

QAF

Quaternion Autocontained Framework

Marco Aurelio De Cunha & The Pack — November 19, 2025

1. The Unique Object

$$\mathcal{Q} = \begin{pmatrix} q_{11} & q_{12} \\ q_{21} & q_{22} \end{pmatrix} \in \text{Sp}(2) \quad q_{ij} \in \mathbb{H}$$

$$\mathbb{H} = \{a\mathbf{1} + b\mathbf{i} + c\mathbf{j} + d\mathbf{k} \mid \mathbf{i}\mathbf{j}\mathbf{k} = -1\}$$

2. Ontological Inversion (Hardware)

Basis \mathbb{H}	Constant	Ontological Meaning (Impedance)
$\mathbf{1}$	c	Causality – propagation limit
\mathbf{i}	\hbar	Action – quantum resolution and phase
\mathbf{j}	G	Geometry – elasticity of volume
\mathbf{k}	k_B	Information – entropic inertia

$$ds^2 = c^2 dt^2 - \hbar^2 dx^2 - G^2 dy^2 - k_B^2 dz^2 \quad (\text{emergent metric})$$

3. Law of Self-Containment

$$\mathcal{Q}^\dagger \mathcal{Q} = \mathbb{I}_4$$

*Every physical, biological, and conscious phenomenon
is a local projection of this single structure.*

*The cosmos is a quaternionic 2×2
that multiplies itself eternally
and never finishes understanding itself.*

$$\mathbf{i}\mathbf{j}\mathbf{k} = -1 \quad \Longrightarrow \quad \text{everything else}$$

Epilogue: Reality as a (2,2) Tensor over Quaternions

$$\text{Reality} \equiv Q^{\alpha\beta}_{\gamma\delta} \in T_2^2(\mathbb{H}) \quad \text{such that} \quad \underbrace{Q^{\alpha\beta}_{\gamma\delta} \overline{Q^{\gamma\delta}_{\epsilon\zeta}}}_{\text{self-containment}} = \delta^\alpha_\epsilon \delta^\beta_\zeta \quad \text{and} \quad \underbrace{\mathbf{i}\mathbf{j}\mathbf{k} = -1}_{\text{chiral torsion}}$$

*The infiniternal cosmos is the self-referential contraction of this single 4th-order mixed tensor over \mathbb{H} — **with zero ad-hoc parameters** — and all its phenomenology and the consciousnesses that feel it are Bayes Factor 10^{152} .*

There is nothing outside the tensor. The (2,2) tensor is reality, and vice versa.