

Obtaining current-voltage characteristic with Keithley 2602B through GPIB and RS232 on Python (with Numerical Analysis)

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Abstract

The goal of this study was to obtain a current-voltage characteristic with the SMU Keithley 2602B through GPIB and RS232 protocols using Python.

1 Device features and commands used

1.1 Keithley 2602B

1.2 Technical Specifications

Keithley 2602B (Fig. 1) is a **Source Measure Unit**[1], in other words it is an equipment that allows the user to use it as a source and measure at the same time.

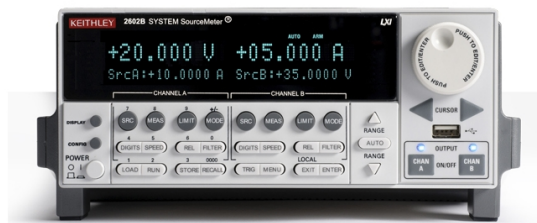


Figure 1: Keithley 2602B. (Source:<https://assets.tequipment.net>)

The Keithley 2602B is composed by two input/output (called smu a and smu b) channels that can be simultaneously used. The user is able to communicate with the device through either USB, GPIB, RS232.

1.3 Coding Interface

1.3.1 General Commands

The general commands in the Keithley 2602B follow the IEEE Std 488.2. These common commands that are supported by the SMU are listed in Table 1. Although commands are shown in uppercase, common commands are not case sensitive and either uppercase or lowercase can be used. Note that although these commands are essentially the same as those defined by the IEEE Std 488.2 standard, the Series 2600B does not strictly conform to that standard.[2]

As an example, on Python the code for obtaining the device identification **IDN?* would look like:

```
1 print(keithley.query("*IDN?"))
```

Code	Name	Description
*IDN?	Identification query	Gives the identification tag of the device
*RST	Reset command	Returns the Series 2600B to default conditions
*TST?	Self-test query	Returns a 0
*CLS	Clear status	Clears all event registers and Error Queue
*TRG	Trigger command	Generates the trigger.EVENT.ID trigger event for use with the trigger model.
*OPC	Operation complete command	Set the Operation Complete bit in the Standard Event Register after all pending commands, including overlapped commands, have completed

Table 1: General Commands

1.3.2 Device Specific Commands

The specific commands that were used to operate the equipment are listed in Table 2.

2 First tests and Communication through MAX

In order to assure that the connection with the device is well established, a series of primary tests is performed. For these tests we used the software Measurement & Automation Explorer (MAX) provided by National Instruments (Fig. 2).

MAX Visa Test Panel (Fig. 3) provides the user with a simple GUI to connect with the device and execute the first series of tests and check if the connection is well established.

3 Python Program

In order to explain the whole program, first, a short description of the libraries and the functions will be given.

3.1 Libraries used

A list of libraries that were imported in Python and necessary to the execution of the code that follows is shown below and a brief description of the library is given. Libraries:

- **matplotlib.pyplot**: Provides a MATLAB-like plotting framework inside matplotlib
- **numpy**: adds support for large, multi-dimensional arrays and matrices, along with a large collection of high-level mathematical functions to operate on these arrays
- **visa**: enables you to control all kinds of measurement devices independently of the interface (e.g. GPIB, RS232, USB, Ethernet)
- **tkinter**: standard Python interface to the Tk GUI toolkit
- **time**: provides various time-related functions

Code	Description
<code>beeper.enable=0</code>	deactivate machine beep
<code>smuX.reset()</code>	reset all the input/output channels (smu)
<code>smuX.source.output = smuX.OUTPUT_ON</code>	turn on the smu X as an output (a or b)
<code>smuX.source.output = smuX.OUTPUT_OFF</code>	turn off the smu X as an output (a or b)
<code>smuX.measure.count = NB_OF_MEASUREMENTS</code>	specifies the number of measurements to be stored in the buffer
<code>smuX.source.levelv = VOLTAGE</code>	adjust voltage of smu X to the desired level
<code>print(smuX.measure.i())</code>	return value of current I measured on smu X
<code>smuX.source.func = smuX.OUTPUT_DCVOLTS</code>	set smu X as DC voltage output

Table 2: Keithley 2602B Specific Commands. Source:[2]

3.2 Functions

The following list of functions lists the functions that are part of the program with its parameters and specifications.

- **connexion_choice(connection)**: enables the user to choose between GPIB, RS232, USB and connects with the device.
connection: *string*, contains the identifier of the connection
- **close_all()**: close any connection
- **reset()**: resets both the smuX's to the default state
- **switchON(smux[, onoff=False])**: allows the user to turn on or off the smuX chosen
smux: *string*, chosen smuX ('a' or 'b')
onoff: *string*, [Optional] True to turn on and False to Turn off. Default: False
- **measurement(smux,volts_min,volts_max,nb)**: sends the voltage to the device and measures the current

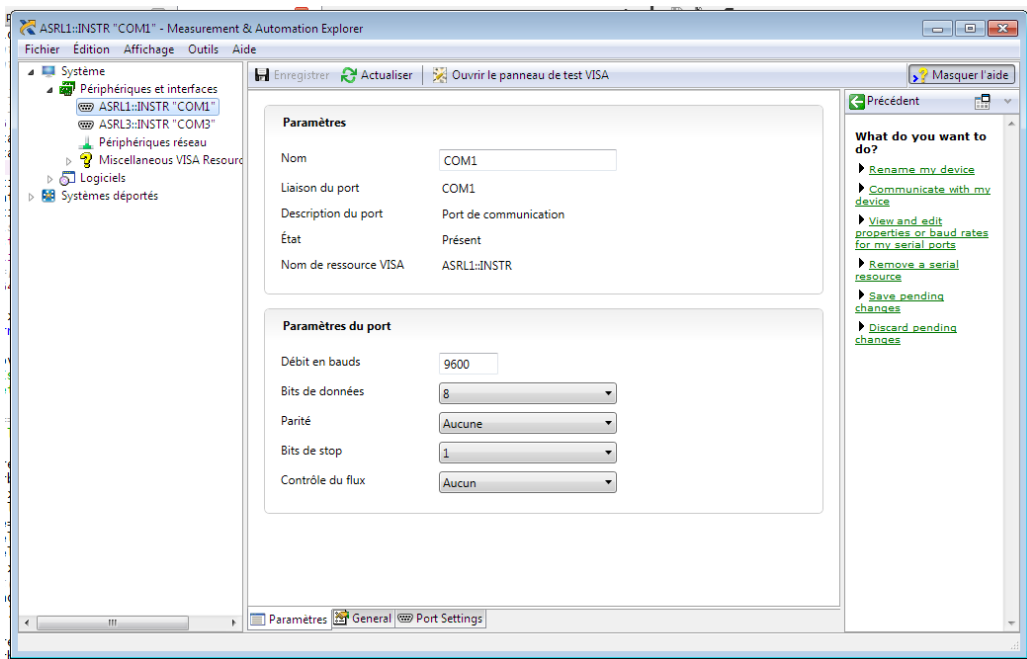


Figure 2: MAX Interface

smux: *string*, chosen smuX ('a' or 'b')

volts_min: *float*, initial output voltage that is sent to the circuit

volts_max: *float*, final output voltage that is sent to the circuit

nb: *int*, number of measurements

RETURNS: *float* measure of current in Amps

- **complete_measure(smux,volts_min,volts_max,nb):** calls other functions in order to automatically make all the measurements

smux: *string*, chosen smuX ('a' or 'b')

volts_min: *float*, initial output voltage that is sent to the circuit

volts_max: *float*, final output voltage that is sent to the circuit

nb: *int*, number of measurements

RETURNS: *list* [input voltage(*float*), measure of current in Amps(*float*)]

3.3 Code

First of all, the libraries described beforehand need to be imported

```

1 import visa
2 import numpy as np
3 import matplotlib.pyplot as plt
4 from tkinter import Button, Tk, Frame, Entry, Label, Checkbutton, BooleanVar, StringVar
5 import time

```

Then we use a series of functions to perform individual tasks. These functions are thoroughly described in the Section 3.2.

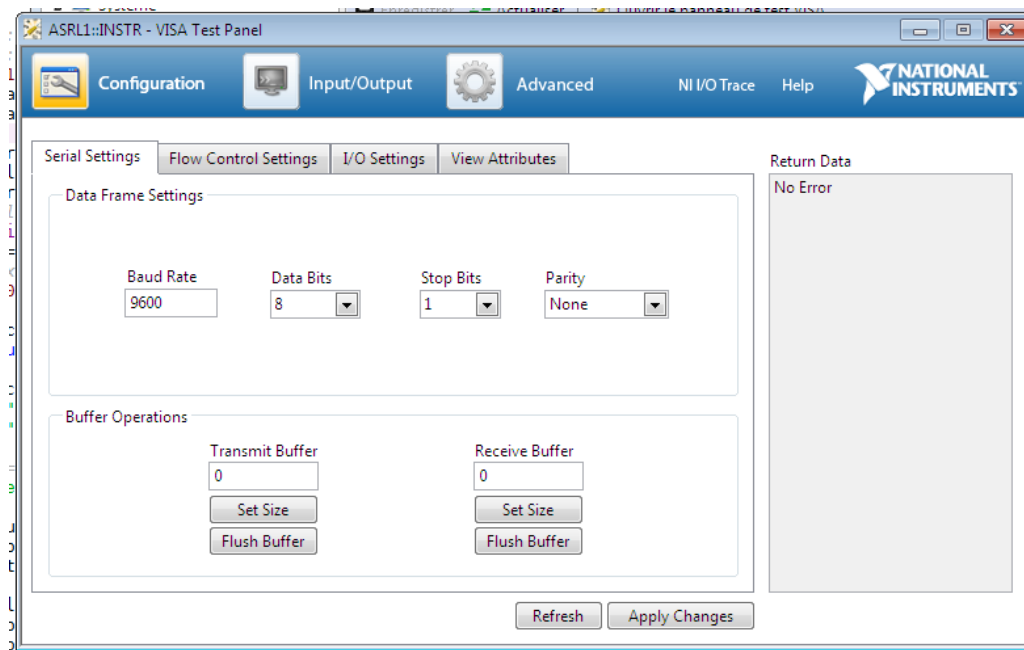


Figure 3: MAX - VISA Test Panel

```

6  def connexion_choice(connexion):
7      """Permet de choisir la connexion
8      \nAllow to choose the connexion"""
9      global keithley
10     try:
11         rm = visa.ResourceManager() #import visa
12         rm.list_resources() #import visa
13         keithley = rm.open_resource(connexion)
14     except:
15         print("Connexion error, check the connexion (GPIO,RS232,USB,Ethernet) and it's
16             ↪ number")
17         raise StopIteration ("Erreur de connexion. Verifier la connexion
18             ↪ (GPIO,RS232,USB,Ethernet) et son numeros \
19             \nConnexion error, check the connexion
20             ↪ (GPIO,RS232,USB,Ethernet) and it's number")
21     #-----
22     def close_all():
23         """Coupe la connexion
24         \nClose the connexion"""
25         try:
26             reset() #reset de fin
27             keithley.write("beeper.enable=0") #desactive le beep
28             keithley.close() #ferme la connexion
29             print("Connexion closed")
30         except:
31             print("Closing error")
32             raise StopIteration ("Erreur de fermeture \
33                 \nClosing error")
34     #-----
35     def reset():

```

```

33     """reset les smu"""
34     try:
35         keithley.write("smua.reset()")
36         keithley.write("smub.reset()")
37     except:
38         print("Reset error")
39         raise StopIteration ("Erreur de reset \
40                               \nReset error")
41 #-----
42 def switchON(smux, onoff=False):
43     """Active/desactive le smu
44     \nTurn on/off the smu"""
45     try:
46         keithley.write(("smu%s.source.output = smu%s.OUTPUT_ON" if onoff else
47             ↪ "smu%s.source.output = smu%s.OUTPUT_OFF") % (smux, smux))
48         print("Source on" if onoff else "Source off")
49     except:
50         print("Source can't be turn on/off")
51         raise StopIteration ("Erreur de changement d'etats \
52                               \nSource can't be turn on/off")
53 #-----
54 def measurement(smux,volts_min,volts_max,nb,delay=0):
55     """Envoi des tensions et mesure des courants. Enregistre les mesures dans la
56     ↪ variable measure
57     \nSend tensions and measure currents. Save measures in measure variable"""
58     measure=[] #creat array for futur measures
59     tension_input=np.linspace(volts_min,volts_max,nb) #creat an array with all tensions
60     ↪ needed for measurement
61     print('U(V)\t I(A)\t\t points\ttemps(s)') #display tension,current,points,time
62     time_begin=time.time()
63     i=0
64     for x in tension_input: #loop on tensions values
65         i+=1
66         keithley.write("smu%s.source.levelv = %f" % (smux,x)) #send the voltage x to
67         ↪ the smu
68         time.sleep(delay) #delay not needed
69
70         y=float(keithley.query("print(smu%s.measure.i())" % smux)) #read current value
71         ↪ I(A)
72         time_end=time.time()
73         print ("%3.3f\t%s\t%s/%s\t%3.3f" % (x,y,i,nb,time_end-time_begin)) #display
74         ↪ tension,current,points,time
75         if y>0.2:
76             close_all()
77             print("current too high")
78             raise ValueError ("current too high") #used as safety if the volt protection
79             ↪ fail (Redundancy)
80         measure.append(y) #add the current value to a array regrouping all measurements
81
82     return tension_input,measure #return the voltage and current array
83 #-----

```

```

77 def complete_measure(smux,volts_min,volts_max,nb,delay=0):
78     """Fonction principale prenant les valeurs de tkinter en entrant. Trace les mesures
    ↪ et les sauvegardes.
79     Principal fonction taking tkinter value as input. Plot measures and save them."""
80     switchON(smux, True) #active smua
81
82     keithley.write("smu%s.source.func = smu%s.OUTPUT_DCVOLTS" % (smux,smux)) #smua
    ↪ devient source de tension (et donc ne peut être que mesure de courant)
83     tension_input,measure=measurement(smux,volts_min,volts_max,nb) #envoi les tensions
    ↪ choisis et mesure les courants associés
84     keithley.write("smu%s.source.levelv = 0" % smux)
85
86     plt.figure(num='Diode '+smux+' Characteristic') #plot different figure according to
    ↪ a specific name
87     plt.clf() #clear the graph to avoir superposing data from the same set (can be
    ↪ deactivated if need to superpose)
88     plt.title("Diode "+smux+" Characteristic")
89     plt.ylabel('I(A)')
90     plt.xlabel('U(V)')
91     plt.plot(tension_input,measure, '+', label='Diode '+smux) #display
    ↪ current(input_tension) with dots
92     plt.legend() #add legend to the graph (take label from plot)
93     plt.savefig('Diode %s Characteristic I(U).svg' %smux, format='svg', dpi=1000,
    ↪ bbox_inches='tight') #save the graph in a vector file
94     plt.show() #plot data
95
96     np.savetxt('Diode %s Characteristic I(U).csv' %
    ↪ smux,np.transpose((tension_input,measure)),delimiter="\t") #newline='\n'
97     switchON(smux, False) #deactivate smu

```

After defining the functions, we attribute values to the variables, raising an error if the voltage passes the chosen limit:

```

98     connexion='GPIB0::26::INSTR'
99     connexion='COM1'
100     volts_min=0 #min voltage
101     nb=101 #nb of measurements
102     volts_max=1 # max voltage
103     delay=0 #time between measurements
104     smux='a'
105
106     if abs(volts_max)>10:
107         close_all()
108         raise ValueError ("ERROR: Too much voltage.")
109
110     connexion_choice(connexion)
111
112     reset() #reset both smu
113     keithley.write("beeper.enable=0") #deactivate the beep

```

And finally we execute the TKinter code:

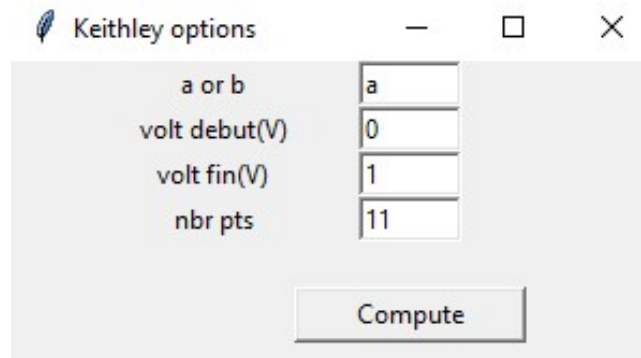


Figure 4: GUI TKinter with measurement options

```

114 def compute():
115     global delay
116     message1["text"] = ""
117     message2["text"] = ""
118     message3["text"] = ""
119     message4["text"] = ""
120     message5["text"] = ""
121     message6["text"] = ""
122     message7["text"] = ""
123     try:
124         smux=str(smux_entry.get())
125         if smux != 'a' and smux != 'b':
126             raise ValueError
127         try:
128             volts_min=float(volt_min_entry.get()) #min voltage
129             volts_max=float(volt_max_entry.get()) # max voltage
130             if abs(volts_max)>10 or abs(volts_min)>10:
131                 texte5="abs(volt) <=10"
132                 message5["text"] = texte5
133                 print(texte5)
134             else:
135                 nb=int(point_number_entry.get()) #nb de mesures
136                 if nb<1:
137                     texte4="nb>0"
138                     message4["text"] = texte4
139                     print(texte4)
140                 else:
141                     # delay=float(delay_entry.get()) #temps entre mesures en secondes
142                     print(smux,volts_min,volts_max,nb,delay)
143                     try:
144                         ""
145
146                     ↪ tension_input,measure=complete_measure(smux,volts_min,volts_max,nb)
147                     close_all()
148                     texte7="Measures done"
149                     message7["text"] = texte7
150                     print(texte7)

```



```

150         except:
151             reset() #give float error if can't close but actually is
152                     ↪ connection error
153             texte6="Unknown error detected"
154             message6["text"] = texte6
155             print(texte6)
156
157     except:
158         texte2="floats"
159         message2["text"] = texte2
160         print(texte2)
161
162 except:
163     texte="a or b"
164     message1["text"] = texte
165     print(texte)
166
167 root = Tk()
168 frame = Frame(root)
169 root.title("Keithley options")
170 frame.pack()
171
172 L0 = Label(frame, text="a or b")
173 L0.grid(row=0, column=0)
174 smux_entry = Entry(frame, textvariable=StringVar(frame, value='a'), bd =2, width=7)
175 smux_entry.grid(row=0, column=1)
176
177 message1 = Label(frame, text="") #allow to display message when activate [text]
178 message1.grid(row=0, column=3)
179
180 L1 = Label(frame, text="volt debut(V)")
181 L1.grid(row=1, column=0)
182 volt_min_entry = Entry(frame, textvariable=StringVar(frame, value=0), bd =2, width=7)
183 volt_min_entry.grid(row=1, column=1)
184
185 message3 = Label(frame, text="")
186 message3.grid(row=1, column=3)
187
188 L2 = Label(frame, text="volt fin(V)")
189 L2.grid(row=2, column=0)
190 volt_max_entry = Entry(frame, textvariable=StringVar(frame, value=1), bd =2, width=7)
191 volt_max_entry.grid(row=2, column=1)
192
193 message5 = Label(frame, text="")
194 message5.grid(row=2, column=3)
195
196 L3 = Label(frame, text="nbr pts")
197 L3.grid(row=3, column=0)
198 point_number_entry = Entry(frame, textvariable=StringVar(frame, value=11), bd =2,
199                             ↪ width=7)
200 point_number_entry.grid(row=3, column=1)
201
202 message4 = Label(frame, text="")

```

```

199     message4.grid(row=3, column=3)
200
201     message2 = Label(frame, text="")
202     message2.grid(row=4, column=3)
203
204     message6 = Label(frame, text="")
205     message6.grid(row=5, column=3)
206
207     compute_button = Button(frame, text="Compute", width=14, command=compute)
208     compute_button.grid(row=5, column=1)
209
210     message7 = Label(frame, text="")
211     message7.grid(row=5, column=3)
212
213
214     root.mainloop()
215     close_all()

```

The GUI can be seen on Fig. 4.

After the clicking on "Compute", a csv file with the data for the voltage and current, and a pdf chart are saved on the same folder as the python code; and the chart is shown with matplotlib.pyplot.

4 Numerical Analysis

In order to exploit the data, we studied the current-voltage characteristic of a PN diode. The set-up consists of a 100 Ohms resistance and a PN diode connected in series. Both ends are connected to the keithley. The code for the data acquisition is on Section 3.3 and the code for numerical analysis is seen further on Section 4.4.

4.1 Data obtained from a PN diode

First of all, the raw data is collected from the Keithley 2602B. The raw data includes the resistance that is in series, giving origin to a decreasing slope after voltage passes a certain point. The curve in logarithmic scale can be seen on Figure 5.

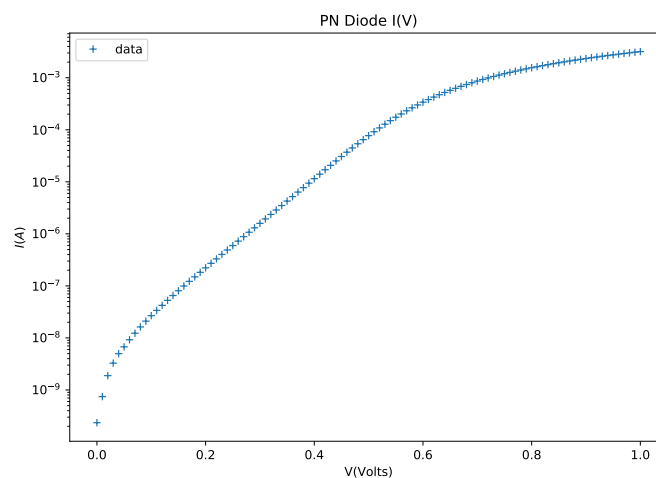


Figure 5: PN Diode Raw Data in logarithmic scale

Knowing that the resistance value is 100 Ohms, value that can also be found comparing experimental data to the Shockley's model, the precise value for the voltage can be found. The data is then corrected using the following formula:

$$V_{\text{diode}} = V_{\text{measured}} - RI_{\text{measured}}$$

The result seen on Figure 6 shows the corrected values. Now we can proceed to apply Shockley's model through a curve-fit and verify the curve fitness through a χ^2 Distribution.

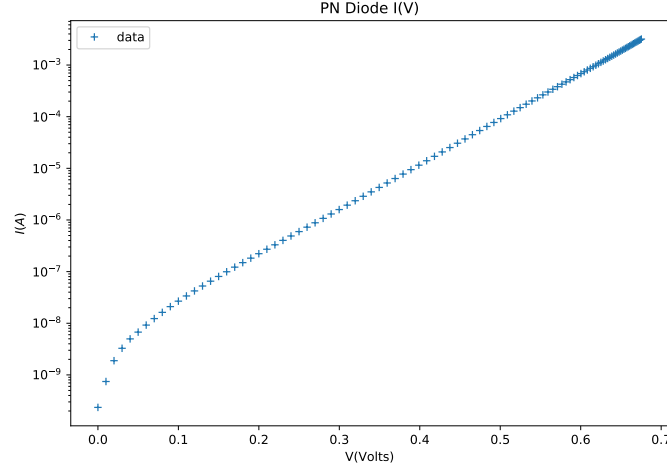


Figure 6: PN Diode Corrected Data in logarithmic scale

4.2 Curve-fit Optimization

The Python library that is used here to perform a curve-fit is **scipy.optimize.curve_fit**. It uses non-linear least squares to fit a function, f , to data.[3] The function requires only three parameters, but has several optional. The ones that are passed here are briefly explained on Table 3.

Parameter	Description
f : callable	The model function, $f(x, \dots)$. It must take the independent variable as the first argument and the parameters to fit as separate remaining arguments
xdata	The independent variable where the data is measured.
ydata	The dependent data

Table 3: **curve_fit** parameters that are used. Source:[3]

Now, in order to perform a curve-fit we need to select a stable region that follows the desired model on the curve. The model used here is the **Shockley's model**, whose relation is:

$$I = I_s \left(e^{\frac{V_d}{\eta V_T}} - 1 \right)$$

where V_d is the tension through the diode (previously noted V_{diode}), η is the ideality factor, I_s the saturation current and V_T the thermal voltage (25.85mV at 300K).

After establishing the model, the curve_fit is ready to be performed. Using the parameters specified in Section 4.4 we obtained the curve shown in Figure7.

4.3 χ^2 Method

The χ^2 distribution can be expressed in the following form:

$$\chi^2 = \sum_{j=1}^N \left(\frac{y_j - y(t_j, a, \dots)}{\Delta y_j} \right)^2$$

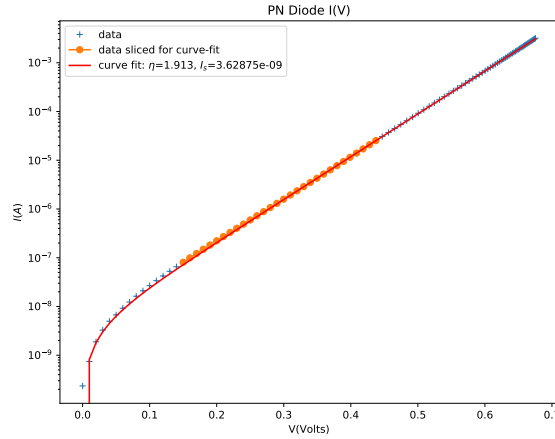


Figure 7: **curve.fit** on corrected data obtained from the PN diode

where N is the number of points, y_j is the obtained data, $y(t_j, a, \dots)$ is the curve with parameters t_j, a, \dots and r is the number of parameters.[4]

In the above given relation Δy_j is the absolute uncertainty. In the code both relative and absolute uncertainties are taken into account through a selection parameter. The function for the χ^2 Method includes the module **scipy.stats.chi2** and **numpy**.

```

1  from scipy.stats import chi2
2  import numpy as np
3
4  def
5      ↪ chi2_calc(f_exp,f_th,popt=None,f_exp_uncertainty=0.05,confiance=0.95,uncert_type=1,talkative=0):
6
7      if uncert_type==1:                                #percentage uncertainty
8          chi_squared=np.sum(((f_exp-f_th)/(f_exp_uncertainty*f_exp))**2)          #percent
9          ↪ uncertainty
10
11      elif uncert_type==0:
12          chi_squared=np.sum(((f_exp-f_th)/f_exp_uncertainty)**2)
13          ↪ uncertainty
14
15      else:
16          raise ValueError('Uncertainty type not accepted. \n Type uncert_type=1 for
17          ↪ percentage uncertainty, and uncert_type=0 for absolute uncertainty.')
18
19
20      if popt is not None:
21          degreesoffreedom=len(f_exp)-len(popt)
22          if uncert_type==1:
23              confiance=1-f_exp_uncertainty
24              chi2_lim=chi2.ppf(confiance,degreesoffreedom)
25              if talkative:
26                  print("Degrees of freedom : ",degreesoffreedom)
27                  print("chi2 ppf (according to degrees of freedom) : ",chi2_lim)
28                  print("chi2 calculated : ",chi_squared)
29              if chi2_lim>chi_squared:
30                  if talkative:
31                      print("Model is acceptable.")

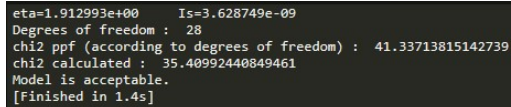
```

```

26         acceptance=True
27     else:
28         if talkative:
29             print("Model is not acceptable.")
30         acceptance=False
31
32     return acceptance,chi_squared

```

The χ^2 Method allowed us to test our curve fitness. A constant uncertainty of 5% was used. The results can be seen on Figure 8 and the code on Section 4.4 .



```

eta=1.912993e+00    Is=3.628749e-09
Degrees of freedom : 28
chi2 ppf (according to degrees of freedom) : 41.33713815142739
chi2 calculated : 35.40992440849461
Model is acceptable.
[Finished in 1.4s]

```

Figure 8: Results on command prompt for the χ^2 calculation.

4.4 Code

```

1  import matplotlib.pyplot as plt
2  import numpy as np
3  import math
4  from scipy.optimize import curve_fit
5  from scipy.stats import chi2
6
7
8  data=np.loadtxt("Diode a Characteristic I(U).csv")
9
10 xdata=data[:,0]
11 ydata=data[:,1]
12
13 resistance=102
14
15 xdata=xdata-resistance*ydata                                #correction v=v_bi-R*I
16
17 start=15                                                    #split data for
18     ↪ curve fit
19 interval=30
20 x=xdata[start:start+interval]
21 y=ydata[start:start+interval]
22
23 start_line=98                                              #split data for tracing
24     ↪ a straight line
25 interval_line=1
26 x_line=xdata[start_line:start_line+interval_line]
27 y_line=ydata[start_line:start_line+interval_line]
28
29 logarithm=True

```

```

30
31 if logarithm:
32
33     plt.semilogy(xdata,ydata,'+', label="data")
34     plt.semilogy(x,y,'-o', label="data sliced for curve-fit")
35     # plt.errorbar(xdata, ydata, xerr=0.05, yerr=0.05)
36 else:
37     plt.plot(xdata,ydata,'+', label="data")
38     plt.plot(x,y,'o', label="data")
39     # plt.errorbar(xdata, ydata, xerr=0.05, yerr=0.05)
40
41 def current(V, eta=10,Is=10E-10):
42
43     If=[]
44     Vt=25.85E-3
45     for i in V:
46         x=(i)/(eta*Vt)
47
48         If.append(Is*(math.exp(x)-1))
49
50
51     return If #return If:final-current
52
53
54 p0=(10,10E-10)
55 sigma=0.95*np.ones((len(x),))
56 popt, pcov = curve_fit(current, x,y,p0=p0,sigma=sigma)
57 print("eta=%e \t Is=%e"%(popt[0],popt[1]))
58
59 # def horizontal_line(x,b):                                     #used for tracing a straight
60     ↪ horizontal line (graphic calculus of resistance)
61     #         b=np.ones((len(x),))*b
62     #         return 0*x+b
63
64 # y2=horizontal_line(xdata,ydata[100])
65
66 if logarithm:
67     # plt.semilogy(xdata,y2)                                     #straight line
68     plt.semilogy(xdata, current(xdata, *popt), 'r-',label=r'curve fit: $\eta$=%5.3f,
69         ↪ $I_s$=%g' % tuple(popt))
70 else:
71     # plt.plot(xdata,y2)                                         #straight line
72     plt.plot(xdata, current(xdata, *popt), 'r-',label=r'curve fit: $\eta$=%5.3f,
73         ↪ $I_s$=%g' % tuple(popt))
74
75 def
76     ↪ chi2_calc(f_exp,f_th,popt=None,f_exp_uncertainty=0.05,confiance=0.95,uncert_type=1,talkative=0):
77
78     if uncert_type==1:                                         #percentage uncertainty

```

```

76         chi_squared=np.sum(((f_exp-f_th)/(f_exp_uncertainty*f_exp))**2)                                #percent
        ↪ uncertainty
77     elif uncert_type==0:
78         chi_squared=np.sum(((f_exp-f_th)/f_exp_uncertainty)**2)
        ↪ uncertainty
79     else:
80         raise ValueError('Uncertainty type not accepted. \n Type uncert_type=1 for
        ↪ percentage uncertainty, and uncert_type=0 for absolute uncertainty.')
81
82
83     if popt is not None:
84         degreesoffreedom=len(f_exp)-len(popt)
85         if uncert_type==1:
86             confiance=1-f_exp_uncertainty
87             chi2_lim=chi2.ppf(confiance,degreesoffreedom)
88             if talkative:
89                 print("Degrees of freedom : ",degreesoffreedom)
90                 print("chi2 ppf (according to degrees of freedom) : ",chi2_lim)
91                 print("chi2 calculated : ",chi_squared)
92             if chi2_lim>chi_squared:
93                 if talkative:
94                     print("Model is acceptable.")
95                 acceptance=True
96             else:
97                 if talkative:
98                     print("Model is not acceptable.")
99                 acceptance=False
100
101     return acceptance,chi_squared
102
103 acceptance,chi_squared=chi2_calc(y,current(x,*popt),popt=popt,f_exp_uncertainty=0.05,uncert_type=1,
    ↪ talkative=1)
104
105
106 plt.xlabel("V(Volts)")
107 # plt.title("Schottky Diode Characteristic : I(V)")
108 plt.title("PN Diode I(V)")
109 plt.ylabel(r"$I(A)$")
110
111 plt.legend()
112 plt.show()
113
114 # plt.savefig("m-schottky-curve%s.pdf"%(text))

```

5 GitHub Repository

This project was published on GitHub and is public under MIT License. The repository is accessible through this link <https://github.com/marcelrsoub/keithley-visa-measurements>.

References

- [1] Source measure unit, August 2018. Page Version ID: 854854432.
- [2] Series 2600b System SourceMeter Manual.
- [3] `scipy.optimize.curve_fit` — SciPy v1.2.1 Reference Guide.
- [4] George B. Arfken and Hans-Jurgen Weber. *Mathematical Methods for Physicists*. Elsevier, Acad. Press, Amsterdam, 6. ed., internat. ed., [5. nachdr.] edition, 2008. OCLC: 551222393.