

The aim of this page is being a **summary**.

See the attached part of the memory for more detail.

Project context

Explained in the first chapter of the document.

Planning

The original planning was:

- GEP
- Requirement analysis, architecture and debugging
- Iteration 1: Pseudo-boolean minimization
- Iteration 2: Timeout
- **(Optional) Iteration 3: Multi-threading**
- **Finalization stage**

The current planning is:

- GEP
- Requirement analysis, architecture and debugging
- Iteration 1: Pseudo-boolean minimization
- Iteration 2: Timeout
- **Finalization stage**
- **(Optional) Iteration 3: Multi-threading**

Once the second iteration was finished, instead of starting the third one, the finalization stage was started. The decision was made in order to guarantee that the required stages were finished.

Because the third iteration is optional, it has been delayed until the documentation is finished and will be done if there is enough time.

The project is expected to be finished without delays according to the planning.

Methodology and rigour

The methodology followed during the development has been Agile with TDD (Test Driven Development).

TDD implied that before writing code all the requirements had been defined i.e the behaviour of that component is fully defined (but not closed to extension). Then, a set of tests are written for each requirement/method and then the

For each requirement/method, a set of tests were written and after that, the implementation starts. The only goal of the implementation is pass tests with the minimum functional code. When the tests pass, a refactor step is done in order to optimize the code.

With TDD, the written code is the only one necessary which helps to simplify its logic. Also, Category-Partition testing has been used, especially in the search strategy implementation, to identify relevant values for the implementation and tests special cases.

Altogether, in particular the test suite, guarantees that the software has been developed with quality, rigour and that works.

It is important to remark that there is no perfect test suite because not all possible combinations of input values can be tested.

Alternatives analysis

This section is explained in more detail in the Development section of the memory.

In a nutshell, for the first iteration there were two alternatives: use PBLib or implement all the functionalities from scratch.

Use PBLib was the selected alternative because it would have taken too much time to implement all the functionalities and the quality would be lowered as PBLib has been developed by experts.

For the second iteration, there were also two alternatives about how to approach the timeout: using processes or threads.

The behaviour wanted was that one part of the program counts for the timeout while the other is executing the solver.

Finally, thread was the selected alternative because creating a thread is cheaper than creating a process.

Knowledge integration

Until now, the following knowledge has been integrated:

- Computer science due to the project's topic and context, search algorithms and methods time complexity.
- Software engineering because TDD has been followed for the implementation and there has been a special emphasis in architecture design to make code reusable and easy to add extensions.
- Operative systems and parallelism have been applied for the second iteration to implement the timeout.

Laws and regulations

For this project, no laws or regulations are applied.

UNIVERSITAT POLITÈCNICA DE CATALUNYA

DESIGN OF AN ENVIRONMENT FOR SOLVING
PSEUDO-BOOLEAN OPTIMIZATION PROBLEMS

Design of an environment for solving pseudo-boolean optimization problems

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UNIVERSITAT POLITÈCNICA DE CATALUNYA

Abstract

Facultat Informàtica de Barcelona
Department of Computer Science

Computer Science Degree

Design of an environment for solving pseudo-boolean optimization problems

by Marc BENEDÍ

TEXT DEL ABSTRACTE explicar amb molt poques paraules el que es veu a cada capítol

Glossary

Abbreviation	Description of the abbreviation
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CNF	
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DNF	
-----	--

PB	
----	--

PBF	
-----	--

SAT	
-----	--

PB-Min	
--------	--

BF	Boolean Formula
----	-----------------

NP	
----	--

BDD	
-----	--

AI	
----	--

TDD	
-----	--

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Chapter 1

Introduction and Context

1.1 Introduction

Technology's world is evolving very fast. Every year new tools, frameworks¹ programming languages, etc. are released. Some of them are living they gold's era, such as blockchain and machine learning, while others are forgotten.

This makes hard for universities decide what to teach: the tools used by companies or the fundamentals of informatics.

This project works with the fundamentals of informatics and logic which won't change either be forgotten.

In this project, we will work with Pseudo-Boolean Minimization widely used by a lot of technologies such as Artificial Intelligence, Planners, Computer Vision, Circuit design, ...

1.2 Context

But before being able to explain the main problem which this project is about, Pseudo-Boolean Minimization, it necessary to do a quick introduction to a much wider topic.

Boolean satisfiability problems (SAT from now on) is the problem of finding a model for a Boolean Formula (BF from now on). In other words, it is the result of evaluating the BF after replacing its variables for true or false.

SAT is widely used in Computer Science because it was the first problem proved to be NP-Complete which allowed a lot of NP problems be reduced to it[1]

1.2.1 What is a Pseudo-Boolean Formula?

In propositional logic, a *BF* is defined as following[2]:

Let P be a set of predicate symbols like p, q, r, \dots

- All predicate symbol of P is a formula.
- If F and G are formulae, then $(F \wedge G)$ and $(F \vee G)$ are formulae too.
- If F is a formula, then $(\neg F)$ is a formula.
- Nothing else is a formula.

This representation has some limitations because it can only express properties which are *true* or *false*.

¹A software framework is an abstraction in which software providing generic functionality can be selectively changed by additional user-written code, thus providing application-specific software. [Wikipedia](#)

1.2.2 What are pseudo-boolean formulae?

Pseudo-Boolean Formulas are functions of the form $f : B^n \rightarrow \mathbb{R}$. For example, the following formula is a *Pseudo-Boolean Formula* (PBF from now on): $3x + 5y$. Therefore, *BF* are a special case of *PBF* where the domain is $d = \{0, 1\}$.

1.2.3 Pseudo-Boolean minimization

Pseudo-boolean optimizations is a linear programming problem:

Linear programming (LP, also called linear optimization) is a method to achieve the best outcome (such as maximum profit or lowest cost) in a mathematical model whose requirements are represented by linear relationships.

Linear programs are problems that can be expressed in canonical formas

$$\begin{array}{ll} \text{maximize} & \mathbf{c}^T \mathbf{x} \\ \text{subject to} & \mathbf{A}\mathbf{x} \leq \mathbf{b} \\ \text{and} & \mathbf{x} \geq \mathbf{0} \end{array}$$

FIGURE 1.1: Linear programming canonical form representation

where \mathbf{x} represents the vector of variables (to be determined), \mathbf{c} and \mathbf{b} are vectors of (known) coefficients, \mathbf{A} is a (known) matrix of coefficients, and is the matrix transpose. The expression to be maximized or minimized is called the objective function ($\mathbf{c}^T \mathbf{x}$ in this case). The inequalities $\mathbf{A}\mathbf{x} \leq \mathbf{b}$ and $\mathbf{x} \geq \mathbf{0}$ are the constraints which specify a convex polytope over which the objective function is to be optimized.

https://en.wikipedia.org/wiki/Linear_programming

Pseudo-boolean minimization is a particular case where the objective function (also called) cost function is minimized, the variables are boolean 0,1 and the variable's coefficients are integers.

In other words, a pseudo-boolean minimization problem has two components:

- A set of pseudo-boolean constraints
of the form $\sum_{i=1}^n x_i w_i \leq k$, where $w_i, k \in \mathbb{I}$ and $x_i \in \{0, 1\}$
- A cost function

The goal is to minimize the cost function $\min(a_1 x_1 + \dots + a_n x_n)$. Find an assignment for the problem's variables in a way that all the constraints are satisfied and the evaluation of the cost function is minimum.

The value m is minimum, if $m-1$ is unsatisfiable.

There is a big research in this field, more specifically in encoding PBF into CNF. In this paper, Hölldobler, Manthey, Steinke[4], some relevant PBF into SAT encodings are explained and a new one is proposed. One of the authors of this paper, Steinke, is also the author of PBLib.

1.3 Background

During the past semester (Q1 2017/2018), under the supervision of [Dr. Jordi Cortadella](#), I had been developing a C++ library.

This tool allows the users to represent *BF* in a C++ program in an intuitive way, do operations between them and convert them into *Binary Decision Diagrams* (BDD from now on). However, the main functionality of this library is the conversion from a *BF* to *CNF*.

As previously explained, *CNF* is a particular type of a *BF*, a conjunction of disjunctions. *CNF* is an important format because it is the standard input for *SAT Solvers*[A.1](#). As shown in this paper, *Mitchell, Selman, and Levesque*[\[6\]](#), there is a correlation between the number of variables, the number of clauses and the hardness of solving the *CNF*.

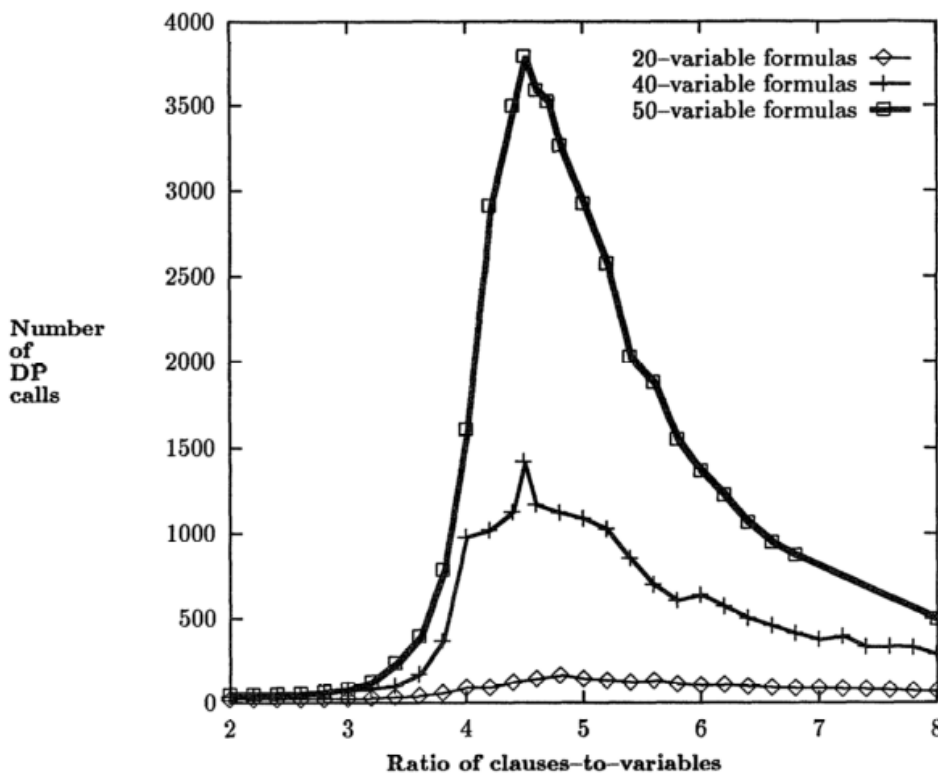


FIGURE 1.2: Median number of recursive DP calls for Random 3-SAT formulas, as a function of the ratio of clauses-to-variables.
Extracted from *Mitchell, Selman, and Levesque*[\[6\]](#)

Therefore, an improvement of the input *CNF* of the *SAT Solver* can reduce a lot the hardness of the problem.

This is the main goal of the library, try to reduce the size of the final *CNF* resulting from applying different converting methods on the original *BF*.

1.4 State-of-the-art

Nowadays there is a well known C++ library called [PBLib](#) developed by Peter Steinke. PBLib allows its users to represent pseudo-boolean constraints and encode them into a *CNF*. It possesses a big repertory of encodings which have been proposed in the past in different papers[\[8\]](#).

At most one	At most K	PB
sequential[11]*	BDD[7, 4]**	BDD
bimander[6]	cardinality networks[1]	adder networks
commander[8]	adder networks[4]	watchdog[10]
k-product[3]	<i>todo: perfect hashing</i> [12]	sorting networks[4]
binary[2]		binary merge[9]
pairwise		sequential weight counter[5]
nested		

* equivalent to BDD, latter and regular encoding
 ** equivalent to sequential counter

FIGURE 1.3: PBLib implemented encodings
 Extracted from Steinke[8]

Apart from having these encodings, PBLib applies the best one for the given pseudo-boolean constraint in a way that provides the most effective translation.

In Chapter 3 - Development 3 PBLib is discussed as a tool for this project. In a nutshell, PBLib is a very good tool developed by professionals and it will be hard to try to do the same with the same quality. For these reasons, and some others explained in more detail in Chapter 3, PBLib has been incorporated in this project as a translator of pseudo-boolean constraints to CNF.

One of the downsides of PBLib is the interface which is not very user-friendly. As can be seen in Chapter 2 Objectives 2, one of the objectives of this project is offering a good interface which means that a layer between the user and PBLib will be added to simplify how the users declare pseudo-boolean constraints.

The second project we will talk about is the explained in the *Background section*. This project adds a new encoding for *BF* which can be extended to *PB Constraints*. This encoding will be studied and if it achieves good metrics it will be implemented to *PB Constraints*.

1.5 Motivations

Informatics Logic is taught in this² faculty. In that course, I realized how important is *logic* through its lecturer, [Dr. Robert Nieuwenhuis](#), and its activities.

In the first coursework, we had to code a *SAT Solver* which used *Unit Propagation*. With this activity, I comprehended how hard and substantial is the study of *logic* and all its context. For example, how *logic* is used in Artificial Intelligence and Planners.

When the time of deciding the *TFG* arrived, I contacted my actual supervisor, [Dr. Jordi Cortadella](#), and he proposed me some topics and ideas. Finally, we agreed on doing this project.

The motivation for this project is trying to deepen into the topic and contribute on it.

Also during the studies, with the transversal competencies, there has been an intention to teach students about sustainability and its importance.

²Facultat Informàtica de Barcelona

As previously told, the subject of this project is widely used in many other areas which have a big footprint because of electricity consumption. This is also a motivation for this project because reducing the execution time will become in a decrease of electricity spent and that will be beneficial for the climate.

1.6 Stakeholders

In this section, the Stakeholders of the project are defined. Stakeholders are entities which are affected, directly or indirectly, by the solution developed in this project.

1.6.1 Target audience

This tool targets all the entities (researchers, companies, ...) which work with *PB minimization* and use *SAT Solvers*.

1.6.2 Users

The users will be C++ programmers due this tool is developed in this language.

1.6.3 Beneficiaries

All those entities which work with *PB minimization*. For example AI, SAT Solvers, Planners, ...

Chapter 2

Project Scope

2.1 Project Formulation

As mentioned before¹, this project is an extension of a previous C++ library. The main goal of this project is to improve the time required to solve *minimization* problems. To achieve this goal, the following objectives have been established.

2.1.1 General objectives

Pseudo-Boolean minimization

For the problems of the formed by some *PB Constraints* $\min(c_1x_1 + c_2x_2 + \dots + c_nx_n \leq k)$ and a cost function, the goal is to find an assignment for $\{x_1, x_2, \dots, x_n\}$ in a way that the cost function is minimum.

$$\min(a_1x_1 + \dots + a_nx_n)$$

Previously¹, it has been explained that this types of problems are *NP-Hard*. This project will try to reduce the time to solve these problems through two approaches:

- Binary search:
Implement the well known *Binary Search*¹ algorithm to find the minimum value for the cost function.
- Linear search:
Some *SAT Solvers* can learn and derive new restrictions from previous problems. To take advantage of this ability it is necessary to implement a *Linear Search* algorithm.

Timeout

For some problems, it is more important to find a solution before a deadline than finding the best possible solution. For instance, a delivery company must have all the route planned for all trucks before the journey starts, therefore, they care more about having a solution than finding the best one.

For this, a *Timeout strategy* will be implemented in case that a good enough solution has been found or the problem does not seem to have one.

¹Binary search is a search algorithm that finds the position of a target value within a sorted array. [\(more\)](#)

Multi-threading (Optional)

This tool will take advantage of multi-core processors trying to split the problem and solving each part separately.

2.2 Scope

2.2.1 What and how?

To achieve all the general objectives² of the project, the following stages have been established:

- Analyze, refactor² and test the existing code to have a solid base.
- Add the functionality of representing *PBF*.
- Study [PBLib](#) library to see which functionalities it has available to work with *minimization*.
- Implement *minimization* strategies.
- Study timeout strategies and implement them.
- Study and implement multithreading. (Optional)

2.2.2 Possible obstacles

In this section, the possible obstacles and its solutions are exposed.

Base project

The existing project *Background section*¹ has not been developed following an adequate methodology. This could be responsible for a poor code quality. Building on top of a program with this characteristics could have terrible consequences because it would produce a lot of bugs and malfunctions hard to solve in the future.

For this reason, it is better to improve the quality of the existing code because it will avoid problems in the future.

Schedule

Because this is a final degree project the scope is limited, in this case until June of 2018. Considering the learning stage, analysis, requirements study, and other deviations which could appear, the time available to develop the project could be drastically reduced. Moreover, this project will be developed in an Erasmus stay which makes harder the planning. For these reasons, a good and realistic planning are key steps to take advantage of time and reduce contingencies.

²Code refactoring is the process of restructuring existing computer code—changing the factoring—without changing its external behavior. ([more](#))

PBLib

One of the main requirements of this project, *Pseudo-Boolean minimization*, is planned to be done with *PBLib* library. This is an obstacle because *PBLib* could not be compatible with the project causing compiling errors and therefore some time would have to be spent solving them. Also, *PBLib* could not have the expected functionalities, in which case a substitute should be found or, even worst, having to implement *PBLib* functionalities which would take a lot of time.

Correctness

As explained in *Rigor and Validation*⁴, correctness in this project is very important because of the context it is in.

Guarantee correctness could be hard and take more time than expected. If this happens, formal correctness could be delayed or reduced.

2.3 Methodology and Rigor

Research is a vast process with no clear path between *a* and *b*. For this, it is important to follow some directions. A methodology will provide some guidelines to avoid possible problems, be more efficient and do the project more manageable.

2.3.1 Methodology

The methodology adopted for this project will be Agile³. It is important to clarify that this methodology will not be followed strictly but adapted to this particular case where there is only one developer and all the objectives are well defined. The main characteristics followed from Agile in this project will be:

- Short cycles
- TDD (Test-Driven Development)
- Weekly scrums with the supervisor

2.3.2 Tools

In this chapter the, development tools will be introduced.

Git

[Git](#) will be used in this project as a Version Control System because it allows maintaining a tracking of all the changes made (commits), and what is more important, return to them at any time. In addition to this, it enforces a short cycle development (because commits are small units of work) and the developer has to document them which matches perfectly with Agile methodology. [GitHub](#) will be the repository service used.

Trello

[Trello](#) is a simple and flexible web board which helps to organize tasks and its state. It will be used in this project to manage tasks and priorities.

³Methodology based on the on the adaptability in front of any change to improve exit possibilities.

2.3.3 Communication

Due to my conditions, I'm currently studying abroad in an Erasmus program, all the communication will be made through electronic means. The majority of it will be made using e-mail but if it is necessary a video conference could be done.

The minimum communication with the supervisor will be a weekly e-mail report where all the tasks done during this period will be explained. Problems or questions will be also exposed if any.

2.3.4 Rigour and Validation

Rigor and Validation for this project are relevant.

The surrounding of it, such as *Artificial Intelligence, Planners, Cryptographic Protocols verification, ...*, are widely used nowadays and have been becoming more popular lately. This means that this project could have a big repercussion and be used by some professionals. For this, it is important to guarantee the validation and correctness of the project.

During the development, TDD will be used to avoid unnecessary code (possible origin of bugs) and assure the correctness of the implementation. It is also possible to formalize and prove all the operations done by the software.

Finally, my supervisor could give me some orientation and validate, if necessary, the operations done.

Chapter 3

Development

3.1 Requirement analysis, architecture and debugging

As previously mentioned, here, this stage has been dedicated to four points:

- Environment preparation
- Refactor
- Requirements
- Architecture

3.1.1 Environment configuration

First things first, before being able to start working I needed to prepare and set up all the tools needed for the project. Some of them were already configured from the previous project, such as the Control Version System, but some others would need to be configured from scratch or modified.

Makefile:

The existing Makefile at the moment was deleted and a new one was created. The goal of a Makefile is to automatize the build of the software and save time. The Makefile would be modified during the development stages to incorporate the new targets/goals. (

Google Test:

TDD (Test Driven Development) was adopted as part of the methodology for the development stages. For this, a testing framework was required. Not many options were considered because Google Test is highly popular and widely used.

Adopting and learning a new framework has some costs, but here the trade-off was clear because the time required for learning it was smaller than the time required for finding and solving bugs. It is also very important that using a testing framework gives confidence in the code because it guarantees that it works.

3.1.2 Refactor

A refactor of the existing code was needed. As it has been previously mentioned, this project has been built onto an existing code which needed to be tested.

Once the Google Test framework was set up I started creating Unit Tests (

Some bugs were found and corrected. Doing this at the beginning of the project was an excellent decision because those bugs would have caused erroneous behaviour difficult to track once the project became bigger.

3.1.3 Requirements

For the requirements, a deeper look at them was done. At this point, it was time to list them and plan how to achieve them. It was important to bear in mind that

for each iteration there would be a planning substage, therefore, the requirements mentioned at that point were the global ones which would affect the architecture. It would have been difficult trying to think about all the requirements at the beginning and inefficient because of the Agile methodology. The global requirements for the software were:

- Testability, upgradeability, etc. For development purposes
- Easy to use
- Fast
-

As you can see, the first requirements are software/development related. Those have been very important during the development stages and they have influenced a lot the architecture.

3.1.4 Architecture

The main goal for the architecture at this point was to respect the SOLID principle.

SOLID stands from:

- Single responsibility principle: A class should have only a single responsibility.
- Open/closed principle: Software entities should be open for extension but closed for modification.
- Liskov substitution principle: Objects should be replaceable by instances of their subtypes.
- Interface segregation principle: "many client-specific interfaces are better than one general-purpose interface."
- Dependency inversion principle: The dependencies should depend upon abstractions and not concretions.
- (
- (

3.2 Objective 1: Pseudo-boolean Minimization

3.2.1 Problem

This iteration addressed some problems: First, make the software easy to use while efficient to work with and second, find the optimal value of a PBMin problem using different techniques.

3.2.2 Possible solutions

One solution was creating from zero the software required to represent PBFormulae and their encoding to CNF or use a well-known C++ library, PBLib, into the project.

The first option was quickly dismissed because it would have taken a lot of time and the existing alternatives were very good and very hard to compete against them. Therefore, the second option was the chosen one because it would be faster and it would provide a better quality solution.

(

3.2.3 Planning

First of all, it was required to add PBLib to the tool's set with the following steps: download and install it.

(
Then modify the Makefile to add the new dependence and compile a simple C++ program which used PBLib and saw if it worked.

Once the whole project was compiling and executing without errors, it was time to start designing the architecture for this first iteration:

(
PBFormula:

This class is the one responsible for representing a Pseudo-Boolean Formula. In order to make it more interoperable with PBLib, it adopted the same representation for variables and weights which are `int32_t` and `int64_t` respectively.

(
PBConstraint:

A Pseudo-Boolean Constraint is represented as a PBFormula and a boundary.

The function `encode` is responsible to convert the Pseudo-Boolean Constraints into a CNF. This is the part done with PBLib.

Note that there is no way of specifying the relational operator of the constraint because it will always be "less equal". Other constraints can be easily converted into this type as specified in (

(
PBMin:

This class is responsible for representing a Pseudo-Boolean Minimization problem. It is formed by a vector of PBConstraint, the cost function which is a PBFormula and the search type which is defined by the enum `SEARCH_TYPE`.

This enum has two values, `BINARY_SEARCH` and `LINEAR_SEARCH`, which are the search strategies specified in the objectives of the project.

This class has the following methods:

-`minisat`: This method is responsible for calling the solver, Minisat, and get the model back if it exists.

-`binary Search`: This method is responsible for executing the Binary Search algorithm to find the optimal value for the problem.

-`linear Search`: This method is responsible for executing the Linear Search algorithm to find the optimal value for the problem.

(
-`getFirstFreshVariable`: This method returns a value called first fresh variable which is required by PBLib in order to encode the constraints into a CNF.

-`solve`: This is the method called by the user once he/she wants to solve the problem.

-`getCostFunctionMax`: This method returns the maximum possible value for the cost function.

-`getCostFunctionMin`: This method returns the minimum possible value for the cost function.

As the reader may have noticed, this contradicts the initial intention which was that this class should be only responsible for representing a Pseudo-Boolean Minimization problem. The methods listed above show that the class is also responsible for calling Minisat, implementing the search strategies and, as a consequence of this, calling PBLib for encoding the problem into a CNF.

(
This had a negative impact on the next iteration which required a redesign of the architecture. It will be explained in (

3.2.4 Development and TDD

(
 The developed started with the leaf class at the hierarchy, as seen in the architecture (
 (
 Following the hierarchy, the next one was PBConstraint and the last one PBMin.
 The first implemented method from PBMin was `int32_t PBMin::getFirstFreshVariable()`. This method has to return the next available literal to be used in the future by PBLib. To achieve this behaviour, this method looks at all the literals that are in the PBMin (constraints and cost function) and returns the maximum absolute literal found plus one.
 (
 The methods `int64_t PBMin::getCostFunctionMax()` and `int64_t PBMin::getCostFunctionMin()` are required to limit the search strategies. The optimal value has to be comprehended between these limits.
 (
 (
`bool PBMin::binarySearch(std::vector< int32_t > & model, int64_t & min)`
`bool PBMin::linearSearch(std::vector< int32_t > & model, int64_t & min)`

3.2.5 Finalization

At this substage, some techniques learned at the Erasmus course, Software Testing, such as Category Partition Testing were applied.

(
 These new tests revealed some bugs in the search strategies implementation for special values for the algorithms.
 (

3.3 Objective 2: Timeout

3.3.1 Problem

It has been previously explained that SAT is an NP-Complete problem which means that there is no known algorithm which can solve it in polynomial time. In other words it can take a lot of time to solve this types of problems. (

Some users need a result before certain time. For instance, a delivery companies need a plan every morning before 08:00 AM for their trucks, packages and drivers. Therefore some users need a result before certain time even if it is not the optimal one.

In order that the software was able to work with this new feature, it needed a new parameter from the user and timeout strategies.

3.3.2 Possible solutions

Two different timeout strategies were considered:

- A maximum time for each call to the solver.
- A maximum time for the whole problem.

Both options were considered useful hence they become a goal for the development substage.

3.3.3 Planning

Some research was done about timeout strategies for solvers.

(

In order to implement the asynchronous behaviour two different approaches were considered:

- Threads:

Threads within the same process can communicate using shared memory.

Threads share the same memory space which could be a source of problems if not handled carefully. In this particular case, this is helpful because the thread would execute the solver call while the parent is waiting for the timeout.

- Processes:

Child processes are easier to work with but in general, they are more expensive. This is because processes have their own code, memory space, files, registers and stack which implies that every time a new child process is created, some of the listed elements need to be copied.

Finally, Threads was the chosen option because of the following reasons:

- They share memory within a process which makes communication much easier. In this particular project, this allowed the code to be more simple.

- They are less expensive to create because no copy of memory is done.

The timeout was thought to be implemented as a signal sent from the parent thread to the child thread.

What happens when there is a timeout?

The answer depends on the timeout strategy selected for the problem: GeneralTimeoutSolver or SimpleTimeoutSolver.

In the first case, the flag `timeoutOccurred` is set to true and the last found solution is returned. With the flag, the user can know if the timeout occurred and therefore the solution may not be optimal.

In the second case, the flag `timeoutOccurred` is also set to true and the current solver execution is killed. However, the search algorithm will keep running with the next values.

(

As can be seen, the architecture suffered an evolution from the previous iteration. As previously mentioned in Iteration 1 (

That architecture would have resulted in a much complex `PBMin` class because it would have to be responsible for the timeouts.

For these reasons the following classes were modified or added:

- `PBMin`: After the refactor, this class is only responsible for representing a Pseudo-boolean minimization problem which was its original mission.

- `SearchStrategy`: One of the functionalities moved outside the `PBMin` class was the search strategy selection and implementation which needed to be moved to another class. For that reason, a hierarchy of classes was created: `SearchStrategy`, `BinarySearchStrategy` and `LinearSearchStrategy`. These set of classes have three methods:

- `init(...)` : The purpose of this method is to prepare the class for the execution of the search algorithm. For example, encode the `PBConstraints` into a CNF.

- `loop(...)` : The purpose of this method is to execute the search algorithm.

- `end(...)` : This method is executed after the loop once the optimal solution is found, there is no solution or a timeout occurred. It has no use by default.

- `BinarySearchStrategy`: This class uses the `loop(...)` method to implement the binary search algorithm.

- `LinearSearchStrategy`: This class uses the `loop(...)` method to implement the linear search algorithm.
- `Solver`: Another behaviour removed from the `PBMin` class is the actual execution of the problem solver. This behaviour was moved to a new class, `Solver`, which is responsible for calling the SAT solver. This class is the solver without a timeout, that it is implemented by its children `SimpleTimeoutSolver` and `GeneralTimeoutSolver`. The main methods are:
 - `run(...)`: This is the function called by the user once he/she wants to solve the problem.
 - `solve(...)`: This method is responsible for calling the SAT solver, passing the CNF and getting back the result.
- `SimpleTimeoutSolver`: This solver overrides the method `solve(...)` and adds the creation of a thread which calls the solver while it counts for the timeout.
- `GeneralTimeoutSolver`: This solver overrides the method `run(...)` and adds the creation of a thread which calls the selected search algorithm while it counts for the timeout.

3.3.4 Development and TDD

The first thing to do was refactor the class `PBMin` and move all the functionalities previously mentioned to the new classes. This also implied a refactor to the `PBMin` tests.

As the previous iteration, the development was done selecting classes in a bottom-up way.

The first class created was `Solver` which does not implement a timeout strategy, therefore it has the same functionality as the old `PBMin`: call the search algorithm and the sat solver. As seen in the architecture diagram (

The next implemented classes were `SearchStrategy`, `BinarySearchStrategy` and `LinearSearchStrategy` hierarchy.

`SearchStrategy` is an abstract class which means it cannot be instantiated. Its purpose is to be a "contract" between search strategies, such as linear search and binary search, and classes which use them. Because it has no code, it is not necessary to be tested.

However, for its children it is mandatory. The first child, `LinearSearch` implements the linear search algorithm which was in the old `PBMin` class. The method `init(...)` encodes the `PBConstraints` of the problem into a CNF. This was done at the `init(...)` method because it has to be done only once.

The method `loop(...)` is the one which actually implements the algorithm. It starts defining the boundaries of the search with the maximum possible value for the cost function and its minimum.

Because of the values given by the algorithm only differ in one unit, starting on the maximum and ending on the minimum, the functionality "Incremental constraints" from `PBLib` could be used. (

(

Finally, the method `end(...)` does nothing.

The other child, `BinarySearchSolver`, implements the binary search algorithm. As before, the method `init(...)` encode the problem constraints into a CNF. The `loop(...)` method implements the binary search algorithm taking as the left value the minimum possible value of the cost function and as the right value its maximum. Unlike before, the Incremental constraints functionality could not be used because the search is not "constant". Finally, as before, the method `end(...)` does nothing.

Finally, the last classes to be implemented were SimpleTimeoutSolver and GeneralTimeoutSolver.

The Template pattern (

The SimpleTimeoutSolver only redefines the method solve(...) to a creation of a thread which calls the sat solver with all its implications.

The GeneralTimeoutSolver only redefines the method run(...) to a creation of a thread which calls the function loop(...) from the SearchStrategy class.

3.3.5 Finalization

The classes Solver, SimpleTimeoutSolver and GeneralTimeoutSolver, apart from their unit tests required by TDD, were tested with integration tests.

(

Integration testing was done to expose defects in the communication of classes and also test the Solver hierarchy with real implementations of SearchStrategy and see that the timeout was working as expected.

3.4 Objective 3: Multi-threading

3.4.1 Problem

3.4.2 Possible solutions

3.4.3 Planning

3.4.4 Development and TDD

3.4.5 Finalization

Chapter 4

Project Planning

4.1 Schedule

4.1.1 Estimated project duration

For this project there have been estimated 450 hours of work, starting on **19th of February** and ending on **23rd of June**.

4.1.2 Considerations

The original plan could be modified to be adapted to deviations. Agile methodology implies that some new requirements can appear which could modify the planning. It is hard to do a realistic planning with Agile methodology because the iteration's requirements are not fully known until the Planning stage.

Because this project will be developed sequentially by only one person, the realization of a PERT diagram has been discarded. Nevertheless, some part of the documentation will be done in parallel.

4.2 Resources

For the development of this project, three types of resources will be needed.

4.2.1 Human Resources

- One person working 20 hours per week until the finalization of the project.

4.2.2 Material Resources

- Lenovo IdeaPad U330T
This laptop will be used to write the documentation and develop the project.

4.2.3 Software Resources

- Trello: Web application to manage project tasks.
- teXstudio: LaTeX editor to write all the documentation.
- e-mail: Communication tool used to contact the supervisor.
- Atom: Text editor to write the code.

- Git: VCS to backup and keep tracking of the project.
- C++: Language used for the development.
- PBLib: C++ library for Pseudo-Boolean encodings.
- CLion: Code editor focused on C++.
- Google Test: Unit testing framework for C++ developed by Google.

4.3 Project Planning

GEP

This task corresponds to the work done during the GEP course. This task has not any dependency but the work done will be used for the final documentation.

The estimated time for this stage is 70 hours.

Initial Stage

This stage will be used for defining the requisites to accomplish, the architecture of the software and refactor the previous code. Also, the required tools will be installed.

The estimated time for this stage is 90 hours.

Iterations

Because Agile methodology will be followed, the project has been divided into iterations. There will be a total of 3 iterations: Pseudo-Boolean minimization, Timeout strategies, and Multithreading, being this last one optional.

For each iteration, 80h of work are estimated.

Planning

This stage will be used for defining the scope of the iteration and goals.

This stage will be 10 hours long.

Development and TDD

In this stage, the iteration will be developed and tested.

This stage will be 60 hours long.

Finalization

In this stage, all possible bugs will be solved and feedback from the supervisor will be taken.

This stage will be 10 hours long.

Final Stage

Here, all the development will be finished and it will be used for finishing all the documentation and prepare the final presentation.

This stage will take 50 hours.

4.3.1 Gantt Diagram

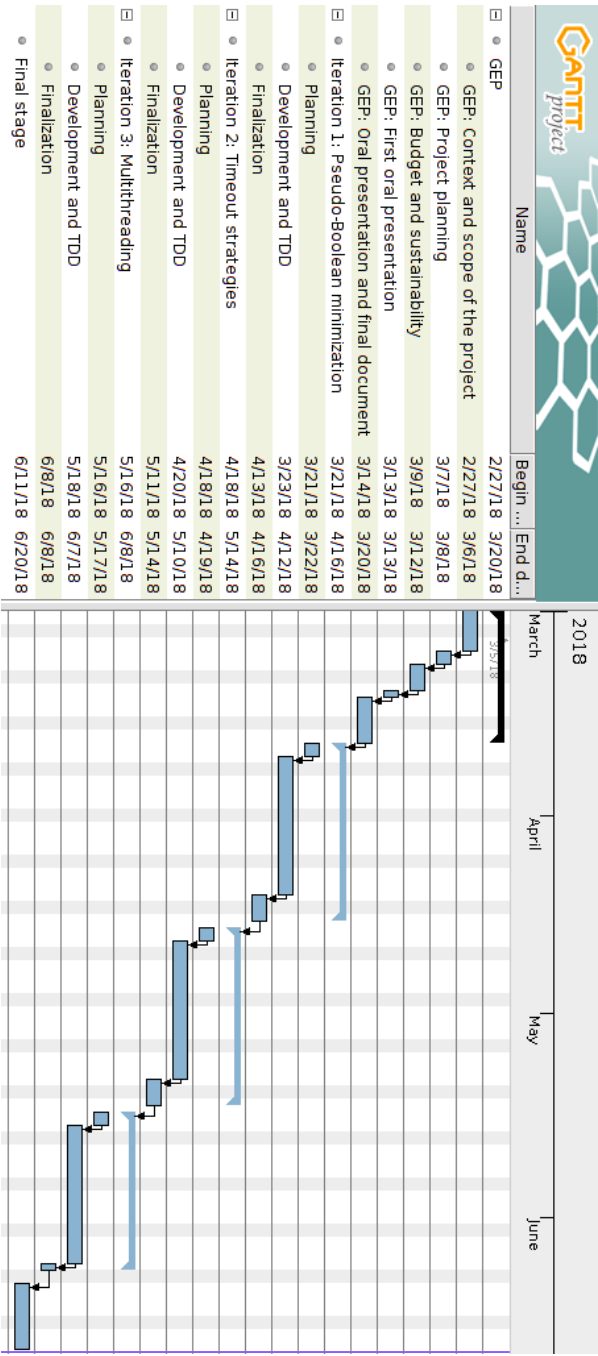


FIGURE 4.1: Gantt diagram of the project

4.4 Alternatives and Action Plans

Because of using an Agile methodology, the project functionalities can be easily adapted during the development.

4.4.1 Potential deviations

Incorrect estimations

It could be that the purposed estimations are not correct and be underestimated or overestimated. In the first case, if some iteration takes less time than expected, the next iteration will be started immediately. On the other case, if an iteration takes more time than expected, more hours will be added, for example, weekend hours. If even with this countermeasures the iteration is delaying the project some optional improvements will be discarded in order to guarantee the main functionalities and the project would be finished before the deadline. The effect on the resources would be more electricity consumed by the laptop on the added hours.

Summer internship

The deadline for this project is the 23rd of June. I have applied for a CERN internship from 4th of June until 31st of August.

In case of being accepted into the program, the final stage would have to be done during the internship. Since the final stage is for doing the final document and the final presentation, it can be lightened by paralleling part of its work during other stages.

The duration of the project is not affected because the only thing that would be done is a different distribution of the work. For the same reason, it would not have any effect on the resources.

Compatibility issues

As explained before, in section X, PBLib could cause some compatibility issues with the existing software which works with another library, Cudd. If this happens, in the best situation some hours will be spent fixing this issue or finding a substitute. In the worst situation, the functionalities of PBLib would have to be implemented which would take a lot of time. The project duration could be affected but it would be always finished before the deadline using weekend hours. The resources which will be used in addition is more electricity consumed by the laptop.

Base project code quality

The existing project could have some quality issues and be a source of bugs which would cause a lot of delays. For this reasons, and as s explained in section Y, the first stage of this project will be focused on assuring quality code of the existing project. The project duration would not be affected because part of the first stage is focused on that guaranteeing project finalization.

As explained in each potential deviation, the priority is to finish the project before the deadline. As said, extra-hours from the weekend can be used to work on the project to accomplish all the objectives. If even these hours are not enough, then the optional objective *Multithreading* will not be realized.

Chapter 5

Economic Management

In this section, all the costs of the project are exposed.

5.1 Direct costs

Direct costs are those that have a direct relationship with the manufacture of the product. In this case, the only direct costs are the human resources.

5.1.1 Human resources

The cost of the human resources has been estimated with the following expression: $Cost = \frac{Salary}{Hour} \times ExpectedHours$. The salaries have been extracted from PagePersonnel study[7]. In this study, the salaries are expressed per year. In average, there are 1.500 working hours per year. To obtain the price per hour, the salary per year has been divided by the working hours per year.

Taking into consideration the Gantt chart from the previous deliverable, the dedication of each role has been defined as follows:

Stage	Project Manager	Software Architect	Developer
GEP	70	0	0
Initial Stage	30	30	30
Iteration 1,2,3	6	147	87
Final Stage	30	0	20

TABLE 5.1: Hours destined to each stage per role

Role	Estimated hours (h)	Price/hour (€)	Total cost (€)
Project Manager	136	27	3.672
Software Architect	177	25	4.425
Developer	137	14	1.918
Total	10.015		

TABLE 5.2: Human resources budget

5.2 Indirect costs

Indirect costs are those that do not have a direct relationship with the manufacture of the product. In this case, the indirect costs are Hardware, Software, and some others.

5.2.1 Hardware

According to *Agencia Tributaria*¹, the maximum number of years to amortize a computer equipment is 8. Therefore the amortization of Hardware resources has been calculated following this expression: $Amortization = \frac{Price}{8 \times 12} \times 5$

Product	Price (€)	Units	Useful life (y)	Amortization (€)
Lenovo IdeaPad U330T	899	1	8	46,83
Total				46,83

TABLE 5.3: Hardware resources budget

5.2.2 Software

For software resources, free tools have been selected and student discounts have been used to minimize the total cost.

Product	Price (€)	Units	Useful life (y)	Amortization (€)
GitHub	6,10/month	5	N/A	30,5
GitHub student pack	-6,10/month	5	N/A	-30,5
Clion	6,90/month	5	N/A	34,5
JetBrains Product Pack for Students	-6,90/month	5	N/A	-34,5
Atom	0,00	1	N/A	0,00
TeXstudio	0,00	1	N/A	0,00
Total				0,00

TABLE 5.4: Software resources budget

5.2.3 Other resources

Internet connexion price has been extracted from Pepephone² plan, which is 34,6€ per month.

kWh price has been extracted from [Selectra](#). The average price per kWh is 0,12€. In office supplies paper packs, books, pens, ... are included.

5.3 Contingency

The contingency percentage for direct costs has been estimated following my experience on past projects. For indirect costs, the budget is easier to estimate therefore a small percentage has been selected.

¹Agencia Tributaria - amortizations

²Pepephone fibra

Product	Price(€)	Units	Total (€)
Internet connexion	0,047/h	450 hours	21,15
Power consumption	51Wh	450 hours	2,75
Print	0,05/page	400 pages	20
Office supplies	50	1	50
Total			93,9

TABLE 5.5: Other resources budget

Concept	Price (€)	Percentage (%)	Total (€)
Direct costs	10.015	30	3.004,5
Indirect costs	140,73	15	21,11
Total			3.025,61

TABLE 5.6: Contingency budget

5.4 Unforeseen

The first unforeseen is that the computer breaks. In this case, a new one will be bought. The other unforeseen events are that the stages of the project being extended. For each stage, a 50% delay has been estimated.

Unforeseen	Cost (€)	Probability (%)	Total (€)
Broken computer	1.300	5	65
Delay GEP stage	945	15	141,75
Delay initial stage	990	15	148,5
Delay iteration 1	842,5	15	126,38
Delay iteration 2	842,5	15	126,38
Delay iteration 3	842,5	15	126,38
Delay final stage	545	15	81,75
Total			816,14

TABLE 5.7: Unforeseen budget

5.5 Total budget

In conclusion, the total budget of the project is:

	Cost (€)
Direct costs	10.015
Indirect costs	140,73
Contingency	3.025,61
Unforeseen	816,14
Total	13.997,48

TABLE 5.8: Total budget

5.6 Control management

The control management mechanisms will be used to study and compare deviations.

The Human Resources is an initial estimation, therefore, the estimated cost and the real cost obtained once the project is finished will be compared. In any case, an hour follow-up will be done for each iteration and the functionalities implemented to see if the planning is accurate, or correct possible deviations and decide which functionalities could be added or deleted in order to accomplish the planning. Another method to solve the possible deviations could be reorganizing the Gantt chart.

At the end of the project, the original estimated budget will be compared with the real one. Finally, a study of which deviations and unforeseen appeared will be done and check if they can be covered by the contingency budget. This analysis will be very useful to realize future budgets and to apply the extracted conclusions.

The indicators used for that are: Variance in cost by rate, efficiency variance, variance in totals, ...

5.7 COMPARACIO EXPECTED VS REAL

Potser posarho en un capitol diferent

Chapter 6

Sustainability and Social Commitment

6.1 Sustainability Matrix

In this section, the sustainability matrix is resumed according to the numbers described here[3].

	PPP	Useful life	Risks
Environmental	7	20	-4
Economical	7	15	-10
Social	8	15	0
Sustainability range	58		

TABLE 6.1: Sustainability matrix

6.2 Economic dimension

6.2.1 PPP

The estimated budget of the project can be found in table 5.8. The estimated budget is 13.997,48€. This number has been estimated taking into account the working hours of each role, the hardware and software used, indirect costs, contingency, and unforeseen events.

6.2.2 Shelf life

Nowadays, the no optimization of Pseudo-Boolean encodings implies that the problems are bigger and harder which causes a long execution and more consumption of resources. With the optimizations that this project will study, the final execution time could be reduced therefore the power needed to solve the problem which translates into a more reduced cost.

6.2.3 Risks

As exposed previously, some risks are problems with the planning, problems with the tools used,...

The main risk is that the optimizations proposed are not useful in a practical environment.

6.3 Environmental dimension

6.3.1 PPP

The estimated electric usage for this project can be found in this table 5.5. The estimation has been done with this expression: $E = \frac{W}{h} \times T$. In this project $E = \frac{51W}{1h} \times 450h = 22,950kW$

It is hard to minimize more the impact of this project. Some strategies are turning off the computer when not using it, minimizing the amount of paper used, ... Some resources are reused, for example, instead of writing all the functionalities, some C++ libraries will be used.

6.3.2 Shelf life

It is hard to measure the footprint of this project along with all its useful life. It will depend on the success of the project and how many people will use it.

Currently SAT problems are executed in SAT-Solvers using some optimizations. As explained before this problem is NP-Complete which among other things implies that there is no known algorithm which can solve it in polynomial time. In other words, solving SAT is very time and resource expensive. Also, SAT is widely used in many fields. For example, computational complexity, databases, programming languages, artificial intelligence and system verification. This translates into a big electricity consumption and a huge footprint. For example, the MareNostrum[5] supercomputer spends 1,3MW/year.

This project purposes more optimizations to reduce the execution time. Even if these optimizations are small, because SAT is widely used, it could have a huge impact. It will have a positive impact because it will reduce the total CO² emissions released by the computers used to solve them.

6.3.3 Risks

The footprint of this project could be worst than expected if the development of it is extended.

6.4 Social dimension

6.4.1 PPP

This first stage of the project, GEP, will improve my management and planning skills, my English abilities, how to document and budget projects.

The other stages will expand my knowledge about informatics and the opportunity to put in practice a lot of skills developed during this degree.

Finally, my ability to present in front of people and defend the work done during these months.

6.4.2 Shelf life

This project will improve a lot of fields because SAT-Solvers are widely used. For example, Planners, Artificial Intelligence, ... which can have an unpredictable impact

in the life of people.

Currently this problem is solved using other techniques. The solution that this project purposes is an addition to them (it is not exclusive). There is a real need for this type of projects because as said previously, SAT is an NP-Complete problem therefore any improvement on this field will reduce the hardness of the problem with all the consequences this implies.

6.4.3 Risks

The only negative impact that this project can have is not being used. In this case, it will not be used and the society will remain unchanged.

Chapter 7

Conclusions

a que aspirava el projecte? comentar els objectius i argumentar si shan assolit
simplificar: si
comentar la importancia del testing TDD i de disenyar be larquitectura

7.1 Future Work

Si no sha fet el tercer objectiu, ferlo.
Afegir mes parametres de configuracio
Deixarho llest per a que la installacio sigui facil
Documentacio de com utilitzar-lo
Altres estrategies de timeout mes intellegents?
Que no nomes suporti minimitzacio, tambe GEQ i EQ

Appendix A

More information

A.1 Why SAT Solvers use CNF as input format?

There are two main reasons for this: Equisatisfiability and Computational Complexity. Let us start with the first one:

Two *BF* are **equisatisfiable** if and only if both have the same *models*. This may seem the same as equality but it is not because in an equality relationship both *BF* have to have the same variables.

This is important because between a *BF* and its result from a *CNF* transformation the equisatisfiability is preserved which means that if the *SAT Solver* finds a *model* for the *CNF*, then this *interpretation* will be also a *model* for the original *BF*.

The second reason is computational complexity. Let us have a look at the following table:

	DNF	CNF
TAUT	NP	P
SAT	P	NP

TABLE A.1: Complexity of deciding if a *BF* is SAT or TAUT depending of its format.

So as a *BF* can be converted into a *CNF* in linear time while preserving equisatisfiability, *SAT Solvers* will use them to target satisfiability.

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