A comparison of conventional and imprecise probability approaches to statistics

Marco Cattaneo
Department of Statistics, LMU Munich

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 - quantity of interest: $P_{\theta}(\sum_{i=n+1}^{n+m} X_i = r) = \binom{r}{m} \theta^r (1-\theta)^s$

Bayesian approach

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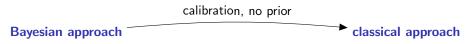
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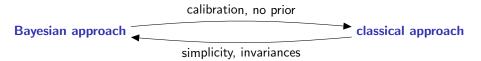
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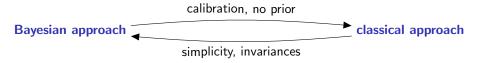
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IP approach

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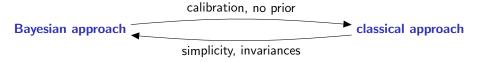
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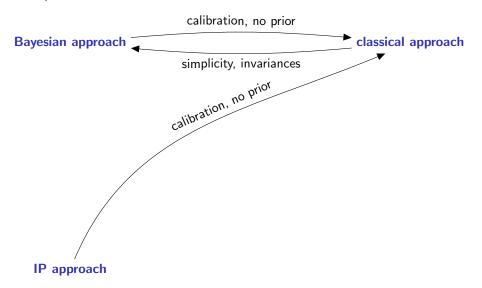
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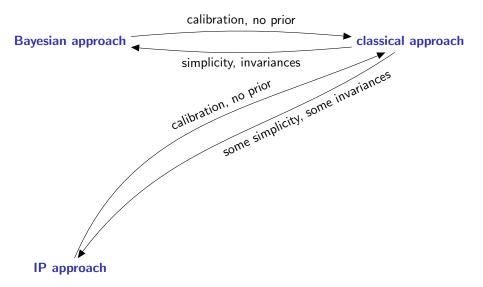
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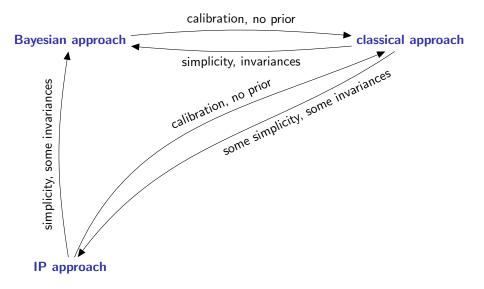
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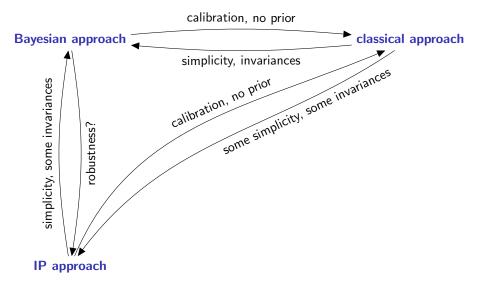
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- (imprecise) expectation of $\binom{r}{m}\theta^r(1-\theta)^s$ analytically or numerically, but is neither a point estimate nor a confidence/credible interval

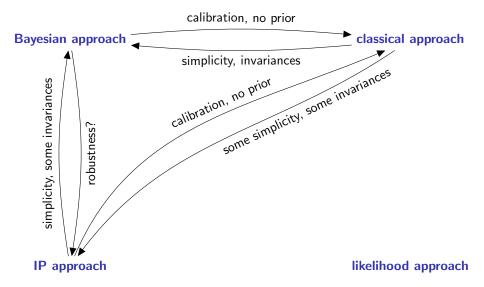












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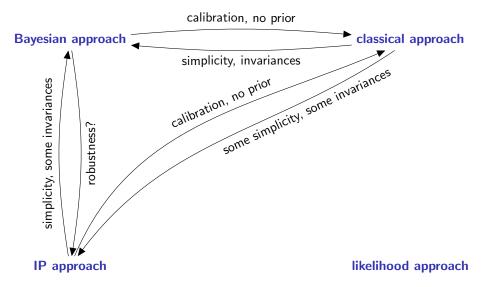
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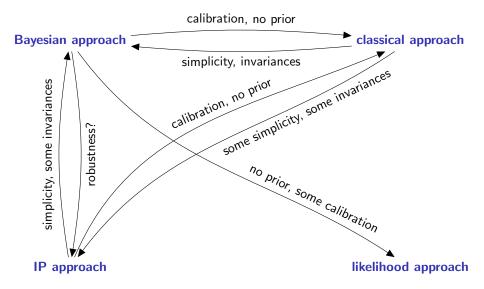
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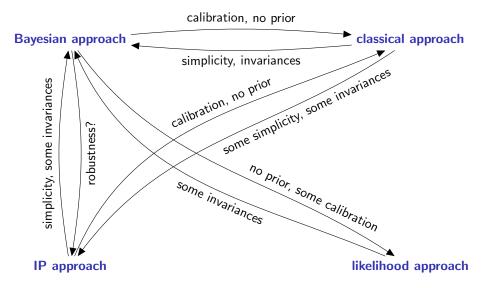
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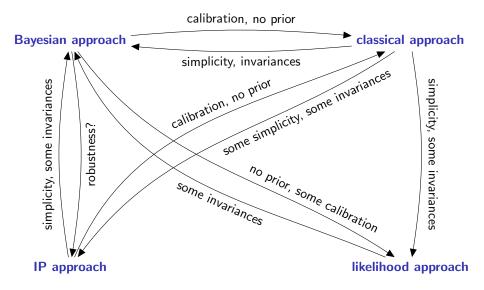
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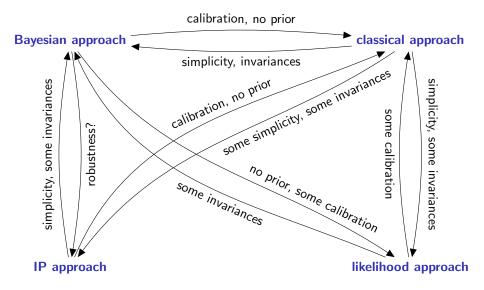
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- repeated sampling calibration is easy (regular problem)

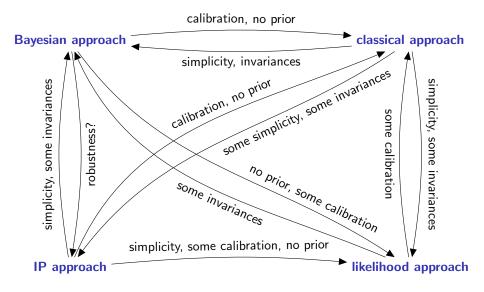


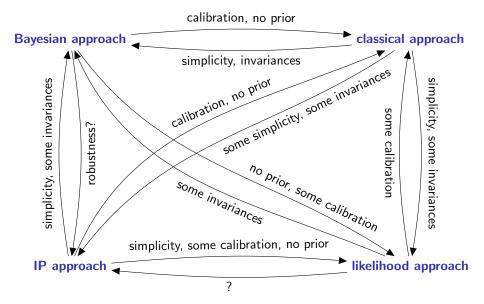












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- the likelihood approach to statistics seems to be a better compromise between the Bayesian and classical ones