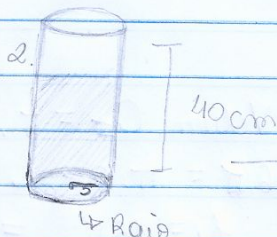
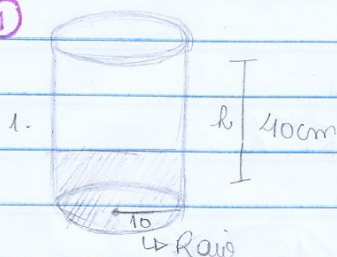


Tarefa básica

CILINDROS E PIRÂMIDES

→ CILINDROS

①



→ $\frac{1}{5}$ vez a capacidade

$$V_1 = \pi \cdot R^2 \cdot h$$

$$V_1 = \pi \cdot 10^2 \cdot 40$$

$$V_1 = 100 \cdot 40 \cdot \pi$$

$$V_1 = 4000\pi \text{ cm}^3$$

$$V_2 = \frac{1}{5} \cdot V_1$$

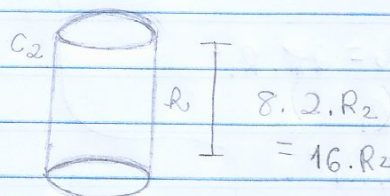
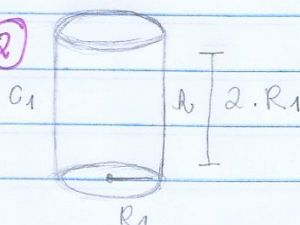
$$\pi \cdot R^2 \cdot h = \frac{1}{5} \cdot 4000\pi$$

$$\pi \cdot 5^2 \cdot h = 800\pi$$

$$h = \frac{800\pi}{25\pi}$$

Alternativa A)

②



$$d = 2 \cdot R$$

$$8 \cdot 2 \cdot R_2 = 16 \cdot R_2$$

$$\frac{\text{Volume } C_1}{\text{Volume } C_2} = \frac{1}{24}$$

$$\frac{\pi \cdot R_1^2 \cdot 2 \cdot R_1}{\pi \cdot R_2^2 \cdot 16 \cdot R_2} = \frac{1}{24}$$

$$\frac{R_1^3}{8 \cdot R_2^3} = \frac{1}{24}$$

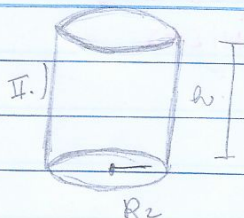
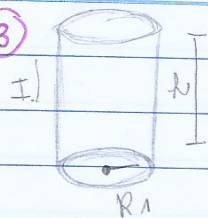
$$\frac{R_1^3}{R_2^3} = \frac{8}{24}$$

$$\sqrt[3]{\frac{R_1^3}{R_2^3}} = \sqrt[3]{\frac{8}{24}}$$

$$\frac{R_1}{R_2} = \frac{2}{3}$$

Alternativa E)

3



aumento de 50%

100% + 50%

150% //

$$R_2 = 150\% \cdot R_1$$

$$R_2 = \frac{150}{100} \cdot R_1$$

$$R_2 = \frac{3}{2} \cdot R_1$$

$$\text{Volume } C_{\pm} = \pi \cdot R_1^2 \cdot h$$

$$16\pi = \pi \cdot R_1^2 \cdot h$$

$$h = \frac{16\pi}{\pi \cdot R_1^2} = \frac{16}{R_1^2} *$$

$$ALC_2 = ATC_1$$

$$2\pi \cdot R_2 \cdot h = 2\pi \cdot R_1 \cdot h + 2\pi \cdot R_1^2$$

$$2\pi \cdot \frac{3}{2} \cdot R_1 \cdot h = 2\pi \cdot R_1 \cdot h + 2\pi \cdot R_1^2$$

$$3\pi \cdot R_1 \cdot h - 2\pi \cdot R_1 \cdot h = 2\pi \cdot R_1^2$$

$$1\pi \cdot R_1 \cdot h = 2\pi \cdot R_1^2$$

$$\pi \cdot R_1 \cdot \frac{16}{R_1^2} = 2\pi \cdot R_1^2$$

$$\frac{16\pi}{R_1} = 2\pi \cdot R_1^2$$

$$R_1^3 = \frac{16\pi}{2\pi}$$

$$R_1 = \sqrt[3]{8}$$

$$R_1 = 2$$

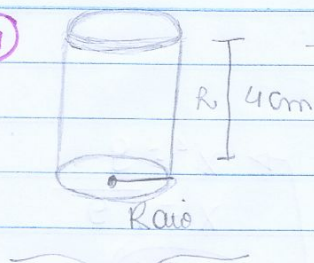
$$* h = \frac{16}{R_1^2}$$

$$h = \frac{16}{2^2}$$

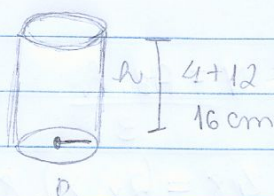
$$h = \frac{16}{4} = 4$$

Alternativa D)

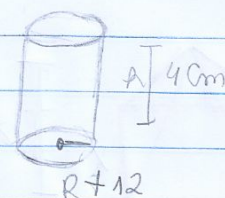
4



→ podendo ser:



OU



$$V_1 = \pi \cdot R^2 \cdot 16$$

$$V_2 = \pi \cdot (R+12)^2 \cdot 4$$

$$\Delta = b^2 - 4 \cdot a \cdot c$$

$$\Delta = (-8)^2 - 4 \cdot 1 \cdot (-48)$$

$$\Delta = 64 + 192$$

$$\Delta = 256$$

$$\pi \cdot R^2 \cdot 16 = \pi \cdot (R+12)^2 \cdot 4$$

$$(R+12)^2 = 4 \cdot R^2$$

$$R^2 + 24R + 144 = 4R^2$$

$$-3R^2 + 24R + 144 = 0 \quad (: -3)$$

$$R^2 - 8R - 48 = 0$$

$$x = \frac{-b \pm \sqrt{\Delta}}{2 \cdot a}$$

$$x' = \frac{8+16}{2} = 12 \text{ cm}$$

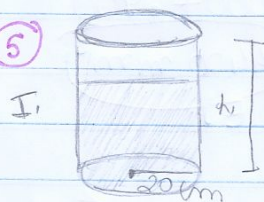
Alternativa A)

$$x = \frac{8 \pm 16}{2}$$

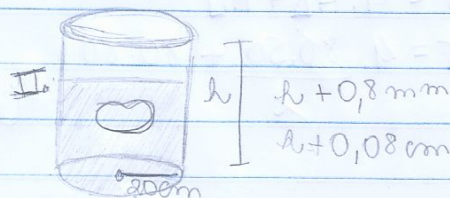
$$x'' = \frac{8-16}{2} = -4 \text{ cm}$$

NÃO CONVEN

5



→



$$V_{\text{pedra}} = V_I - V_{II}$$

$$V_p = \pi \cdot 20^2 \cdot (h+0,08) - \pi \cdot 20^2 \cdot h$$

$$V_p = \pi \cdot 400 \cdot (h+0,08 - h)$$

$$V_p = \pi \cdot 400 \cdot 0,08 = 32\pi$$

$$V_p = 32 \cdot 3,14$$

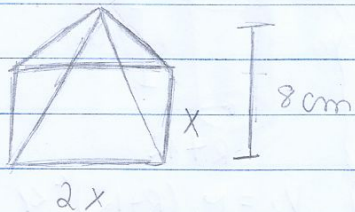
$$V_p = 100,5 \text{ cm}^3$$

Alternativa B)



→ PIRÂMIDES

1



$$V = \frac{A_B \cdot h}{3}$$

$$48 = \frac{(2x \cdot x) \cdot 8}{3}$$

$$144 = 16x^2$$

$$x^2 = \frac{144}{16}$$

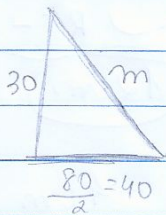
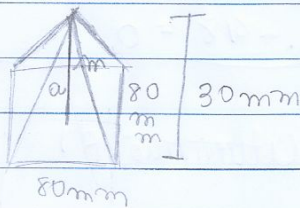
$$\rightarrow x^2 = 9$$

$$x = \sqrt{9}$$

$$x = 3$$

Alternativa C)

2



$$m^2 = 30^2 + 40^2$$

$$m^2 = 900 + 1600$$

$$m = \sqrt{2500}$$

$$m = 50\text{mm}$$

$$AT = 4 \cdot A_{\Delta} + A_B$$

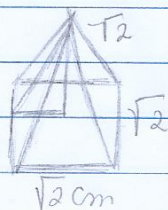
$$AT = 4 \cdot \frac{80 \cdot 50}{2} + 80 \cdot 80$$

$$AT = 8000 + 6400$$

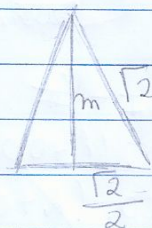
$$AT = 14400 \text{ mm}^2$$

Alternativa E)

3

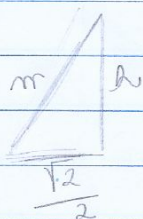


→ face lateral



$$(\sqrt{2})^2 = m^2 + \left(\frac{\sqrt{2}}{2}\right)^2$$

$$2 = m^2 + \frac{2}{4}$$



$$m^2 = h^2 + \left(\frac{\sqrt{2}}{2}\right)^2$$

$$h^2 = \frac{3}{2} - \frac{2}{4} = \frac{3}{2} - \frac{1}{2} = 1$$

$$h = \sqrt{1} = 1\text{ cm}$$

$$\rightarrow h^2 = \frac{2}{2}$$

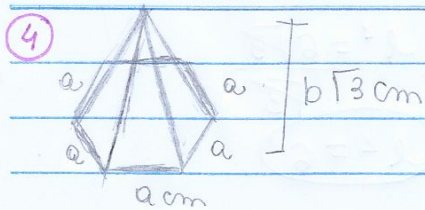
$$h = \sqrt{1}$$

$$h = 1\text{ cm}$$

$$\frac{2 - 1}{2} = m^2$$

$$m^2 = \frac{4 - 1}{2} = \frac{3}{2}$$

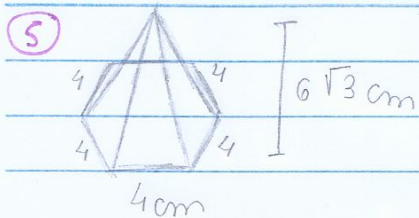
Alternativa C)



$$V = \frac{1}{3} \cdot \frac{6}{4} \cdot a^2 \sqrt{3} \cdot b \sqrt{3}$$

$$V = \frac{2}{4} \cdot a^2 \cdot b \cdot (\sqrt{3})^2$$

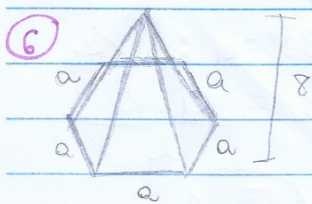
$$V = \frac{3a^2 \cdot b \text{ cm}^2}{2} \quad \text{Alternativa A)}$$



$$V = \frac{1}{3} \cdot \frac{6}{4} \cdot 4^2 \sqrt{3} \cdot 6 \sqrt{3}$$

$$V = 2 \cdot 4 \cdot 6 \cdot (\sqrt{3})^2$$

$$V = 48 \cdot 3 = 144 \text{ cm}^3 \quad \text{Alternativa D)}$$



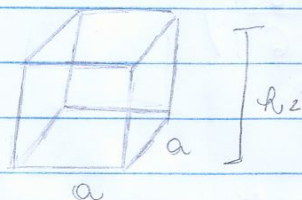
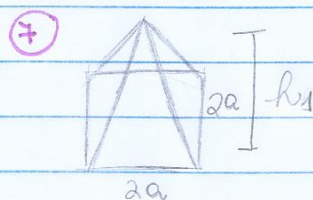
Perimetro $\hexagon = 6 \text{ cm}$
 $6a = 6$
 $a = \frac{6}{6} = 1 \text{ cm}$

$$V = \frac{1}{3} \cdot \frac{6}{4} \cdot 1^2 \sqrt{3} \cdot 8$$

$$V = 2 \cdot 2 \cdot \sqrt{3}$$

$$V = 4\sqrt{3} \text{ cm}^3$$

Alternativa A)



* $V_{\text{pirâmide}} = V_{\text{prisma}}$

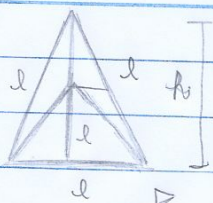
$$\frac{1}{3} \cdot 2a \cdot 2a \cdot h_1 = a \cdot a \cdot h_2$$

$$\frac{h_1}{h_2} = \frac{a^2 \cdot 3}{4a^2} = \frac{3}{4}$$

Alternativa

A)

8



$$AT = 6\sqrt{3}$$

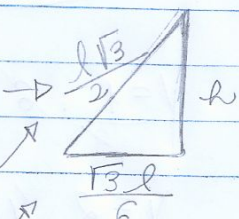
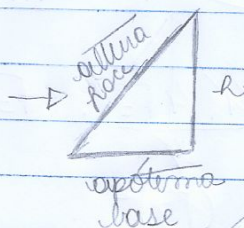
$$4 \cdot A_{\Delta} = 6\sqrt{3}$$

$$4 \cdot \frac{l^2 \sqrt{3}}{4} = 6\sqrt{3}$$

$$l^2 = 6\sqrt{3}$$

$$l^2 = 6$$

Triângulo equilátero

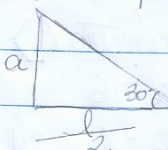
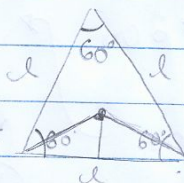


$$* h_{\Delta} = \frac{l\sqrt{3}}{2}$$

$$* a_{\Delta} = \frac{\sqrt{3}l}{6}$$

(triângulo equilátero)

cálculo do apótema =



$$\begin{aligned} \operatorname{tg} 30^\circ &= a : l/2 \\ \frac{\sqrt{3}}{3} &= \frac{a \cdot 2}{l} \end{aligned}$$

$$a = \frac{\sqrt{3} \cdot l}{6}$$

$$\left(\frac{l\sqrt{3}}{2} \right)^2 = h^2 + \left(\frac{\sqrt{3}l}{6} \right)^2$$

$$h^2 = \frac{3l^2}{4} - \frac{3l^2}{36}$$

$$h^2 = \frac{27l^2}{36} - \frac{3l^2}{36}$$

$$h^2 = \frac{24l^2}{36}$$

$$\rightarrow h = \sqrt{\frac{36}{9}} = \frac{6}{3} = 20m$$

Alternativa A)