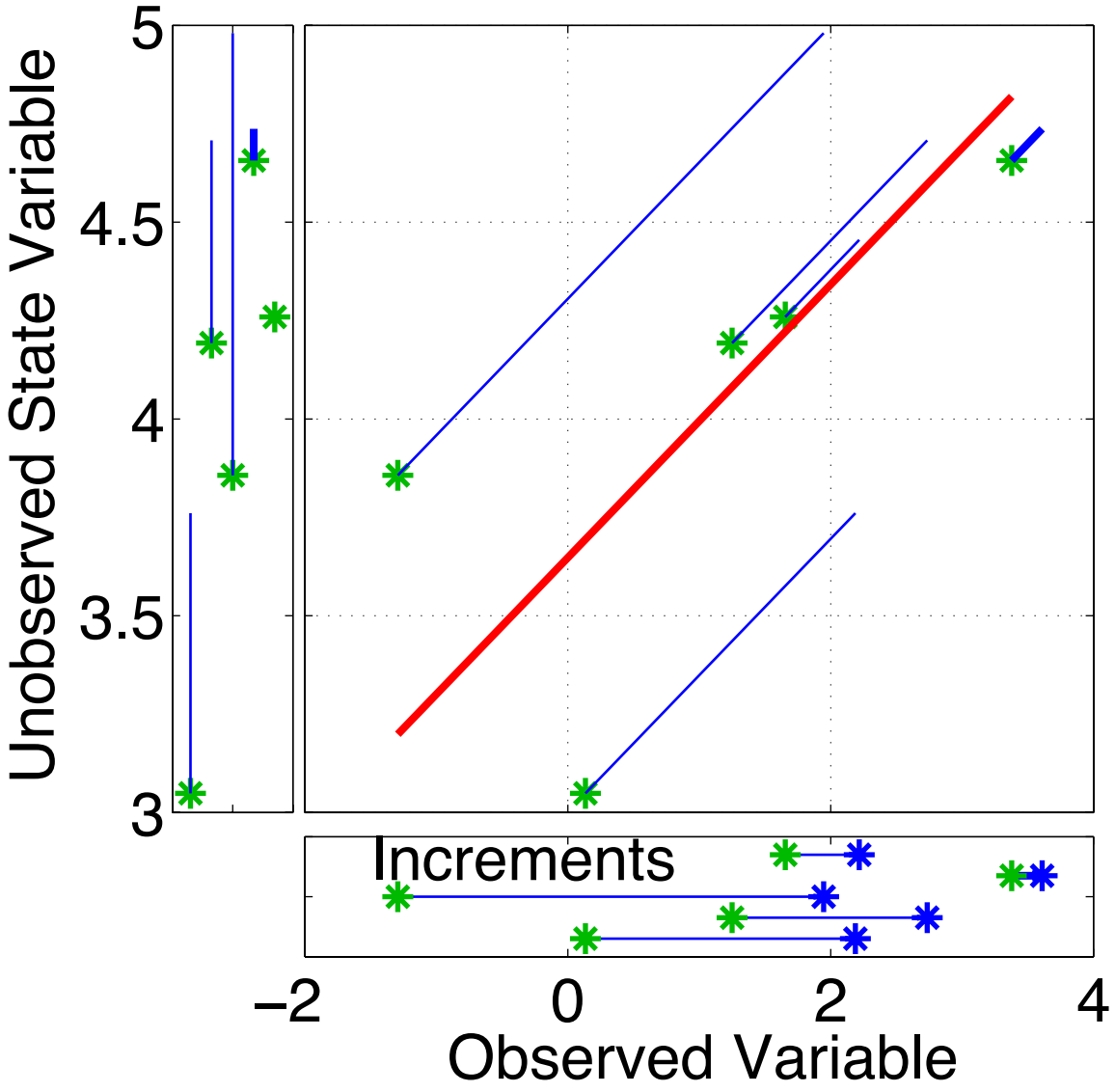

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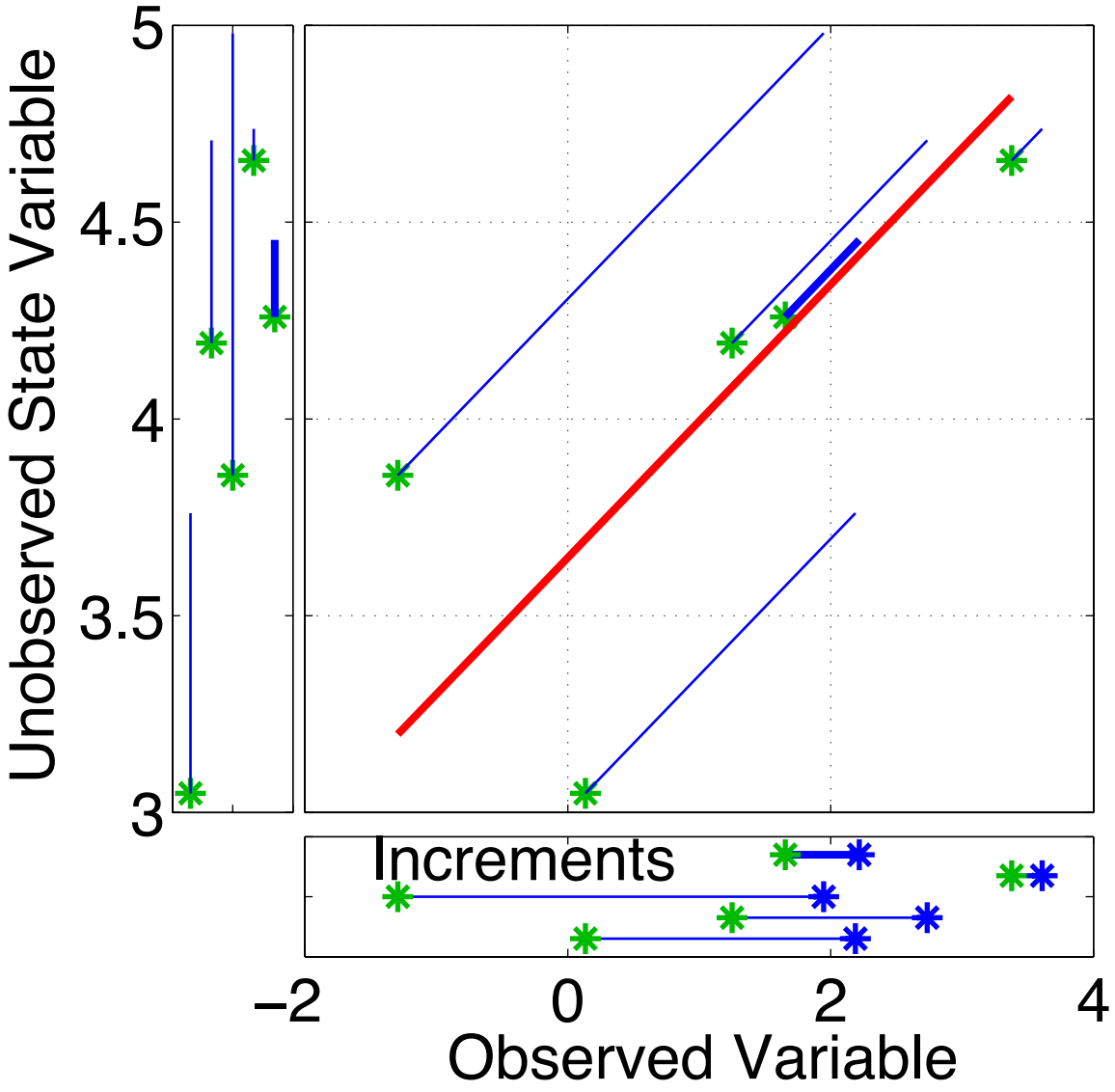

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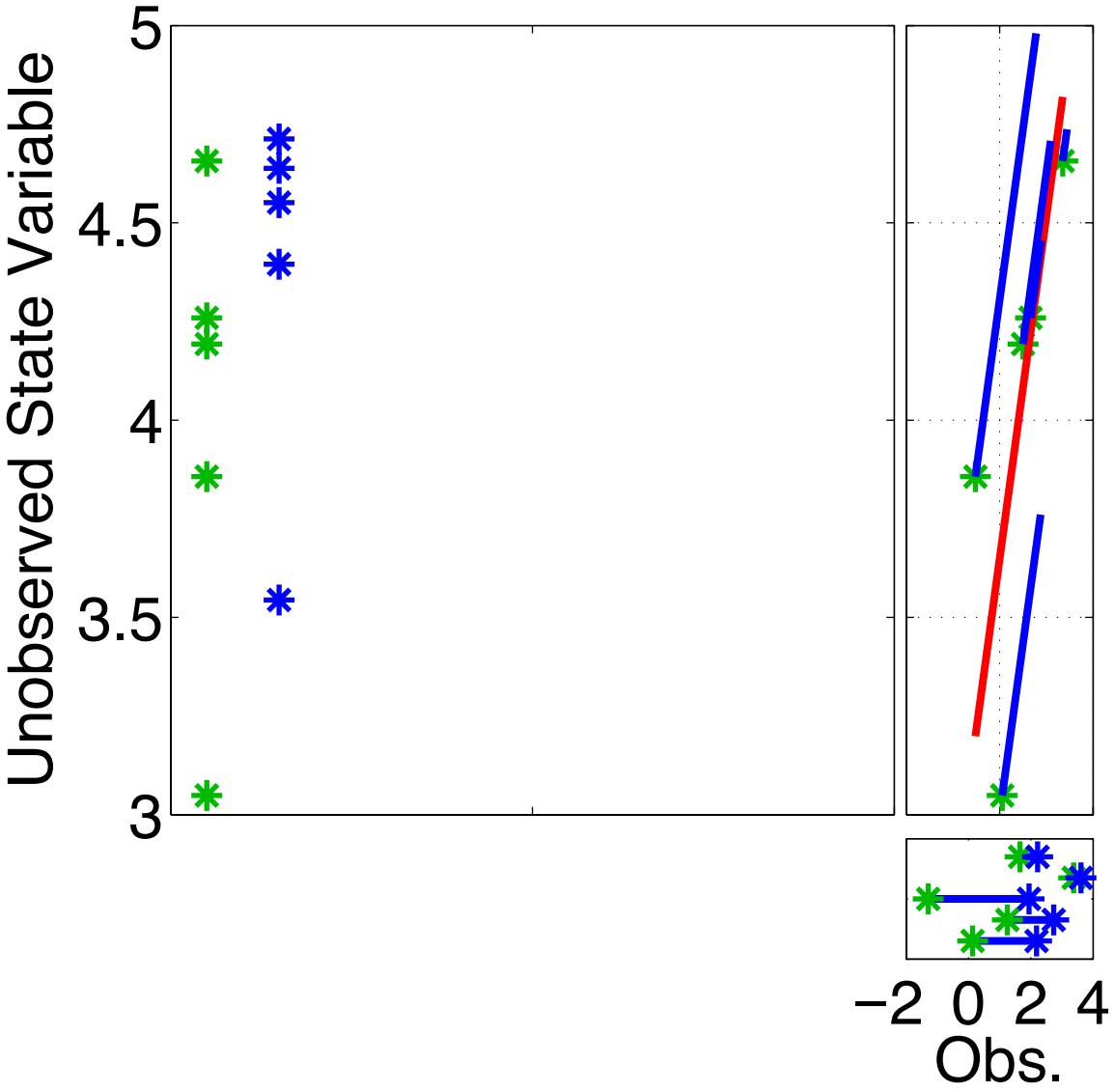
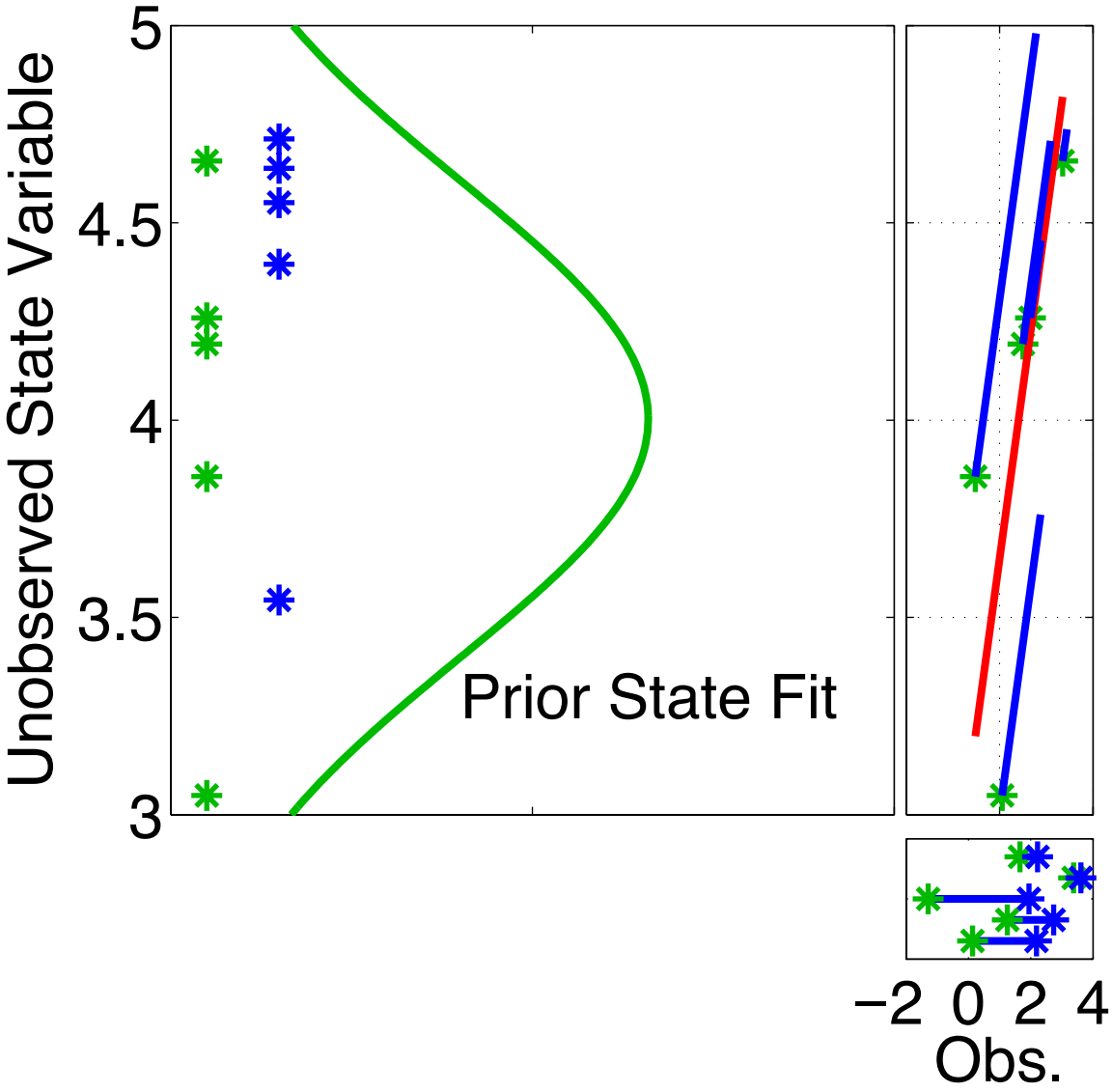


Now have an updated (posterior) ensemble for the unobserved variable.

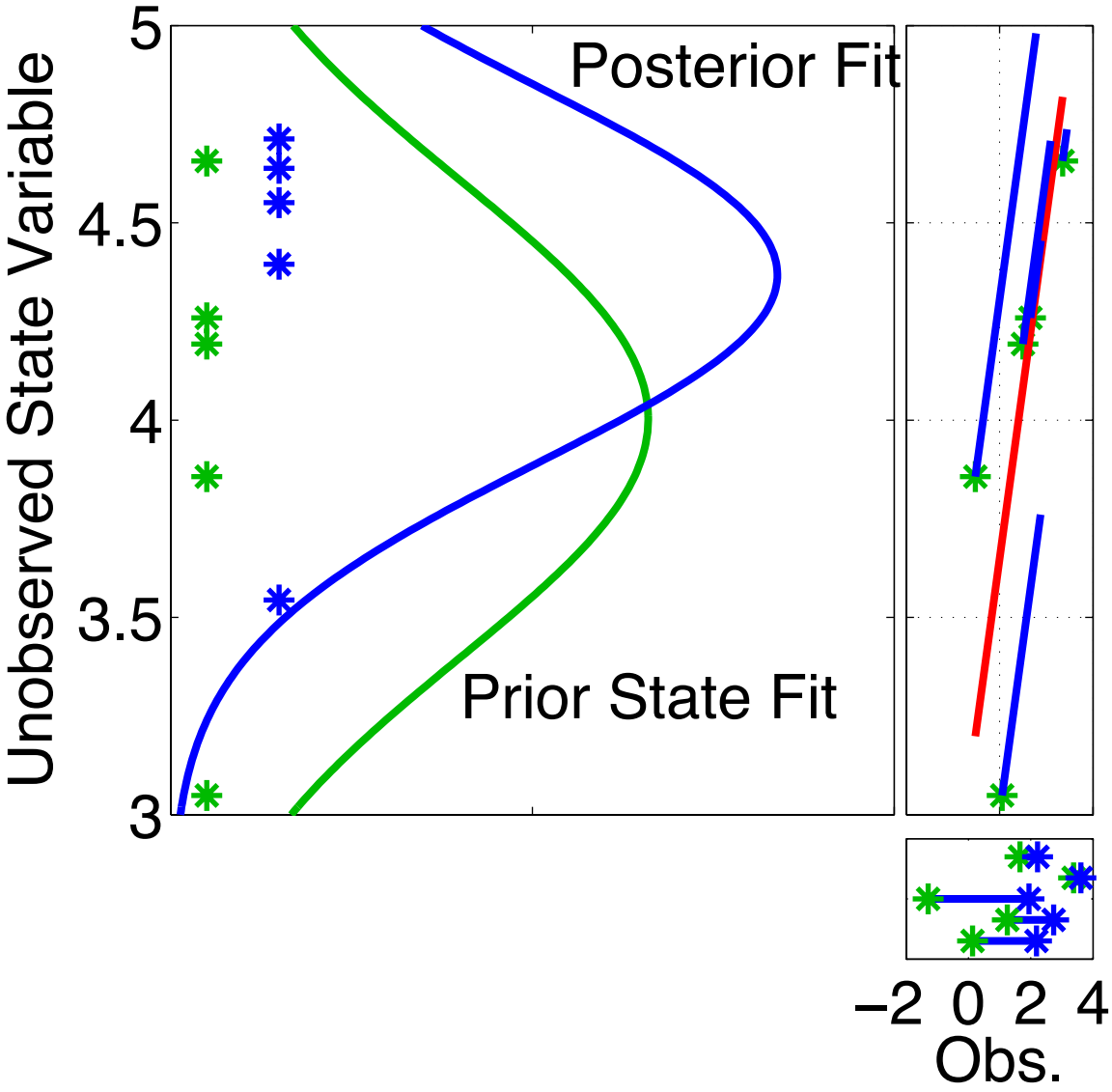
Ensemble filters: Updating additional prior state variables



Now have an updated (posterior) ensemble for the unobserved variable.

Fitting Gaussians shows that mean and variance have changed.

Ensemble filters: Updating additional prior state variables

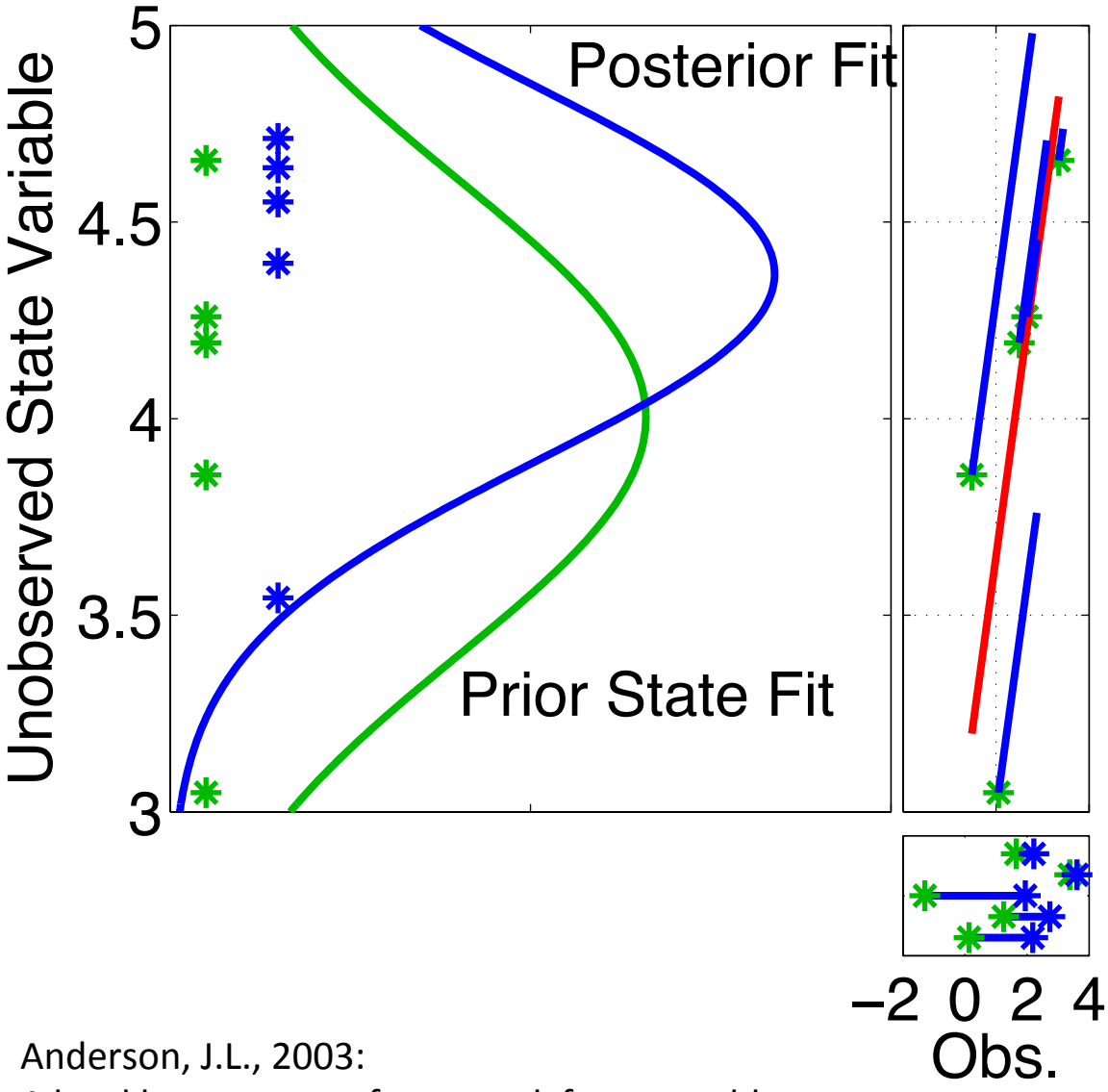


Now have an updated (posterior) ensemble for the unobserved variable.

Fitting Gaussians shows that mean and variance have changed.

Other features of the prior distribution may also have changed.

Ensemble filters: Updating additional prior state variables



CRITICAL POINT:

Since impact on unobserved variable is simply a linear regression, can do this INDEPENDENTLY for any number of unobserved variables!

Could also do many at once using matrix algebra as in traditional Kalman Filter.

Anderson, J.L., 2003:
A local least squares framework for ensemble filtering. *Mon. Wea. Rev.*, !"!, 634-642

Multivariate assimilation with DART:

The basic regression code is trivial:

However, DART advanced options can obscure the code.

See *assimilation_code/modules/assimilation/assim_tools_mod.f90*

```
subroutine update_from_obs_inc
```

To generate output from a multivariate Lorenz_63 experiment (the value of *cutoff* is presumed to be large – set in Section 3):

```
cd models/lorenz_63/work; ./filter
```

Now do Matlab diagnostics (see section 1).

- Does multivariate do better?
- Be sure to record the error values for comparison.
- Can you identify any obvious performance differences?

Multivariate assimilation in Lorenz 63:

What happens if not all state variables are observed?

1. Try observing only x and y (ignore z observations from above).
   In *models/lorenz_63/work* edit *input.nml*

```
&filter_nml
   …
   async                    = 0,
   adv_ens_command          = "./advance_model.csh",

   obs_sequence_in_name     = "obs_seq.out",
   obs_sequence_out_name    = "obs_seq.final",
   …
```

Change to obs_seq.out.xy

Execute ***./filter*** to produce new assimilation.

Look at the error statistics and time series with Matlab.

Record the error and spread values and compare to univariate case.

Multivariate assimilation in Lorenz 63:

What happens if not all state variables are observed?

3. Try observing only z (ignore x and y observations from above).
   In *models/lorenz_63/work* edit *input.nml*

```
&filter_nml
   …
   obs_sequence_in_name      = "obs_seq.out.x"
   …
&assim_tools_nml
   …
   cutoff                    = 0.00001
```

Change to obs_seq.out.z

Change to 1000000.0

Execute ***./filter*** to produce new assimilation;
look at the error statistics and time series with Matlab.

Record the error and spread values and compare to univariate case.
Dynamics for x and y are symmetric; z can NOT distinguish them.
How do we want filter to handle this?
Does it do what we want in this case?

DART Tutorial Index to Sections