# Excercise 3 - Grey-box models (continued)

## Models for the heat dynamics of a building

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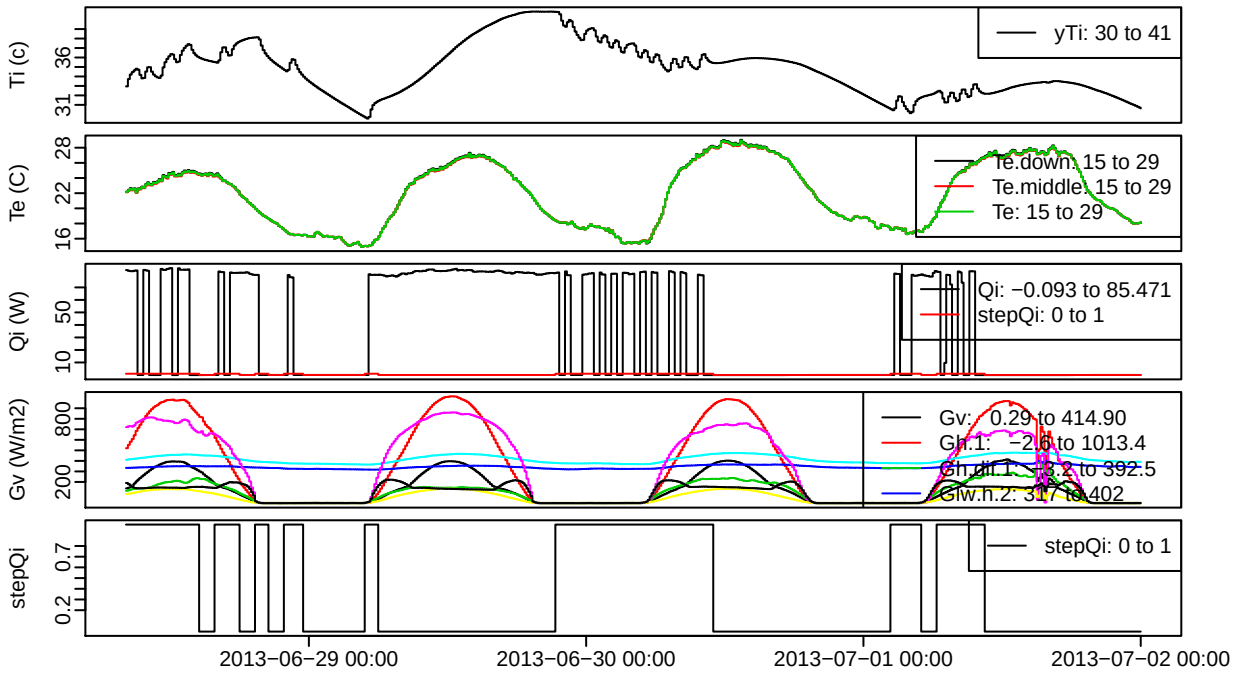
The exercise is focused on grey-box modelling of the heat dynamics of a (small) building using stochastic differential equations (SDEs). In addition to the first exercise on greybox modelling, we will in this exercise test different techniques to:

1. Alter the noise level or system uncertainty to account for e.g. non-linear phenomena.
2. Build a semi-parametric model to take into account that the solar penetration (i.e. relation between measured solar radiation and radiation entering into the building) as function of the position of the sun.
3. Balance heat gains to the air temperature and the temperature of the thermal mass.

The data consists of several measurement from a small test box with a single window. In this exercise the following signals are used:

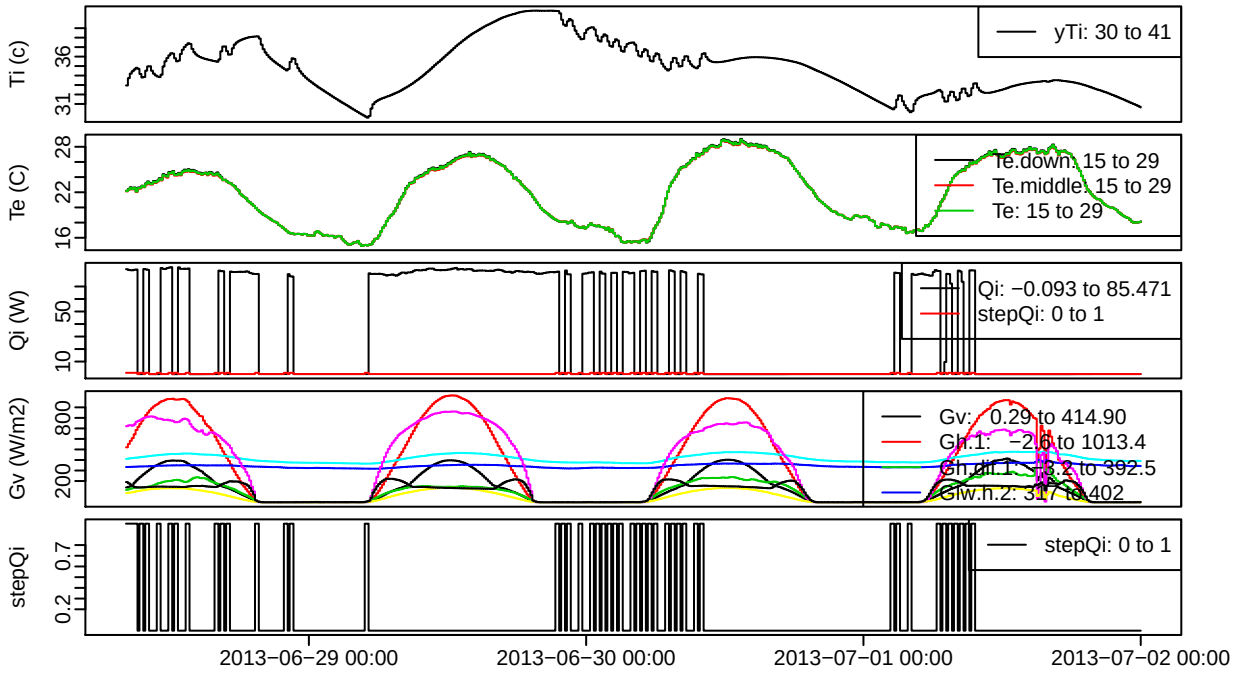
- Ti (yTi in data) the observed indoor temperatures. (C)
- Qi (Qi in data) the heat emitted by the electrical heaters in the test box (W)
- Te (Te in data) the ambient temperature (C)
- Gv (Gv in the data) the vertical south total solar radiation (W/m2)
- Gvn (Gvn in data) the vertical north total solar radiation (W/m2)

# Question 1




The lower time series plot is of stepQi, which goes from 0 to 1. Try to change the argument samples_after_Qi_step in the function preparing the data. How does it change stepQi?

Changing the stepQi makes the ON or OFF intervals longer or shorter and makes it able to correspond better to the actual heater's behavior. Like below with a step = 0.5




## Comparing the two models

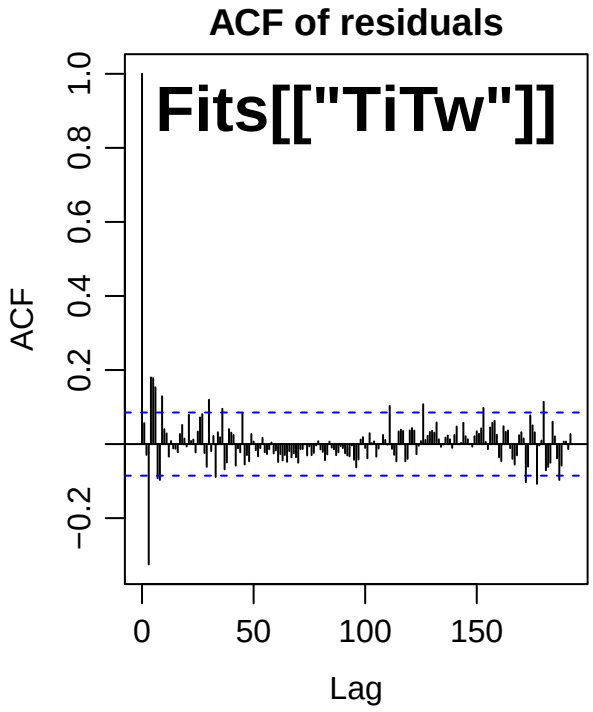
Now compare the two models implemented in **functions/sdeTiTw.R** and **functions/sdeTiTw_sigmalevels.R**. What is the difference?

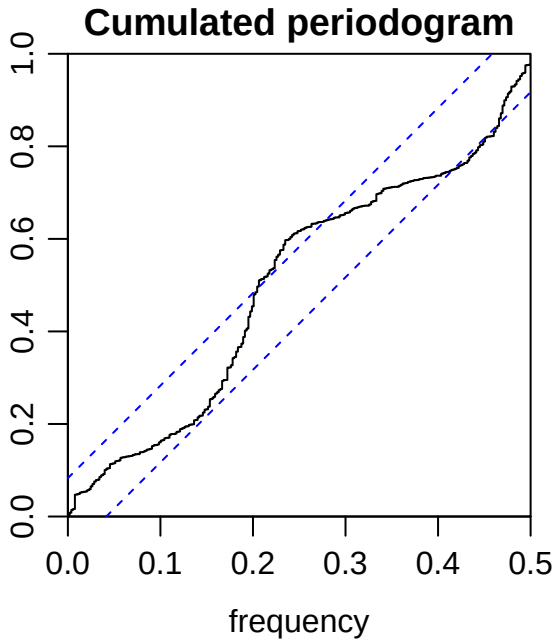
The second model includes with sigma levels include:

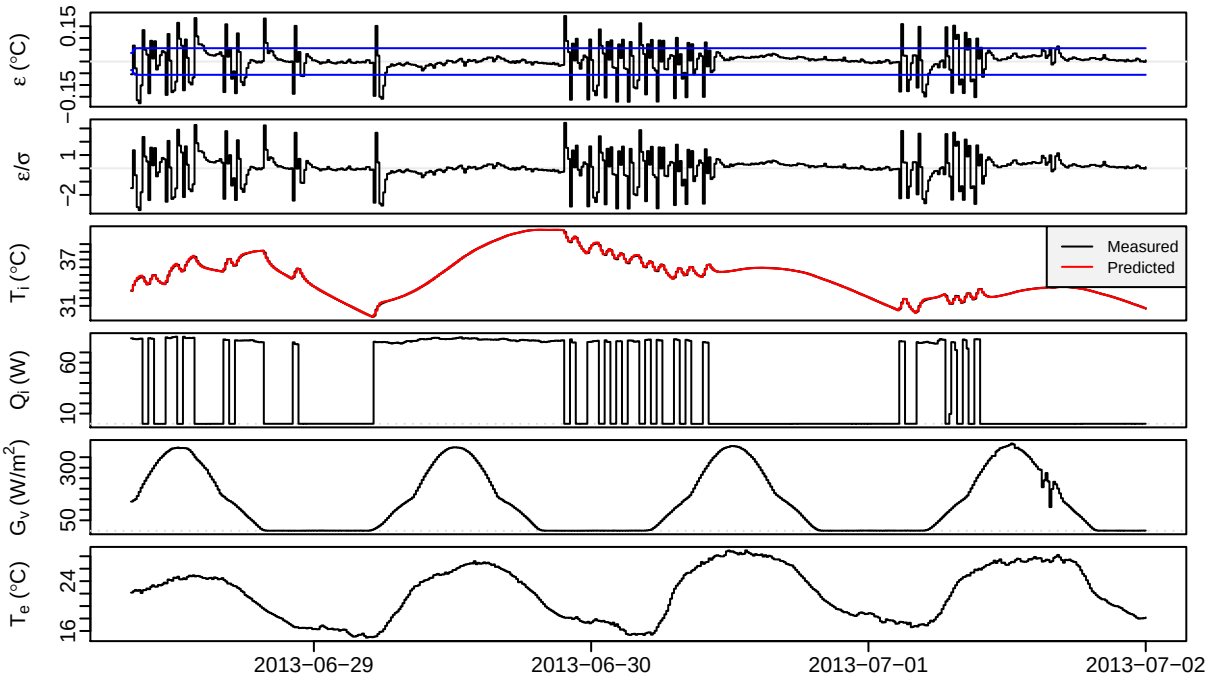
$(1 + (stepQi * sigmalevel))$

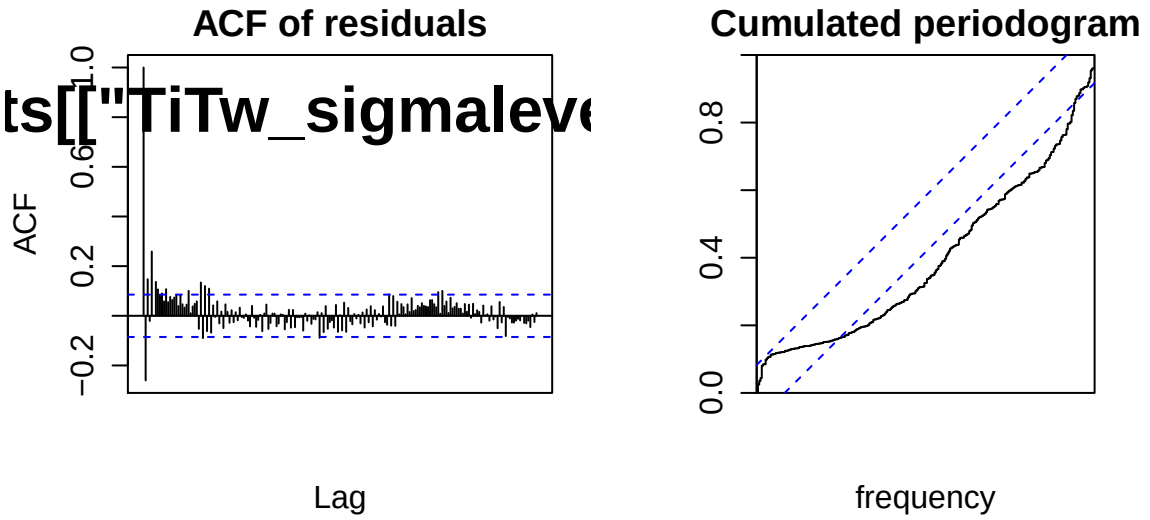
in the error term allowing to account for the noise of turning ON and OFF the heater.

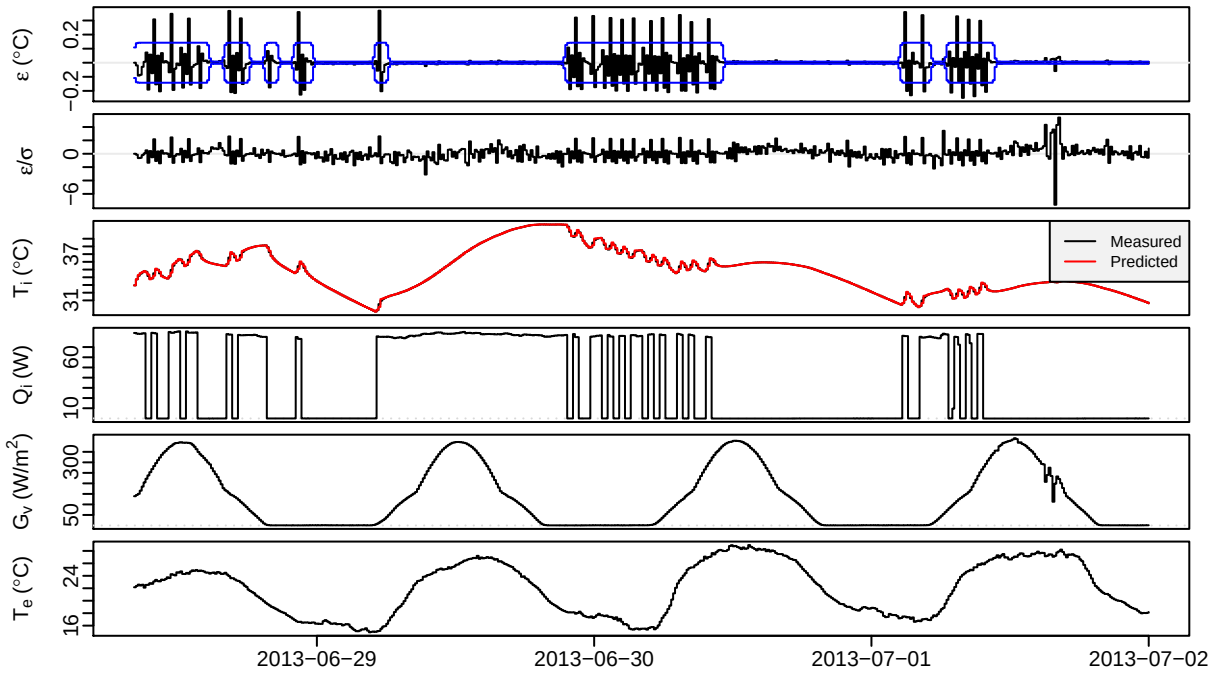
Now go to the script and fit the two models. Compare the results:


ACF of residuals
Fits[["TiTw"]]
ACF
1.0
0.8
0.6
0.4
0.2
−0.2
0
50
100
150
Lag


Cumulated periodogram
1.0
0.8
0.6
0.4
0.2
0.0
0.0
0.1
0.2
0.3
0.4
0.5
frequency


ε (°C)
0.15
−0.15
ε/σ
1
−2
T_i (°C)
37
31
Measured
Predicted
Q_i (W)
60
10
G_v (W/m²)
300
50
T_e (°C)
24
16
2013−06−29
2013−06−30
2013−07−01
2013−07−02




What is plotted in the upper two plots? (You maybe have to look into the analyzeFit() function).

The upper plot is the residuals of the predicted variable **yTi**. The lower plot is the standarized residuals (residuals / sd(yTi)), the y-axis changes as the errors are now divided by the standard deviation (sigma)

What is indicated by the blue lines in the upper plot? Step back in the plots and compare the results, and look at the summary output.

The blue lines in the upper plot are the standard deviation of the predicted variable (**yTi**) by which the residuals are divided to be standarized in the second graph below.

Step back in the plots and compare the results, and look at the summary output. Which of the two models will you prefer and why? The one with sigma level because it allows the variance to change with time and captures better the variability of the process and that is shown in its residuals.When comparing their Log-Likelihood, also the model with sigma-levels has a larger likelihood.

# References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