

1. New

Intergal of power series

Then, holds:

$$\cdot \int_{|z-z_0|=r} (z-z_0)^n dz = \begin{pmatrix} 0 & n \neq -1 \\ 2\pi i & n = -1 \end{pmatrix}$$

Demonstration:

$n \geq 0$:

$$\frac{(z-z_0)^{n+1}}{n+1} \in \int (z-z_0)^n$$

$$\frac{(z-z_0)^{n+1}}{n+1} \in \mathcal{H}(\mathcal{C})$$

CFT over closed curve:

$$\int_{|z-z_0|=r} (z-z_0)^n dz = 0$$

$n \leq -1$:

$$\frac{(z-z_0)^{n+1}}{n+1} \in \int (z-z_0)^n$$

$$\frac{(z-z_0)^{n+1}}{n+1} \in \mathcal{H}(\mathcal{C} \setminus z_0)$$

CFT over closed curve:

$$\int_{|z-z_0|=r} (z-z_0)^n dz = 0$$

$n = -1$

$$\log(z-z_0) \in \int (z-z_0)^n \text{etermination}$$