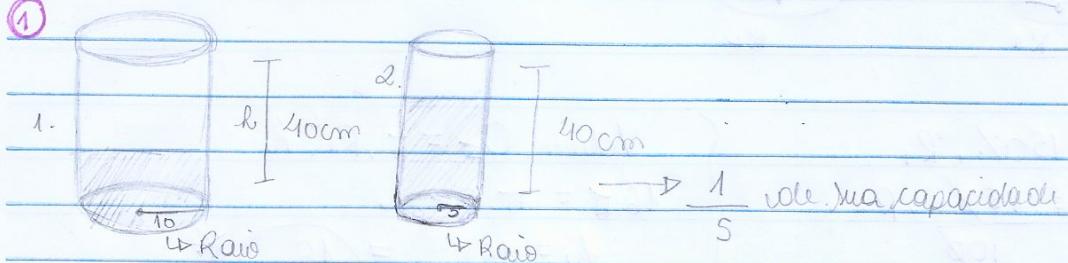


Tarefa Básica

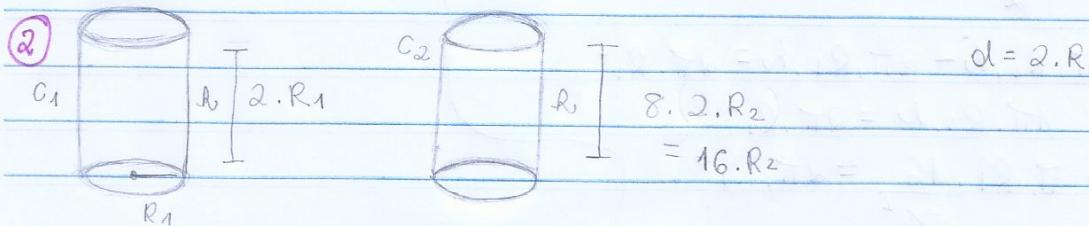
CILINDROS E PIRÂMIDES

→ CILINDROS

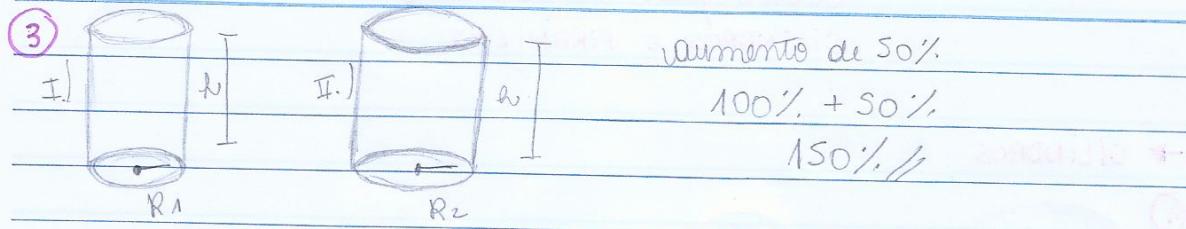
①



$$\left. \begin{array}{l} V_1 = \pi \cdot R^2 \cdot h \\ V_1 = \pi \cdot 10^2 \cdot 40 \\ V_1 = 100 \cdot 40 \cdot \pi \\ V_1 = 4000\pi \text{ cm}^3 \end{array} \right\} \begin{array}{l} V_2 = \frac{1}{S} \cdot V_1 \\ \pi \cdot 8^2 \cdot h = \frac{1}{S} \cdot 4000\pi \\ \pi \cdot 64 \cdot h = 4000\pi \end{array} \left. \begin{array}{l} h = 800\pi \\ 25\pi \\ h = 32\text{cm} \end{array} \right\} \text{Alternativa A})$$



$$\left. \begin{array}{l} \text{Volume } C_1 = \frac{1}{2^4} \\ \text{Volume } C_2 = \frac{1}{16^4} \\ \pi \cdot R_1^2 \cdot 2R_1 = \frac{1}{2^4} \\ \pi \cdot R_2^2 \cdot 16R_2 = \frac{1}{16^4} \end{array} \right\} \begin{array}{l} \frac{R_1^3}{R_2^3} = \sqrt[3]{\frac{8}{2^4}} \\ \sqrt[3]{R_1^3} = \sqrt[3]{2^3} \\ \sqrt[3]{R_2^3} = \sqrt[3]{3^3} \\ \frac{R_1}{R_2} = \frac{2}{3} \end{array} \left. \begin{array}{l} R_1^3 = 1 \\ 8 \cdot R_2^3 = 2^4 \\ \frac{R_1^3}{R_2^3} = \frac{8}{2^4} \end{array} \right\} \text{Alternativa E})$$



$$R_2 = 150\%, R_1 \quad \left. \begin{array}{l} \text{Volume } C_2 = \pi \cdot R_2^2 \cdot h \\ 16\pi = \pi \cdot R_1^2 \cdot h \\ h = \frac{16\pi}{\pi \cdot R_1^2} = \frac{16}{R_1^2} \end{array} \right\} *$$

$$R_2 = \frac{150}{100} \cdot R_1$$

$$R_2 = \frac{3}{2} \cdot R_1$$

$$\text{ALC}_2 = \text{ATC}_1$$

$$2\pi \cdot R_2 \cdot h = 2\pi \cdot R_1 \cdot h + 2\pi \cdot R_1^2$$

$$\cancel{2\pi} \cdot \frac{3}{2} \cdot R_1 \cdot h = 2\pi \cdot R_1 \cdot h + 2\pi \cdot R_1^2$$

$$3\pi \cdot R_1 \cdot h - 2\pi \cdot R_1 \cdot h = 2\pi \cdot R_1^2$$

$$1\pi \cdot R_1 \cdot h = 2\pi \cdot R_1^2$$

$$\pi \cdot R_1 \cdot 16 = 2\pi \cdot R_1^2$$

$$\frac{16\pi}{R_1} = 2\pi \cdot R_1^2$$

$$R_1^3 = \frac{16\pi}{2\pi}$$

$$R_1 = \sqrt[3]{8}$$

$$R_1 = 2$$

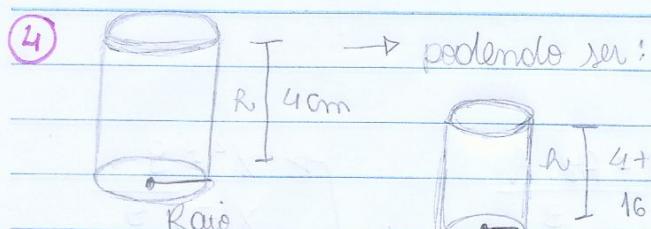
$$*\frac{h}{R_1^2} = 16$$

$$h = \frac{16}{2^2}$$

$$h = \frac{16}{4} = 4$$

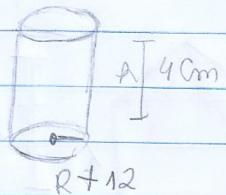
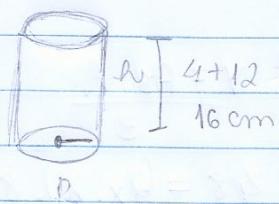
Alternativa D)

4



\rightarrow pede-nos ser:

OU



$$V_1 = \pi \cdot R^2 \cdot 16$$

$$V_2 = \pi \cdot (R+12)^2 \cdot 4$$

$$D = b^2 - 4 \cdot a \cdot c$$

$$\pi \cdot R^2 \cdot 16 = \pi \cdot (R+12)^2 \cdot 4$$

$$D = (-8)^2 - 4 \cdot 1 \cdot (-48)$$

$$(R+12)^2 = 4 \cdot R^2$$

$$D = 64 + 192$$

$$R^2 + 24R + 144 = 4R^2$$

$$D = 256$$

$$-3R^2 + 24R + 144 = 0 \quad (: -3)$$

$$R^2 - 8R - 48 = 0$$

$$x = \frac{-b \pm \sqrt{D}}{2a}$$

$$x' = \frac{8+16}{2} = 12 \text{ cm}$$

Alternativa A)

$$x = \frac{8-16}{2}$$

$$x'' = \frac{8-16}{2} = -4 \text{ cm}$$

NÃO CONVEN

5



\rightarrow II.



$h + 0,08 \text{ mm}$
 $h + 0,08 \text{ cm}$

$$V_{\text{pedra}} = V_{\text{II}} - V_{\text{I}}$$

$$V_p = \pi \cdot 20^2 \cdot (h + 0,08) - \pi \cdot 20^2 \cdot h$$

$$V_p = \pi \cdot 400 \cdot (h + 0,08 - h)$$

$$V_p = \pi \cdot 400 \cdot \frac{8}{100} = 32\pi$$

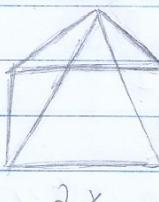
$$V_p = 32 \cdot 3,14$$

$$V_p = 100,5 \text{ cm}^3$$

Alternativa B)

→ PIRÁMIDES

①



$$V = A_B \cdot h$$

$$48 = 3 \cdot 8$$

$$48 = 24$$

$$144 = 16x^2$$

$$x^2 = 144$$

$$x = 12$$

$$x = 3$$

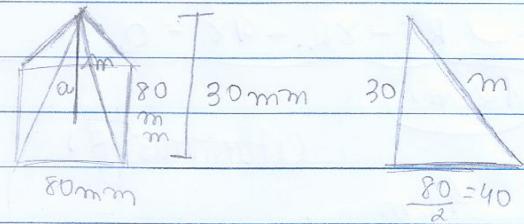
$$\Rightarrow x^2 = 9$$

$$x = \sqrt{9}$$

$$x = 3$$

Alternativa C)

②



$$m^2 = 30^2 + 40^2$$

$$m^2 = 900 + 1600$$

$$m = \sqrt{2500}$$

$$m = 50 \text{ mm}$$

$$AT = 4 \cdot A_{\Delta} + A_B$$

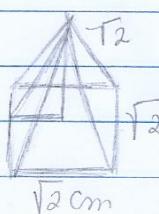
$$AT = 4 \cdot \frac{80 \cdot 50}{2} + 80 \cdot 80$$

$$AT = 8000 + 6400$$

$$AT = 14400 \text{ mm}^2$$

Alternativa E)

③



$$l^2 = 1^2 + \left(\frac{\sqrt{2}}{2}\right)^2$$

$$l^2 = 1 + \frac{1}{2}$$

$$l^2 = \frac{3}{2}$$

$$l = \sqrt{\frac{3}{2}}$$

$$l = \sqrt{1.5}$$

$$l = \sqrt{1.5} \cdot \sqrt{2} / \sqrt{2}$$

$$l = \sqrt{3}$$

$$(l^2)^2 = m^2 + \left(\frac{\sqrt{2}}{2}\right)^2$$

$$2 = m^2 + \frac{1}{4}$$

$$2 - \frac{1}{4} = m^2$$

$$2 - 0.25 = m^2$$

$$1.75 = m^2$$

$$m^2 = 4 - 1 = 3$$

$$m^2 = 3$$

$$m = \sqrt{3}$$

↓

1 cm

Alternativa C)

④

$$V = \frac{1}{3} \cdot 6 \cdot a^2 \sqrt{3} \cdot b\sqrt{3}$$

$$V = 2 \cdot a^2 \cdot b \cdot (\sqrt{3})^2$$

$$V = \frac{(3a^2 \cdot b \text{ cm}^2)}{2} \quad \text{Alternativa A)}$$

⑤

$$V = \frac{1}{3} \cdot 6 \cdot 4^2 \cdot 6\sqrt{3} \cdot 6\sqrt{3}$$

$$V = 2 \cdot 4 \cdot 6 \cdot (\sqrt{3})^2$$

$$V = 48 \cdot 3 = 144 \text{ cm}^3 \quad \text{Alternativa D)}$$

⑥

$$\text{Perímetro } \diamond = 6 \text{ cm} \rightarrow V = \frac{1}{3} \cdot 6 \cdot 1^2 \sqrt{3} \cdot 8$$

$$6a = 6$$

$$a = \frac{6}{6} = 1 \text{ cm} \quad V = 2 \cdot 2 \cdot \sqrt{3}$$

$$(V = 4\sqrt{3} \text{ cm}^3) \quad \text{Alternativa A)}$$

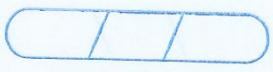
⑦

$$V_{\text{pirâmide}} = V_{\text{prisma}}$$

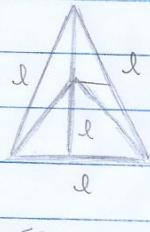
$$\frac{1}{3} \cdot 2a \cdot 2a \cdot h_1 = a \cdot a \cdot h_2$$

$$\frac{h_1}{h_2} = \frac{a^2 \cdot 3}{4a^2} = \frac{3}{4}$$

Alternativa A)



8



$$A\Delta = 6\sqrt{3}$$

$$4 \cdot A\Delta = 6\sqrt{3}$$

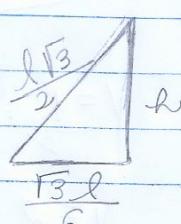
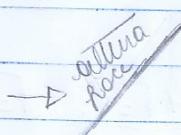
$$4 \cdot l^2\sqrt{3} = 6\sqrt{3}$$

$$\rightarrow l^2 = 6\sqrt{3}$$

$\sqrt{3}$

$$l^2 = 6$$

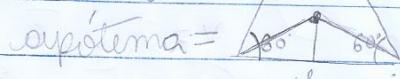
Triângulo equilátero



$$\left\{ \begin{array}{l} h_{\Delta} = l\sqrt{3} \\ a_{\Delta} = \frac{l\sqrt{3}}{2} \end{array} \right.$$

(triângulo equilátero)

cálculo da



$$\operatorname{tg} 30^\circ = \frac{a}{l} \Rightarrow l/a = \sqrt{3}/3$$

$$\sqrt{3} = a \cdot 2/3 \Rightarrow a = \frac{\sqrt{3} \cdot l}{2}$$

$$a = \frac{\sqrt{3} \cdot l}{6}$$

$$\left(\frac{l\sqrt{3}}{2} \right)^2 = h^2 + \left(\frac{\sqrt{3}l}{6} \right)^2$$

$$\frac{3l^2}{4} = 3l^2 - \frac{3l^2}{36}$$

$$h^2 = 27l^2 - 3l^2$$

$$h^2 = \frac{24l^2}{36}$$

$$\rightarrow h = \sqrt{\frac{36}{9}} = \frac{6}{3} = 2 \text{ m}$$

Alternativa A)