block name 1

Incremental quotient

Let:

$$\cdot \mathcal{U} \subset \mathbb{C} \text{ open}$$

 $\cdot f : \mathcal{U} \to \mathbb{C}$
 $\cdot p \in \mathcal{U}$

We name incremental quotient of f in p to:

$$\cdot \lim_{z \to p} \frac{f(z) - f(p)}{z - p}$$

We denote:

$$\cdot f'(p)$$

Holomorphic function

Let:

$$\cdot \mathcal{U} \subset \mathbb{C} \text{ open}$$

 $\cdot f : \mathcal{U} \to \mathbb{C}$
 $\cdot p \in \mathcal{U}$

Then, f is holomorphic over p if:

$$\exists f'(p)$$

Then, f is holomorphic over U if:

$$y p \in \mathcal{U}$$
: $\exists f'(p)$

We denote:

$$\begin{array}{l} \cdot \left\{ f : \mathcal{U} \to \mathbb{C} \mid f \text{ holomorphic over } \mathcal{U} \right\} : \mathcal{H}(\mathcal{U}) \\ \cdot f \in \mathcal{H}(\mathbb{C}) : f \text{ entire} \end{array}$$

Real components

Let:

$$f \in \mathcal{H}(\mathcal{U})$$

We name $% \left(1\right) =\left(1\right) \left(1\right) =\left(1\right) \left(1\right)$ in the first real component of f to:

$$f_{Re}: \mathcal{U} \longrightarrow \mathbb{R}$$

$$z \longmapsto Re(z)$$

We name second real component of f to:

$$\begin{array}{ccc}
f_{Im} : \mathcal{U} & \longrightarrow & \mathbb{R} \\
z & \longmapsto & Im(z)
\end{array}$$

2 0 unit name

Real dual

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Let:
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$$f \in \mathcal{H}(\mathcal{U})$$

 f_{Re}, f_{Im} real components of f

We name real dual of
$$f$$
 to:

$$f_{\mathbb{R}^2} : \mathbb{R}^2 \longrightarrow \mathbb{R}^2$$

$$(x,y) \longmapsto (f_{Re}(x+yi), f_{Im}(x+yi))$$

We denote:

 $\cdot property : notation$