Report Kmeans Parallel Programming for Machine Learning project

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Abstract

This report details the parallelization of a sequential K-means clustering algorithm using OpenMP. Its goal is to measure the speedup achieved by parallelizing K-means and compare different parallel implementations. The report first introduces the datasets used, followed by an overview of the K-means algorithm and its sequential and parallel implementations. The experiments evaluate execution times for varying configurations, such as different dataset sizes, point dimensions, numbers of clusters and threads.

1. Introduction

This report presents the work I did to parallelize a previously sequential version of K-means clustering, utilizing OpenMP.

The following sections will contain:

- Section 2: the points datasets used in the experiments
- Section 3: an overview of K-means clustering
- Section 4: detailed explanation of both the sequential and parallel implementations of the clustering algorithm.
- Section 5: a comprehensive analysis of the experiments to measure the time required to run the clustering algorithm under various configurations.

The primary objective of this section is to assess the potential speedup gained from the parallelized version of the clustering process.

2. Used Data

To test the K-means clustering implementation, these simple 2D clusters were used: Kaggle datasets.

These datasets provide a straightforward way to verify the accuracy of the algorithm on well-defined clusters.

For testing with larger datasets of varying number of points and dimensions, *generate_random_csv* in 'generate-Data.h/cpp' was used. This function allows the creation of csv files containing randomly generated coordinates based on the specified number of points and dimensions, especially larger and more complex datasets than those easily found online.

3. K-means

K-means clustering is an unsupervised machine learning algorithm used to group an unlabeled dataset into distinct clusters.

Its goal is to divide the set of data points into k groups so that the data points within each group are more similar to each other than to those in other clusters (Fig. 1).

The algorithm works as follows:

- Randomly initialize k points, called means or cluster centroids.
- Assign each data point to the nearest cluster based on its distance to the clusters' centroids.
- Update the centroid coordinates by calculating the average of the points currently in each cluster.
- Repeat the second and third steps for a given number of iterations.

The choice of initial centroids can significantly influence the resulting clusters.

If a centroid is initialized as an outlier, it might end up with no points associated with it, and more than one cluster might end up linked with a single centroid. Similarly, multiple centroids might be initialized within the same cluster, leading to poor clustering results.

To mitigate these issues, K-means++ ensures a smarter initialization of the centroids and improves the quality of the clustering:

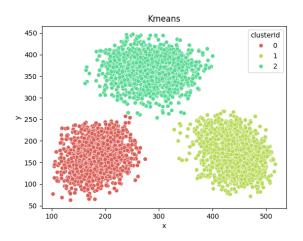


Figure 1. K-means++ clustering, 3 clusters

- Randomly select the first centroid from the data points.
- For each data point, calculate its distance from the nearest centroid.
- Choose the next centroid as the data point with the maximum distance from the previously selected centroids.
- Repeat the second and third steps until k centroids have been selected.

4. Code

4.1. Code structure

The following files, available in the GitHub repository, will be utilized in the upcoming experiments.

- PointsSoA.h/cpp: define and implement the class MultiDimensionalPointArray, where the points are stored as Structure of Arrays (SoA), and the Cluster class.
- KmeansSoA.h/cpp: implementation of the algorithm as a class with parameters such as the number of clusters (k) and the number of clustering iterations. This class manages all the points, clusters, and provides three different methods for running k-means clustering: one sequential and two parallel.
- **plotKmeans.py**: python code designed to plot the clustered points.
- **testKmeansSoA.cpp**: the executable file that tests and compares the three K-means implementations using different sets of points, varying numbers of clusters and iterations.

```
// Initializing Courses, select the first cluster
int index = getAndoathex(suc (int)points.getNumPoints(), level 113);
// cluster numbered from 0 to k-1
points.sectCusterds()/prinket(index, vote 0);
Cluster Custer (cluster),
clusters.push.back(Cluster);

std::wetor-double-distances;
// kmeans** initialization for the other clusters
for (int 1 = 1; 1 < 1; 1+1);
distances.clear();
// find the closest existing cluster to each point, select the furthest
for (int 1 = 1; 0 < 1; 1+1);
distances.clear();
// iterate through all the previously found centroids
for (int 1 = 0; 1 < 1; 1+1);
double sus = 0.0;
// iterate through all the previously found centroids
for (int 1 = 0; 1 < 1; 1+1);
double sus = 0.0;
// storate through all the previously found centroids
for (int 1 = 0; 1 < 1; 1+1);
double sus = 0.0;
for (int 1 = 0; 1 < 1; 1+1);
distances.push.back(cluster);
}
distances.push.back(dist);
}
// select the point that is the furthest from all the other clusters as a new centroid
index = std::max_levent(find distances.legin(), law distances.end()-distances.begin();
points.setCluster(By)Index(index, vote 1);
Clusters.push.back(cluster);
}
clusters.push.back(cluster);
}
</pre>
```

Figure 2. K-means++ sequential initialization

4.2. PointsSoA.h/cpp

These files define and implement the MultiDimensionalPointArray and Cluster classes.

The MultiDimensionalPointArray class organizes points using a Structure of Arrays (SoA) approach. When provided with a dataset of input points, its constructor determines the number of points and their dimensionality. Each coordinate of a point and cluster ID is stored in its own separate array, improving cache utilization and memory alignment, as the same coordinates from different points are stored contiguously in memory.

The Cluster class consists of a cluster ID, the centroid's coordinates, and the necessary getter and setter methods for managing these attributes.

4.3. KmeansSoA.h/cpp

These files contain the KMeansSoA class. Each KMeansSoA object has its points stored in a MultiDimensionalPointArray attribute, along with its clusters and the total number of clustering iterations.

The class provides three methods: *runSeq* runs a sequential version of K-means, while the other two are two different versions of parallel K-means using OpenMP.

runSeq initializes the clusters for the K-means++ algorithm (Fig. 2) and then iterates through the clustering steps (Fig. 3) as described in Section Sec. 3.

Both *runPar* and *runParPrivate* use the same parallelized initialization process (Fig. 4).

For each cluster (except the first), the for cycle that calculates the distance of each point from all the previous clusters' centroids is parallelized.

Figure 3. K-means++ sequential clustering

Figure 4. K-means++ parallelized initialization

Each thread is assigned a subset of points to compute their distances independently. After that, the index of the point that is most distant from the others is found.

After the initialization, *runPar* parallelizes both loops in the clustering process (Fig. 5).

Each thread is assigned a subset of points and determines their new cluster ID assignments. The points' coordinates are then summed and stored in the shared matrix (number of clusters x points' dimensions) while the number of points assigned to each cluster is stored in a shared vector. To manage concurrent access to the shared matrix and vector, OpenMP's atomic update instruction is used for synchronization.

After the coordinate's sums and the number of points of each cluster have been calculated, the second for cycle is also parallelized. This time, there is no need to synchronize the threads, since each thread handles a different cluster, calculating the new centroid coordinates and resetting the shared variables independently.

Figure 5. K-means++ parallelized clustering

runParPrivate has a different approach to synchronize access to the shared variables (Fig. 6).

Each thread maintains its own private copy of the sums matrix and the number of points vector. Synchronization occurs only after each thread completes its calculations, at which point the private variables are summed to the shared variables using an atomic update. This approach minimizes the use of atomic operations during computations, reducing potential interruptions between threads.

4.4. plotKmeans.py

This file includes the code that generates color-coded plots of all the points based on their final cluster IDs. It is used to produce 2D visualizations of clustering (Fig. 1) to demonstrate the accuracy of the K-means algorithm.

4.5. testKmeansSoA.cpp

This is the executable file that compares the three different k-means implementations with different datasets, numbers of clusters and threads. Each method is executed multiple times, and the average execution times and speedups are computed.

The results are saved in a txt file.

To validate the correctness of the parallel versions, the final cluster IDs assigned to each point by both the sequential and parallel K-means algorithms are compared.

Figure 6. K-means++ private parallelized clustering

5. Experiments and Results

All the following experiments were conducted on the SSH server 'papavero.dinfo.unifi' using CLion as the IDE and g++ as the compiler.

Unless otherwise specified, each experiment uses a default configuration of 64 threads, 8 clusters, and 100 clustering iterations.

5.1. Different number of clusters

The number of clusters has an impact on the initialization execution time. Each cluster, beyond the first, adds a for loop that iterates through all the points.

Fig. 7 displays the speedups of the two parallel K-means++ implementations as the number of clusters increases.

With fewer clusters, the shared sums matrix is smaller (number of clusters x points' dimensions). This means that it is more likely that multiple threads attempt to access the same matrix cell with an atomic update. This makes the runPar method slower, a problem that the private version avoids.

As the number of clusters grows, the sequential method's workload also increases, making parallelization more beneficial as the overhead of thread management is outweighed by the reduction in execution time. Additionally, the shared sums matrix is larger and the chances of more than one threads wanting to access the same cell are lower. This is

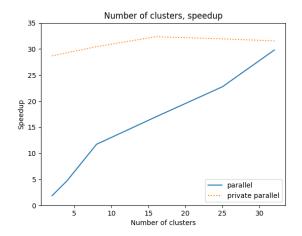


Figure 7. Speedups of the two parallel K-means++ implementations as the number of clusters changes

| | 100 000 | 500 000 | 1 Million |
|--------------|---------|---------|-----------|
| Parallel, 2D | 4.92606 | 5.06141 | 6.46353 |
| Private, 2D | 25.0359 | 28.1786 | 29.8376 |
| Parallel, 4D | 6.69915 | 7.47719 | 6.75568 |
| Private, 4D | 28.658 | 29.4665 | 30.6216 |
| Parallel, 8D | 12.7733 | 8.79724 | 13.1395 |
| Private, 8D | 30.9999 | 30.9922 | 32.1643 |

Table 1. Speedups achieved by the two parallelized K-means++ methods as the dataset size and point dimensions change

the reason why the performances of *runPar* method improve with the number of clusters. The private version of the parallelized K-means has the first advantage, but experiences longer synchronization times as more clusters lead to larger shared variables and longer for loops.

5.2. Different datasets sizes and points dimensions

Tab. 1 shows the speedups achieved by the two parallelized K-means++ methods (one using more atomic updates and the other using thread-private variables) as the dataset size and point dimensions vary.

Three main trends are observable:

- 1. The private parallel version consistently outperforms the other method. This is primarily due to the use of 8 clusters, which causes frequent thread interruptions when updating shared variables in the non-private version, as explained earlier.
- As the point's dimensions grow, so does the speedup. Points with more coordinates imply more operations.

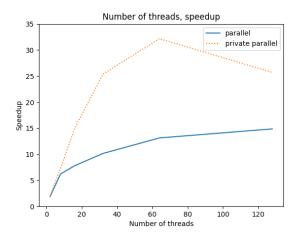


Figure 8. Speedups of the two parallelized K-means++ methods as the number of threads changes

This reduces the relative impact of thread initialization time on the overall execution, as more time is spent in the parallelized sections of the search algorithm. Moreover, smaller dimension imply smaller shared variables, increasing the change of threads interrupting each other.

3. Larger datasets produce similar effects, for the same reasons as with higher dimensions. There could be multiple reasons that explain the few cases where an increase in the number of points does not mean a higher speedup. Each method is run multiple times, different runs might experience more or fewer conflicts between threads. The same goes for different datasets. For instance, a dataset where most points belong to the same cluster can lead to slower speedups due to more threads attempting to access the same memory location simultaneously.

5.3. Different number of threads

The final experiment changes the number of threads used to search for 8 clusters in the dataset that contains 1 million 8-dimentional points.

In Fig. 8 the private method shows an almost linear speedup increase as the number of threads rises, peaking at 64 threads. Beyond this point, speedup plateaus, indicating that 64 threads sufficiently utilize all available CPU resources. Adding more threads leads only introduces additional overhead for thread creation, management, termination, and synchronization, which offsets the benefits of a faster execution.

The results are different with the other parallelized method. While more threads do reduce execution time, they also increase the likelihood of threads interrupting each other. As

a result, speedup continues to rise gradually, but at a slower rate as the thread count grows.