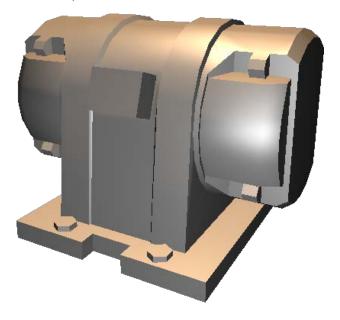
5 Bump Maps, Normal Maps, Displacement Maps

Interactive Computer Graphics
Marc Stamminger



Bump Mapping

- Bump/Normal-Mapping
 - simple geometric model with low detail
 - adapt light normal with more detailled texture
 - surface detail only in lighting
 - → silhouettes still from coarse mesh







Bump Maps

Non-Graphics Application: "Solarscreens"

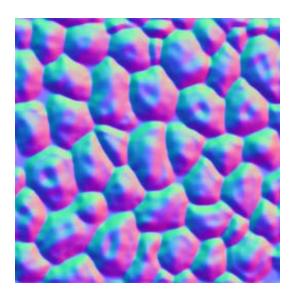




Bump Mapping

Normal Map

- texture with 3D normals encoded in RGB
- 8 Bit per component sufficient
 - but also 3x10 Bit, 4x16 Bit unsigned, floating point
- [-1,1] to [0;1]
 - R = x/2 + 0.5, G = y/2 + 0.5, ...
 - x = 2R-1, ...

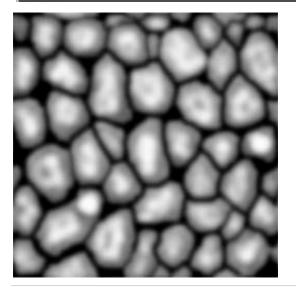


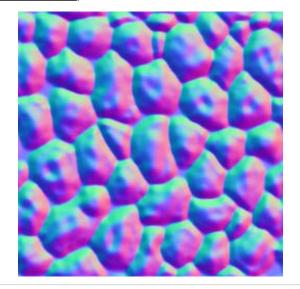


from height fields

 $N(x,y) = \begin{pmatrix} 2\Delta x \\ 0 \\ h(x+\Delta x, y) - h(x-\Delta x, y) \end{pmatrix} \times \begin{pmatrix} 0 \\ 2\Delta x \\ h(x, y+\Delta y) - h(x, y-\Delta y) \end{pmatrix}$



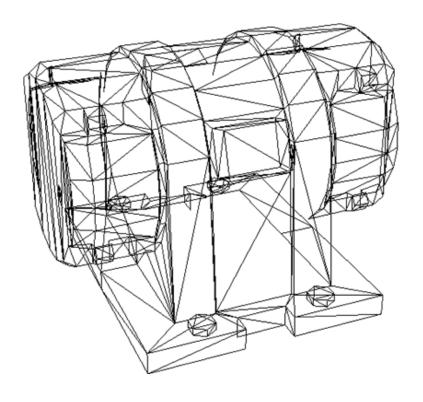




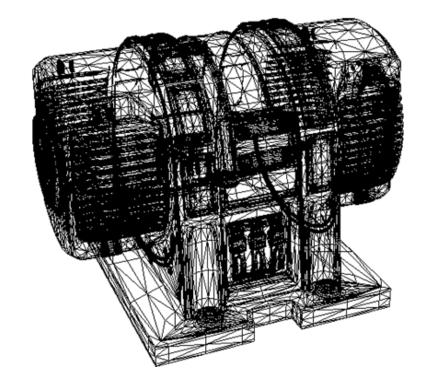




• Low/High Poly models



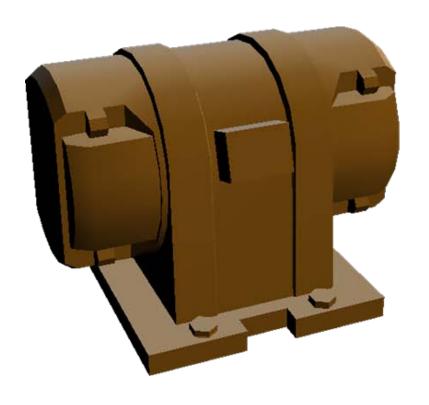


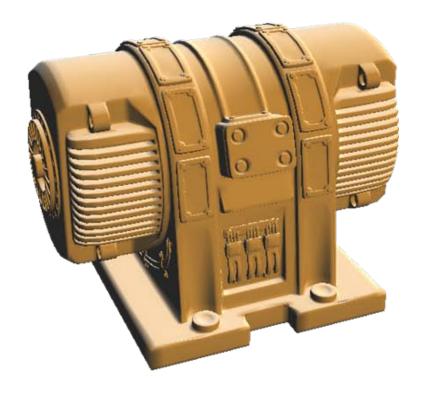


~115.000 tris



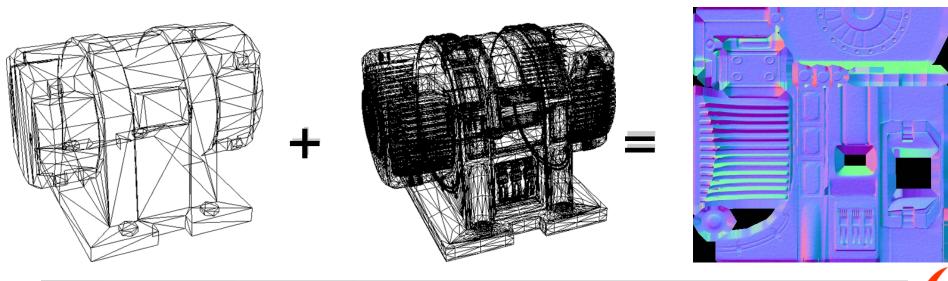
• Low/High Poly models





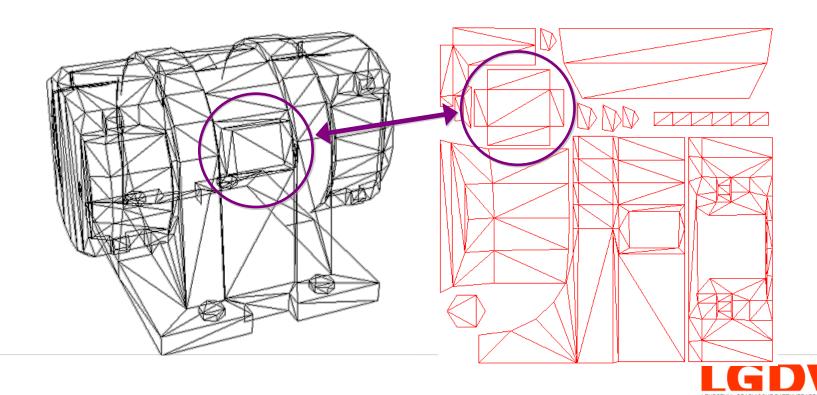


- missing detail in coarse mesh reintroduced by normal map
- generation by different tools
 - ATI Normalmapper, NVIDIA Melody, Crytek Polybump, xNormal (www.xnormal.net)



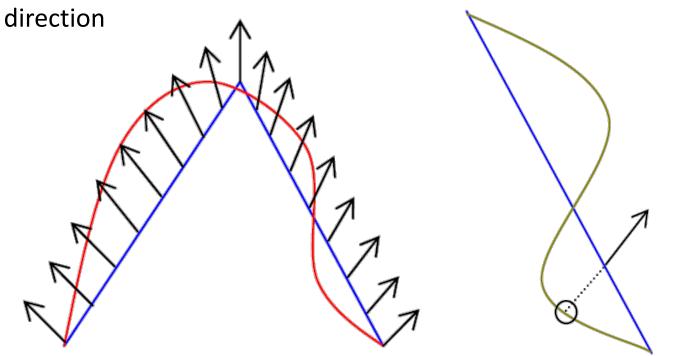


- Input
 - fine mesh: vertices and normals
 - coarse mesh: additional 2D parameterization
 - "texture atlas"



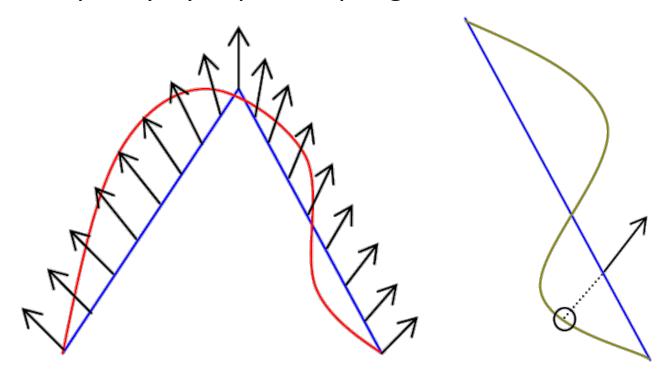
- for each texel of bump map
 - determine coordinate (on low-poly mesh)

determine closest intersection with high-poly mesh in normal





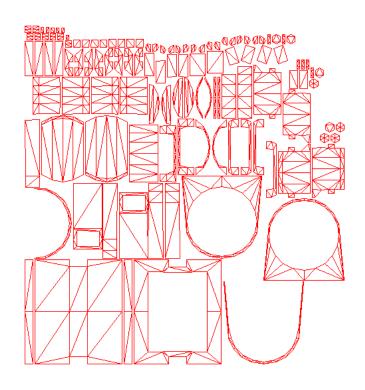
- computation using ray tracing
- intersection can also be in negative direction
- better quality by supersampling

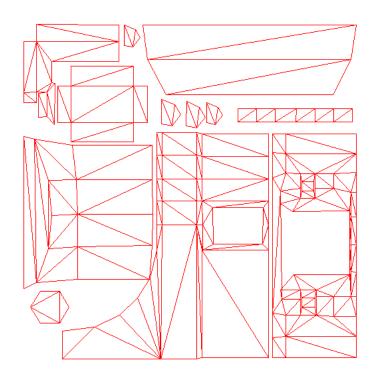




Texture Atlas

- 2D parameterization
 - automatic vs. manual
 - distortion vs. number of charts

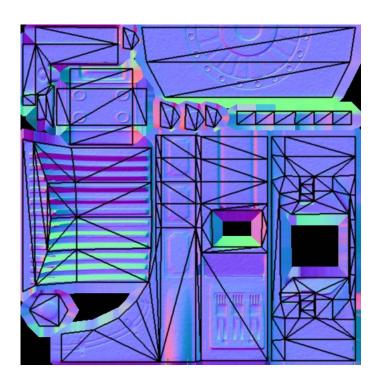


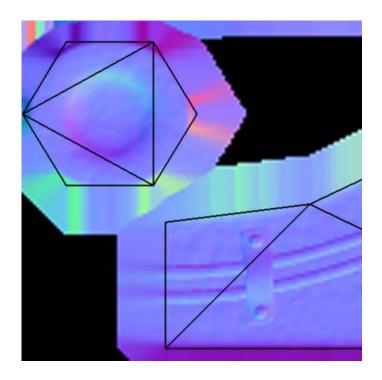




Texture Atlas

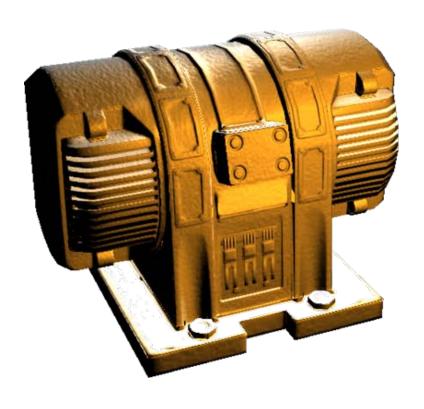
- Texture Lookups
 - bilinear filtering and mip-mapping
 - requires dilatation

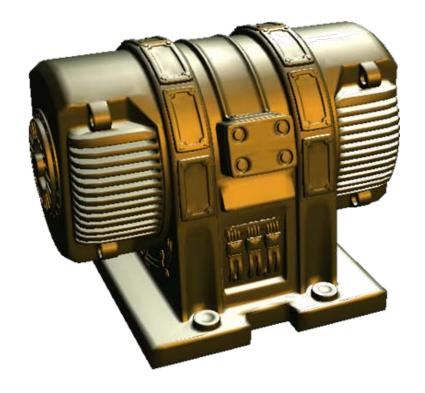






result







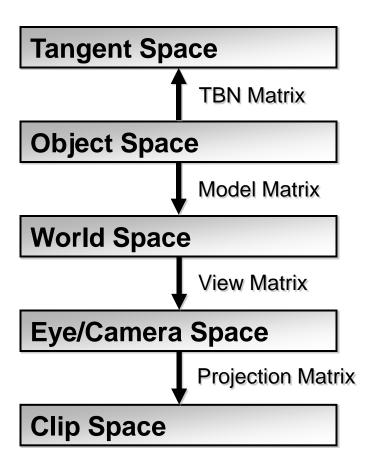
Coordinate Systems

- bump maps: color coded normal
 - but: in which coordinate system?
 - or: why are bump maps blue?
- (not so good) solution 1: object coordinates
 - same coordinate system as vertices
 - can be generated by normal mapping tools
 - no reusage of bump maps for different objects!
 - no tiling!



Coordinate Systems

- where do we compute lighting?
 - object space
 - native space for normals
 - world space
 - native space for light sources and environment map
 - eye/camera space
 - nativespace for view vector
 - Tangent Space
 - for bump maps!

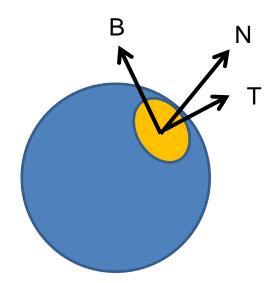




- better solution: compute light in tangent space
- orthonormal basis in every vertex
 - normal = z-axis (= blue)
 - tangent: gradient of texture coordinate1
 - bitangent: cross product of normal and tangent
 - interpolation of base vectors per pixel



- surface normal is z-axis of tangent space
- x and y are aligned according to texture coordinate directions
- call vectors T, B, N
- T: tangent vector
- B: bitangent
- N: normal





- given triangle P₀, P₁, P₂ with texture coordinates (s_i,t_i)
- how to determine tangent space ?
- point Q on triangle with texcoords (s,t):

$$Q = P_0 + (s-s_0)T + (t-t_0)B$$



$$\bullet \quad \mathbf{Q_1} = \mathbf{P_1} - \mathbf{P_0}$$

$$Q_2 = P_2 - P_0$$

•
$$\mathbf{Q_1} = \mathbf{P_1} - \mathbf{P_0}$$
 $\mathbf{Q_2} = \mathbf{P_2} - \mathbf{P_0}$
• $<\Delta s_1, \Delta t_1> = < s_1 - s_0, t_1 - t_0>$ $<\Delta s_2, \Delta t_2> = < s_2 - s_0, t_2 - t_0>$

$$<\Delta s_2, \Delta t_2> = < s_2 - s_0, t_2 - t_0>$$

linear equations

-
$$\mathbf{Q_1} = \Delta \mathbf{S_1} \mathbf{T} + \Delta \mathbf{t_1} \mathbf{B}$$

-
$$\mathbf{Q_2} = \Delta \mathbf{s_2} \mathbf{T} + \Delta \mathbf{t_2} \mathbf{B}$$

$$\left(\mathbf{Q_1}\right)_{\mathsf{X}}\left(\mathbf{Q_1}\right)_{\mathsf{y}}\left(\mathbf{Q_1}\right)_{\mathsf{z}}$$

$$(\mathbf{Q_2})_{\mathsf{X}} (\mathbf{Q_2})_{\mathsf{V}} (\mathbf{Q_2})_{\mathsf{Z}}$$

$$\Delta s_1 \Delta t_1$$

$$\Delta s_2 \Delta t_2$$

$$T_x$$
 T_y T_z

$$\mathbf{B}_{x}$$
 \mathbf{B}_{y} \mathbf{B}_{z}



• invert:

$$\begin{bmatrix}
\mathbf{T}_{x} & \mathbf{T}_{y} & \mathbf{T}_{z} \\
\mathbf{B}_{x} & \mathbf{B}_{y} & \mathbf{B}_{z}
\end{bmatrix} = \frac{1}{\Delta s_{1} \Delta t_{2} - \Delta s_{2} \Delta t_{1}} \begin{bmatrix}
\Delta t_{2} - \Delta t_{1} \\
-\Delta s_{2} \Delta s_{1}
\end{bmatrix} (\mathbf{Q}_{1})_{x} (\mathbf{Q}_{1})_{y} (\mathbf{Q}_{1})_{z} \\
(\mathbf{Q}_{2})_{x} (\mathbf{Q}_{2})_{y} (\mathbf{Q}_{2})_{z}$$

-> delivers unnormalized T and B



- compute T,B,N for all triangles
- for every vertex: average TBN over surrounding triangles
 - → vertex attribute
 - → TBN interpolated over triangles
 - → per-pixel tangent space



Bump Mapping

- influences lighting computation only
- requires per-pixel lighting (cheap nowadays)
- no shadows due to bumps
 - but: horizon maps, parallax mapping (follow)
- mip-mapping
 - theoretically: supersampling of light results
 - practically: averaged normals
 - unsolved problem, mainly empirical results

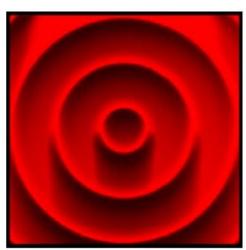


Interactive Horizon Mapping

- - bumps should cast shadows
 - compute horizon around a point P
 - horizon height depends on direction
 - shadow if light source below horizon
 - example:



normal map



horizon height for direction NORTH

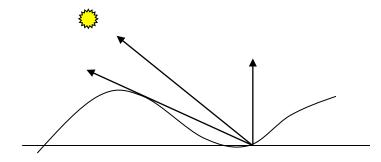


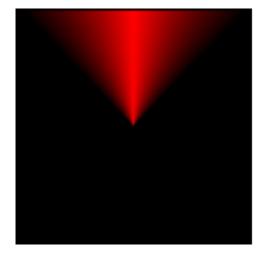
Sloan and Cohen 2000

Interactive Horizon Mapping

Sloan and Cohen 2000

- idea: precompute horizon height for eight directions (N,NE,E,...)
- compute "height angle" of light source
- for all eight directions:
 - test whether light above horizon
 -> 0/1 shadow result
 - blend 0/1 results with basis function textures
 - one basis function texture for each direction (one in main direction, blend to zero for other directions)
- put four textures into one's RGBA-channels
- difficult to apply with standard
 OpenGL, but possible (see paper)



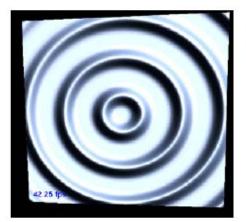


NORTH basis function texture



Interactive Horizon Mapping

examples



without shadows



with shadows



with bright shadows









- elegant extension of bump mapping with texture
 - bumps should result in parallax effect on texture
 - estimate parallax due to bump texture
 - apply parallax by texture coordinate offset

original idea:

 Tomomichi Kaneko, et al. "Detailed Shape Representation with Parallax Mapping", ICAT, 2001.

extended:

 Walsh, "Parallax Mapping with Offset Limiting", Infiniscape Tech Report, 2004



Texture map

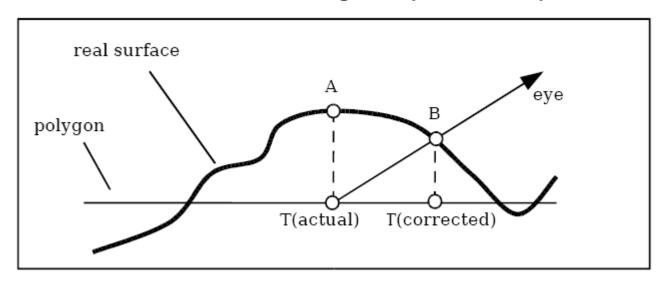
Texture map and bump mapping

No parallax mapping

Parallax mapping



- eye sees polygon point T(actual)
- but T(actual) is offset to A by bump map
- what eye sees is B
- and B is textured according to T(corrected)

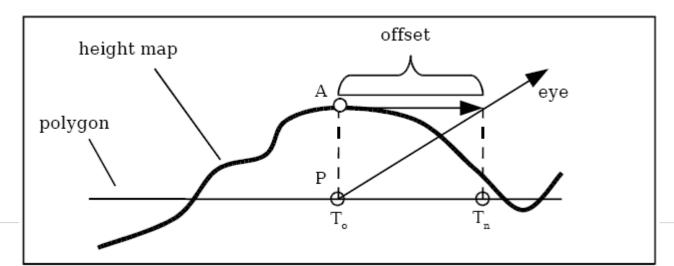


how can we compute T(corrected)?



Kaneko:

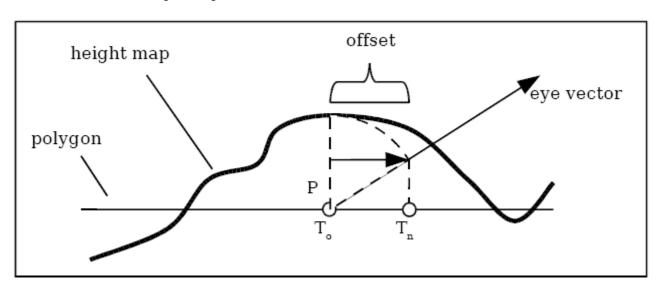
- eye sees polygon point P with texture coordinate T0
- P is moved to A by bump map
- compute parallax offset by assuming that bump map is constant around P
- new texture coordinate Tn = T0 + F*eye.xy/eye.z
 (eye in texture coordinate space, F factor due to bump height)
- approximation, in particular for grazing angles (eye.z small)





- Welsh: parallax mapping with offset limiting
 - Kanekos approximation particularily wrong for grazing angles
 - limit offset for grazing angles:

$$Tn = T0 + F*eye.xy$$





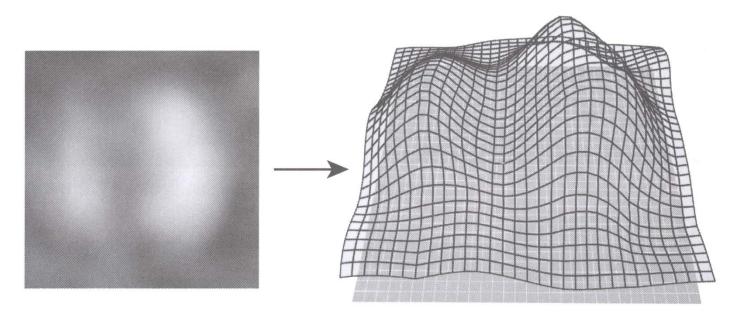
demo





Displacement Mapping

- data like for bump maps
- but really generate displaced geometry





Displacement Mapping

bump mapping

displacement mapping

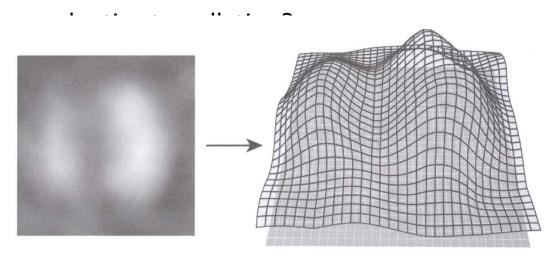






Vertex based displacement maps

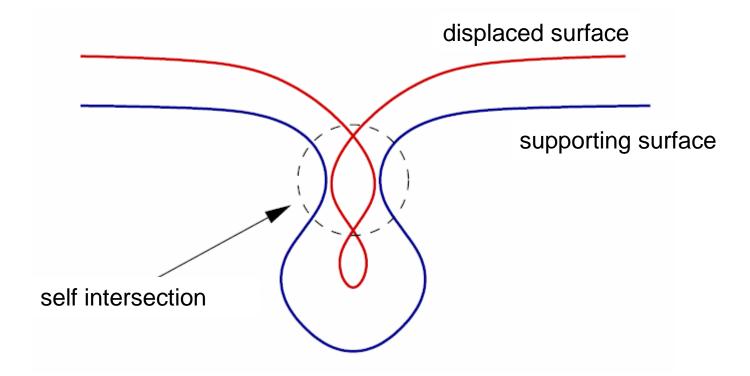
- displacement in vertex shader
 - render finely tessellated basis mesh with texture coordinates
 - vertex shader reads texture, displaces vertices
- issues:
 - how to generate tessellated basis mesh?





Displacement Mapping

- caveat: self intersections
 - positive displacement in concave regions
 - negative displacement in convex regions





coarse mesh + displacement texture

assume only negative displacement

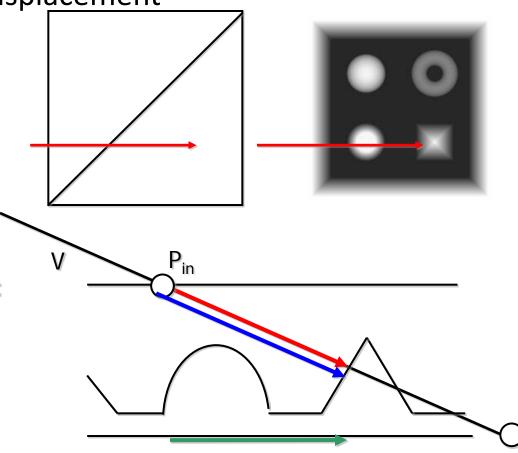
 → ray casting in fragment shader

find intersetion point:

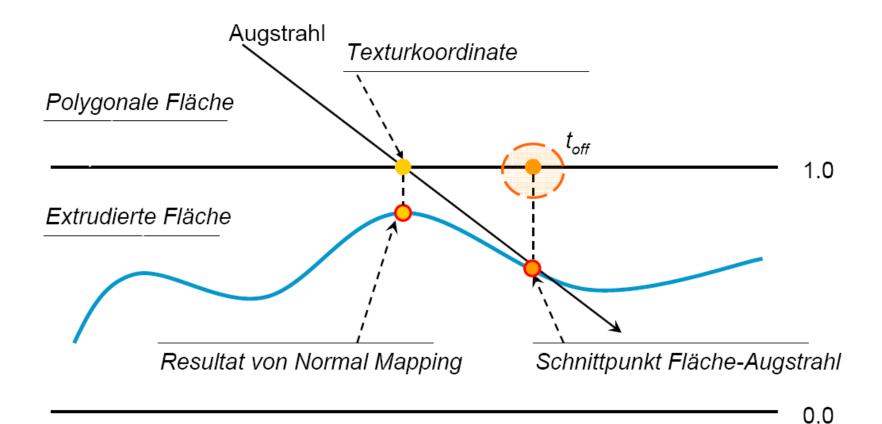
$$P=P_{in}+d*V$$

find displaced texture coordinate:

$$T=T_{in}+s*V_{t}$$



Raycasting in Fragment Shader

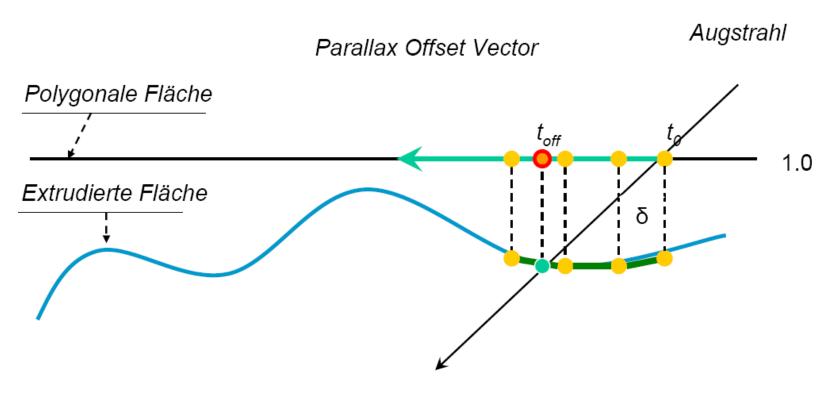




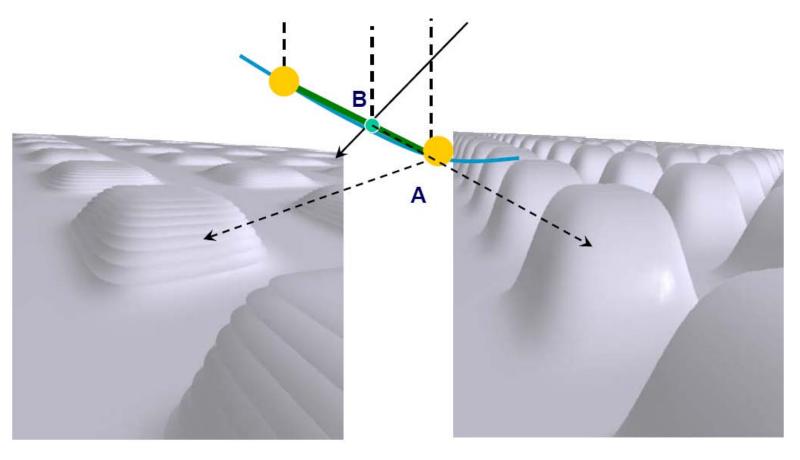
- per vertex
 - determine eye ray, light ray etc. in tangent space
- per fragment
 - find intersection of eye ray with height field
 - → offsetted surface point and texture coordinate
 - + shadow ray to light source



- walk along ray in small steps, search for intersection
- interpolate height field linearily



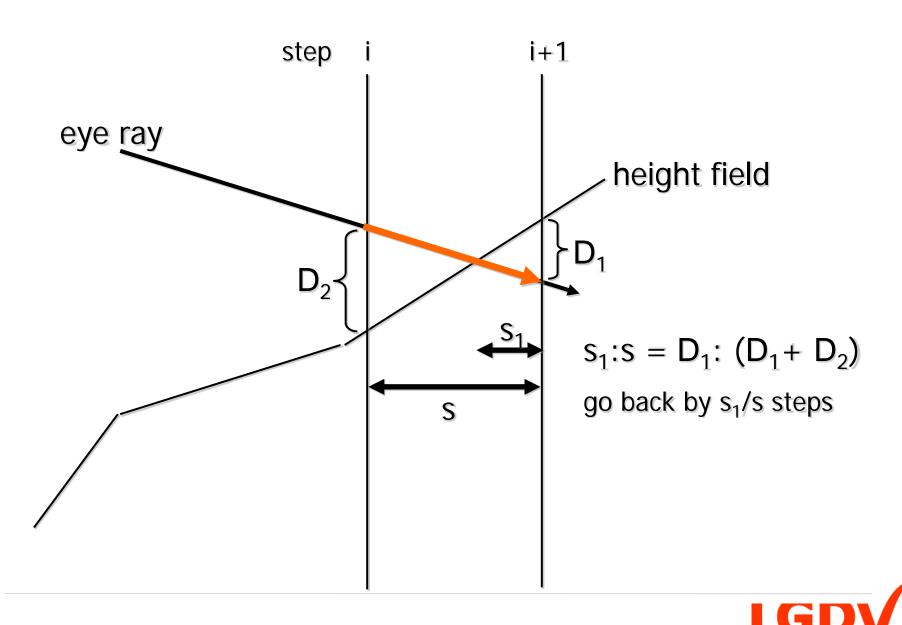
linear interpolation is important



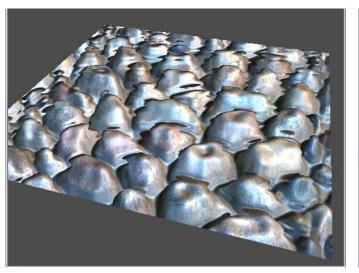
piecewise constant

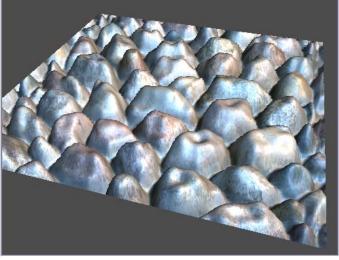
piecewise linear





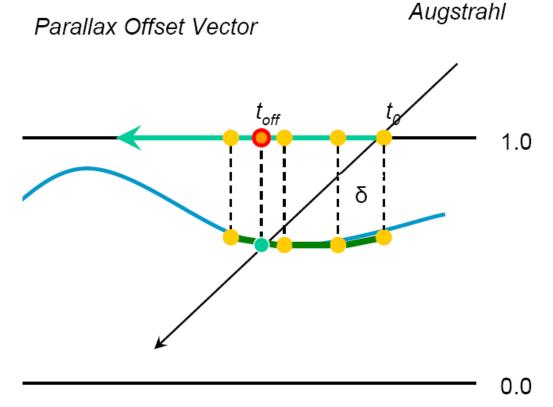
step size is important





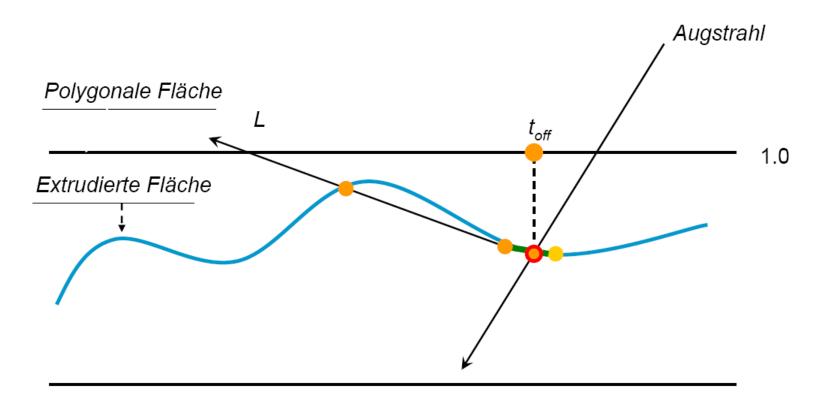


- adapt step size dynamically
 - select step size such that step size corresponds to pixel size of height map



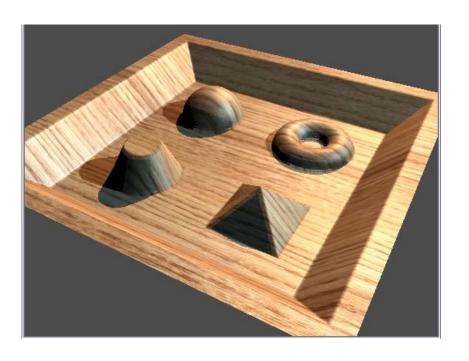


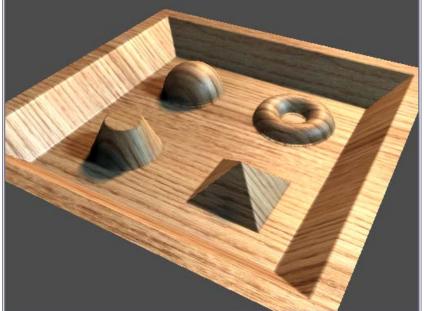
 second ray casting step, now from offsetted hit point back to light





trick for soft shadows







- step along shadow ray towards light source (n steps)
- search largest height difference
 - → shadow value
 - max [$(h_i-h_0)/n*$ scaling]

