

# Prova 1 de GED13

## Questão 1

### Inicialização

```
library(tidyverse)
library(ggplot2)
library(quantmod) # Para usar o "getSymbols"
library(data.table) # Para usar o "shift"
library(ggpubr) # Para usar o "ggarrange" e "annotate_figure"
library(cowplot) # Para fazer "qqplot" junto com histograma
library(gridExtra) # Para inserir tabela no "qqplot"
start <- as.Date("2022-01-01")
end <- as.Date("2022-09-01")
```

### Dados do SP 500

```
dados.sp500 <- quantmod::getSymbols("^GSPC", src = "yahoo", from = start, to = end, auto.a
dados.sp500
```

##	GSPC.Open	GSPC.High	GSPC.Low	GSPC.Close	GSPC.Volume	GSPC.Adjusted
## 2022-01-03	4778.14	4796.64	4758.17	4796.56	2775190000	4796.56
## 2022-01-04	4804.51	4818.62	4774.27	4793.54	3641050000	4793.54
## 2022-01-05	4787.99	4797.70	4699.44	4700.58	3733540000	4700.58
## 2022-01-06	4693.39	4725.01	4671.26	4696.05	3371250000	4696.05
## 2022-01-07	4697.66	4707.95	4662.74	4677.03	3279870000	4677.03
## 2022-01-10	4655.34	4673.02	4582.24	4670.29	3621800000	4670.29
## 2022-01-11	4669.14	4714.13	4638.27	4713.07	3421600000	4713.07
## 2022-01-12	4728.59	4748.83	4706.71	4726.35	3060040000	4726.35
## 2022-01-13	4733.56	4744.13	4650.29	4659.03	3539830000	4659.03
## 2022-01-14	4637.99	4665.13	4614.75	4662.85	3483530000	4662.85
## 2022-01-18	4632.24	4632.24	4568.70	4577.11	3324960000	4577.11
## 2022-01-19	4588.03	4611.55	4530.20	4532.76	3387370000	4532.76
## 2022-01-20	4547.35	4602.11	4477.95	4482.73	3473060000	4482.73
## 2022-01-21	4471.38	4494.52	4395.34	4397.94	3945810000	4397.94
## 2022-01-24	4356.32	4417.35	4222.62	4410.13	5172540000	4410.13
## 2022-01-25	4366.64	4411.01	4287.11	4356.45	3989420000	4356.45
## 2022-01-26	4408.43	4453.23	4304.80	4349.93	4046270000	4349.93
## 2022-01-27	4380.58	4428.74	4309.50	4326.51	4074330000	4326.51
## 2022-01-28	4336.19	4432.72	4292.46	4431.85	3936030000	4431.85
## 2022-01-31	4431.79	4516.89	4414.02	4515.55	4001950000	4515.55
## 2022-02-01	4519.57	4550.49	4483.53	4546.54	3796450000	4546.54
## 2022-02-02	4566.39	4595.31	4544.32	4589.38	3777170000	4589.38
## 2022-02-03	4535.41	4542.88	4470.39	4477.44	3596830000	4477.44
## 2022-02-04	4482.79	4539.66	4451.50	4500.53	3673700000	4500.53
## 2022-02-07	4505.75	4521.86	4471.47	4483.87	3291600000	4483.87

##	2022-02-08	4480.02	4531.32	4465.40	4521.54	3509330000	4521.54
##	2022-02-09	4547.00	4590.03	4547.00	4587.18	3662810000	4587.18
##	2022-02-10	4553.24	4588.92	4484.31	4504.08	4490500000	4504.08
##	2022-02-11	4506.27	4526.33	4401.41	4418.64	4164960000	4418.64
##	2022-02-14	4412.61	4426.22	4364.84	4401.67	3466170000	4401.67
##	2022-02-15	4429.28	4472.77	4429.28	4471.07	3363200000	4471.07
##	2022-02-16	4455.75	4489.55	4429.68	4475.01	3478750000	4475.01
##	2022-02-17	4456.06	4456.06	4373.81	4380.26	3596510000	4380.26
##	2022-02-18	4384.57	4394.60	4327.22	4348.87	3871340000	4348.87
##	2022-02-22	4332.74	4362.12	4267.11	4304.76	4007780000	4304.76
##	2022-02-23	4324.93	4341.51	4221.51	4225.50	3814340000	4225.50
##	2022-02-24	4155.77	4294.73	4114.65	4288.70	5070560000	4288.70
##	2022-02-25	4298.38	4385.34	4286.83	4384.65	3941780000	4384.65
##	2022-02-28	4354.17	4388.84	4315.12	4373.94	4594010000	4373.94
##	2022-03-01	4363.14	4378.45	4279.54	4306.26	4679400000	4306.26
##	2022-03-02	4322.56	4401.48	4322.56	4386.54	4409090000	4386.54
##	2022-03-03	4401.31	4416.78	4345.56	4363.49	4062080000	4363.49
##	2022-03-04	4342.12	4342.12	4284.98	4328.87	4558250000	4328.87
##	2022-03-07	4327.01	4327.01	4199.85	4201.09	5506330000	4201.09
##	2022-03-08	4202.66	4276.94	4157.87	4170.70	6237000000	4170.70
##	2022-03-09	4223.10	4299.40	4223.10	4277.88	4220180000	4277.88
##	2022-03-10	4252.55	4268.28	4209.80	4259.52	4008690000	4259.52
##	2022-03-11	4279.50	4291.01	4200.49	4204.31	3877430000	4204.31
##	2022-03-14	4202.75	4247.57	4161.72	4173.11	4757600000	4173.11
##	2022-03-15	4188.82	4271.05	4187.90	4262.45	4331170000	4262.45
##	2022-03-16	4288.14	4358.90	4251.99	4357.86	5002240000	4357.86
##	2022-03-17	4345.11	4412.67	4335.65	4411.67	4174170000	4411.67
##	2022-03-18	4407.34	4465.40	4390.57	4463.12	6681510000	4463.12
##	2022-03-21	4462.40	4481.75	4424.30	4461.18	3961050000	4461.18
##	2022-03-22	4469.10	4522.00	4469.10	4511.61	3962880000	4511.61
##	2022-03-23	4493.10	4501.07	4455.81	4456.24	4014360000	4456.24
##	2022-03-24	4469.98	4520.58	4465.17	4520.16	3573430000	4520.16
##	2022-03-25	4522.91	4546.03	4501.07	4543.06	3577520000	4543.06
##	2022-03-28	4541.09	4575.65	4517.69	4575.52	3696850000	4575.52
##	2022-03-29	4602.86	4637.30	4589.66	4631.60	4239660000	4631.60
##	2022-03-30	4624.20	4627.77	4581.32	4602.45	3665390000	4602.45
##	2022-03-31	4599.02	4603.07	4530.41	4530.41	3782040000	4530.41
##	2022-04-01	4540.32	4548.70	4507.57	4545.86	3828290000	4545.86
##	2022-04-04	4547.97	4583.50	4539.21	4582.64	3833500000	4582.64
##	2022-04-05	4572.45	4593.45	4514.17	4525.12	3906230000	4525.12
##	2022-04-06	4494.17	4503.94	4450.04	4481.15	4137080000	4481.15
##	2022-04-07	4474.65	4521.16	4450.30	4500.21	4054010000	4500.21
##	2022-04-08	4494.15	4520.41	4474.60	4488.28	3453040000	4488.28
##	2022-04-11	4462.64	4464.35	4408.38	4412.53	3452540000	4412.53
##	2022-04-12	4437.59	4471.00	4381.34	4397.45	3451990000	4397.45
##	2022-04-13	4394.30	4453.92	4392.70	4446.59	3273140000	4446.59

##	2022-04-14	4449.12	4460.46	4390.77	4392.59	3634740000	4392.59
##	2022-04-18	4385.63	4410.31	4370.30	4391.69	3509340000	4391.69
##	2022-04-19	4390.63	4471.03	4390.63	4462.21	3197930000	4462.21
##	2022-04-20	4472.26	4488.29	4448.76	4459.45	3678040000	4459.45
##	2022-04-21	4489.17	4512.94	4384.47	4393.66	3833570000	4393.66
##	2022-04-22	4385.83	4385.83	4267.62	4271.78	3930660000	4271.78
##	2022-04-25	4255.34	4299.02	4200.82	4296.12	4061070000	4296.12
##	2022-04-26	4278.14	4278.14	4175.04	4175.20	3760420000	4175.20
##	2022-04-27	4186.52	4240.71	4162.90	4183.96	3876340000	4183.96
##	2022-04-28	4222.58	4308.45	4188.63	4287.50	3969440000	4287.50
##	2022-04-29	4253.75	4269.68	4124.28	4131.93	3943480000	4131.93
##	2022-05-02	4130.61	4169.81	4062.51	4155.38	4474060000	4155.38
##	2022-05-03	4159.78	4200.10	4147.08	4175.48	3877530000	4175.48
##	2022-05-04	4181.18	4307.66	4148.91	4300.17	4236210000	4300.17
##	2022-05-05	4270.43	4270.43	4106.01	4146.87	4197620000	4146.87
##	2022-05-06	4128.17	4157.69	4067.91	4123.34	4254300000	4123.34
##	2022-05-09	4081.27	4081.27	3975.48	3991.24	4746120000	3991.24
##	2022-05-10	4035.18	4068.82	3958.17	4001.05	4630150000	4001.05
##	2022-05-11	3990.08	4049.09	3928.82	3935.18	4683220000	3935.18
##	2022-05-12	3903.95	3964.80	3858.87	3930.08	4964130000	3930.08
##	2022-05-13	3963.90	4038.88	3963.90	4023.89	4142950000	4023.89
##	2022-05-16	4013.02	4046.46	3983.99	4008.01	3824320000	4008.01
##	2022-05-17	4052.00	4090.72	4033.93	4088.85	3846580000	4088.85
##	2022-05-18	4051.98	4051.98	3911.91	3923.68	4428960000	3923.68
##	2022-05-19	3899.00	3945.96	3876.58	3900.79	4212140000	3900.79
##	2022-05-20	3927.76	3943.42	3810.32	3901.36	4278520000	3901.36
##	2022-05-23	3919.42	3981.88	3909.04	3973.75	3392770000	3973.75
##	2022-05-24	3942.94	3955.68	3875.13	3941.48	3901640000	3941.48
##	2022-05-25	3929.59	3999.33	3925.03	3978.73	4322190000	3978.73
##	2022-05-26	3984.60	4075.14	3984.60	4057.84	3961940000	4057.84
##	2022-05-27	4077.43	4158.49	4077.43	4158.24	3560560000	4158.24
##	2022-05-31	4151.09	4168.34	4104.88	4132.15	5192220000	4132.15
##	2022-06-01	4149.78	4166.54	4073.85	4101.23	4145710000	4101.23
##	2022-06-02	4095.41	4177.51	4074.37	4176.82	3604930000	4176.82
##	2022-06-03	4137.57	4142.67	4098.67	4108.54	3107080000	4108.54
##	2022-06-06	4134.72	4168.78	4109.18	4121.43	3852050000	4121.43
##	2022-06-07	4096.47	4164.86	4080.19	4160.68	3476470000	4160.68
##	2022-06-08	4147.12	4160.14	4107.20	4115.77	3090180000	4115.77
##	2022-06-09	4101.65	4119.10	4017.17	4017.82	3192330000	4017.82
##	2022-06-10	3974.39	3974.39	3900.16	3900.86	3936120000	3900.86
##	2022-06-13	3838.15	3838.15	3734.30	3749.63	4572820000	3749.63
##	2022-06-14	3763.52	3778.18	3705.68	3735.48	4126400000	3735.48
##	2022-06-15	3764.05	3837.56	3722.30	3789.99	4474610000	3789.99
##	2022-06-16	3728.18	3728.18	3639.77	3666.77	4511200000	3666.77
##	2022-06-17	3665.90	3707.71	3636.87	3674.84	6954110000	3674.84
##	2022-06-21	3715.31	3779.65	3715.31	3764.79	4124600000	3764.79

##	2022-06-22	3733.89	3801.79	3717.69	3759.89	4342270000	3759.89
##	2022-06-23	3774.71	3802.58	3743.52	3795.73	4078100000	3795.73
##	2022-06-24	3821.75	3913.65	3821.75	3911.74	6742870000	3911.74
##	2022-06-27	3920.76	3927.72	3889.66	3900.11	3385120000	3900.11
##	2022-06-28	3913.00	3945.86	3820.14	3821.55	3590980000	3821.55
##	2022-06-29	3825.09	3836.50	3799.02	3818.83	3458850000	3818.83
##	2022-06-30	3785.99	3818.99	3738.67	3785.38	4032260000	3785.38
##	2022-07-01	3781.00	3829.82	3752.10	3825.33	3268240000	3825.33
##	2022-07-05	3792.61	3832.19	3742.06	3831.39	4427900000	3831.39
##	2022-07-06	3831.98	3870.91	3809.37	3845.08	3613120000	3845.08
##	2022-07-07	3858.85	3910.63	3858.85	3902.62	3337710000	3902.62
##	2022-07-08	3888.26	3918.50	3869.34	3899.38	2844620000	3899.38
##	2022-07-11	3880.94	3880.94	3847.22	3854.43	3023830000	3854.43
##	2022-07-12	3851.95	3873.41	3802.36	3818.80	3138460000	3818.80
##	2022-07-13	3779.67	3829.44	3759.07	3801.78	3166580000	3801.78
##	2022-07-14	3763.99	3796.41	3721.56	3790.38	3447500000	3790.38
##	2022-07-15	3818.00	3863.62	3817.18	3863.16	3537130000	3863.16
##	2022-07-18	3883.79	3902.44	3818.63	3830.85	3414470000	3830.85
##	2022-07-19	3860.73	3939.81	3860.73	3936.69	3160350000	3936.69
##	2022-07-20	3935.32	3974.13	3922.03	3959.90	3452150000	3959.90
##	2022-07-21	3955.47	3999.29	3927.64	3998.95	3586030000	3998.95
##	2022-07-22	3998.43	4012.44	3938.86	3961.63	3246220000	3961.63
##	2022-07-25	3965.72	3975.30	3943.46	3966.84	2988650000	3966.84
##	2022-07-26	3953.22	3953.22	3910.74	3921.05	3083420000	3921.05
##	2022-07-27	3951.43	4039.56	3951.43	4023.61	3584170000	4023.61
##	2022-07-28	4026.13	4078.95	3992.97	4072.43	3882850000	4072.43
##	2022-07-29	4087.33	4140.15	4079.22	4130.29	3817740000	4130.29
##	2022-08-01	4112.38	4144.95	4096.02	4118.63	3540960000	4118.63
##	2022-08-02	4104.21	4140.47	4079.81	4091.19	3880790000	4091.19
##	2022-08-03	4107.96	4167.66	4107.96	4155.17	3544410000	4155.17
##	2022-08-04	4154.85	4161.29	4135.42	4151.94	3565810000	4151.94
##	2022-08-05	4115.87	4151.58	4107.31	4145.19	3540260000	4145.19
##	2022-08-08	4155.93	4186.62	4128.97	4140.06	3604650000	4140.06
##	2022-08-09	4133.11	4137.30	4112.09	4122.47	3337150000	4122.47
##	2022-08-10	4181.02	4211.03	4177.26	4210.24	3998590000	4210.24
##	2022-08-11	4227.40	4257.91	4201.41	4207.27	3925060000	4207.27
##	2022-08-12	4225.02	4280.47	4219.78	4280.15	3252290000	4280.15
##	2022-08-15	4269.37	4301.79	4256.90	4297.14	3087740000	4297.14
##	2022-08-16	4290.46	4325.28	4277.77	4305.20	3792010000	4305.20
##	2022-08-17	4280.40	4302.18	4253.08	4274.04	3293430000	4274.04
##	2022-08-18	4273.13	4292.53	4261.98	4283.74	2871990000	4283.74
##	2022-08-19	4266.31	4266.31	4218.70	4228.48	3210680000	4228.48
##	2022-08-22	4195.08	4195.08	4129.86	4137.99	3365220000	4137.99
##	2022-08-23	4133.09	4159.77	4124.03	4128.73	3117800000	4128.73
##	2022-08-24	4126.55	4156.56	4119.97	4140.77	3056910000	4140.77
##	2022-08-25	4153.26	4200.54	4147.59	4199.12	2976050000	4199.12

```
## 2022-08-26 4198.74 4203.04 4057.66 4057.66 3175260000 4057.66
## 2022-08-29 4034.58 4062.99 4017.42 4030.61 2963020000 4030.61
## 2022-08-30 4041.25 4044.98 3965.21 3986.16 3190580000 3986.16
## 2022-08-31 4000.67 4015.37 3954.53 3955.00 3797860000 3955.00
```

```
nasdaq <- na.omit(dados.nasdaq)
```

```
## Error in na.omit(dados.nasdaq): object 'dados.nasdaq' not found
```

## Cria o vetor de preco de fechamento

```
preco_fechamento <- dados.sp500$"GSPC.Close"
```

### 1. Media do Preco de Fechamento

```
media_pf <- mean(preco_fechamento)
media_pf
```

```
## [1] 4222.706
```

### 2. Moda do Preco de Fechamento

```
tab_preco_fechamento <- table(preco_fechamento)
moda_pf <- names(tab_preco_fechamento)[which(tab_preco_fechamento==max(tab_preco_fechamento))]
moda_pf
```

```
## [1] "3666.77002" "3674.840088" "3735.47998" "3749.629883" "3759.889893" "3764.790039"
## [14] "3821.550049" "3825.330078" "3830.850098" "3831.389893" "3845.080078" "3854.429932"
## [27] "3911.73999" "3921.050049" "3923.679932" "3930.080078" "3935.179932" "3936.689941"
## [40] "3986.159912" "3991.23999" "3998.949951" "4001.050049" "4008.01001" "4017.820068"
## [53] "4091.189941" "4101.22998" "4108.540039" "4115.77002" "4118.629883" "4121.430176"
## [66] "4140.060059" "4140.77002" "4145.189941" "4146.870117" "4151.939941" "4155.169922"
## [79] "4176.819824" "4183.959961" "4199.120117" "4201.089844" "4204.310059" "4207.27002"
## [92] "4277.879883" "4280.149902" "4283.740234" "4287.5" "4288.700195" "4296.120117"
## [105] "4348.870117" "4349.930176" "4356.450195" "4357.859863" "4363.490234" "4373.939941"
## [118] "4397.939941" "4401.669922" "4410.129883" "4411.669922" "4412.529785" "4418.640137"
## [131] "4471.069824" "4475.009766" "4477.439941" "4481.149902" "4482.72998" "4483.870117"
## [144] "4521.540039" "4525.120117" "4530.410156" "4532.759766" "4543.060059" "4545.859863"
## [157] "4631.600098" "4659.029785" "4662.850098" "4670.290039" "4677.029785" "4696.049805"
```

### 3. Mediana do Preco de Fechamento

```
mediana_pf <- median(preco_fechamento)
mediana_pf
```

```
## [1] 4207.27
```

#### 4. Variancia Nao Viesada

```
variancia_pf <- var(preco_fechamento)
variancia_pf

##           GSPC.Close
## GSPC.Close    72749.01
```

#### 5. Desvio-padrao

```
desv_pad_pf <- sd(preco_fechamento)
desv_pad_pf

## [1] 269.7202
```

#### 6. Grafico de linha do Preco de Fechamento

```
ggplot(dados.dj, aes(x = index(dados.dj), y = preco_fechamento)) + geom_line() +
  labs(title="Grafico do SP 500", subtitle="Preco de Fechamento", caption="Fonte: http") +
  theme(plot.title = element_text(hjust = 0.5), plot.subtitle = element_text(hjust = 0.5)) +
  scale_x_date(date_labels = "%b %y", date_breaks = "1 month")

## Error in ggplot(dados.dj, aes(x = index(dados.dj), y = preco_fechamento)): object 'dados.dj' not found
```

#### 7. Retorno, com base no Preco de Fechamento

```
retorno_pf <- (preco_fechamento - shift(preco_fechamento, 1L, type="lag"))/shift(preco_fechamento, 1L, type="lag")
retorno_pf <- na.omit(retorno_pf)
tabela_preco_retorno <- cbind(preco_fechamento, retorno_pf)
head(tabela_preco_retorno)

##           GSPC.Close    GSPC.Close.1
## 2022-01-03    4796.56             NA
## 2022-01-04    4793.54 -0.0006296221
## 2022-01-05    4700.58 -0.0193927578
## 2022-01-06    4696.05 -0.0009637689
## 2022-01-07    4677.03 -0.0040502168
## 2022-01-10    4670.29 -0.0014410312
```

#### 8. Grafico de linha do Retorno

```
ggplot(retorno_pf, aes(x = index(retorno_pf), y = 100*retorno_pf)) + geom_line() +
  labs(title="Grafico do SP 500", subtitle="Retorno", caption="Fonte: https://finance.yahoo.com") +
  theme(plot.title = element_text(hjust = 0.5), plot.subtitle = element_text(hjust = 0.5)) +
  scale_x_date(date_labels = "%b %y", date_breaks = "1 month")

## Don't know how to automatically pick scale for object of type xts/zoo. Defaulting to continuous scale.
## plot of chunk unnamed-chunk-11
```

## 9. Box plot para dados originais (Preco de Fechamento e Retorno) e padronizados

```
boxplot_pf <- ggplot(data = preco_fechamento, aes(x = "", y = preco_fechamento))+  
  geom_violin(trim = FALSE, color="blue") +  
  geom_boxplot(width=0.4, color="blue", alpha = 1, outlier.size = 1) +  
  labs(x = "Preco", y = "") +  
  scale_y_continuous(breaks = seq(16, 23, by = 1))  
  
z_preco_fechamento <- (preco_fechamento - mean(preco_fechamento)) / sd(preco_fechamento)  
  
boxplot_z_pf <- ggplot(data = z_preco_fechamento, aes(x = "", y = z_preco_fechamento)) +  
  geom_violin(trim = FALSE, color="goldenrod3") +  
  geom_boxplot(width=0.4, color="red", alpha = 1, outlier.size = 1)+  
  labs(x = "Preco Padronizado", y = "") +  
  scale_y_continuous(breaks = seq(-5, 23, by = 1))  
  
boxplots_pf <- ggarrange(boxplot_pf, boxplot_z_pf, ncol = 2, nrow = 1)  
annotate_figure(boxplots_pf, top = text_grob("Boxplot/Violplot do Preco de Fechamento\ne Preco",  
  color = "black", size = 14),  
  bottom = text_grob("Fonte: https://finance.yahoo.com/", color = "black", size = 10))
```

plot of chunk unnamed-chunk-12

```
boxplot_retorno <- ggplot(data = retorno_pf, aes(x = "", y = 100*retorno_pf)) +  
  geom_violin(trim = FALSE, color="blue") +  
  geom_boxplot(width=0.4, color="blue", alpha = 1, outlier.size = 1) +  
  labs(x = "Retorno (%)", y = "") +  
  scale_y_continuous(breaks = seq(-7, 6, by = 2))  
  
z_retorno_pf <- (retorno_pf - mean(retorno_pf))/(sd(retorno_pf))  
  
boxplot_z_retorno_pf <- ggplot(data = z_retorno_pf, aes(x = "", y = z_retorno_pf)) +  
  geom_violin(trim = FALSE, color="red") +  
  geom_boxplot(width=0.4, color="red", alpha = 1, outlier.size = 1) +  
  labs(x = "Retorno Padronizado", y = "") +  
  scale_y_continuous(breaks = seq(-3, 11, by = 2))  
  
boxplots_retorno <- ggarrange(boxplot_retorno, boxplot_z_retorno_pf, ncol = 2, nrow = 1)  
annotate_figure(boxplots_retorno, top = text_grob("Boxplot/Violplot do Retorno\ne Retorno Padronizado",  
  color = "Black", face = "bold", size = 14),  
  bottom = text_grob("Fonte: https://finance.yahoo.com/",  
  color = "black", hjust = 1.02, x = 1, size = 10))
```

plot of chunk unnamed-chunk-12

## 10. Histograma para dados originais (Preco de Fechamento e Retorno) e padronizados

```

histograma_pf <- ggplot(data = preco_fechamento, aes(x = preco_fechamento)) +
  geom_histogram(color="blue", fill = "white", bins = 30) +
  labs(y = "Quantidade", x = "Preco") +
  scale_x_continuous(breaks = seq(17, 22, by = 0.5)) +
  scale_y_continuous(breaks = seq(0, 30, by = 5)) +
  theme(plot.title = element_text(hjust = 0.5))

histograma_z_pf <- ggplot(data = z_preco_fechamento, aes(x = z_preco_fechamento)) +
  geom_histogram(color="red", fill = "white", bins = 30) +
  labs(y = "Quantidade", x = "Preco Padronizado") +
  scale_x_continuous(breaks = seq(-2, 3.5, by = 0.5)) +
  scale_y_continuous(breaks = seq(0, 50, by = 5)) +
  theme(plot.title = element_text(hjust = 0.5))

histogramas_pf <- ggarrange(histograma_pf, histograma_z_pf, ncol = 1, nrow = 2)
annotate_figure(histogramas_pf, top = text_grob("Histograma do Preco de Fechamento",
  color = "Black", face = "bold", size = 14),
  bottom = text_grob("Fonte: https://finance.yahoo.com/",
  color = "black", hjust = 1.02, x = 1, size = 10))

```

plot of chunk unnamed-chunk-13

```

histograma_retorno <- ggplot(data = retorno_pf, aes(x = 100*retorno_pf)) +
  geom_histogram(color="blue", fill = "white", bins = 25) +
  labs(y = "Quantidade", x = "Retorno (%)") +
  scale_x_continuous(breaks = seq(-6, 6, by = 1)) +
  scale_y_continuous(breaks = seq(0, 40, by = 5)) +
  theme(plot.title = element_text(hjust = 0.5))

histograma_z_retorno <- ggplot(data = z_retorno_pf, aes(x = z_retorno_pf)) +
  geom_histogram(color="red", fill = "white", bins = 25) +
  labs(y = "Quantidade", x = "Retorno Padronizado") +
  scale_x_continuous(breaks = seq(-6, 6, by = 1)) +
  scale_y_continuous(breaks = seq(0, 35, by = 5)) +
  theme(plot.title = element_text(hjust = 0.5))

histogramas_retorno <- ggarrange(histograma_retorno, histograma_z_retorno, ncol = 1, nrow = 2)
annotate_figure(histogramas_retorno, top = text_grob("Histograma do Retorno",
  color = "Black", face = "bold", size = 14),
  bottom = text_grob("Fonte: https://finance.yahoo.com/",
  color = "black", hjust = 1.02, x = 1, size = 10))

```

plot of chunk unnamed-chunk-13

## 11. QQPlot do retorno.



```
qqplot_retorno <- ggplot(data = retorno_pf, aes(sample = 100*as.vector(retorno_pf))) +
  stat_qq(size = 0.6) + labs(x = "Quantis Teoricos", y = "Quantis Am")
  title = "QQPlot do Retorno (%)") + theme(plot.title = element_text(
  scale_y_continuous(breaks = seq(-6, 4.5, by = 1.5))
```

## 12. QQLine do retorno (fazer junto com o QQPlot).

```
histograma_retorno_qqplot <- ggplot(data = retorno_pf, aes(x = 100*retorno_pf)) +
  geom_histogram(aes(y=..density..), color="blue", fill =
  stat_function(fun = dnorm, args = list(mean = mean(100
  col="red", lwd=1)) + theme(axis.text.x = element_blank(),
  labs(y = "", x = ""))

qqplot_linha_retorno <- ggplot(data = retorno_pf, aes(sample = 100*as.vector(retorno_pf))) +
  stat_qq(size = 0.6) + labs(x = "Quantis Teoricos", y = "Quantis Am")
  theme(plot.title = element_text(hjust = 0.5)) + scale_y_conti
  stat_qq_line(col = 2, lwd=1, lty=1)

plot_principal <- qqplot_linha_retorno

plot_para_inserir <- histograma_retorno_qqplot

plot.com.insercao <- ggdraw() + draw_plot(plot_principal) + draw_plot(plot_para_inserir, x
## Don't know how to automatically pick scale for object of type xts/zoo. Defaulting to cont
plot.com.insercao
```

plot of chunk unnamed-chunk-15

## 13. Assimetria amostral nao viesada do retorno.

```
n <- length(retorno_pf)
somatorio <- c()
for(i in 1:n){
  somatorio[i] <- ((retorno_pf[i] - mean(retorno_pf))/ sd(retorno_pf))^3
}
p1_s3 <- n/((n -1)*(n-2))
p2_s3 <- sum(somatorio)
s3 <- p1_s3*p2_s3
s3
## [1] -0.212796
```

## 14. Curtose amostral nao viesada do retorno.

```
n <- length(retorno_pf)
somatorio <- c()
for(i in 1:n){
```

```

    somatorio[i] <- ((retorno_pf[i] - mean(retorno_pf))/ sd(retorno_pf))^4
  }
  p1_s4 <- (n*(n +1))/((n -1)*(n-2)*(n-3))
  p2_s4 <- (sum(somatorio))
  p3_s4 <- (3*((n-1)^2))/((n-2)*(n-3))
  s4 <- p1_s4 * p2_s4 - p3_s4
  s4
## [1] -0.1196638

library("knitr")
knit("./q1/q1_sp500.rmd", output = "./q1/q1_sp500.md")
## Warning in file(con, "r"): cannot open file './q1/q1_sp500.rmd': No such file or director
## Error in file(con, "r"): cannot open the connection

```