

1 Euclides' proof of there being infinitely many prime numbers

1.1 Statement

Let P be prime numbers. There are infinitely many of them.

1.2 Statement

Equivalently, let P be prime numbers. There is no $p \in P$ such that $\forall p' \in P \leq p$.

1.2.1 Proof

Assume there is p as defined above. then $(p \cdot p - 1) - 1$ is not divisible by any p' , and is greater than p , which gives us contradiction, which could only be because the assumption is false, thus, there is no maximum element in P .

2 Mersenne's proof that for composite n $M_n = 2^n - 1$ is composite as well

2.1 proof

consider $n = a \cdot b$ and $2^n - 1 = ((2^a)^{b-1} \cdot 2^a) - 1$. Then ...