

Cohen's Medians ($L[1, \dots, n]$)

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$$\frac{n}{2} \log \frac{n}{2}$$

Cohen's Medians ($L[1, \dots, n]$)

$$\sqrt{n} \cdot n^{\frac{1}{2}} \log n^{\frac{1}{2}} = \frac{1}{2} \sqrt{n} \cdot \log n \in O(n)$$

Cohen's Medians ($L[1, \dots, n]$)

$$\sqrt{n} \cdot n^{\frac{1}{2}} \log n^{\frac{1}{2}} = \frac{n}{2} \log \frac{n}{2}$$

$$= \frac{1}{2}\sqrt{n} \cdot \log n \in O(n)$$

Cohen-Medians ($L[1, \dots, n]$) $\lceil n^{\frac{3}{4}} \rceil$

$$\sqrt{n} \cdot n^{\frac{1}{2}} \log n^{\frac{1}{2}} = \frac{n}{2} \log \frac{n}{2}$$

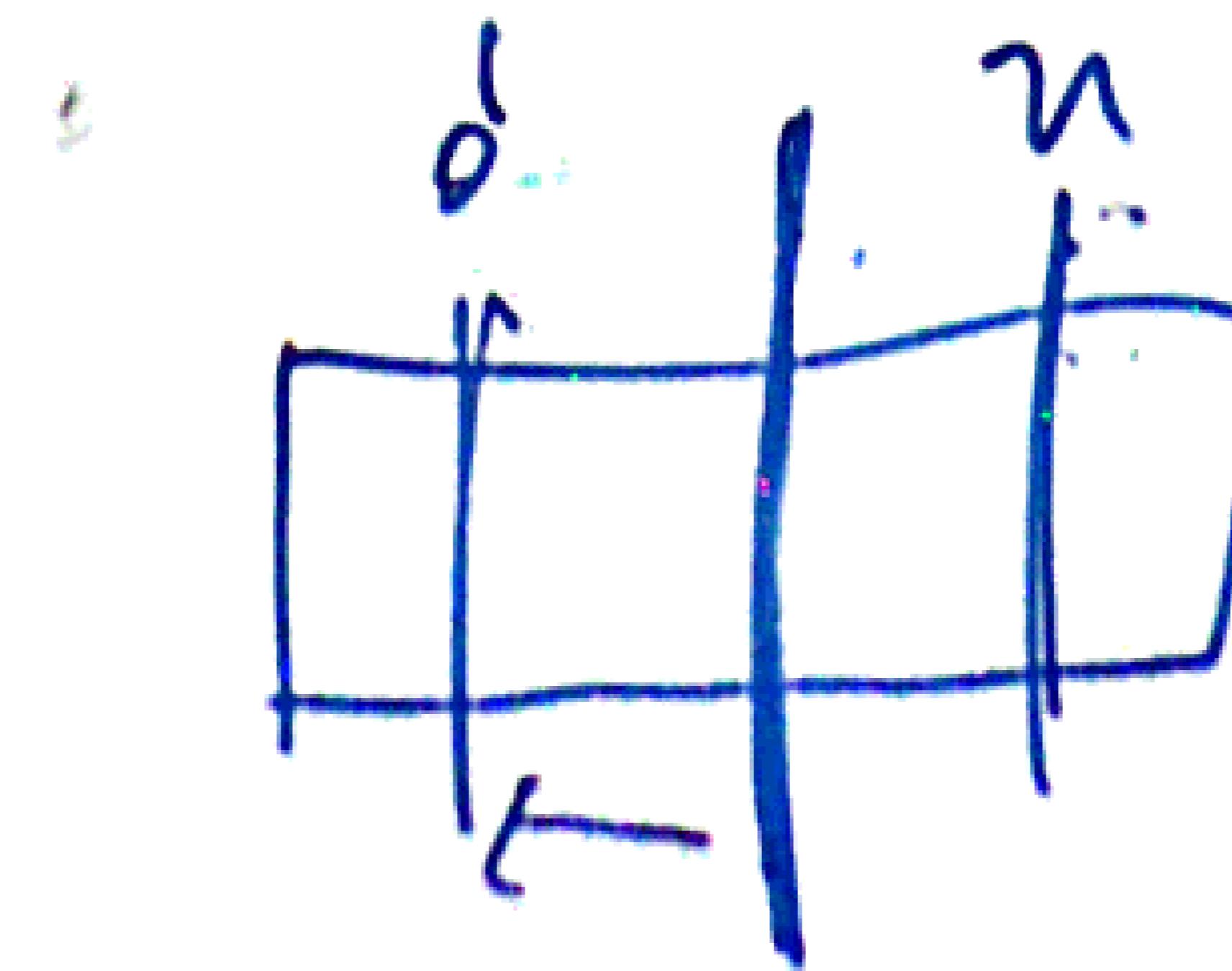
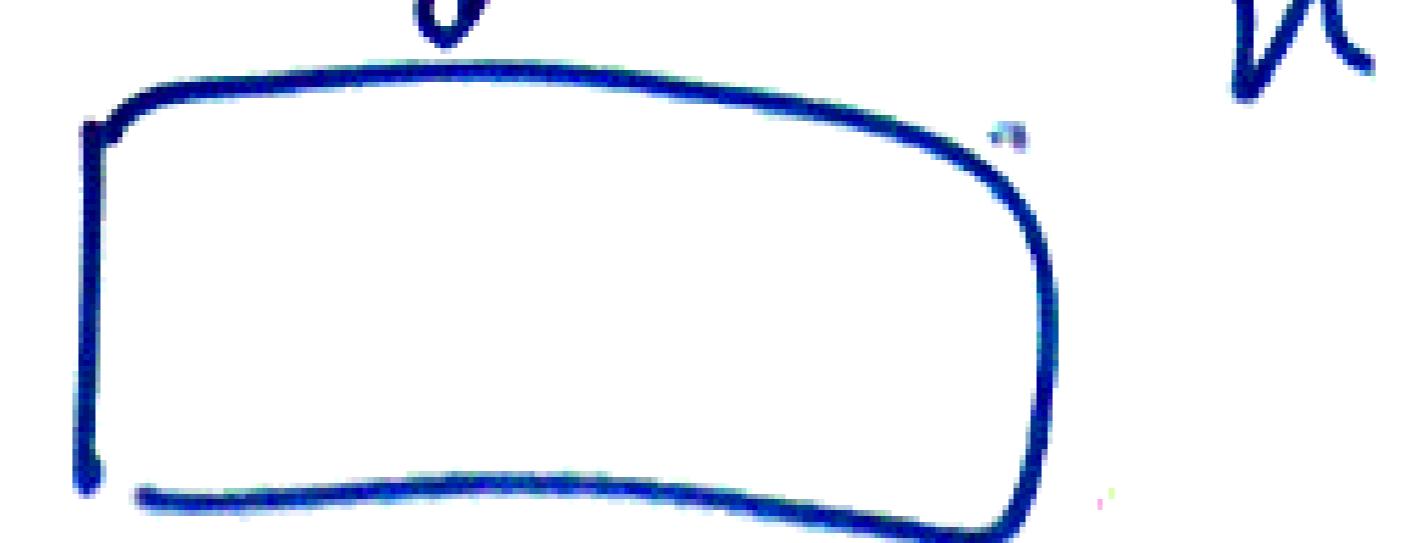
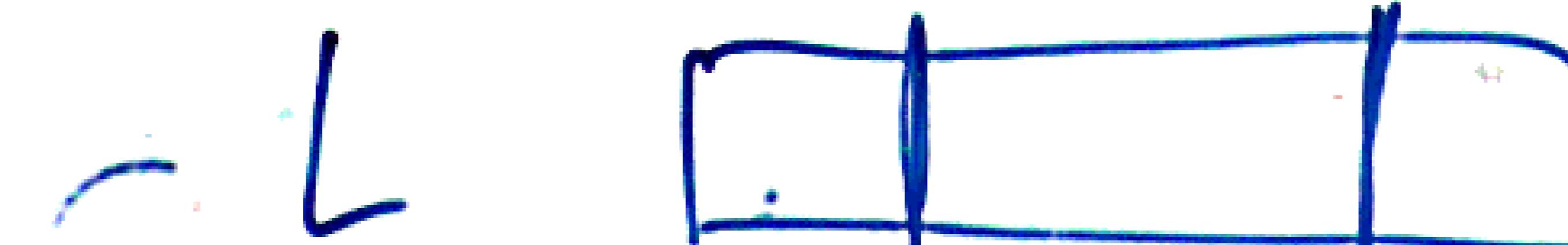
$$= \frac{1}{2}\sqrt{n} \cdot \log n \in O(n)$$

Cohen's Medians ($L[1, \dots, n]$)

[37]

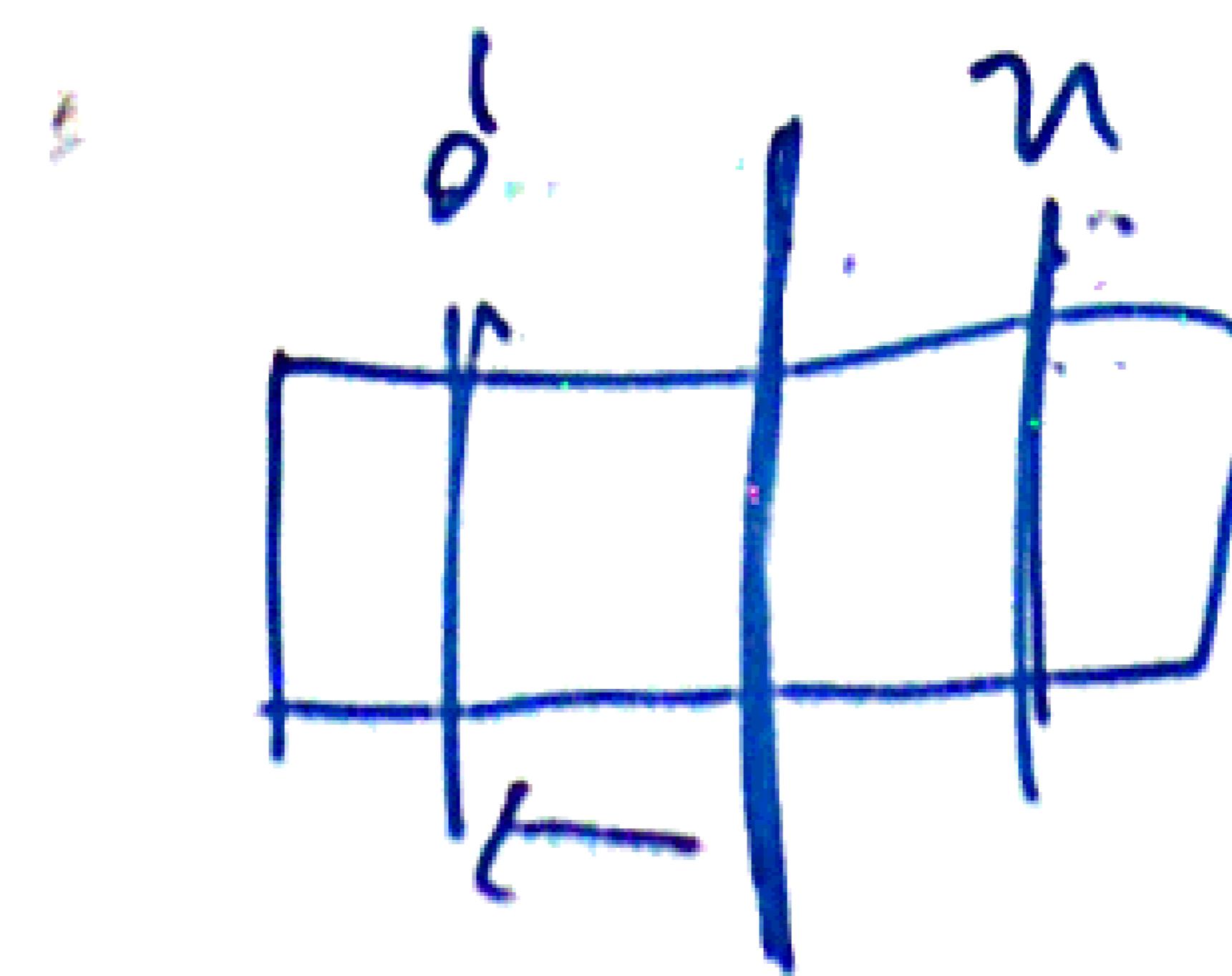
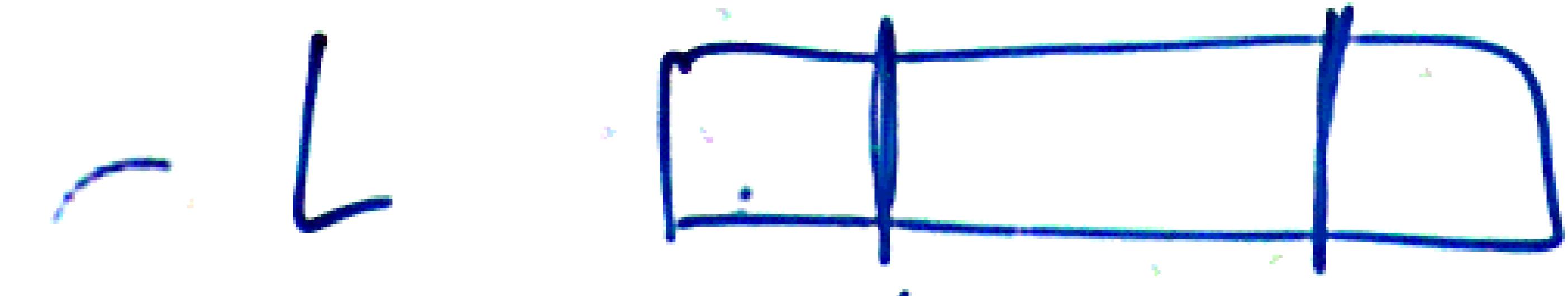
Cohen's Medians ($L[1, \dots, n]$)

[3]

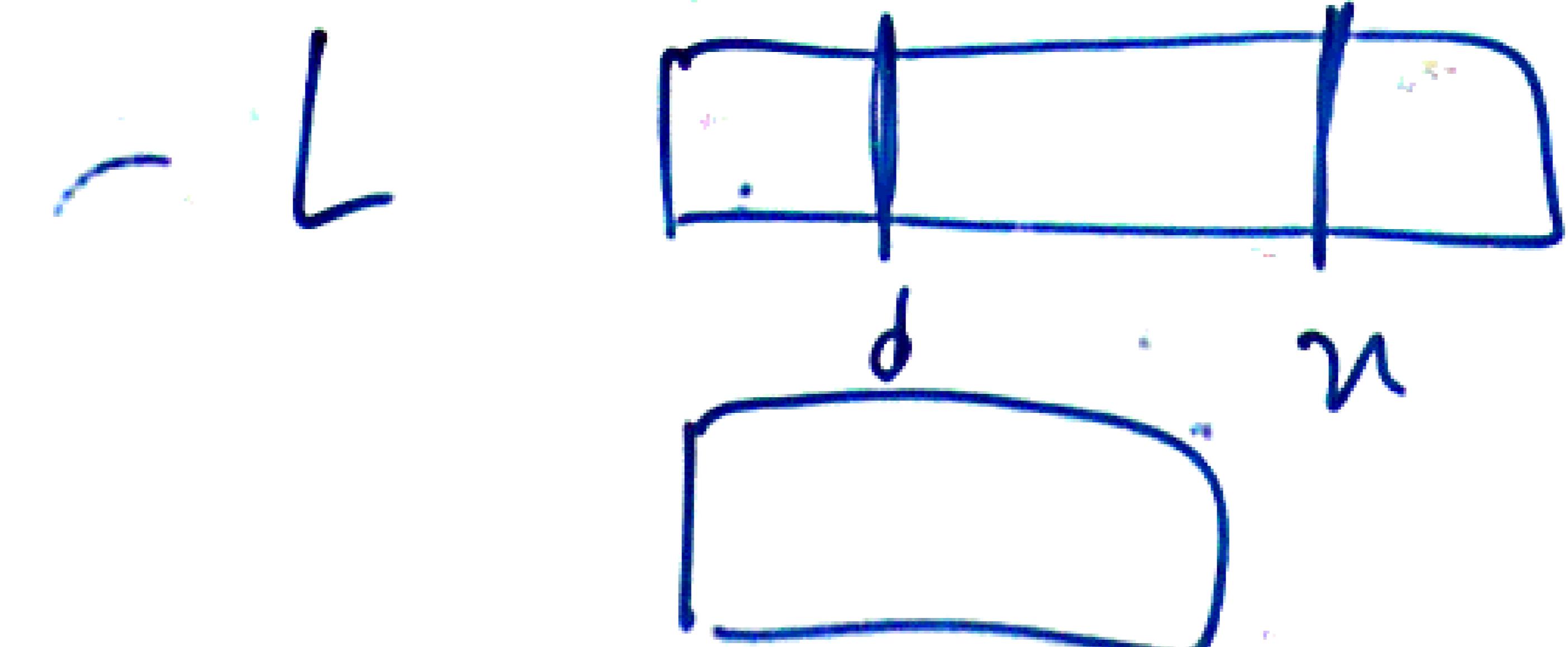


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Cohen's Medians ($L[1, \dots, n]$)

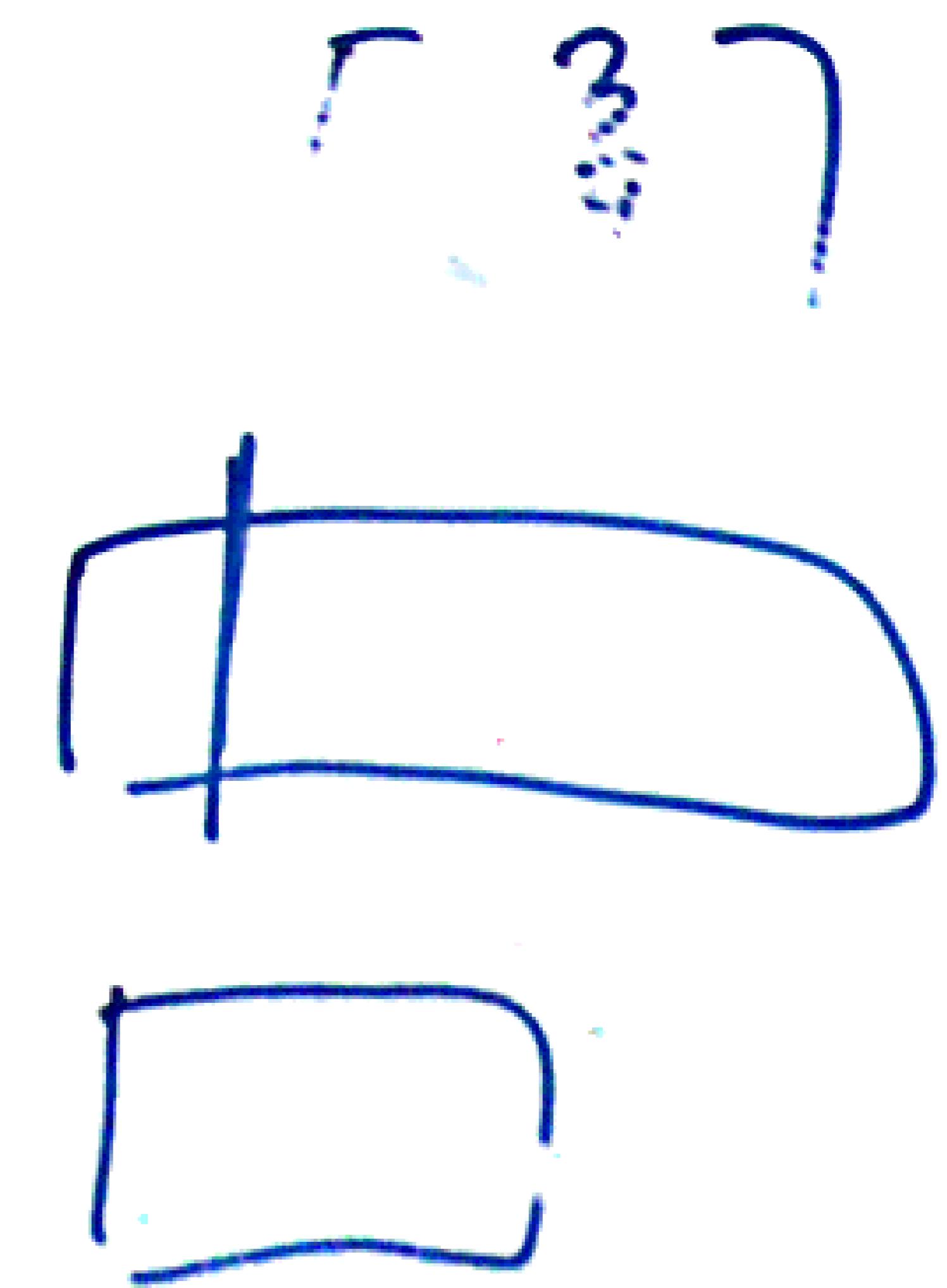
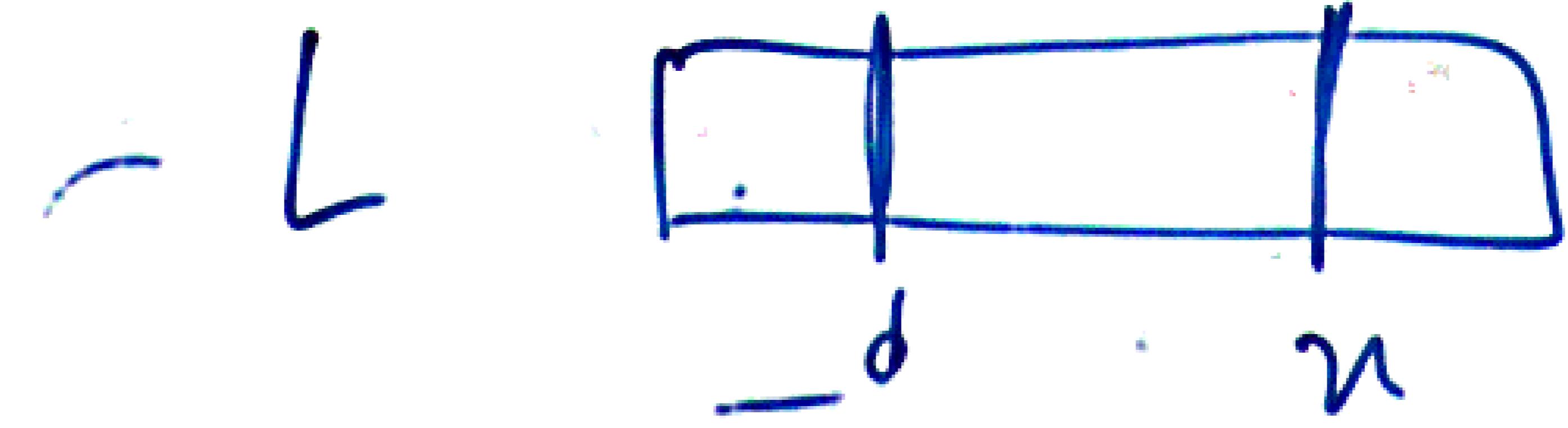


Cohen's Medians ($L[1, \dots, n]$)

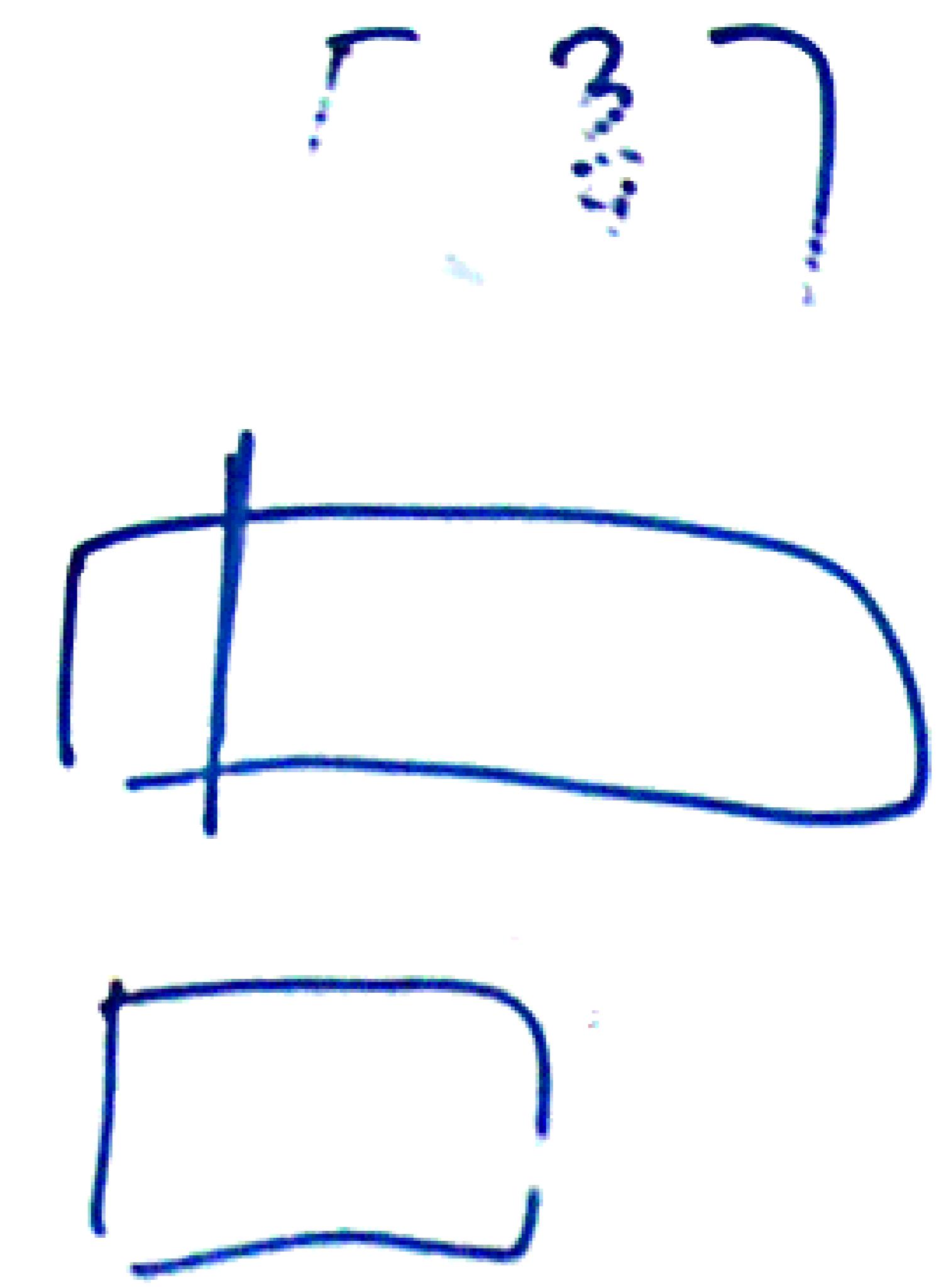
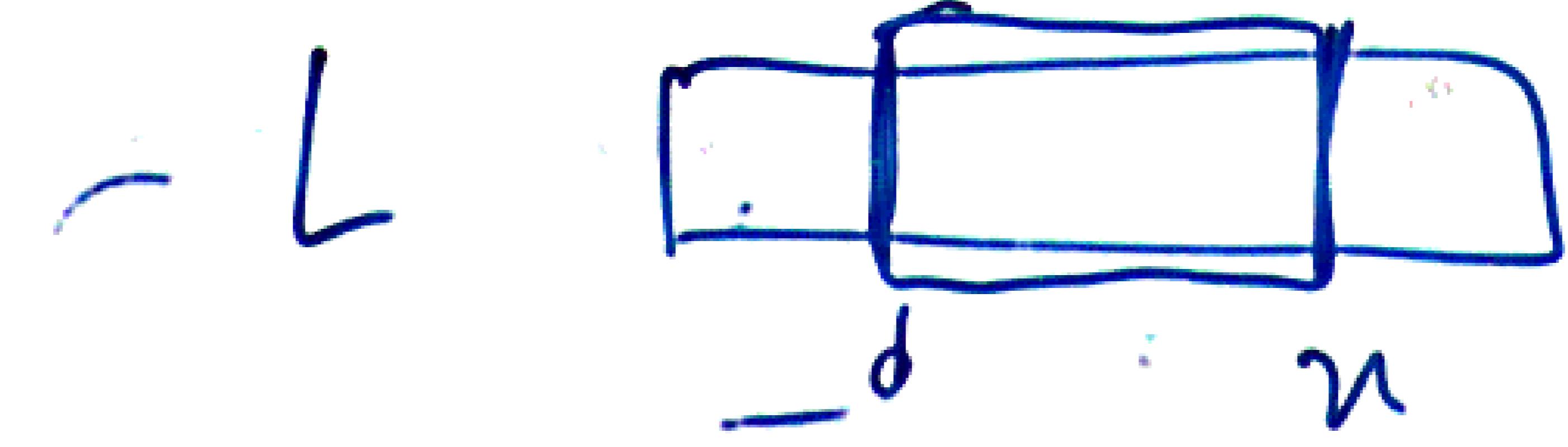


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Cohen's Medians ($L[1, \dots, n]$)

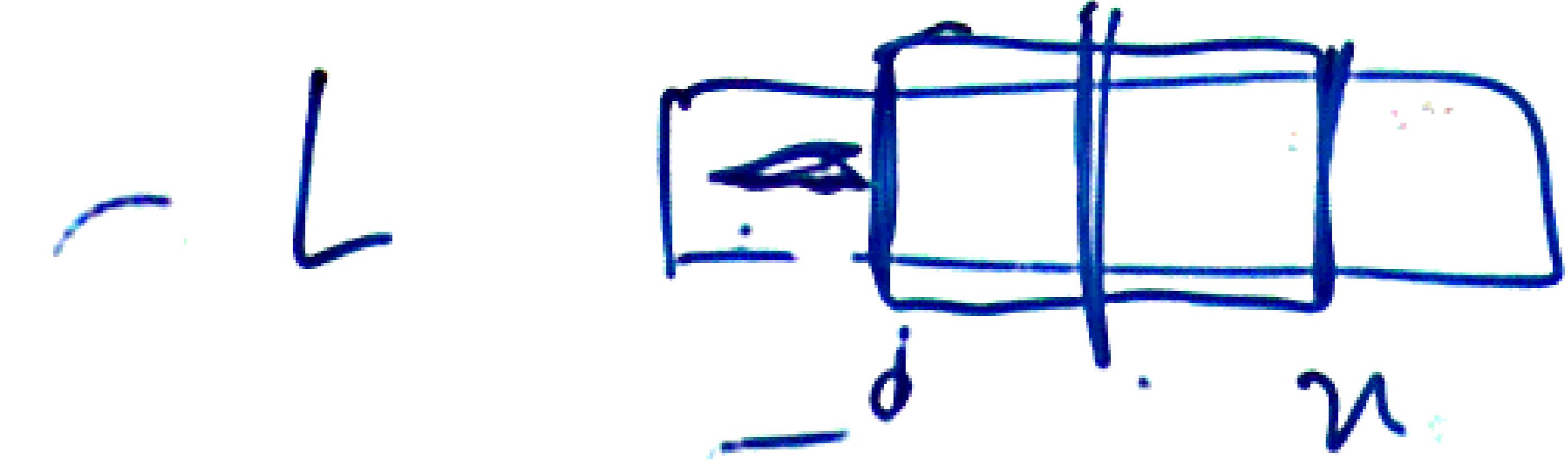


Cohen's Medians ($L[1, \dots, n]$)

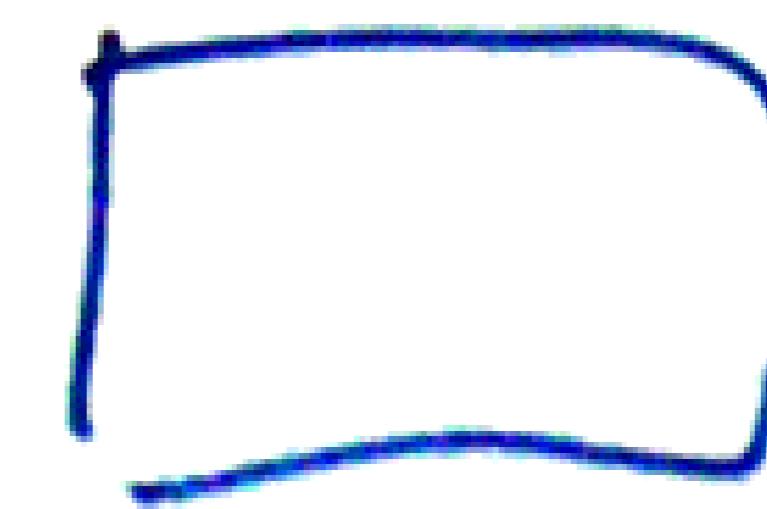


Cohen's Medians ($L[1, \dots, n]$)

$\sim L$



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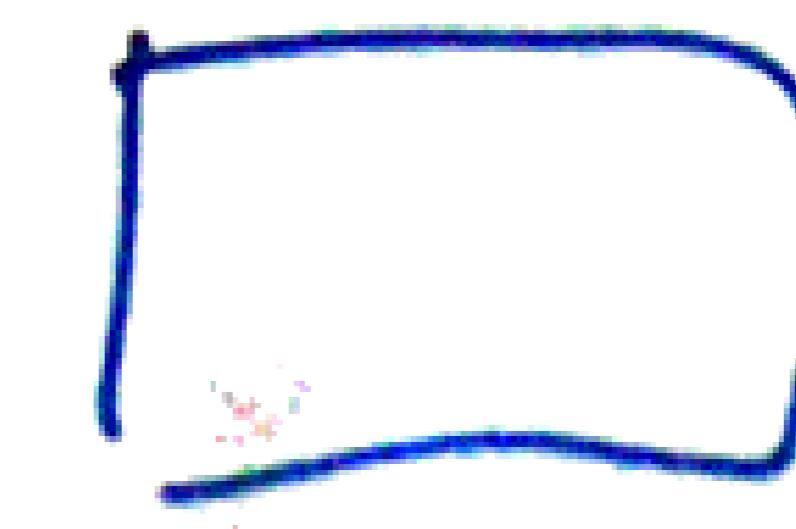
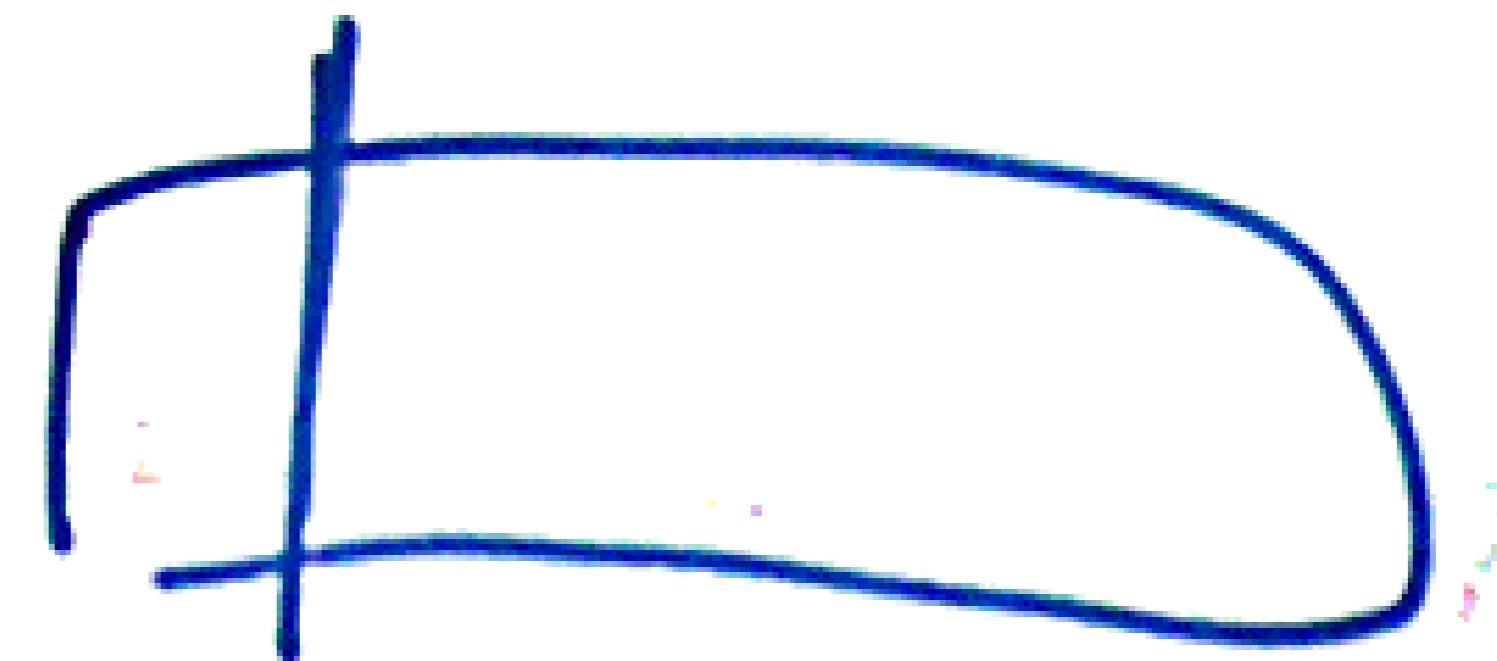


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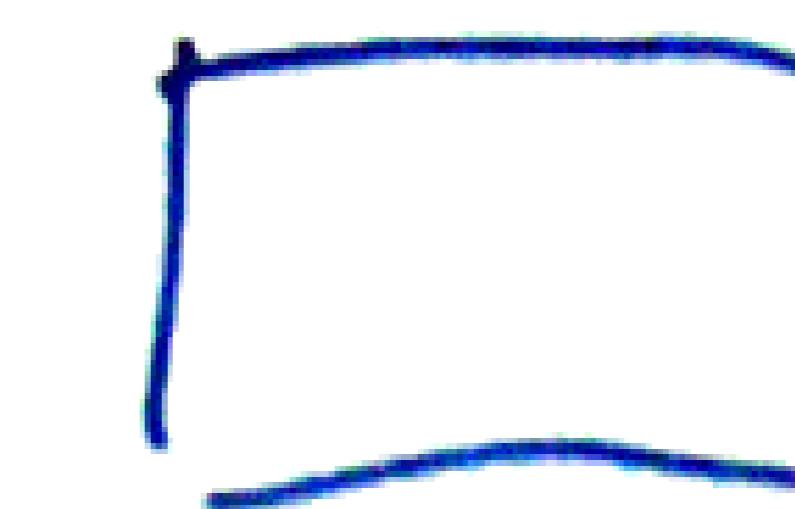
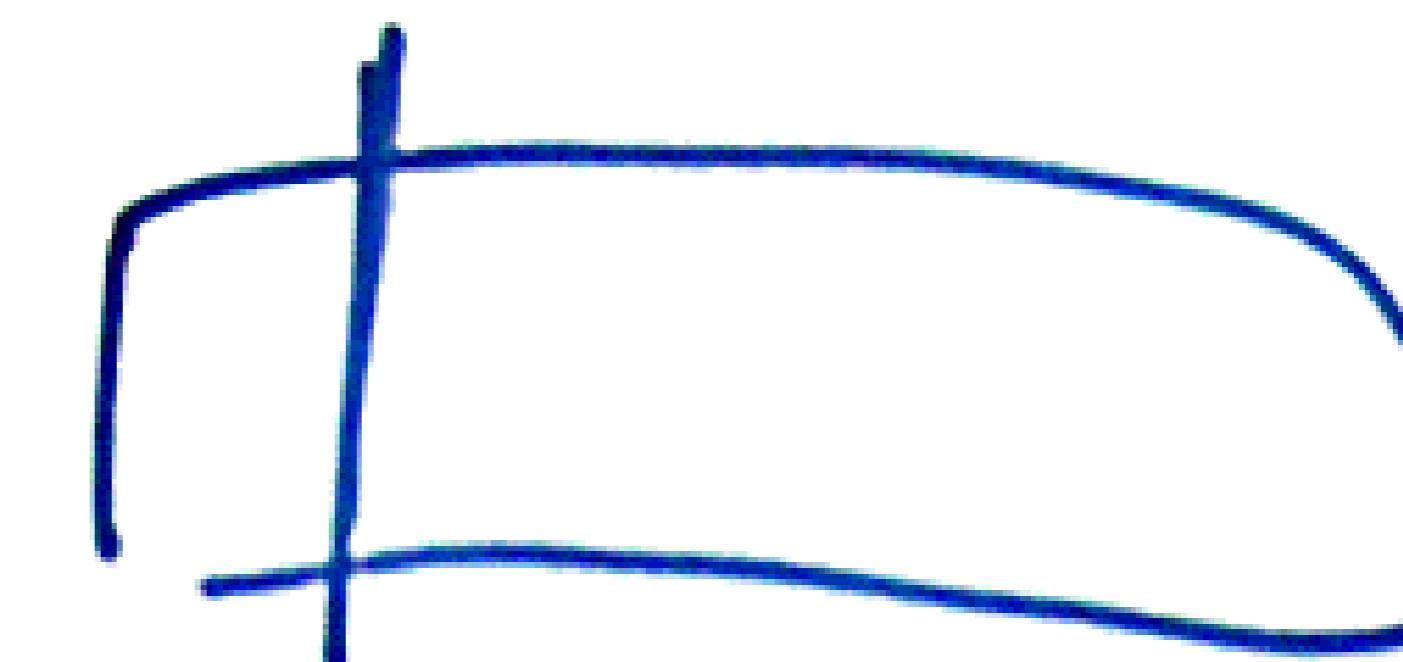


Cohen's Medians ($L[1, \dots, n]$)

$\sim L$

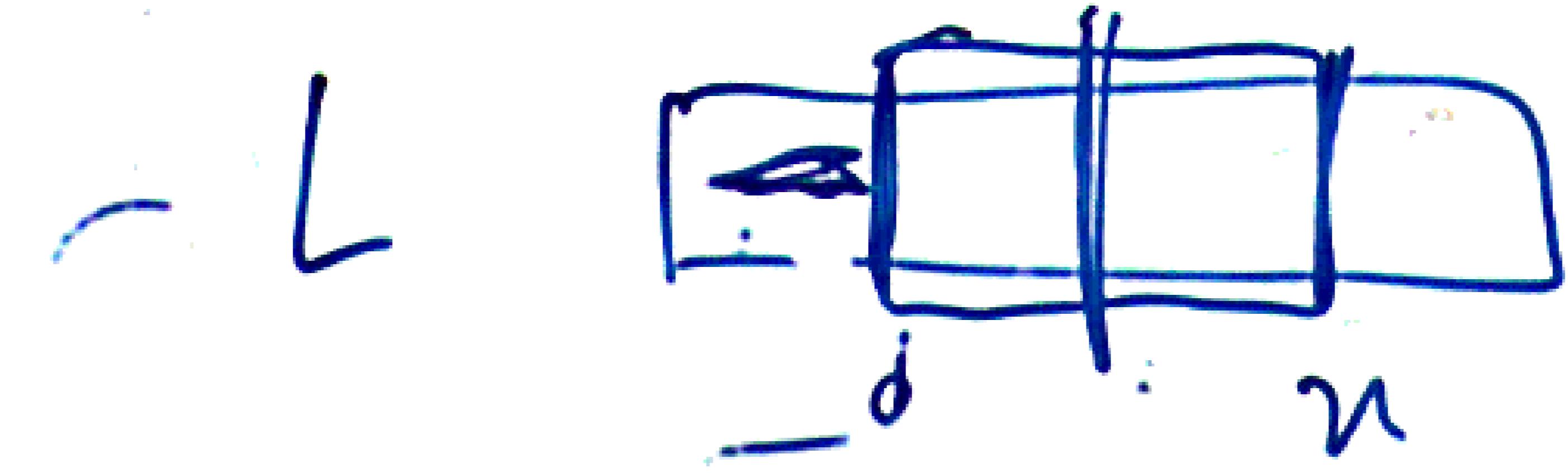


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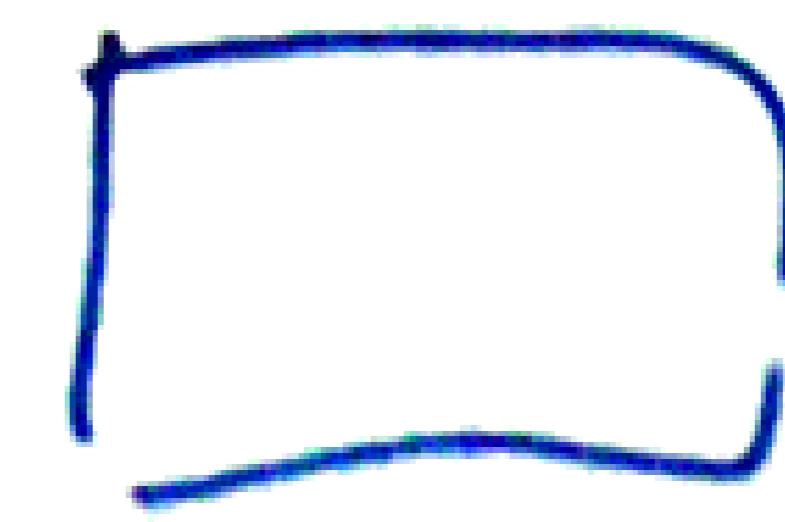
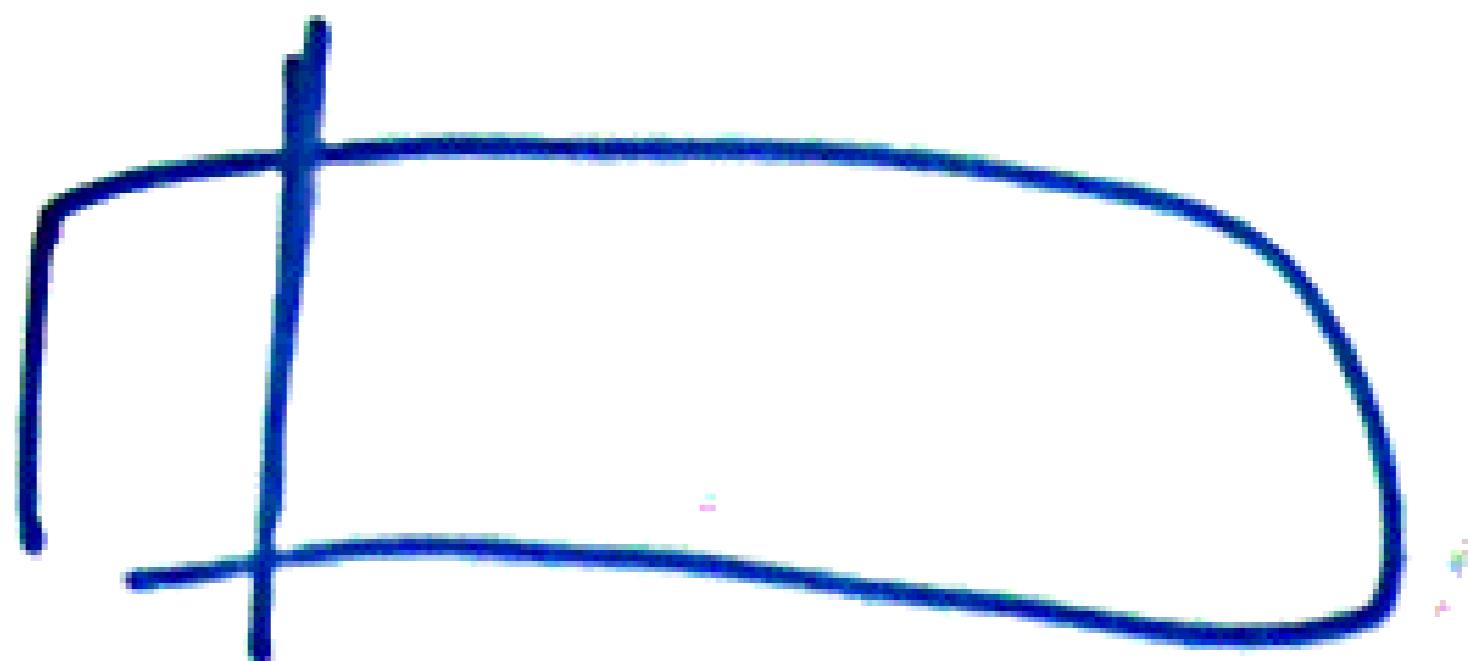


Cohen's Medians ($L[1, \dots, n]$)

$\sim L$



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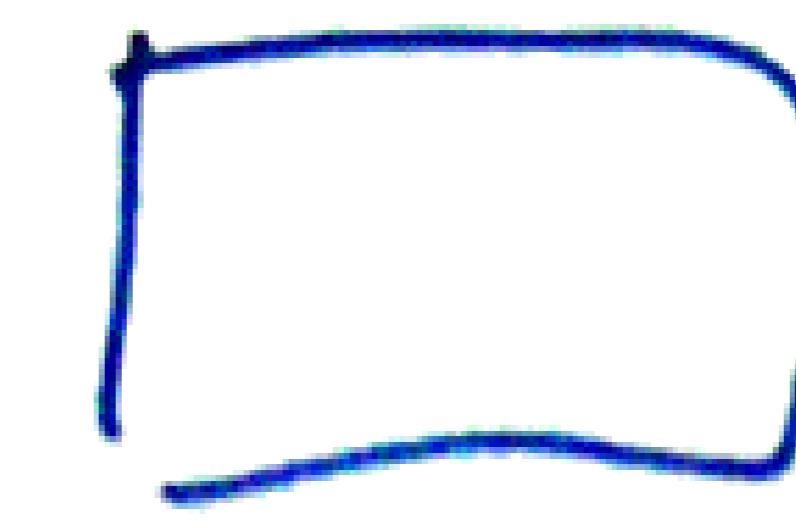
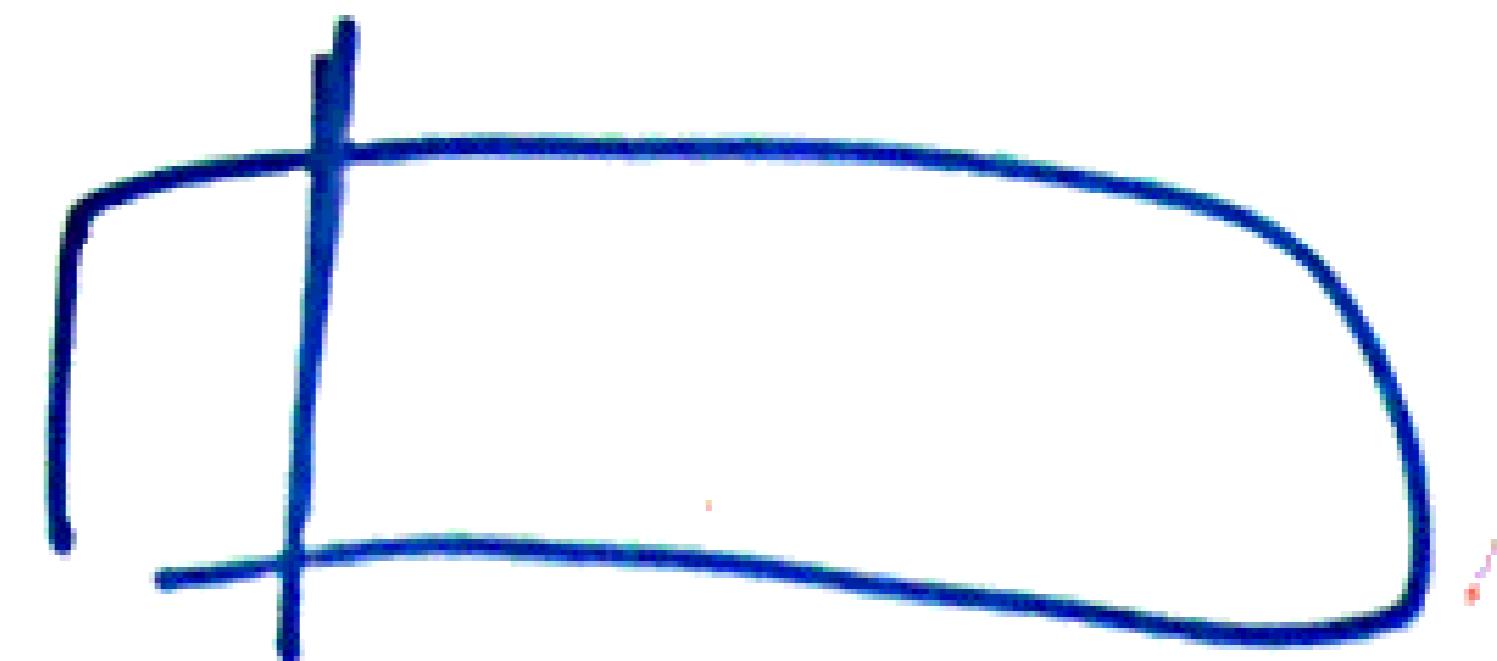


Cohen's Medians ($L[1, \dots, n]$)

- L



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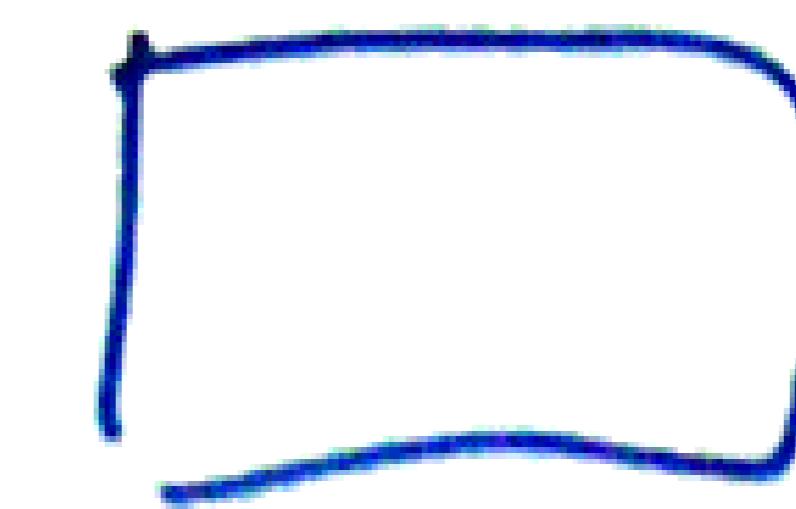
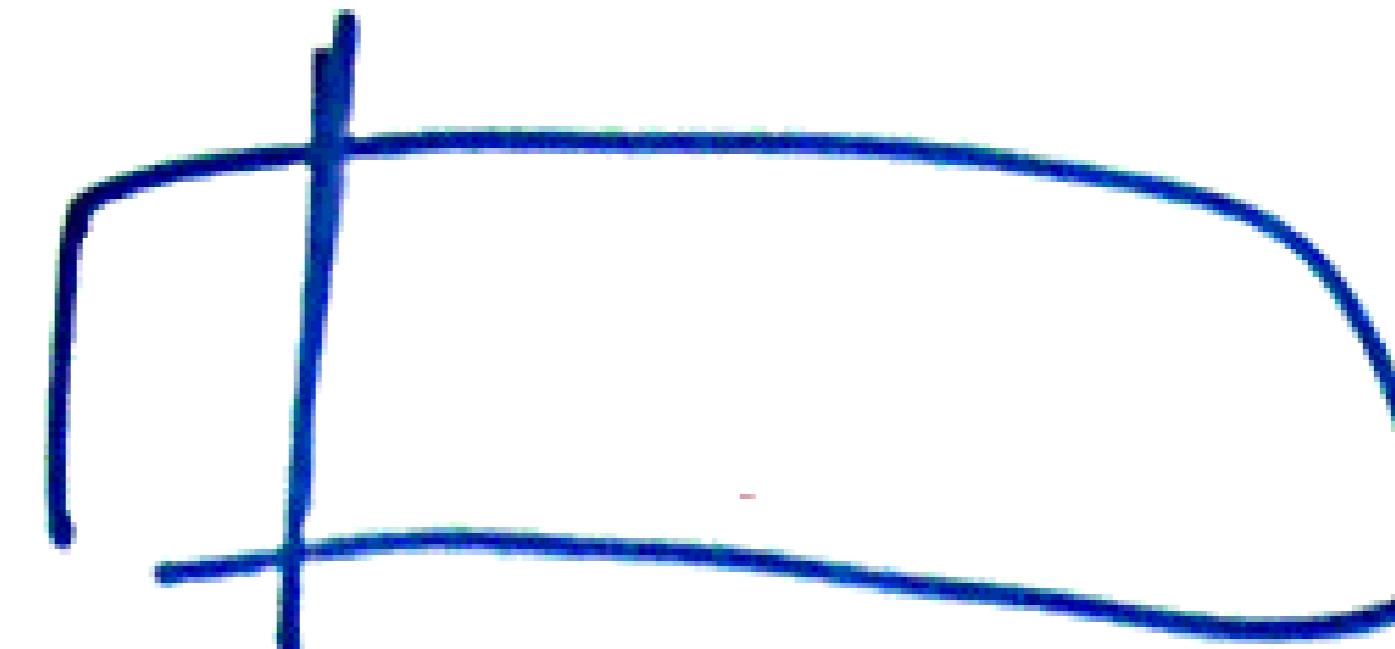


Cohen's Medians ($L[1, \dots, n]$)

$\sim L$



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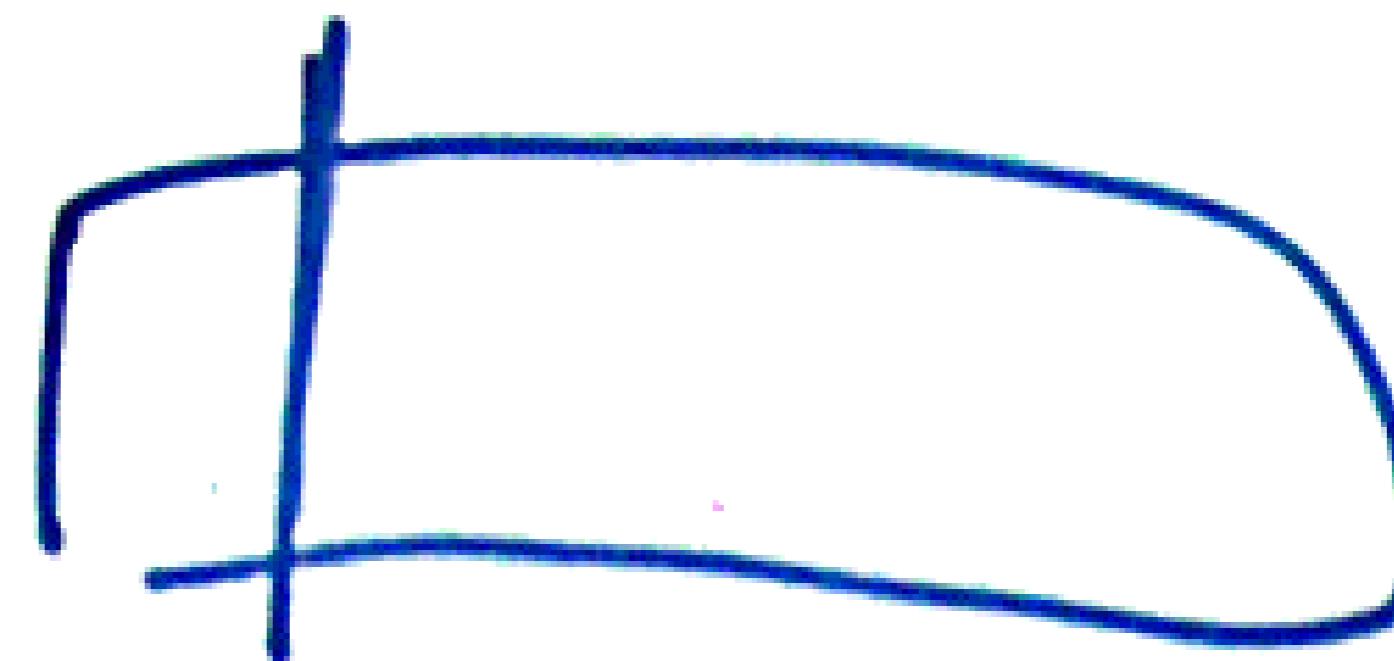


Cohen's Medians ($L[1, \dots, n]$)

$\sim L$

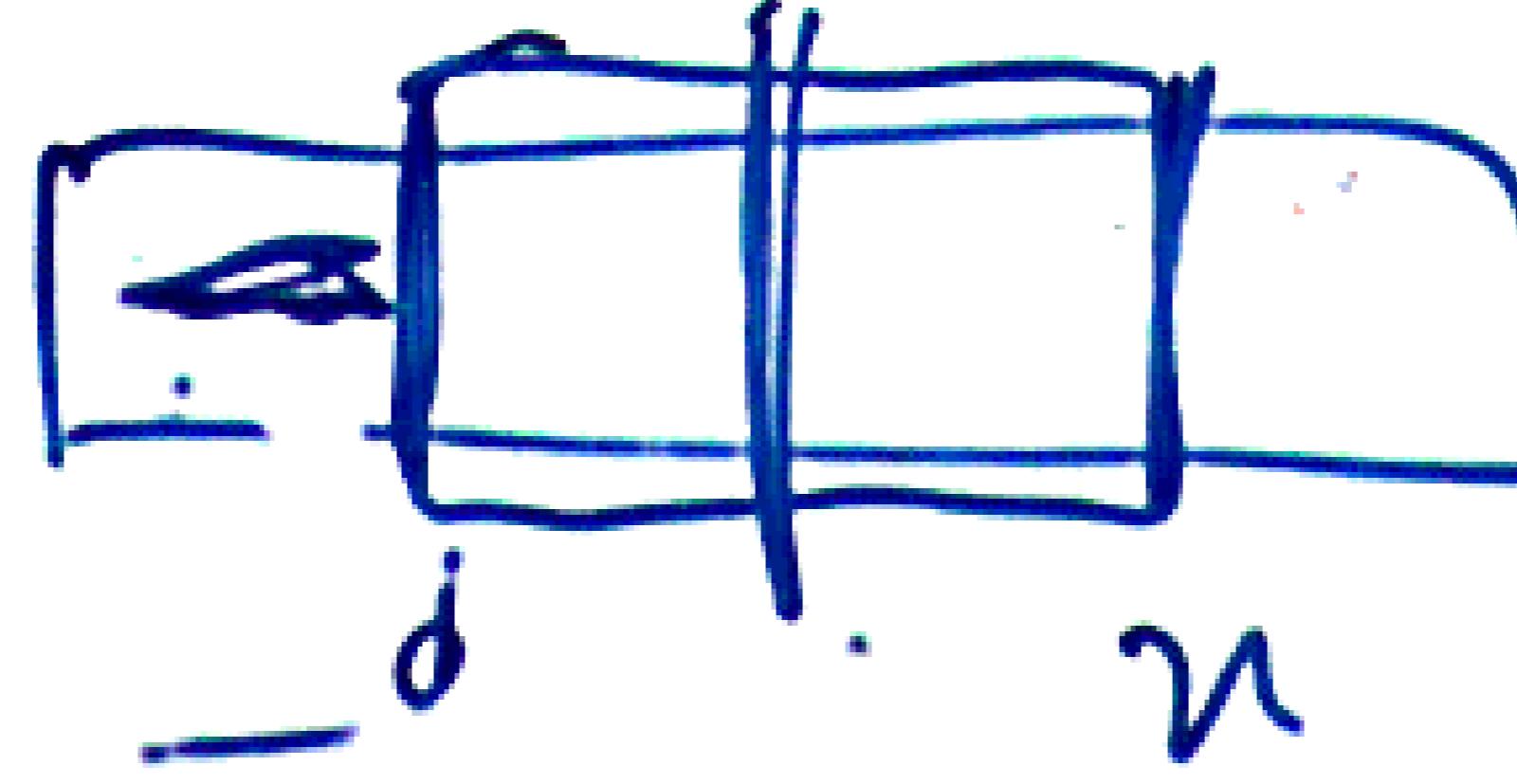


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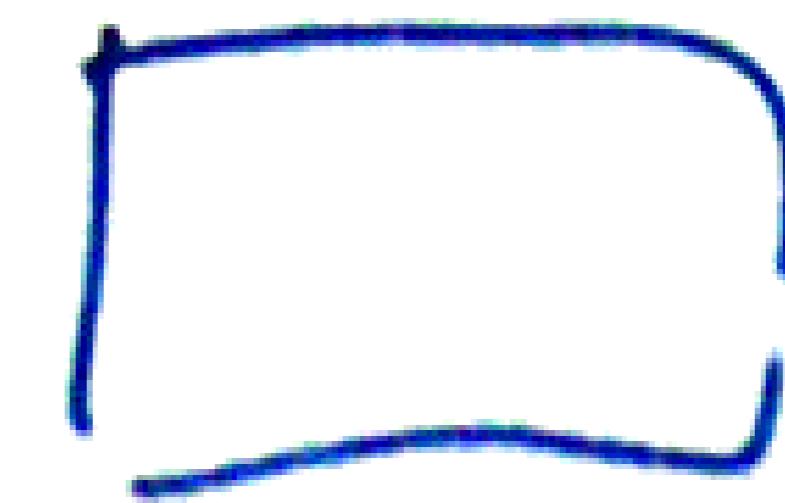
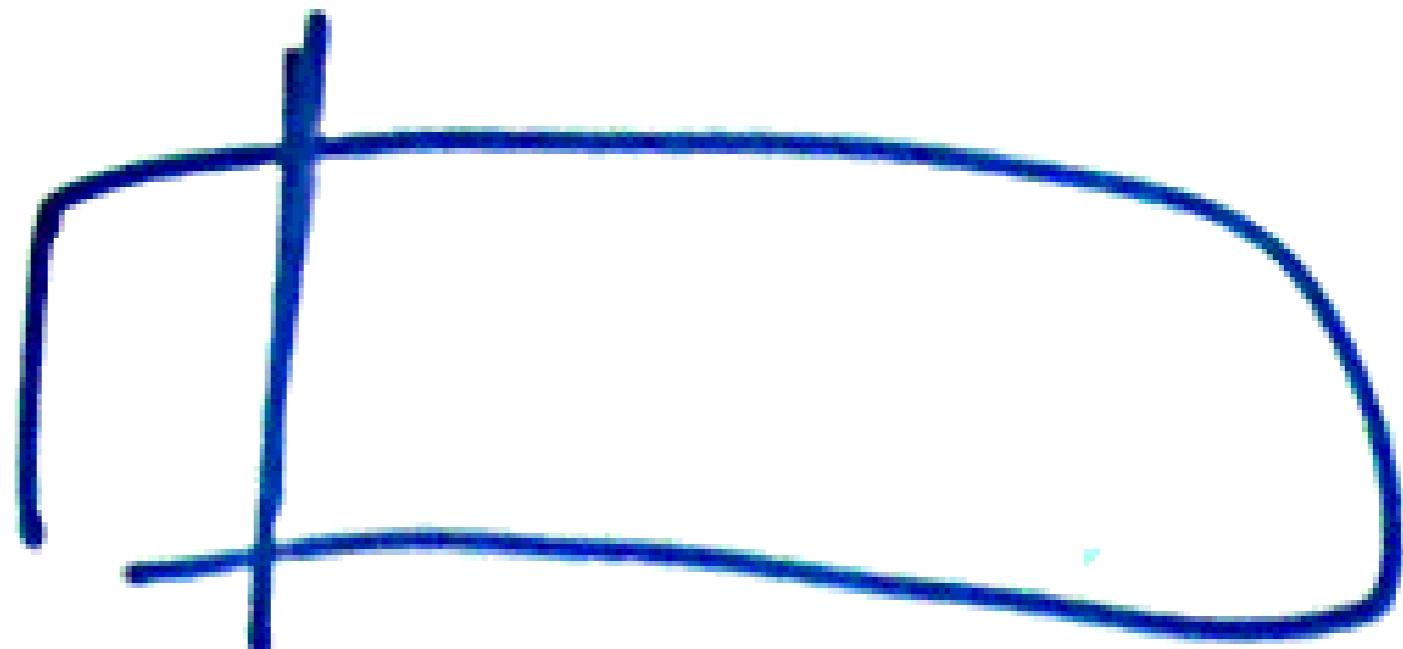


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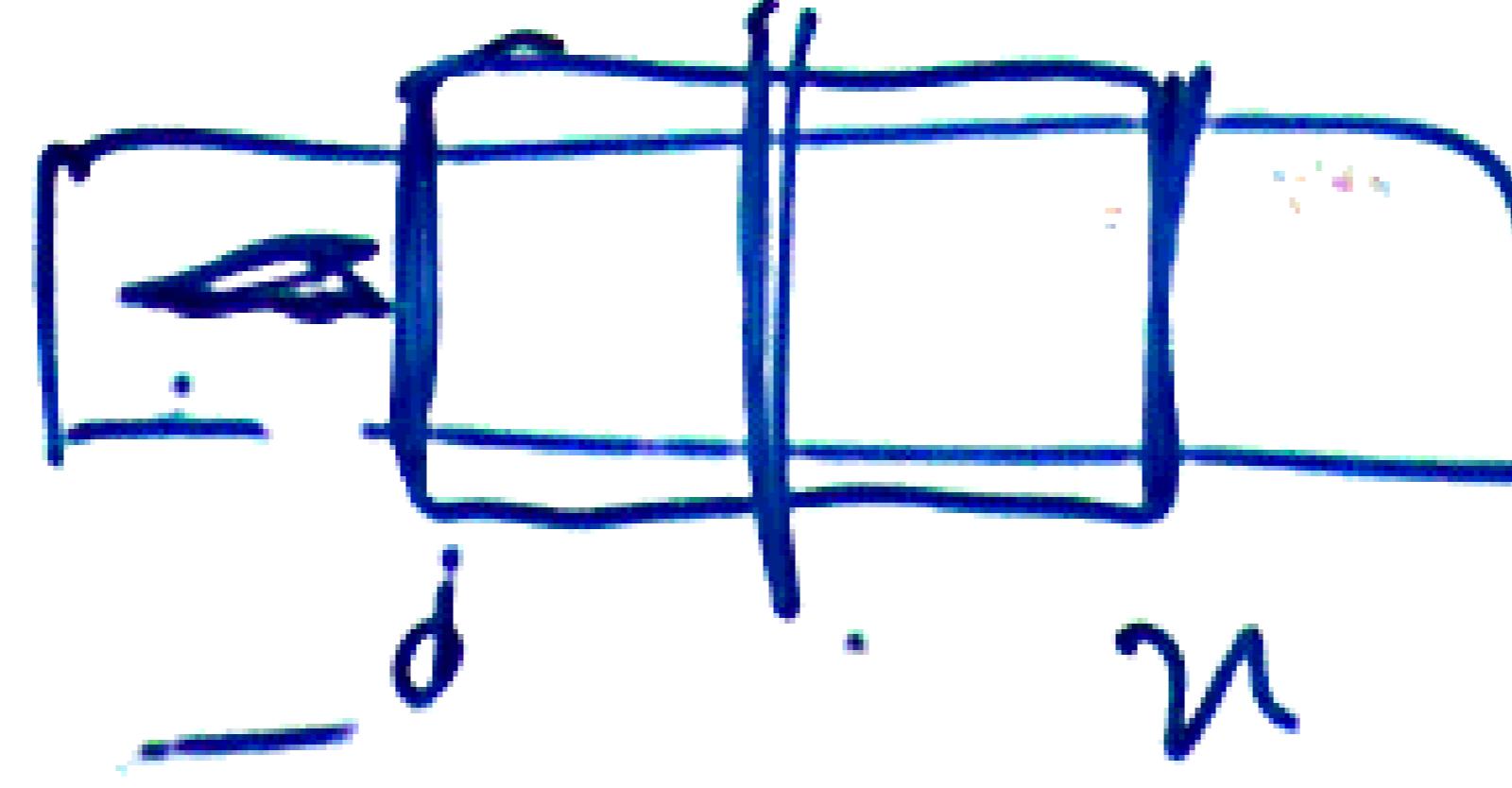


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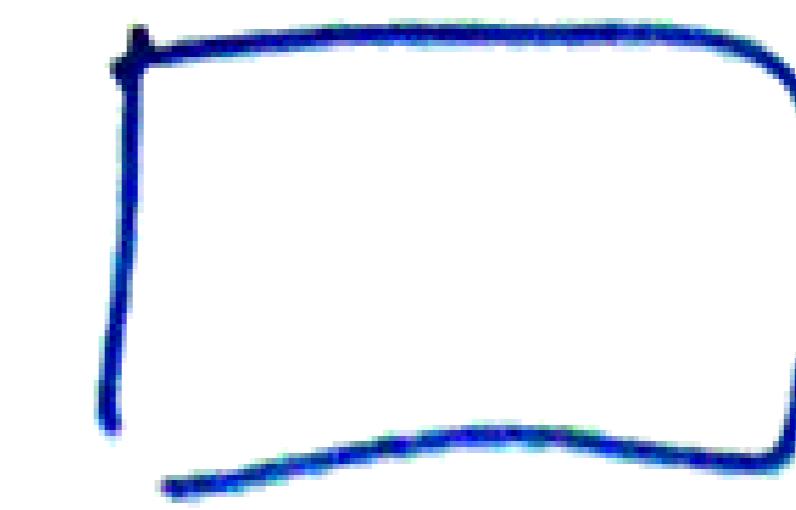
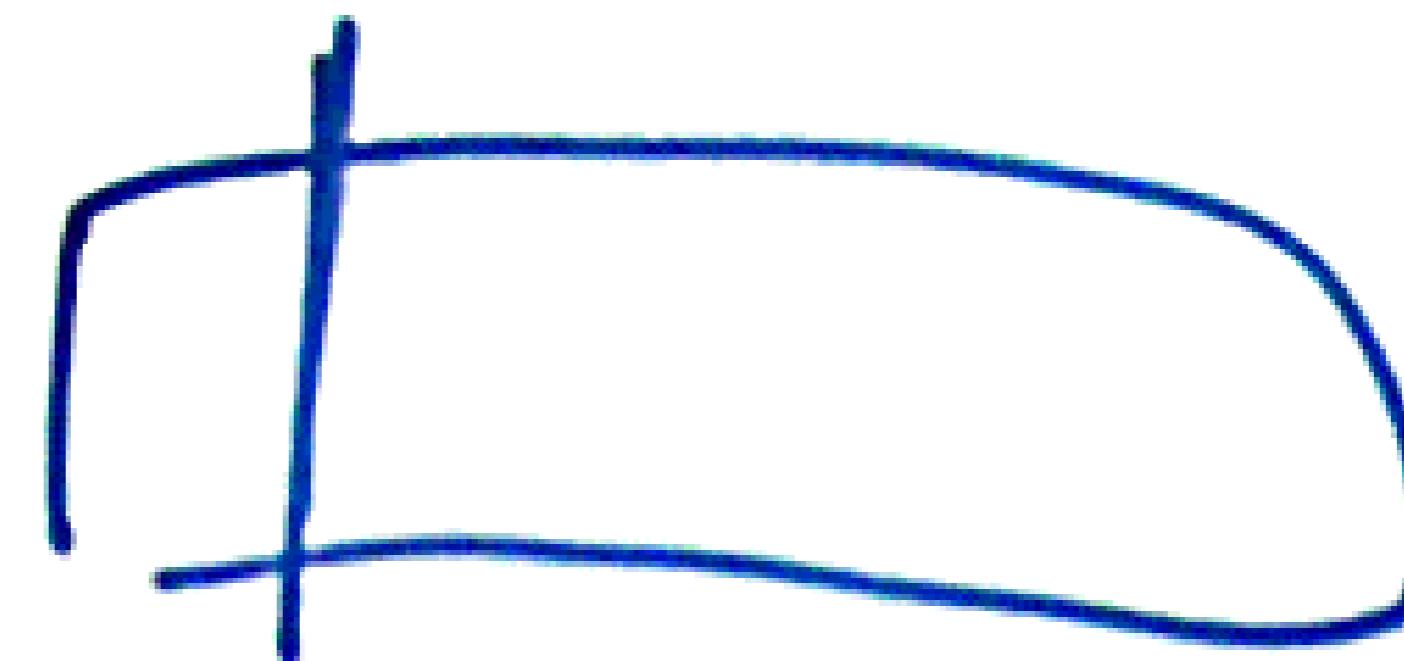


Cohen's Medians ($L[1, \dots, n]$)

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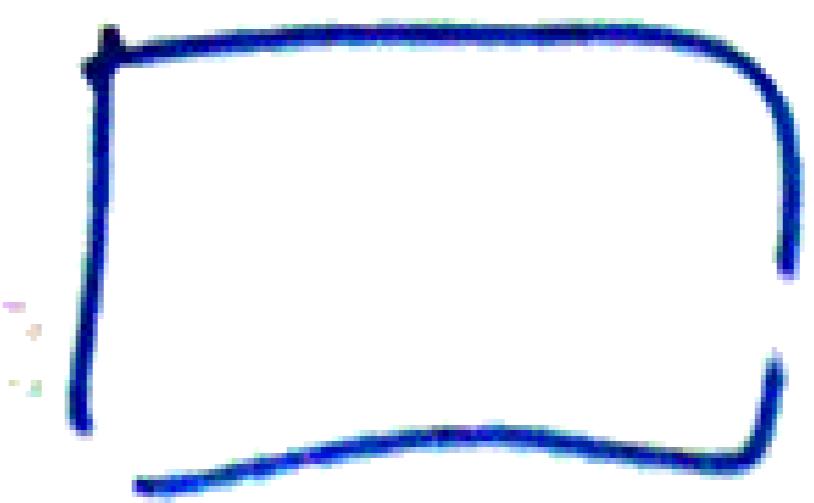
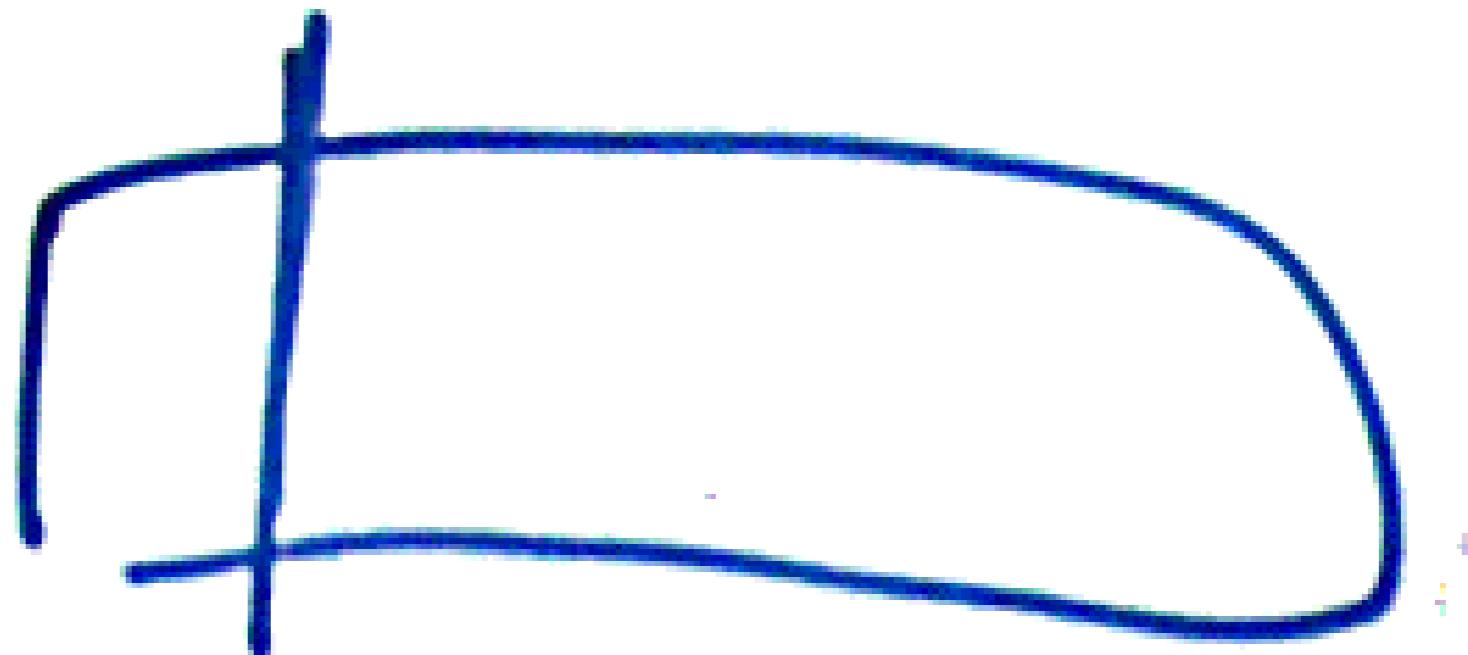
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Cohen's Medians ($L[1, \dots, n]$)

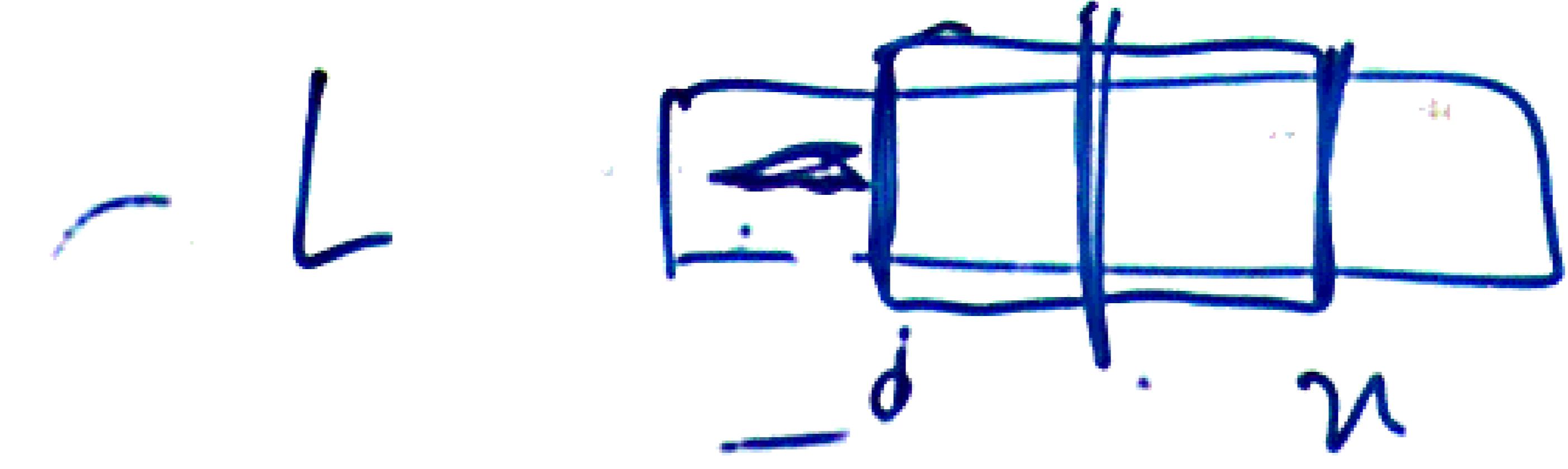


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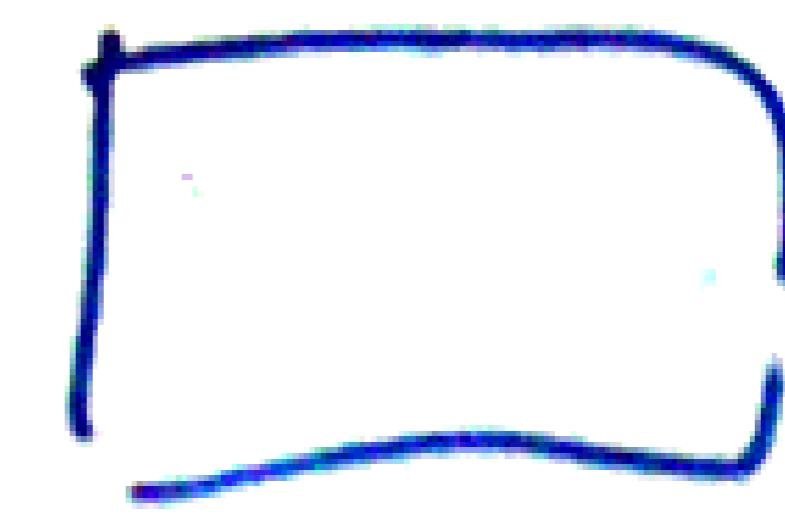


Cohen's Medians ($L[1, \dots, n]$)

- L

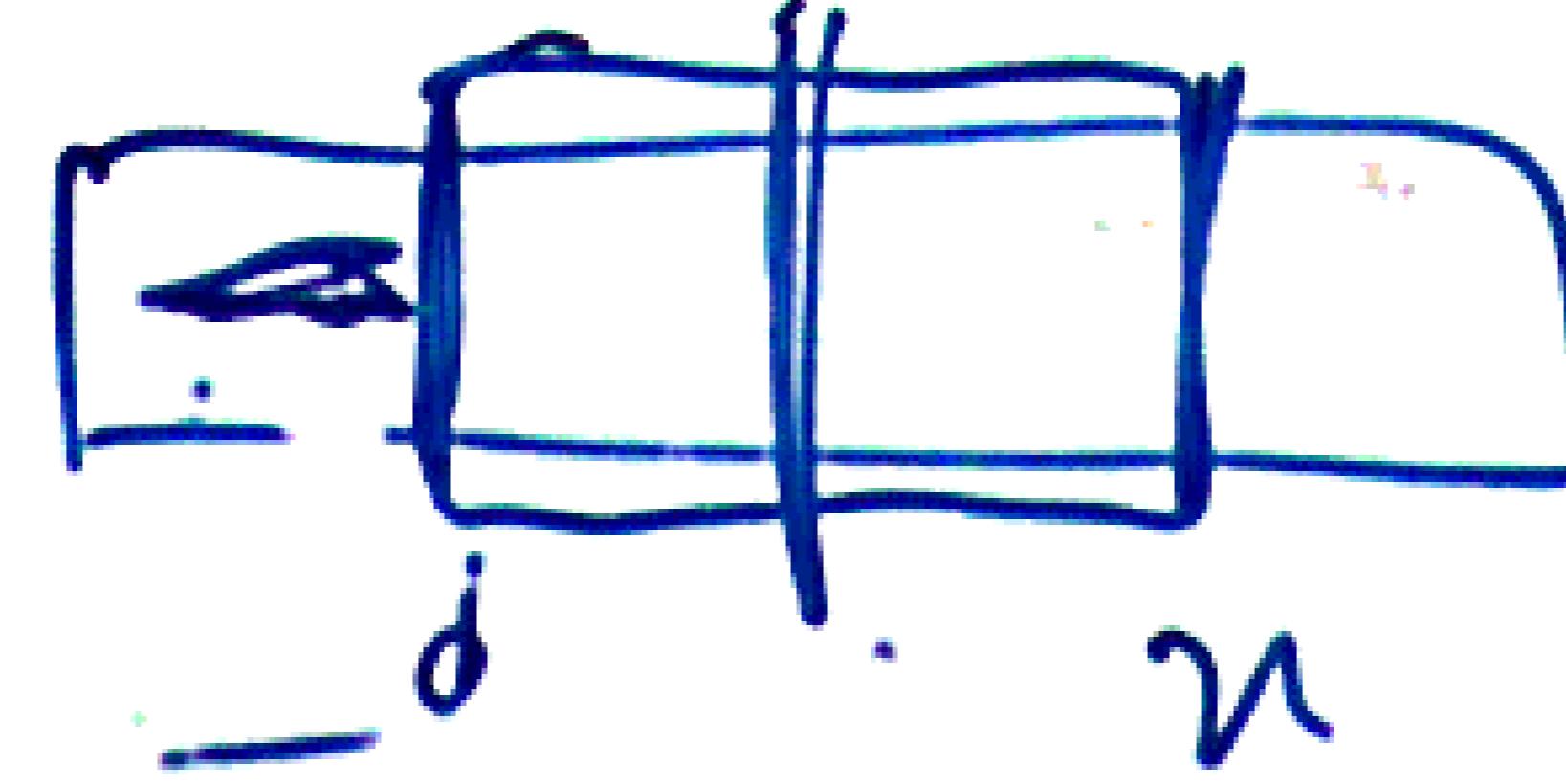


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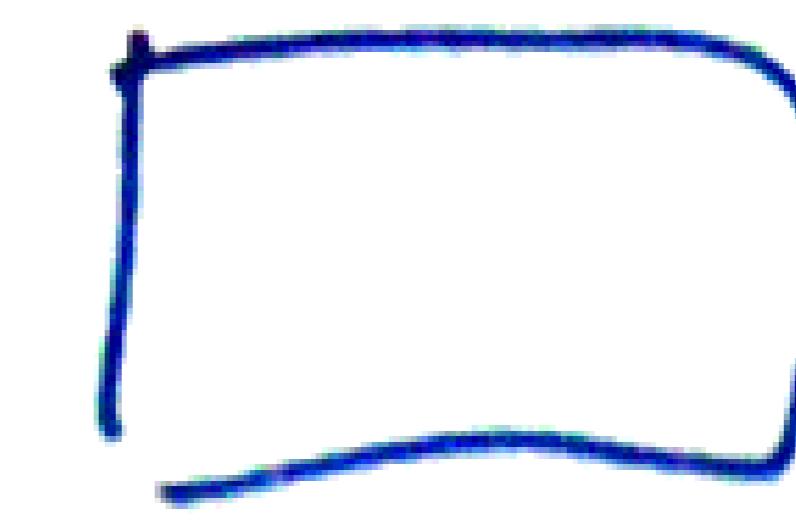
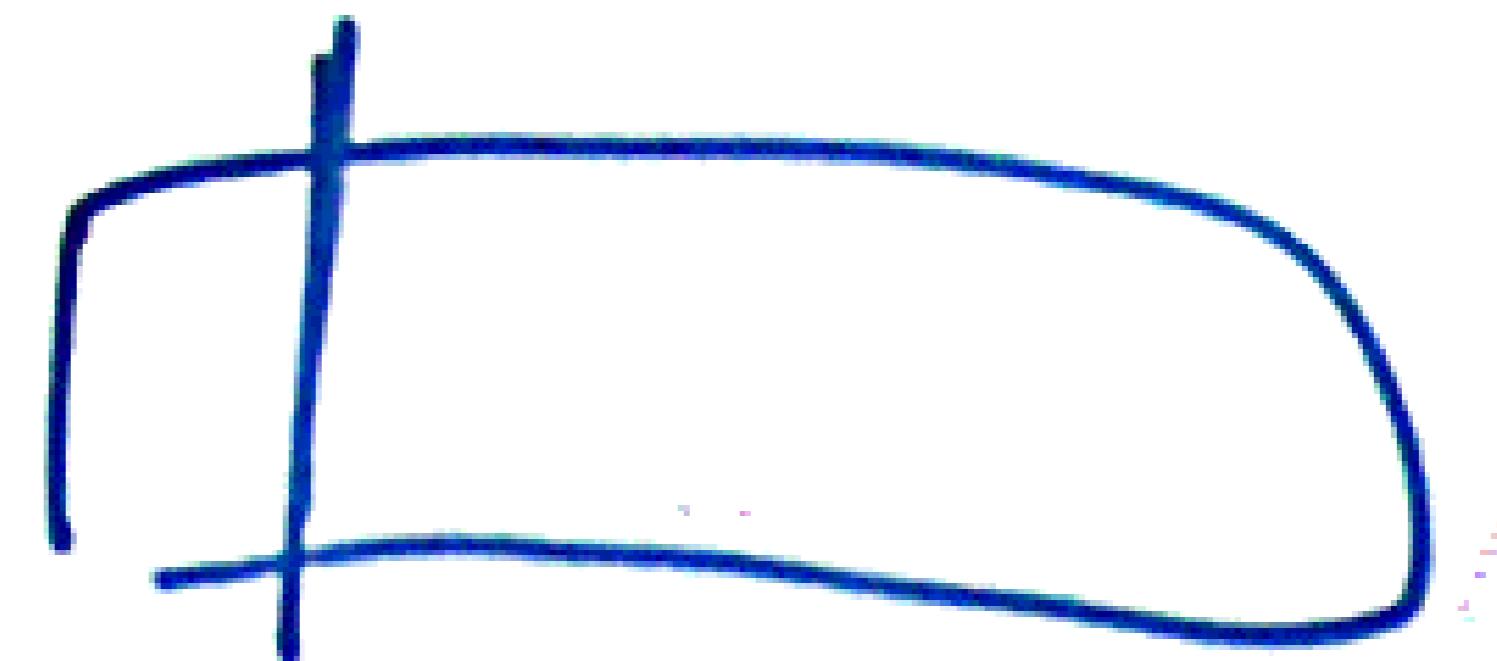


Cohen's Medians ($L[1, \dots, n]$)

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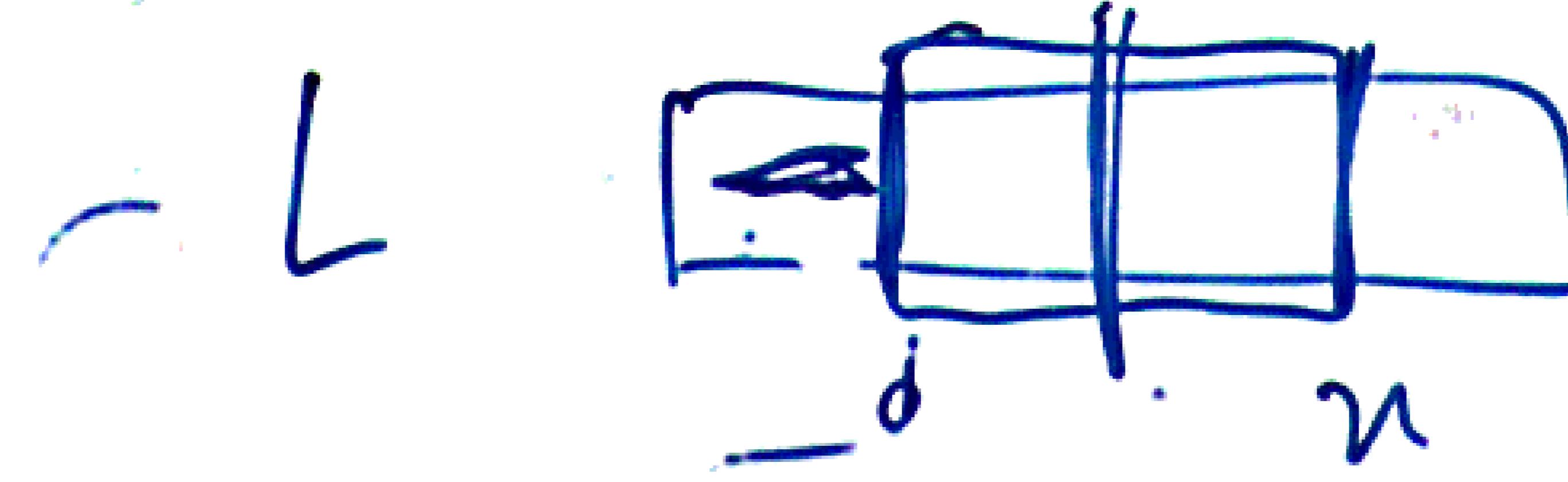


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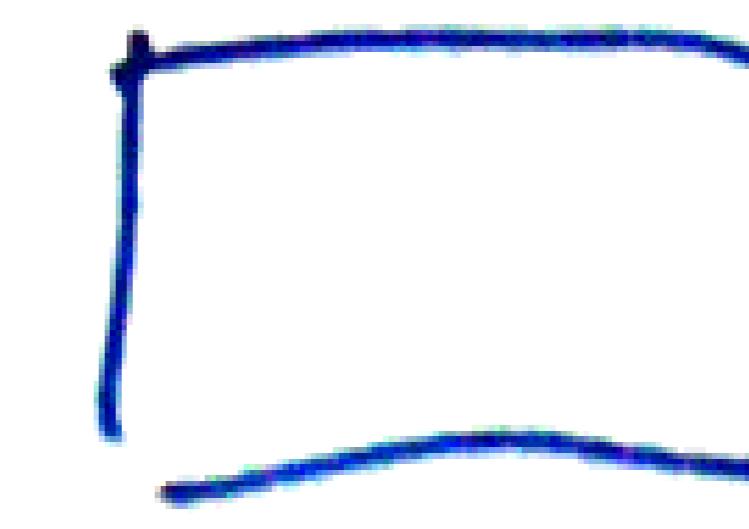
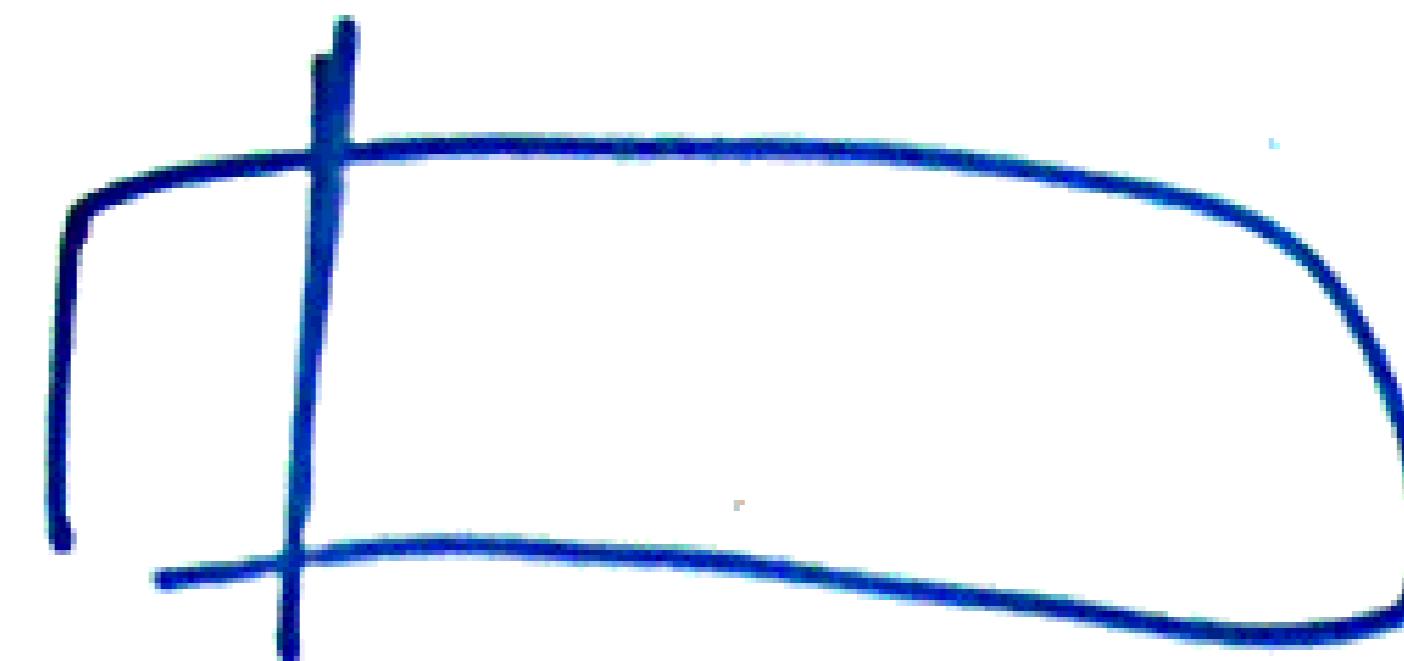


Cohen's Medians ($L[1, \dots, n]$)

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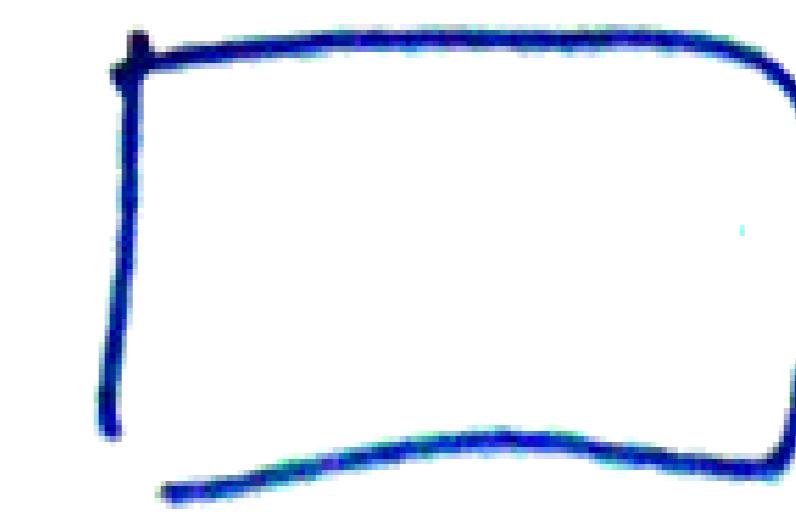
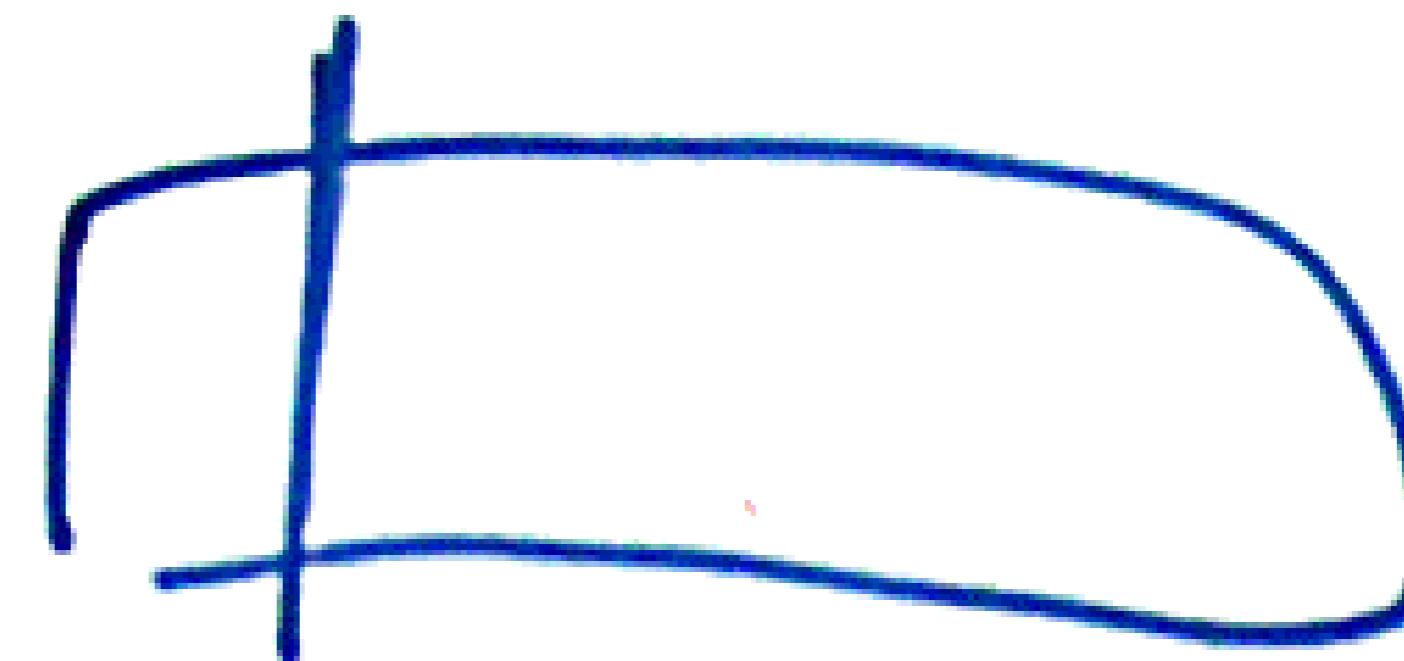


Cohen's Medians ($L[1, \dots, n]$)

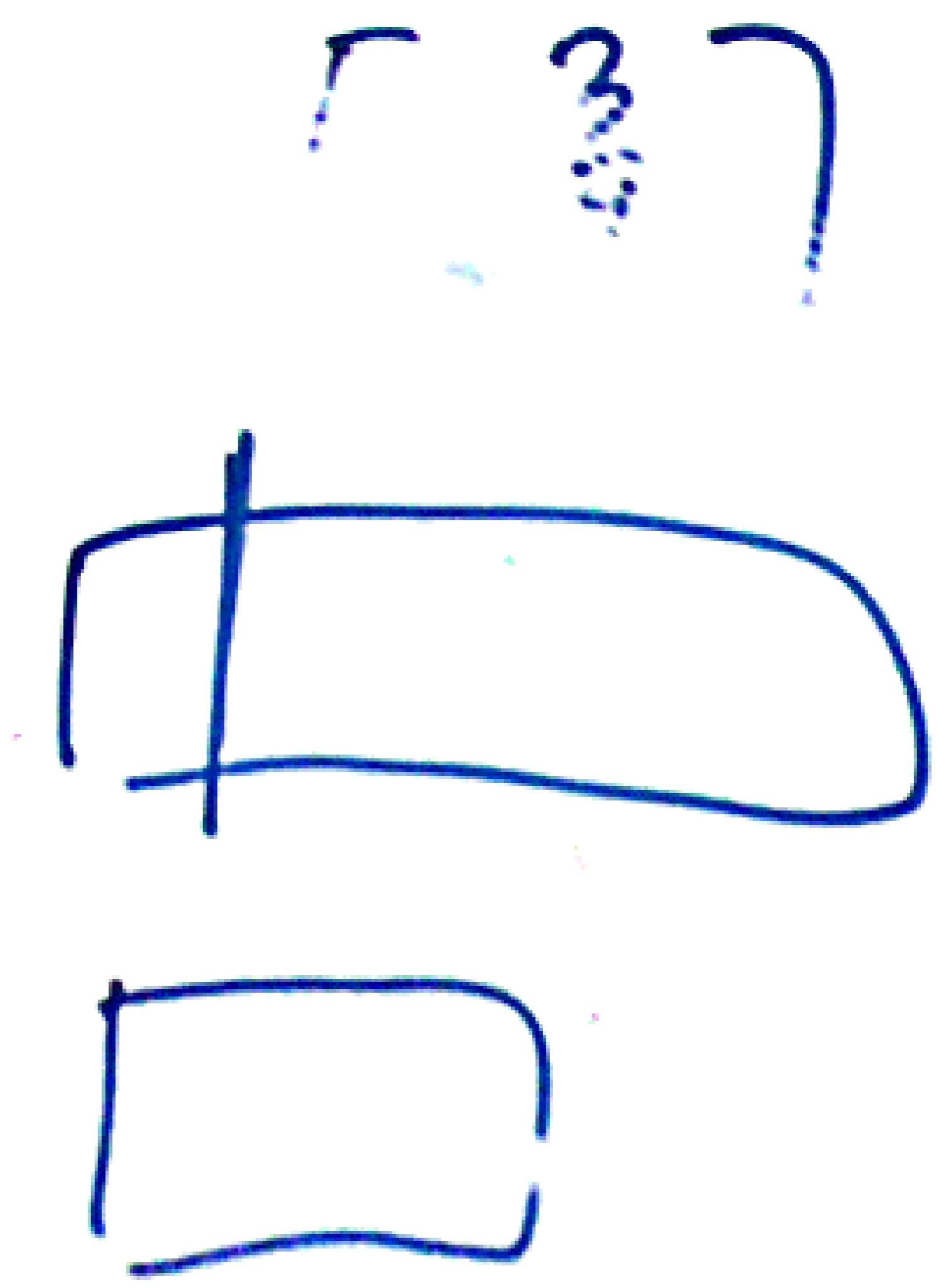
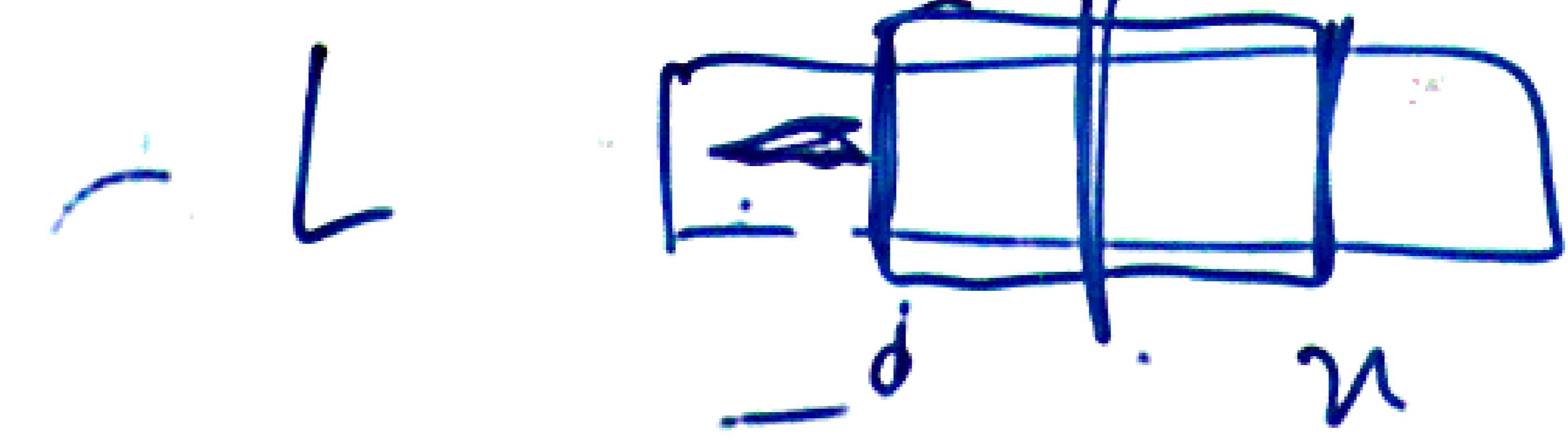
$\sim L$



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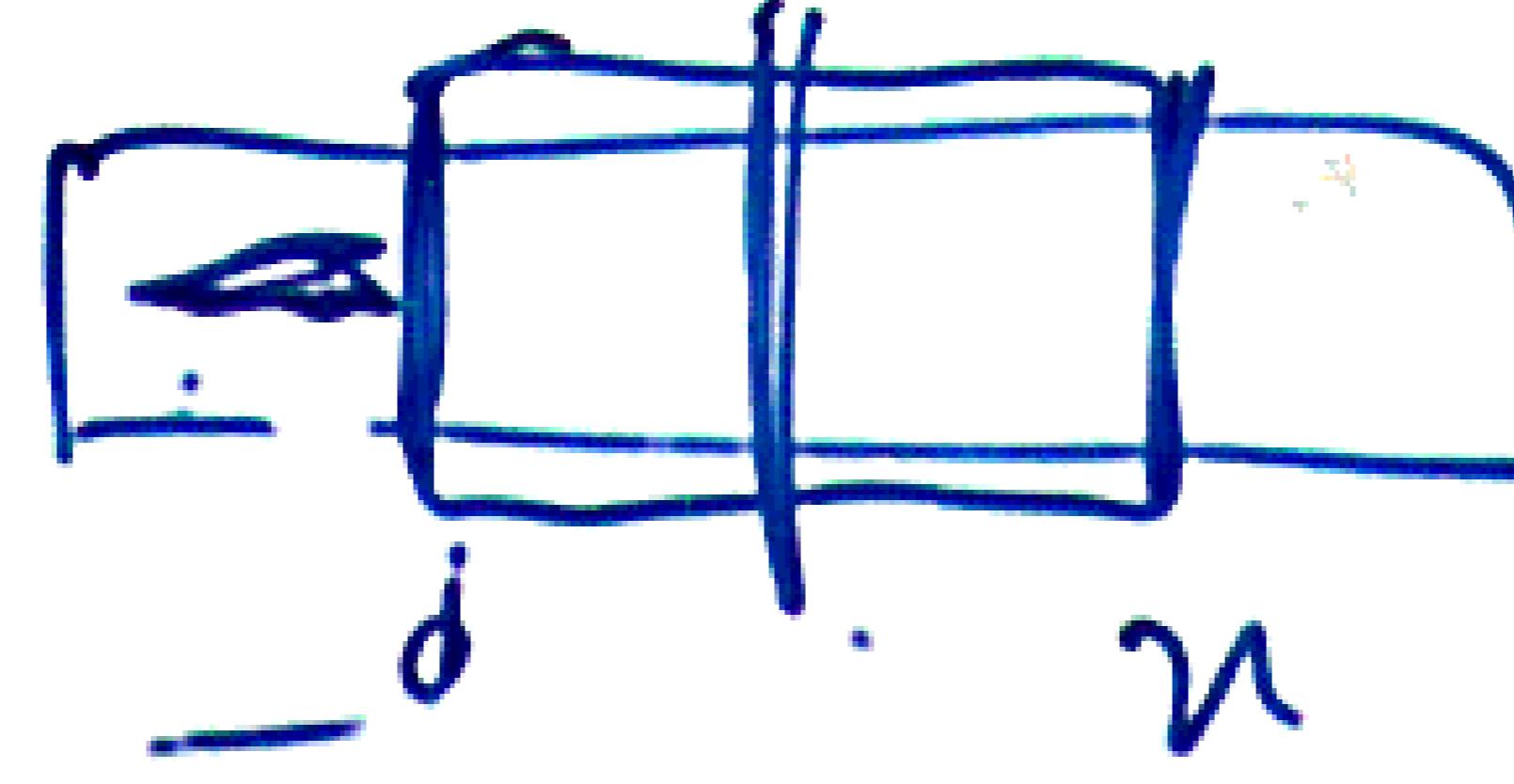


Cohen's Medians ($L[1, \dots, n]$)

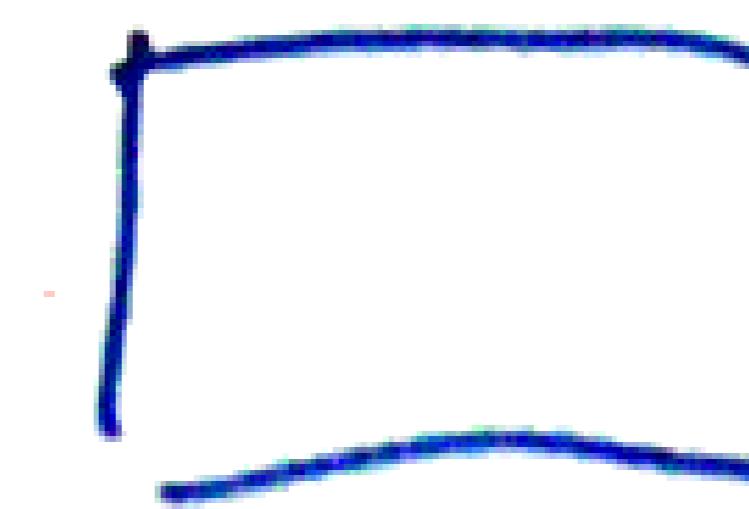
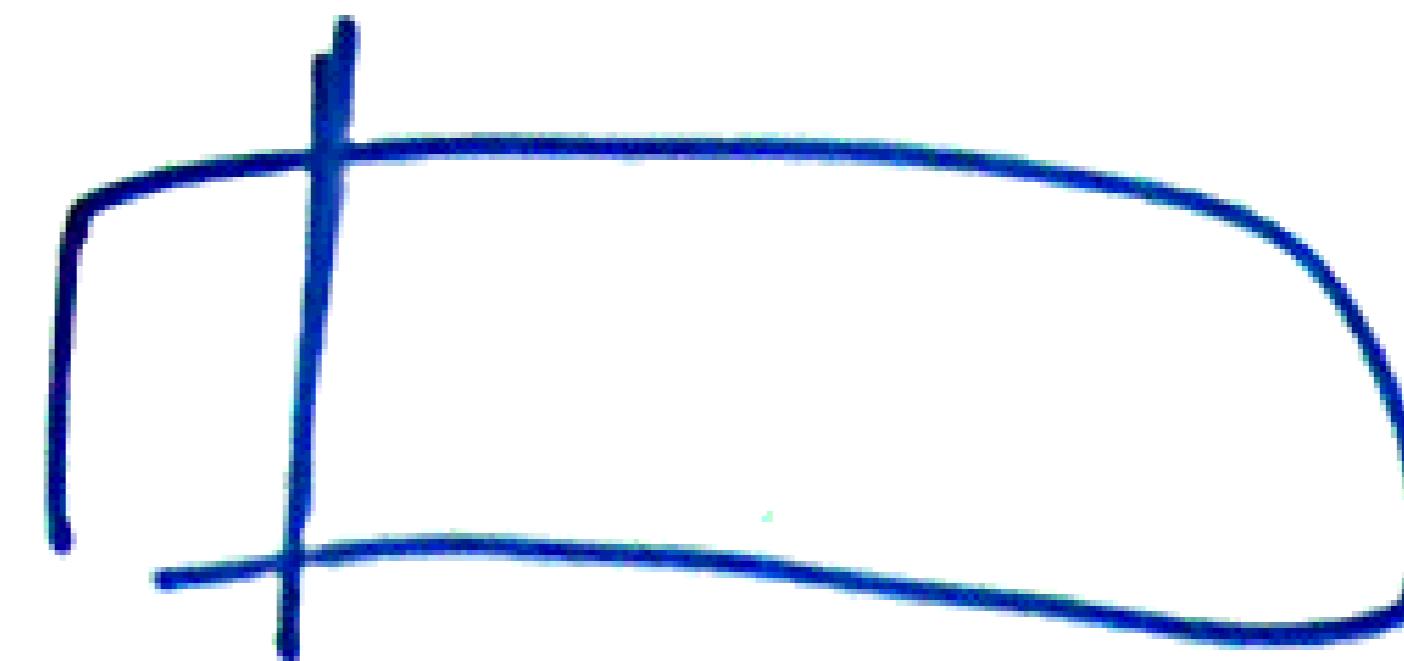


Cohen's Medians ($L[1, \dots, n]$)

$\sim L$



[3]







$$Y_1 = \left| \{ i \in \{1, \dots, n\} \mid R[i] \leq m \} \right|$$

$$Y_1 = |\{i \in \{1, \dots, n\} \mid R[i] \leq m\}|$$

$$Y_2 = |\{i \in \{1, \dots, n\} \mid R[i] \geq m\}|$$

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$$\Pr(Y_1 < s)$$

$$Y_1 = \left| \{i \in \{1, \dots, n\} \mid R[i] \leq m\} \right|$$

$$Y_2 = \left| \{i \in \{1, \dots, n\} \mid R[i] \geq n\} \right|$$

$$Y_1 \leq L^1$$

$$Y_1 = \left| \{i \in \{1, \dots, \lceil n^{\frac{3}{4}} \rceil\} \mid R[i] \leq m\} \right|$$

$$Y_1 < \lfloor \frac{1}{2} n^{\frac{3}{4}} - n^{\frac{1}{2}} \rfloor$$

$$Y_1 = \left| \{i \in \{1, \dots, \lceil n^{3/4} \rceil\} \mid R[i] \leq m\} \right|$$

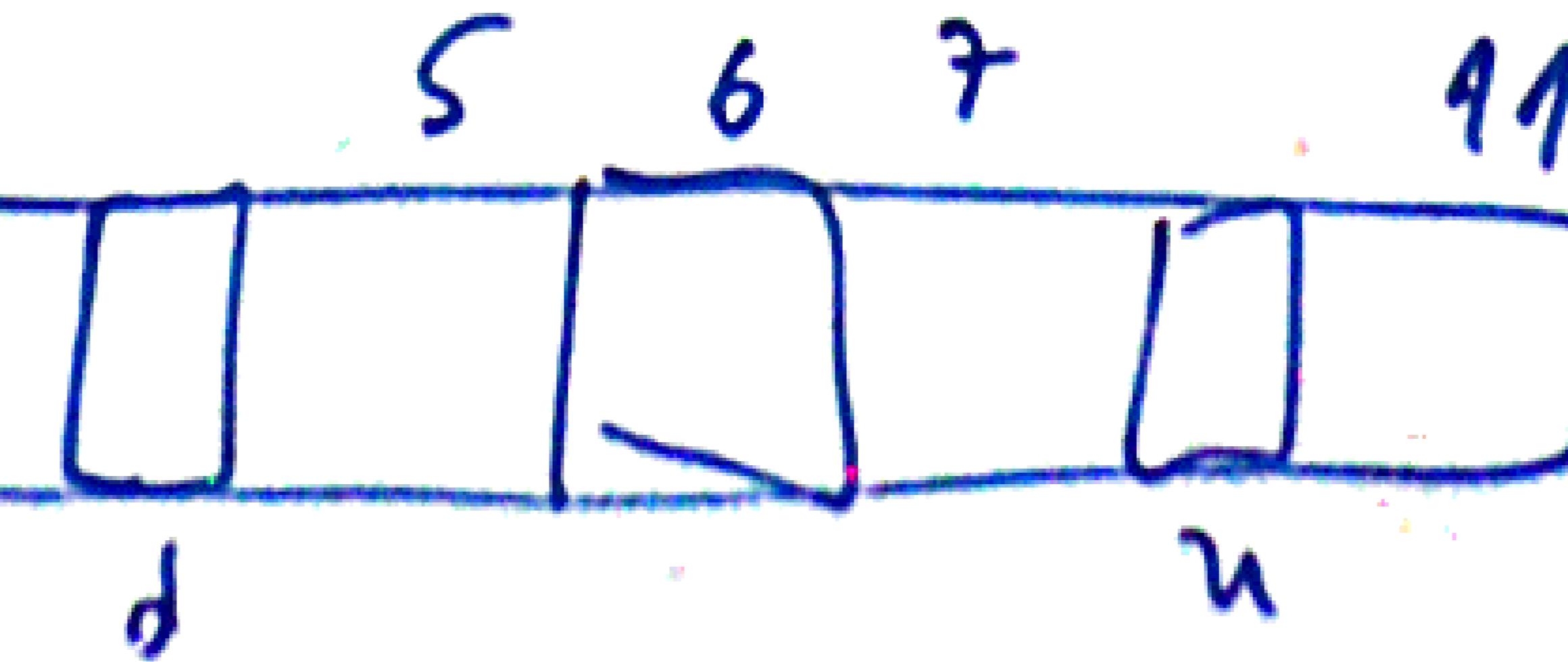
$$Y_1 < \lfloor \frac{1}{2}n^{3/4} - n^{1/2} \rfloor \quad d = R[\lfloor \frac{1}{2}n^{3/4} - n^{1/2} \rfloor]$$

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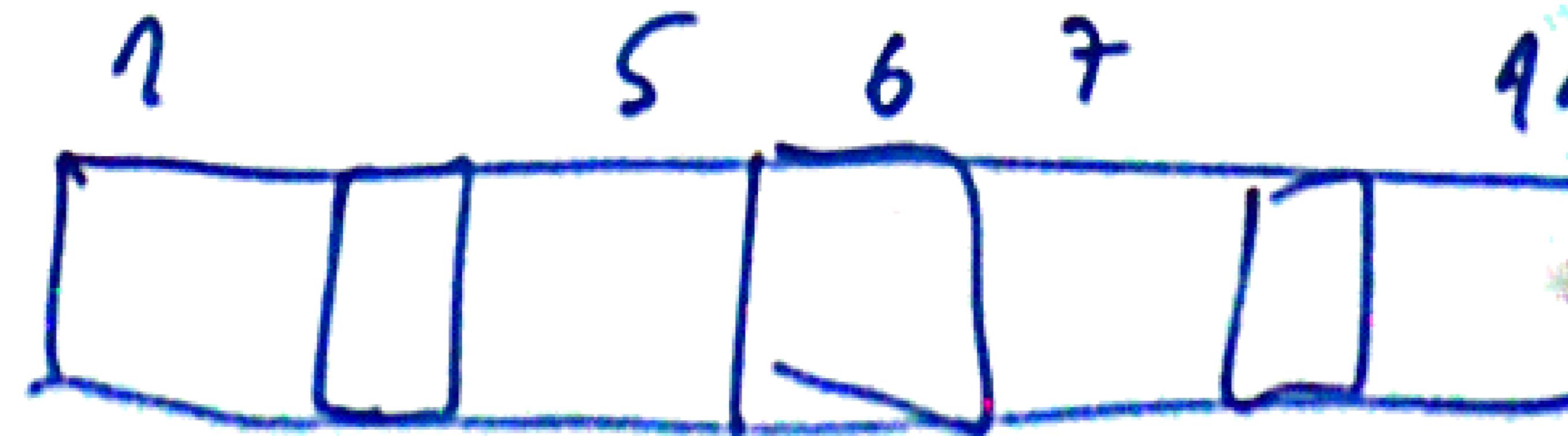
$$\delta = R[\lfloor \frac{1}{2}n^{3/4} - n^{1/2} \rfloor]$$

$$Y_1 = \left| \{i \in \{1, \dots, \lceil n^{\frac{3}{4}} \rceil\} \mid R[i] \leq m\} \right|$$
$$Y_1 < \left\lfloor \frac{1}{2} n^{\frac{3}{4}} - n^{\frac{1}{2}} \right\rfloor$$



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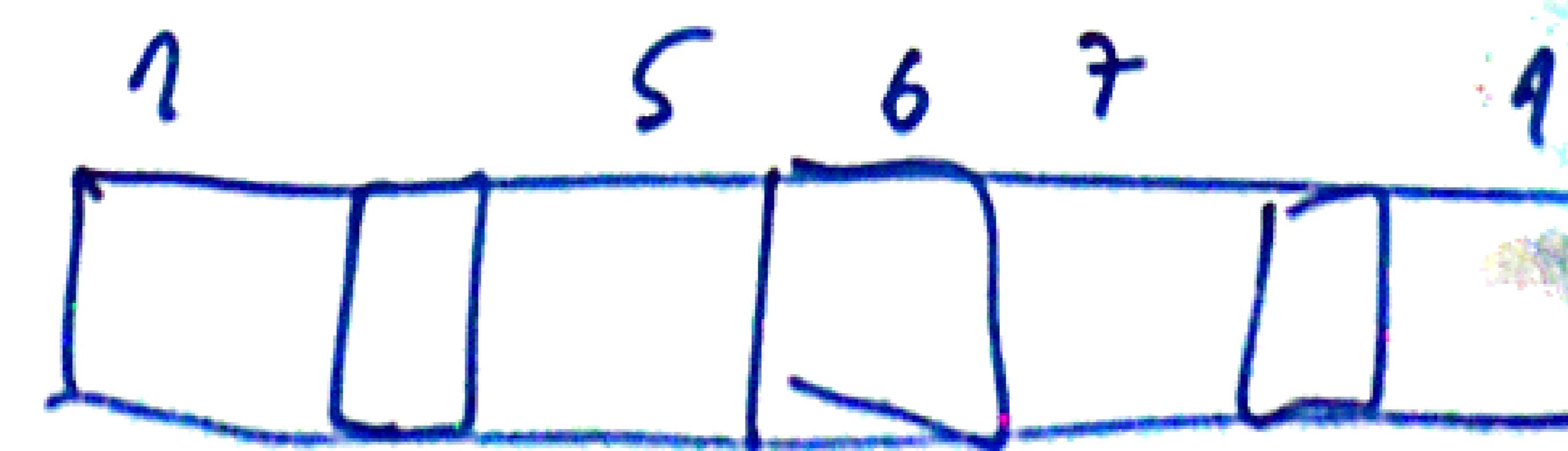


$$Y_1 = \left| \{i \in \{1, \dots, \lceil n^{3/4} \rceil\} \mid R[i] \leq m\} \right|$$

$$Y_1 \leq \lfloor \frac{1}{2}n^{3/4} - n^{1/2} \rfloor \quad d = R[\lfloor \frac{1}{2}n^{3/4} - n^{1/2} \rfloor]$$

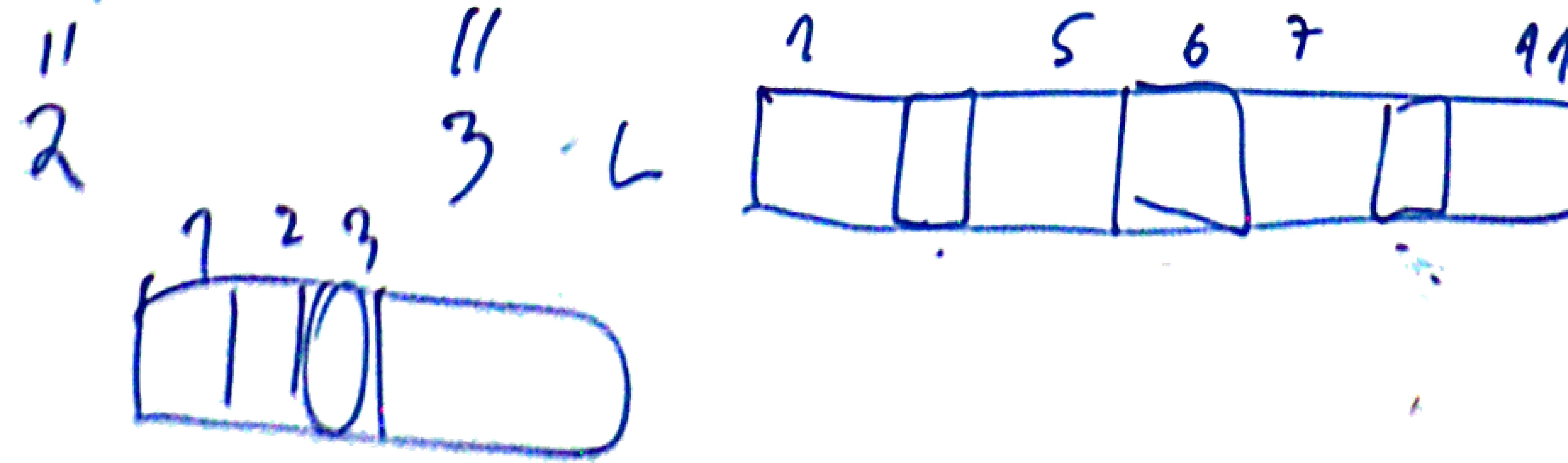
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2

11
3



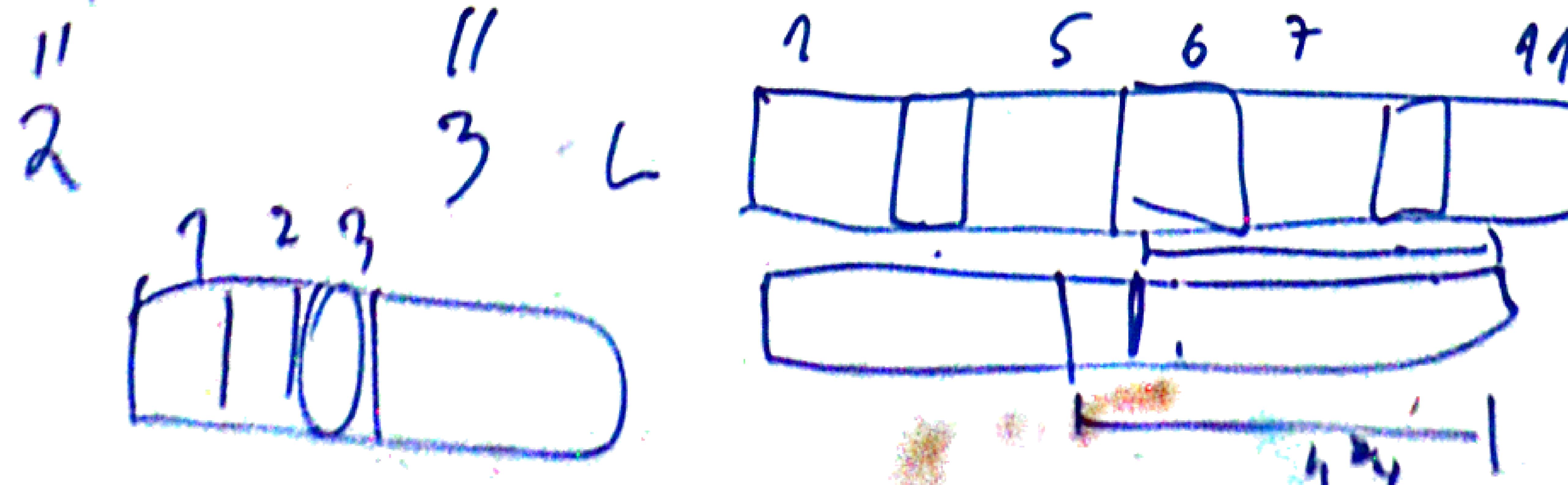
$$Y_1 = \left| \left\{ i \in \{1, \dots, \lceil n^{3/4} \rceil\} \mid R[i] \leq m \right\} \right|$$

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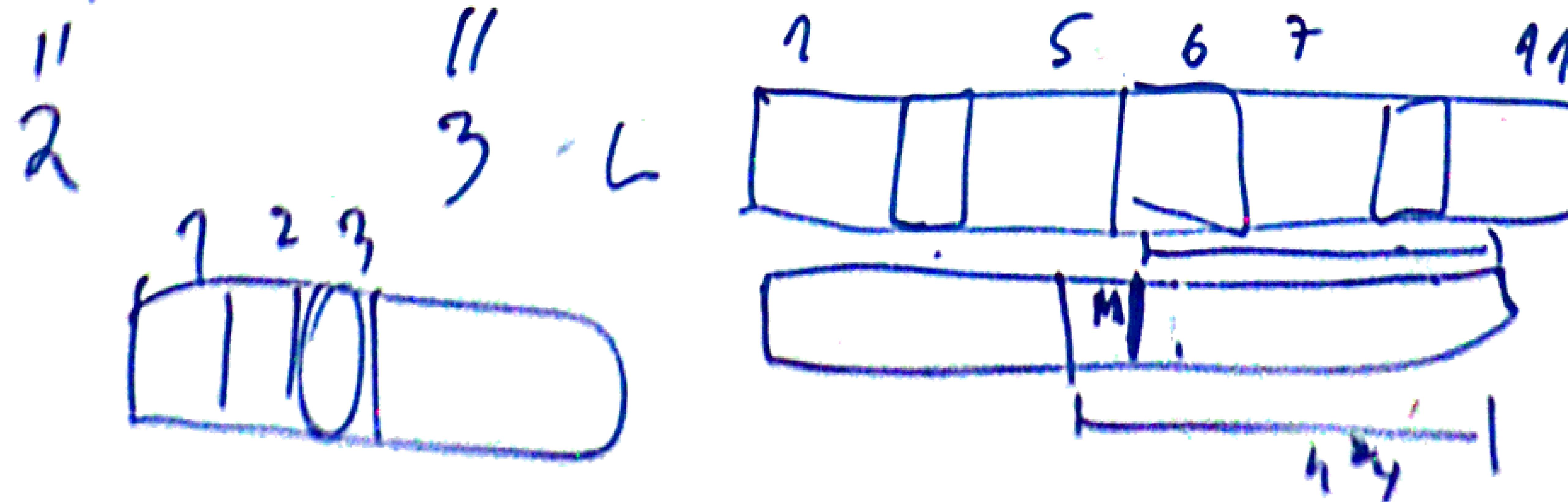
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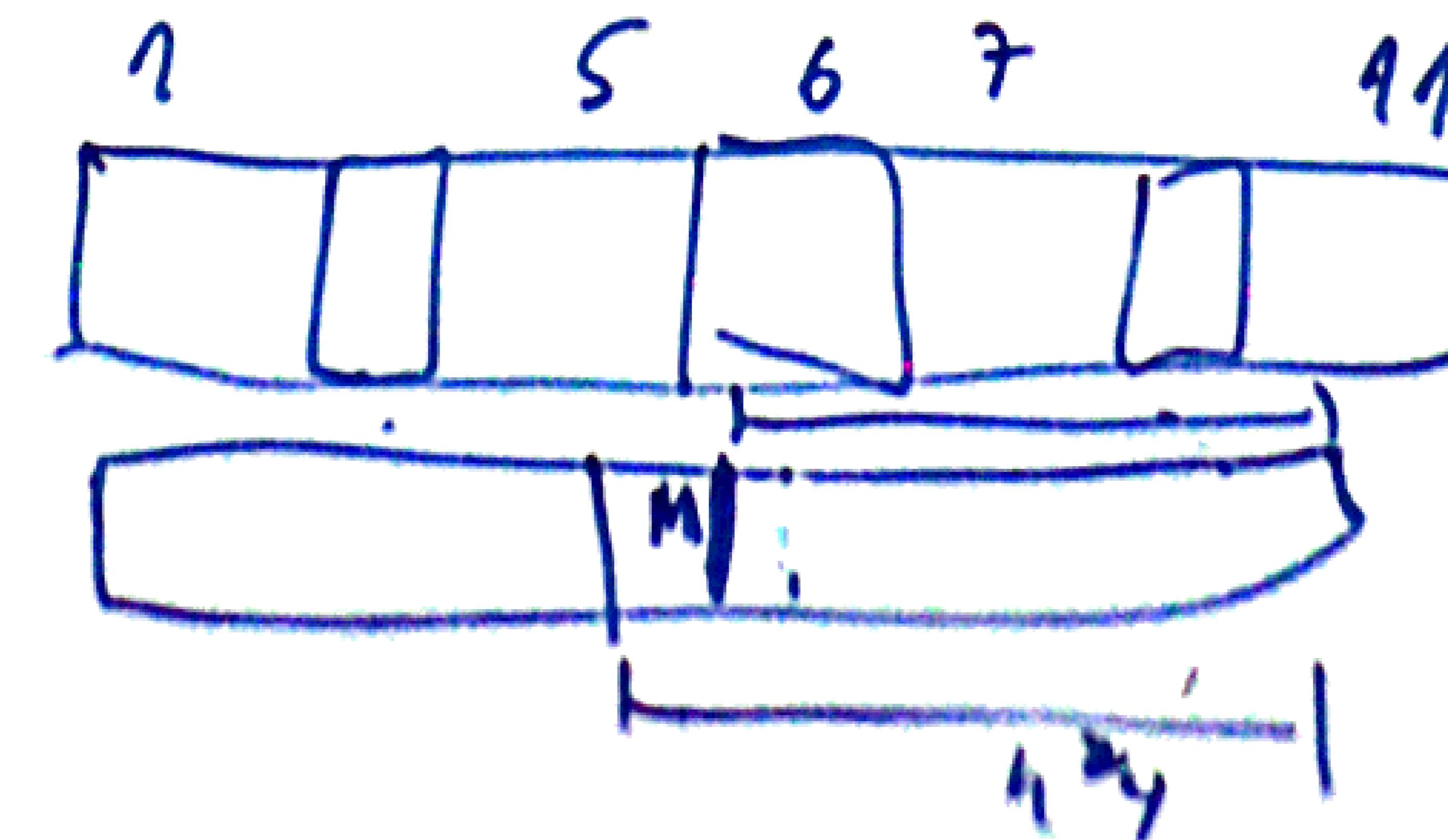
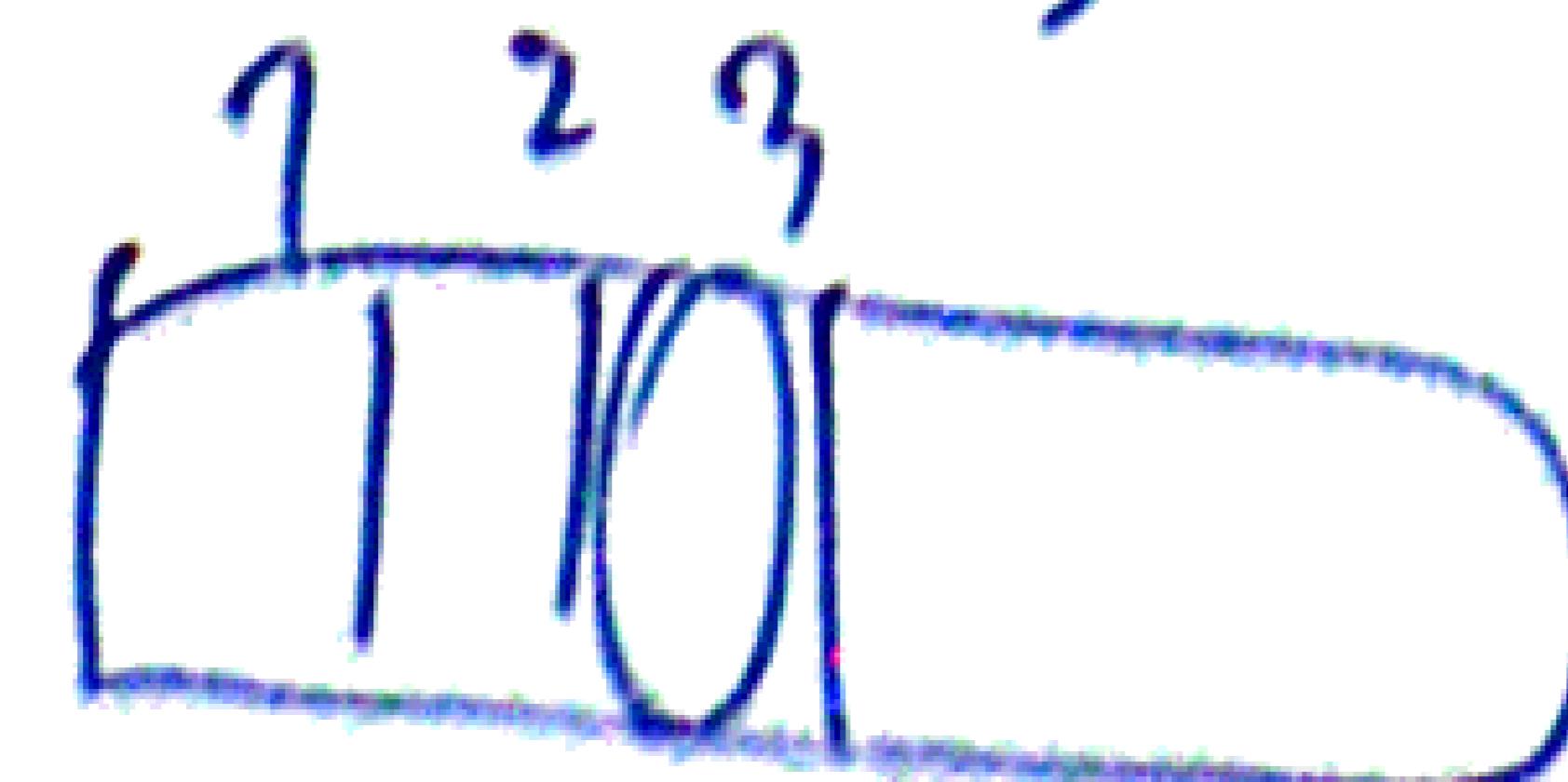
$$\Pr(A \cup B \cup C) \leq$$

$\Pr(A) +$
 $\Pr(B) +$
 $\Pr(C)$

$$Y_1 = \left| \{i \in \{1, \dots, \lceil n^{3/4} \rceil\} \mid R[i] \leq m\} \right|$$

$$Y_1 \leq \left\lfloor \frac{1}{2} n^{3/4} - n^{1/2} \right\rfloor \quad d = R \left[\left\lfloor \frac{1}{2} n^{3/4} - n^{1/2} \right\rfloor \right]$$

$$\begin{matrix} 1 & 2 & 3 \\ 11 & 2 & 3 \end{matrix}$$



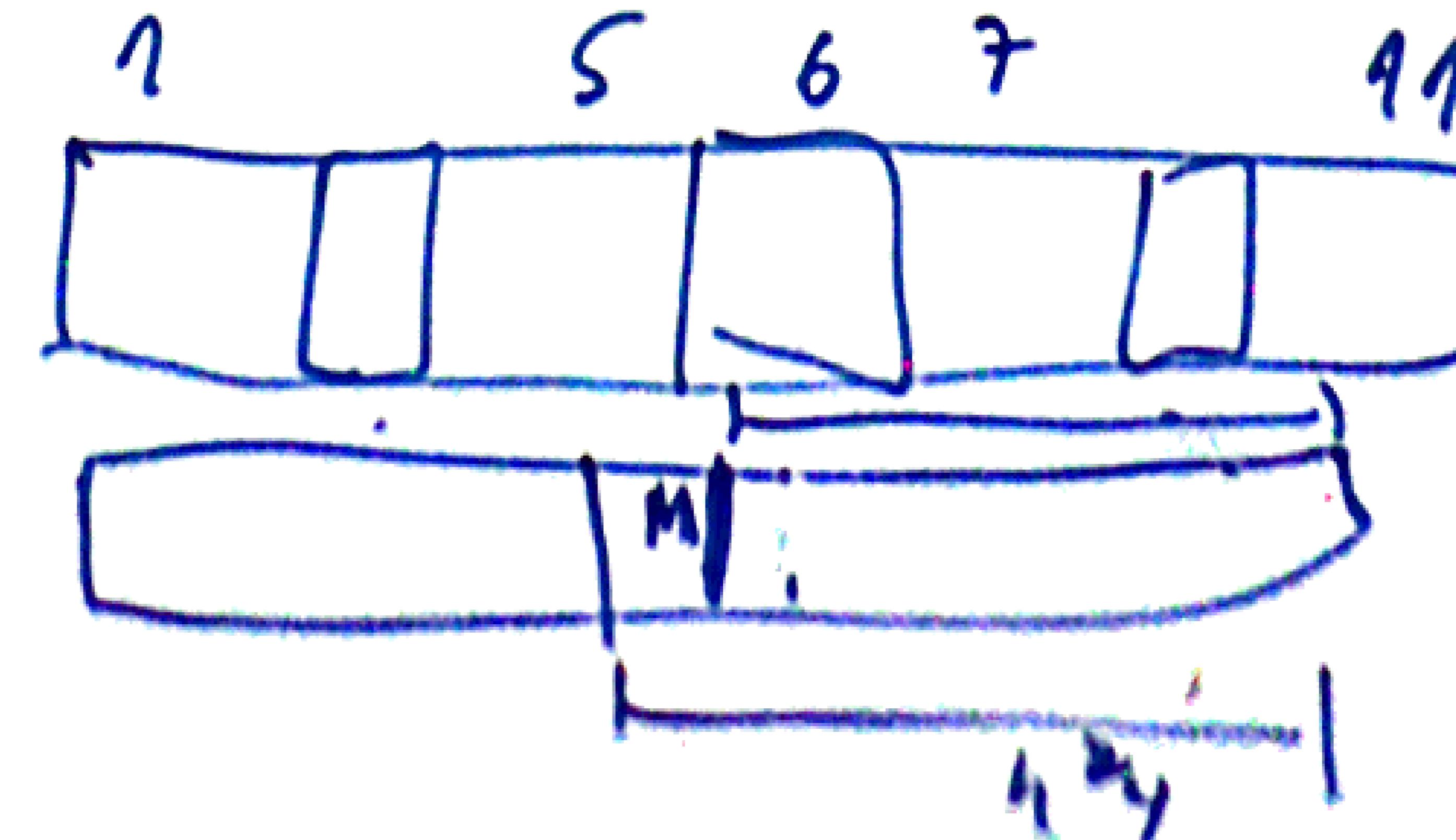
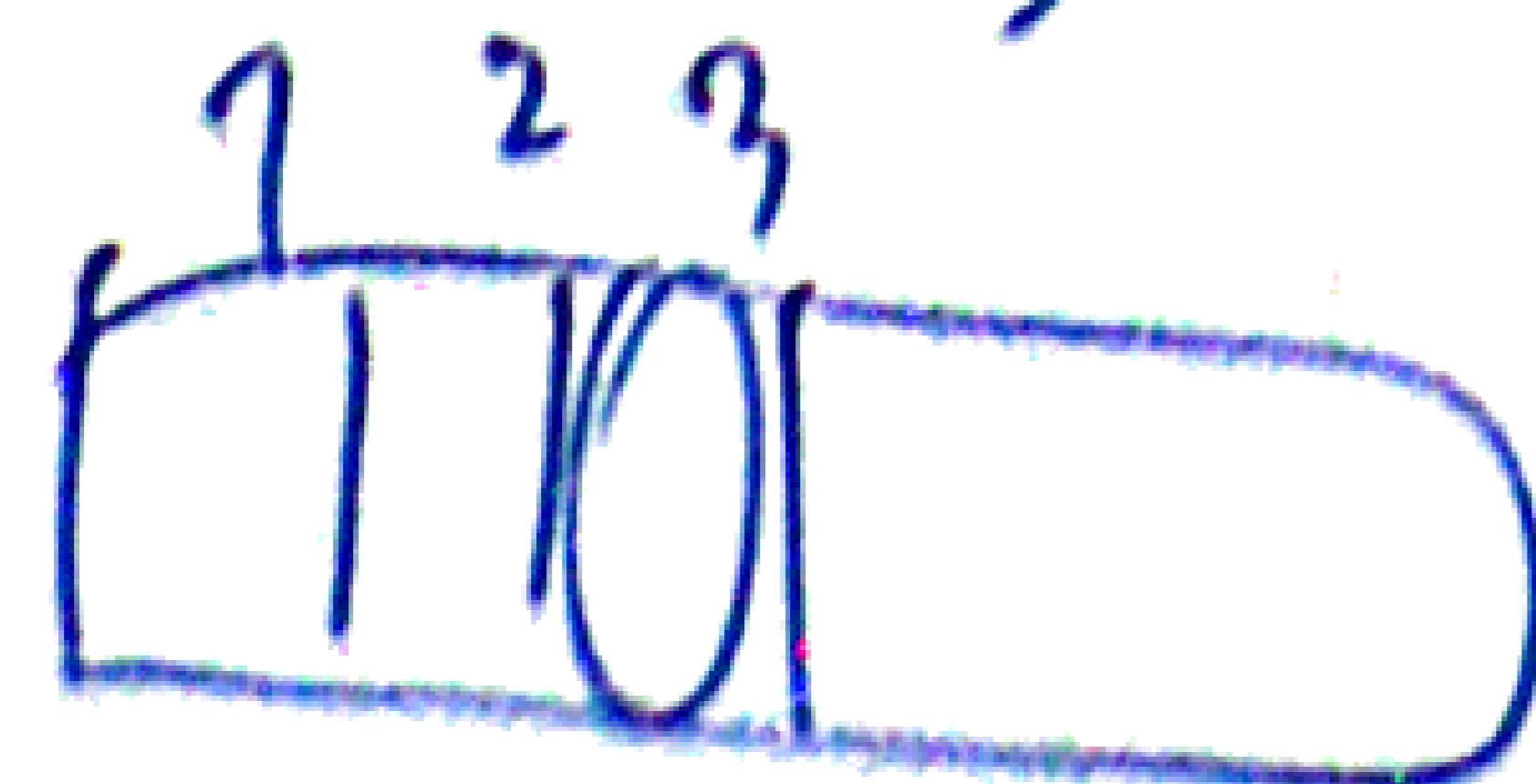
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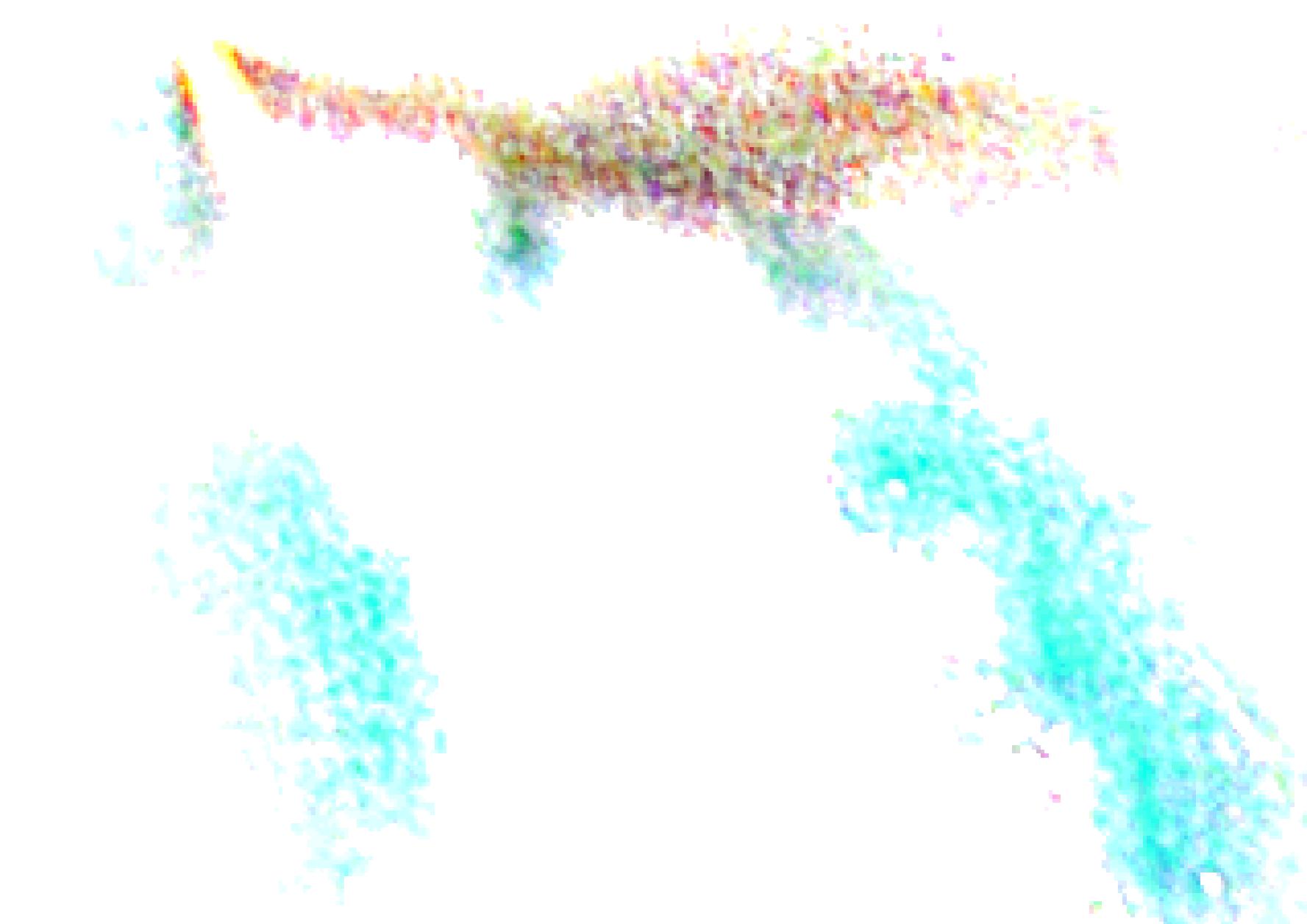
$$Y_1 \leq \lfloor \frac{1}{2} n^{3/4} - n^{1/2} \rfloor \quad d = R[\lfloor \frac{1}{2} n^{3/4} - n^{1/2} \rfloor]$$

$$\begin{matrix} 1 & 2 & 3 & \dots & L \\ 11 & 22 & 33 & \dots & \end{matrix}$$



$$E(X) \geq$$

$$d \cdot \Pr(X \geq R)$$



$$\Pr(A \cup B \cup C) \leq$$

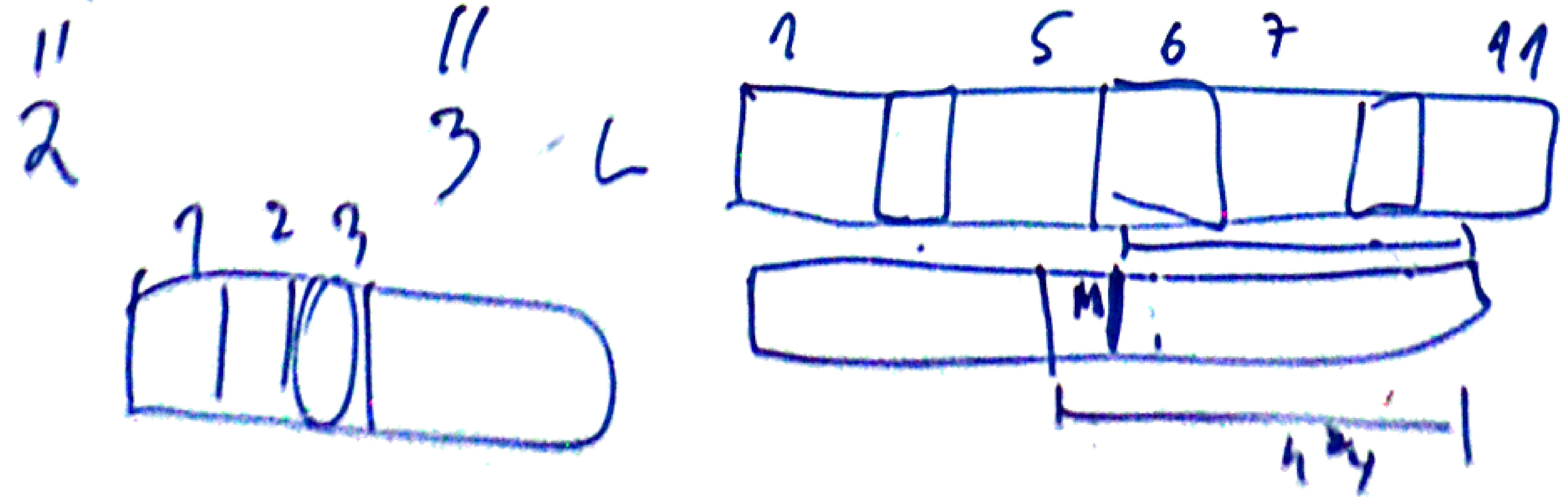
$\Pr(A)$

$\Pr(B)$

$\Pr(C)$

$$Y_1 = |\{i \in \{1, \dots, \lceil n^{3/4} \rceil\} \mid R[i] \leq m\}|$$

$$Y_1 \leq \lfloor \frac{1}{2}n^{3/4} - n^{1/2} \rfloor \quad d = R[\lfloor \frac{1}{2}n^{3/4} - n^{1/2} \rfloor]$$



$$E(X) \geq$$

$$d \cdot \Pr(X \geq R)$$

$$\Pr(|X - E[X]| \geq a)$$
$$= \Pr((X - E[X])^2 \geq a^2)$$

$$\Pr(A \cup B \cup C) \leq$$

$\Pr(A) +$
 $\Pr(B) +$
 $\Pr(C)$

$$E[X] \geq$$
$$a \cdot \Pr(X \geq a)$$

$$\Pr(|X - E[X]| \geq a)$$

$$= \Pr((X - E[X])^2 \geq a^2)$$

$$\leq \frac{E((X - E[X])^2)}{a^2} = \frac{\text{Var}(X)}{a^2}$$

$$\Pr(A \cup B \cup C) \leq$$

$$\Pr(A) +$$
$$\Pr(B) +$$
$$\Pr(C)$$

$$E(X) \geq$$
$$a \cdot \Pr(X \geq a)$$

$$\Pr(|X - E[X]| \geq a)$$

$$= \Pr((X - E[X])^2 \geq a^2)$$

$$\leq \frac{E((X - E[X])^2)}{a^2} = \frac{\text{Var}(X)}{a^2}$$

$$\Pr(A \cup B \cup C) \leq \Pr(A) + \Pr(B) + \Pr(C)$$

$$E(|X - E[X]|) \leq$$

$$U(X) \geq a \cdot \Pr(X \geq a)$$

$$\Pr(|X - E[X]| \geq a)$$

$$= \Pr((X - E[X])^2 \geq a^2)$$

$$\leq \frac{E((X - E[X])^2)}{a^2} = \frac{\text{Var}(X)}{a^2}$$

$$\Pr(A \cup B \cup C) \leq$$

$\Pr(A) +$
 $\Pr(B) +$
 $\Pr(C)$

$$E(|X - E[X]|)$$

$$E(X) \geq a \cdot \Pr(X \geq a)$$

1, 2, 1

$$\Pr(|X - E[X]| \geq a)$$

$$= \Pr((X - E[X])^2 \geq a^2)$$

$$\leq \frac{E((X - E[X])^2)}{a^2} = \frac{\text{Var}(X)}{a^2}$$

$$\Pr(A \cup B \cup C) \leq$$

$\Pr(A) +$
 $\Pr(B) +$
 $\Pr(C)$

$$E(|X - E[X]|)$$

$$E(X) \geq a \cdot \Pr(X \geq a)$$

—
1, 2, 1

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$$= \Pr((X - E[X])^2 \geq a^2)$$

$$\leq \frac{E((X - E[X])^2)}{a^2} = \frac{\text{Var}(X)}{a^2}$$

$$\Pr(A \cup B \cup C) \leq \Pr(A) + \Pr(B) + \Pr(C)$$

$$E(X) \geq a \cdot \Pr(X \geq a)$$

$$\overline{1} \approx 1$$

$$\Pr(|X - E[X]| \geq a)$$

$$= \Pr((X - E[X])^2 \geq a^2)$$

$$\leq \frac{E((X - E[X])^2)}{a^2} = \frac{\text{Var}(X)}{a^2}$$

$$\Pr(A \cup B \cup C) \leq \Pr(A) + \Pr(B) + \Pr(C)$$

$$a(X) \geq a \cdot \Pr(X \geq a)$$

