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function REACH(bddfsm, init)
  reach  $\leftarrow$  init
  new  $\leftarrow$  POST(bddfsm, reach)
  while new  $\neq$  INTERSECTION(reach, new) do
    reach  $\leftarrow$  UNION(DIFF(new, reach), reach)
    new  $\leftarrow$  POST(bddfsm, reach)
  end while
  return reach
end function

function BACKWARD_IMAGE_COMP(bddfsm, counter_examples, init)
  images  $\leftarrow$  []
  counter_example  $\leftarrow$  PICK_ONE_STATE_RANDOM(counter_examples)
  pre_counter_example  $\leftarrow$  counter_example
  counter_example_original  $\leftarrow$  counter_example
  APPEND(images, counter_example)
  while INTERSECTION(init, pre_counter_example)  $\neq$   $\emptyset$  do
    counter_example  $\leftarrow$  pre_counter_example
    pre_counter_example  $\leftarrow$  PRE(bddfsm, counter_example)
    INSERT(images, pre_counter_example)
  end while
  return images, counter_example_original
end function

function FIND_TRACE(bddfsm, init, images, counter_example_original)
  trace  $\leftarrow$  []
  start  $\leftarrow$  init
  for i  $\leftarrow$  1 to n do  $\triangleright$  LENGTH(images - 1)
    start  $\leftarrow$  INTERSECTION(start, images[i])
    next_state  $\leftarrow$  PICK_ONE_STATE(start)
    APPEND(trace, next_state)
    post  $\leftarrow$  INTERSECTION(POST(start), images[i + 1])
    inputs  $\leftarrow$  GET_INPUTS_BETWEEN_STATES(start, post)
    APPEND(trace, PICK_ONE_INPUTS(inputs))
    start  $\leftarrow$  post
  end for
  APPEND(trace, counter_example_original)
  return trace
end function

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function CHECK_EXPLAIN_INV_SPEC( $(bddfsm, spec)$ )
   $nspec \leftarrow \neg(spec)$ 
   $bddspec \leftarrow \text{SPEC\_TO\_BDD}(bddfsm, nspec)$ 
   $reach \leftarrow \text{REACH}(bddfsm, init)$ 
  if  $\text{INTERSECTION}(bddspec, reach) = \emptyset$  then
    return  $(True, None)$ 
  else
     $counter\_examples \leftarrow \text{INTERSECTION}(bddspec, reach)$ 
     $images, counter\_example\_original \leftarrow$ 
       $\text{BACKWARD\_IMAGE\_COMP}(bddfsm, counter\_examples, init)$ 
     $trace \leftarrow$ 
       $\text{FIND\_TRACE}(bddfsm, init, images, counter\_example\_original)$ 
    return  $(False, trace)$ 
  end if
end function

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