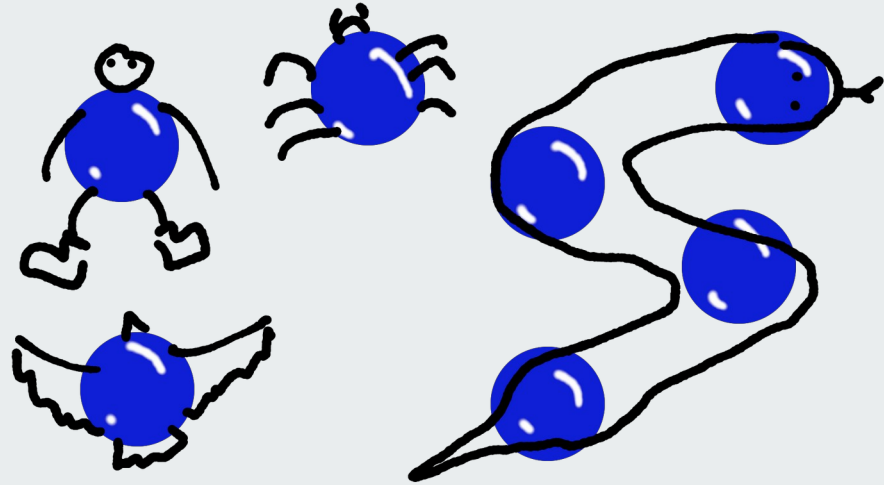




Birds, hikers, snakes and ants

Bio-inspired optimisation algorithms



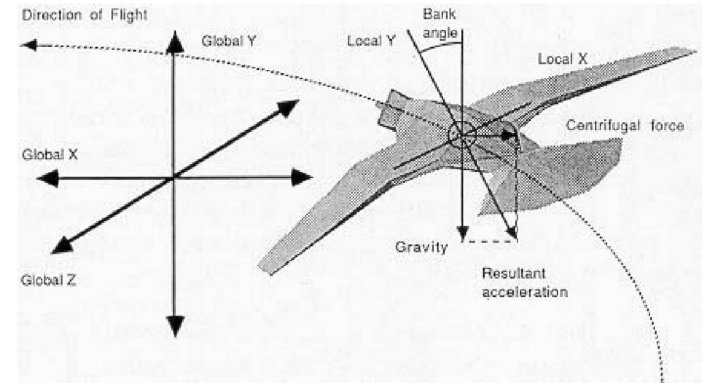
Animals are particles with simple behaviours

Reynolds introduced “Boids”, probably the first biological use of particles

Boids are particles (3D points in R^3 space)

They follow a simple logic:

- Follow,
- Avoid,
- Group





Boids

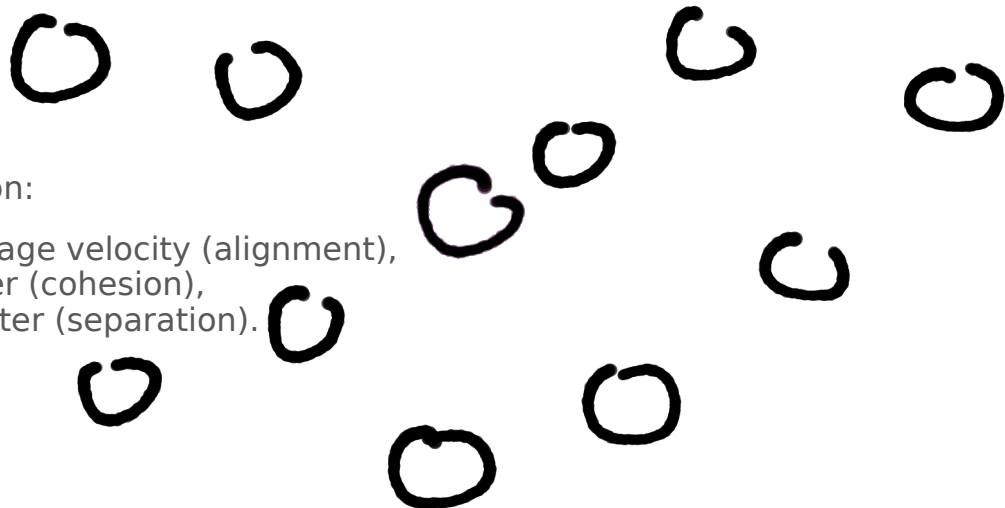
3 forces to change the particle's acceleration:

- a force in direction of neighbors' average velocity (alignment),
- a force in direction of neighbors center (cohesion),
- a force in opposition of neighbors center (separation).

And that's all!

[Little demo](#)

Local behaviour = global pattern



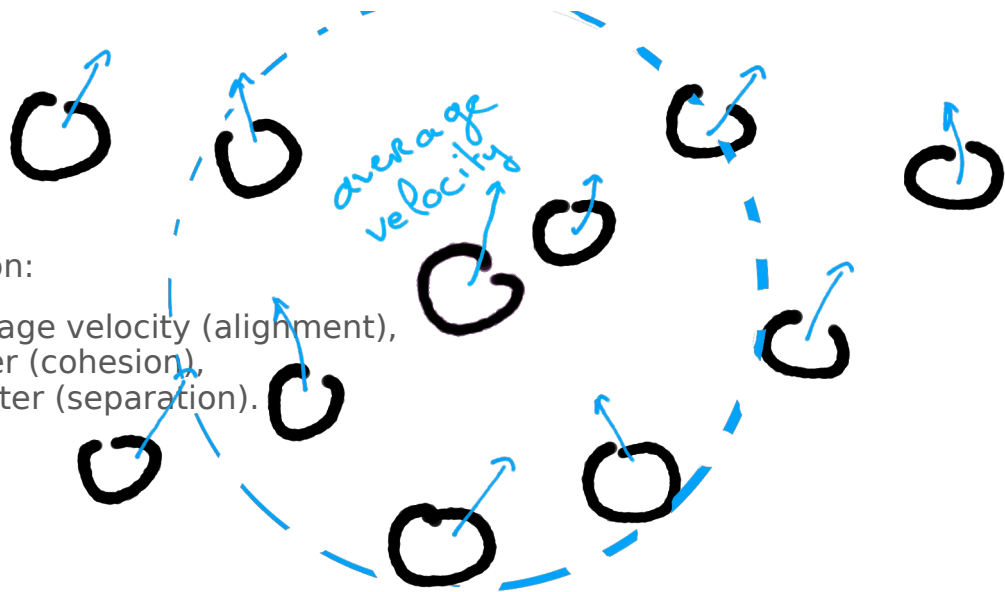
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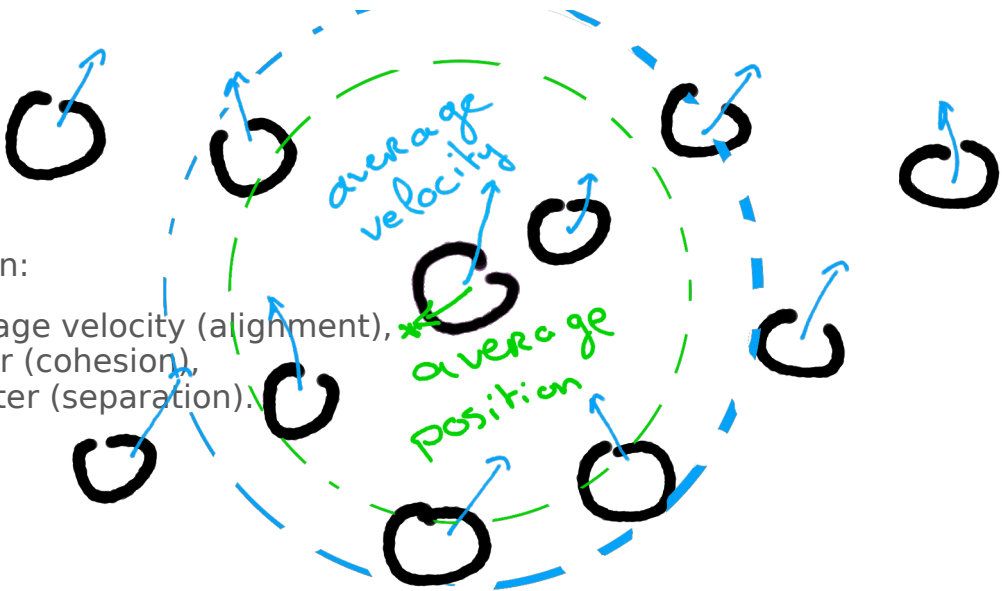
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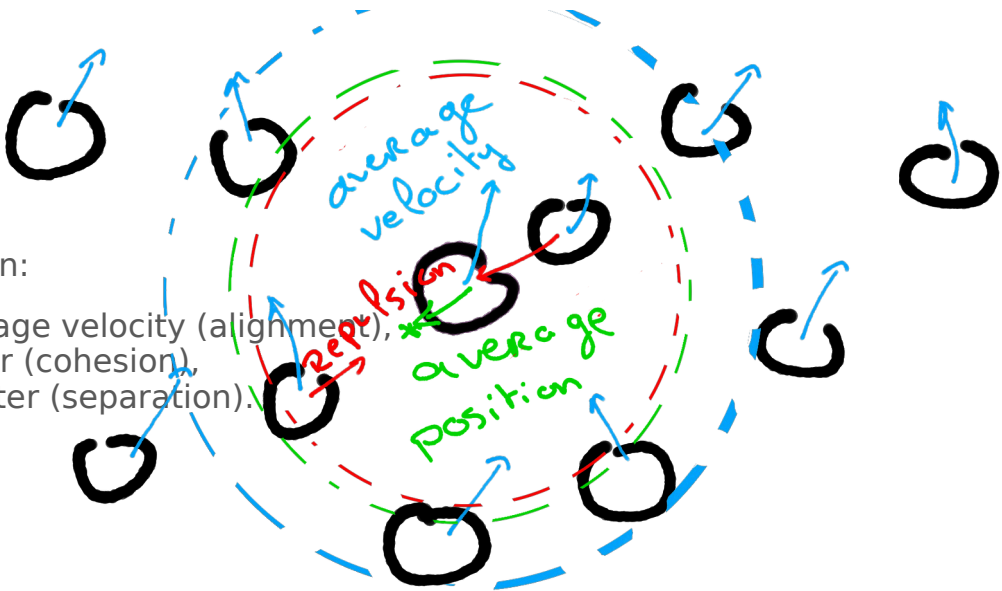
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[Little demo](#)



Local behaviour = global pattern

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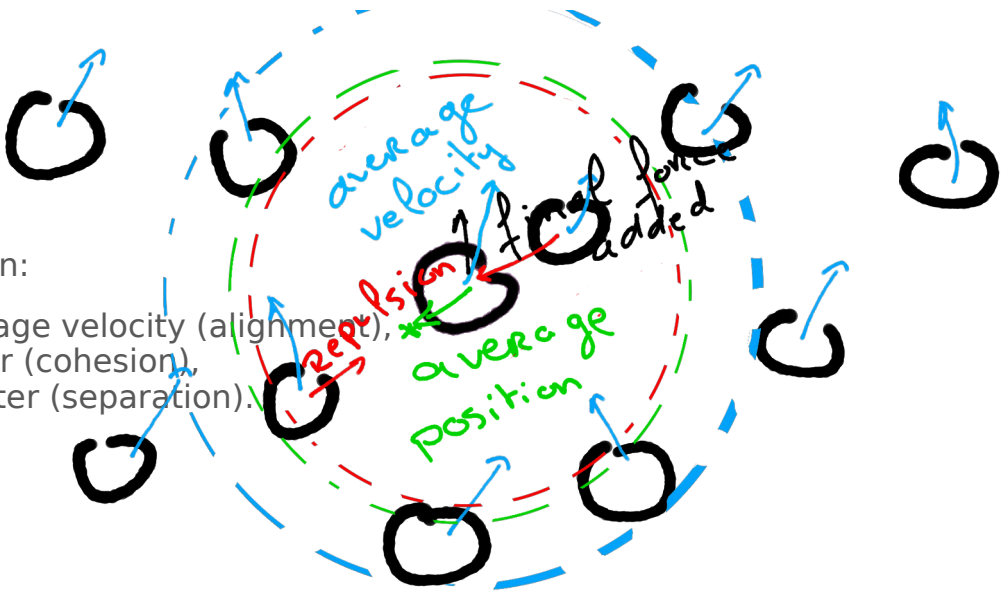
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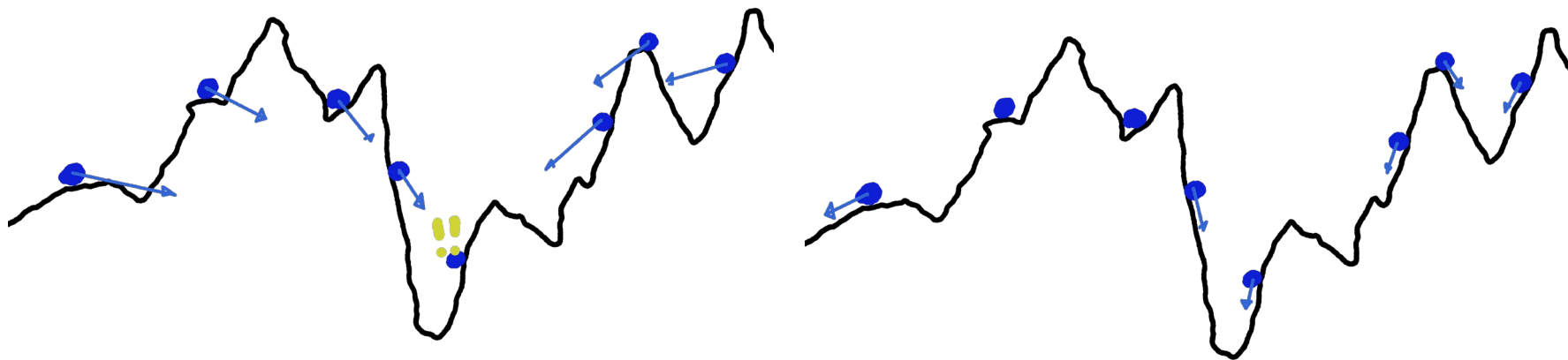


Social particles for optimisation

Particle Swarm Optimisation (PSO), a global minimum algorithm against Gradient Descent weaknesses.

No need for differentiation, no problem on non-differentiable function.

A single evaluation per step, even on N-dimensional spaces!



PSO idea

Algorithm:

Each particle has a position
Evaluate the function
Keep track of the best evaluation made so far
Move a little bit toward the group's best evaluation and your own best evaluation

[Little demo](#)

Gradient Descent idea

Algorithm:

Each particle has a position
Evaluate the function and the gradient <ul style="list-style-type: none">- You probably want to compute the finite difference method to compute the slope in each direction independently
Move in the direction of the gradient for an unknown distance <ul style="list-style-type: none">- If the slope is null, you're dead- If there is a discontinuity, you're dead- If the slope is gentle, it's going to be a long ride

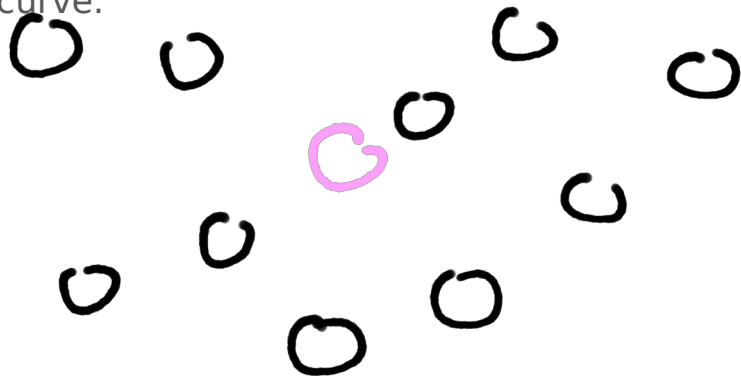
[Little demo](#)



Introduce neighborhood

Increase searching area by having interconnected subgroups: “neighborhoods”

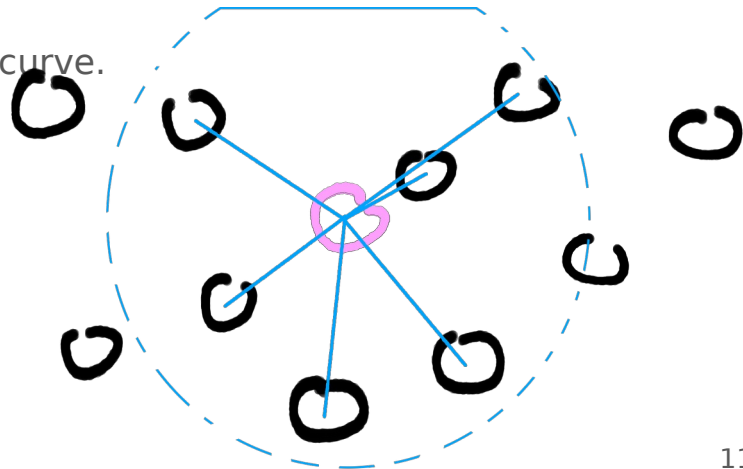
One of the simplest neighborhood: a simply connected curve.



Introduce neighborhood

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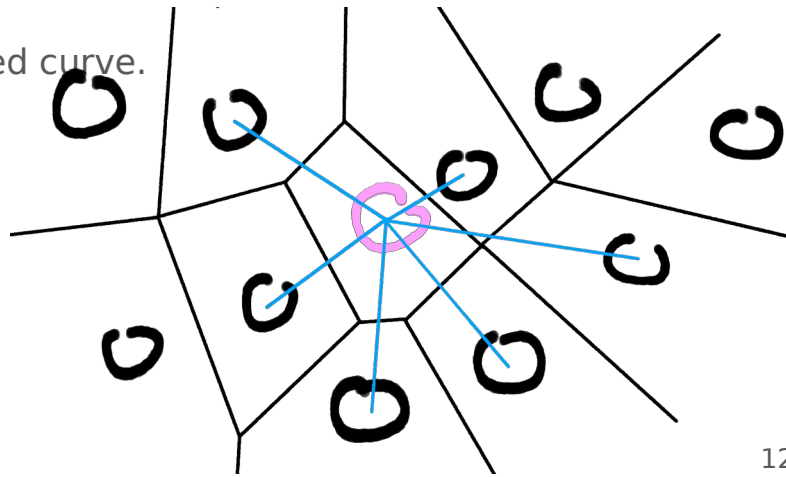
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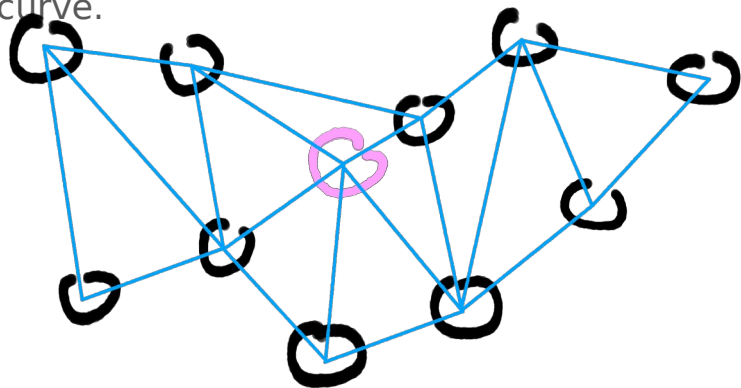
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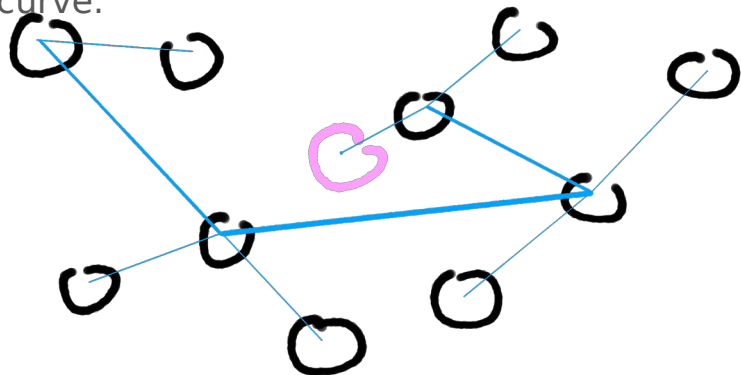
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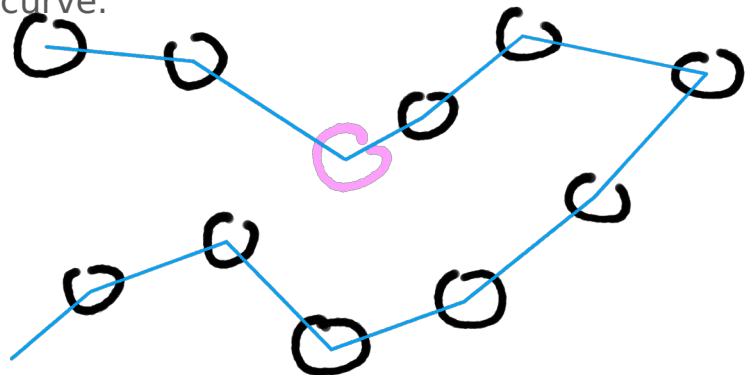
One of the simplest neighborhood: a simply connected curve.



Introduce neighborhood

Increase searching area by having interconnected subgroups: “neighborhoods”

One of the simplest neighborhood: a simply connected curve.





Local constraints instead of global constraints

We've seen that particles can locally create a global behaviour,

We've seen that particles can locally find optimal minimisations,

We'll see that particles can do both at once.



Snake, the active contours algorithm

Algorithm:

- Each particle is linked by springs with 2 neighbors
- Each particle follow the gradient of a function.

The end.

[Little demo](#)



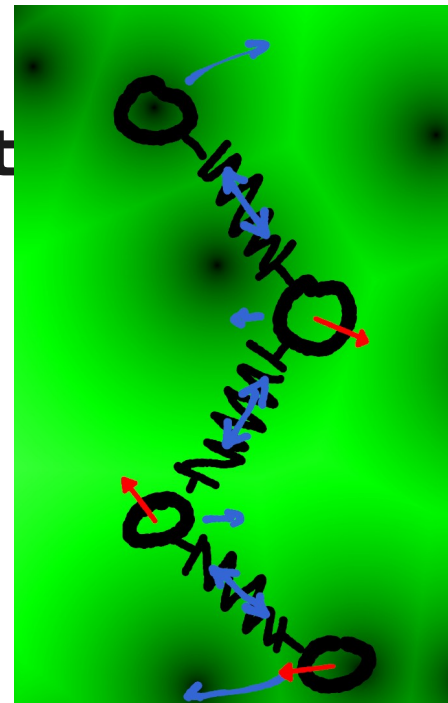
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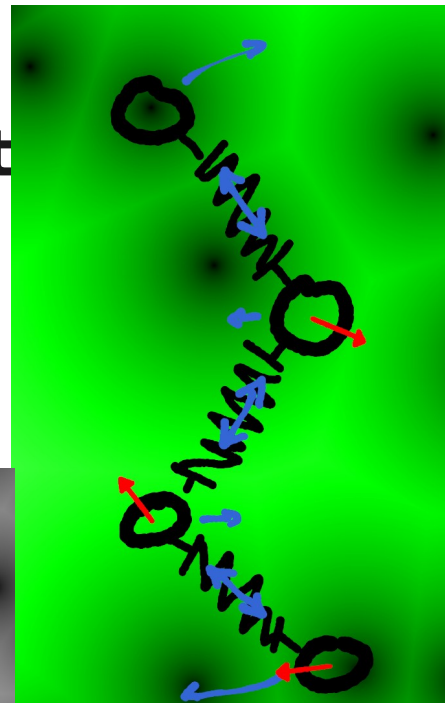
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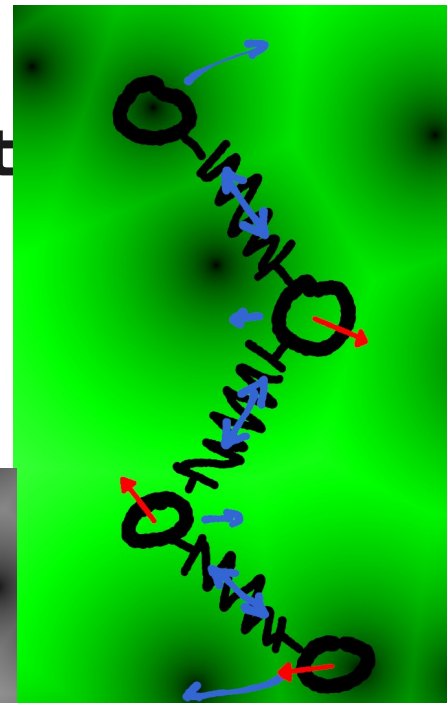
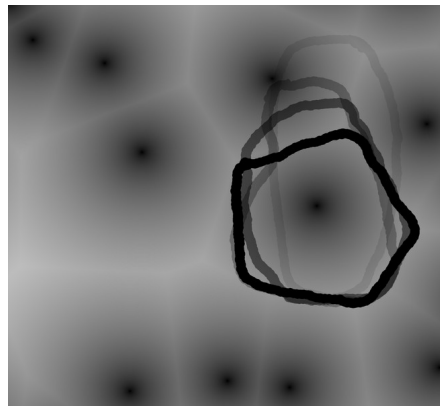
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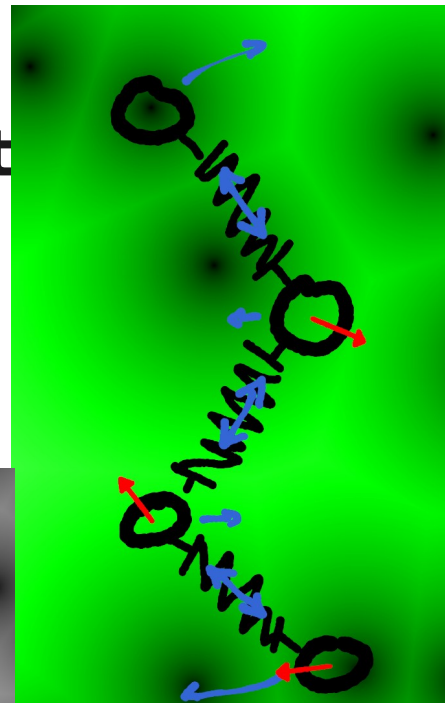
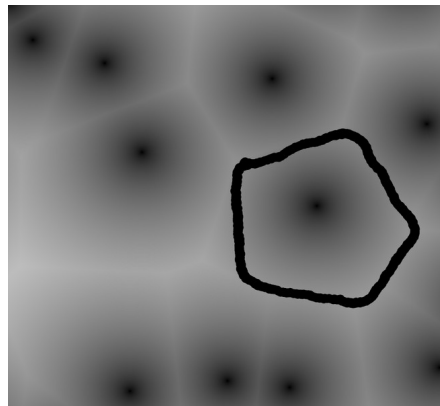
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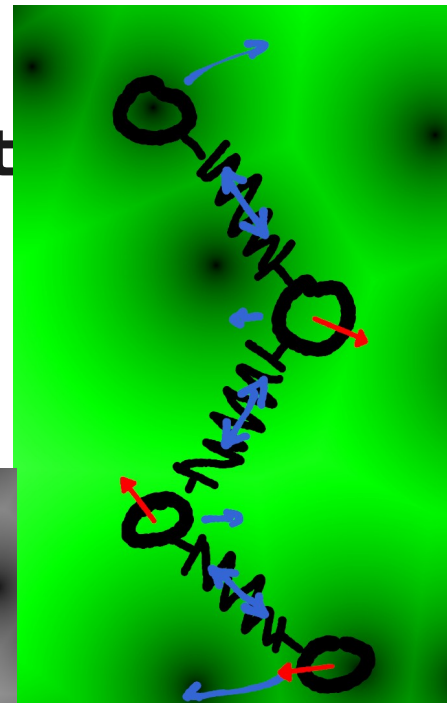
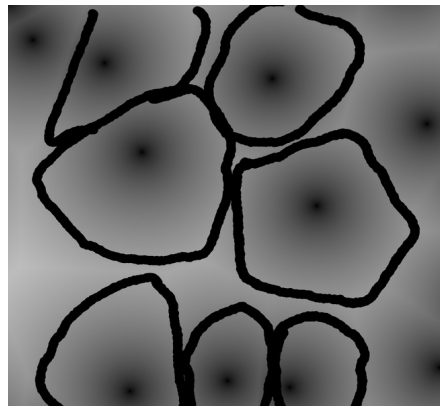
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Snake, easy to compute

Minimisation of energy in a system

- Internal energy (controls locally the shape)
 - “Continuity”
 - “Curvature”
- External energy (controls the positioning of the shape, what we want to optimise)
 - “Image”

$$\begin{aligned} E_{\text{snake}}^* &= \int_0^1 E_{\text{snake}}(\mathbf{v}(s)) ds \\ &= \int_0^1 E_{\text{int}}(\mathbf{v}(s)) + E_{\text{image}}(\mathbf{v}(s)) \\ &\quad + E_{\text{con}}(\mathbf{v}(s)) ds \end{aligned}$$

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$$E_{\text{image}} = w_{\text{line}}E_{\text{line}} + w_{\text{edge}}E_{\text{edge}} + w_{\text{term}}E_{\text{term}}$$

$$= \int_0^1 E_{\text{int}}(\mathbf{v}(s)) + E_{\text{image}}(\mathbf{v}(s))$$

$$E_{\text{line}} = -(G_{\sigma} * \nabla^2 I)^2$$

“Do whatever you want”

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$$\begin{aligned} E_{\text{term}} &= \frac{\partial \theta}{\partial \mathbf{n}_{\perp}} \\ &= \frac{\partial^2 C / \partial \mathbf{n}_{\perp}^2}{\partial C / \partial \mathbf{n}} \\ &= \frac{C_{yy}C_x^2 - 2C_{xy}C_xC_y + C_{xx}C_y^2}{(C^2 + C^2)^{3/2}} \end{aligned}$$

"Do whatever you want"

$$+ E_{\text{con}}(\mathbf{v}(s)) ds$$



Snake, awful to tune

Perfect when the “object” is at the center of the space.

Perfect when there is a “global gradient” towards the object.

Perfect when the initial curve is already in a “good initial position”.

But what if...

- the gradient is null around a vertex,
- the slope is too gentle in the whole area,
- we don't have the good initial conditions,
- ...?



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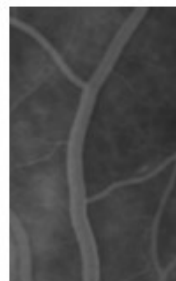
Snake, some improvements

- Null gradient around the shape:
 - Force the contours to grow
- We don't know how to choose the initial conditions:
 - Use of dual-snakes



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(a)



(b)



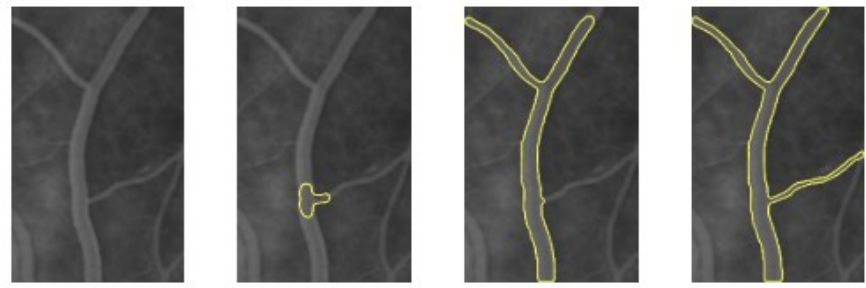
(c)



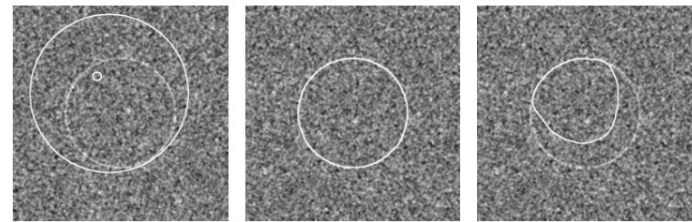
(d)

Snake, some improvements

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(a) (b) (c) (d)



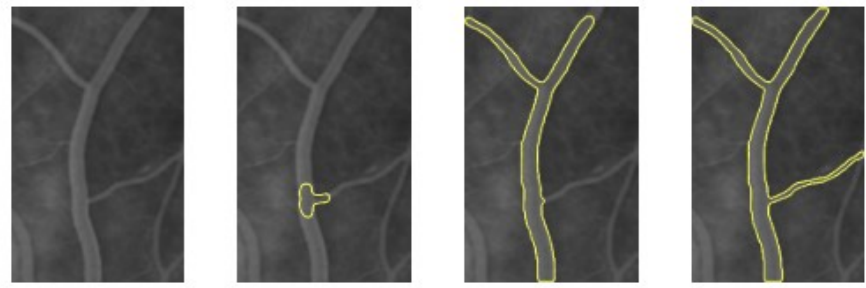
(a) Example Initialisation (b) Example Dual Result (c) Example Kass result



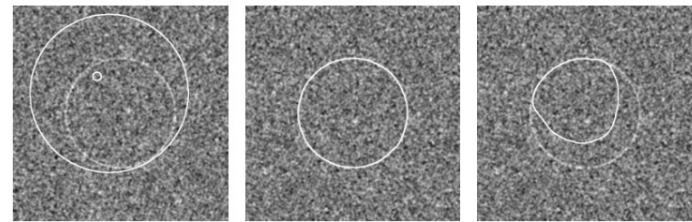
(d) Cup Initialisation (e) Dual Cup Result (f) Kass Cup Result

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- Null gradient around the shape:
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(a) (b) (c) (d)



(a) Example Initialisation (b) Example Dual Result (c) Example Kass result



(d) Cup Initialisation (e) Dual Cup Result (f) Kass Cup Result

Snakes: Active contour models

M Kass, A Witkin, D Terzopoulos - International journal of computer vision, 1988 - Springer

... Figure 5 shows an example of such a **snake** exposed to a standard subjective **contour** illusion [7]. The shape of the **snake contour** between the edges and lines in the illusion is entirely ...



Snake, my Todo list

- Find a good initial curve placement using the [Ant Colony Optimisation](#)
- Mixing PSO and Snake for speeding up the convergence