Excercise 3 - Grey-box models (continued)

Models for the heat dynamics of a building

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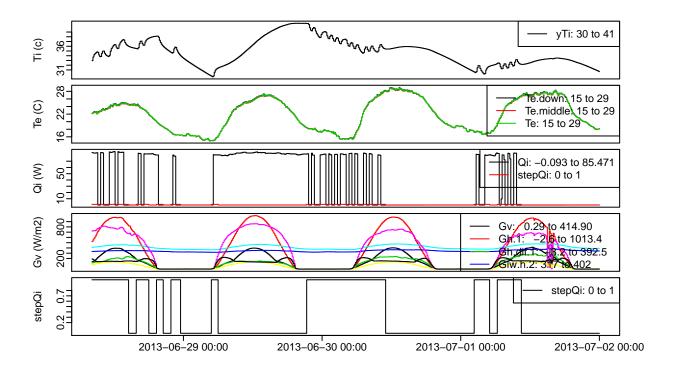
The exercise is focused on grey-box modelling of the heat dynamics of a (small) building using stochastic differential equations (SDEs). In addition to the first exercise on greybox modelling, we will in this exercise test different techniques to:

- 1. Alter the noise level or system uncertainty to account for e.g. non-linear phenomena.
- 2. Build a semi-parametric model to take into account that the solar penetration (i.e. relation between measured solar radiation and radiation entering into the building) as function of the position of the sun.
- 3. Balance heat gains to the air temperature and the temperature of the thermal mass.

The data consists of several measurement from a small test box with a single window. In this exercise the following signals are used:

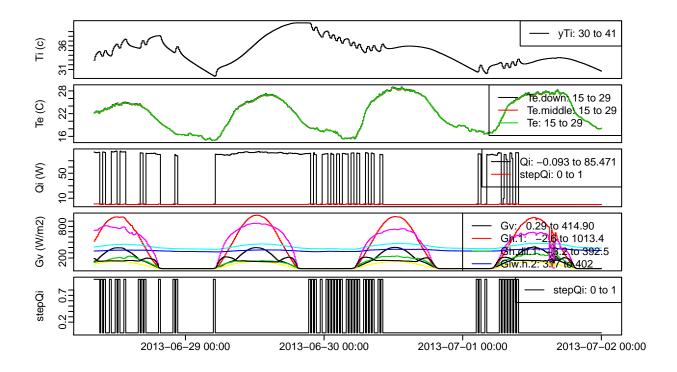
- Ti (yTi in data) the observed indoor temperatures. (C)
- Qi (Qi in data) the heat emitted by the electrical heaters in the test box (W)
- Te (Te in data) the ambient temperature (C)
- Gv (Gv in the data) the vertical south total solar radiation (W/m2)
- Gvn (Gvn in data) the vertical north total solar radiation (W/m2)

Question 1



The lower time series plot is of stepQi, which goes from 0 to 1. Try to change the argument samples_after_Qi_step in the function preparing the data. How does it change stepQi?

Changing the stepQi makes the ON or OFF intervals longer or shorter and makes it able to correspond better to the actual heater's behavior. Like below with a step = 0.5



Comparing the two models

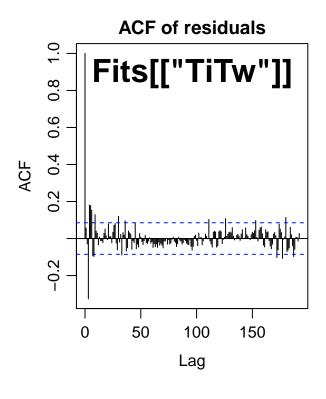
Now compare the two models implemented in functions/sdeTiTw.R and $functions/sdeTiTw_sigmalevels.R$. What is the difference?

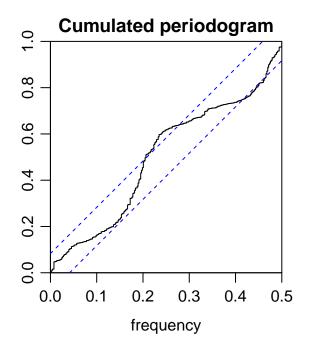
The second model includes with sigma levels include:

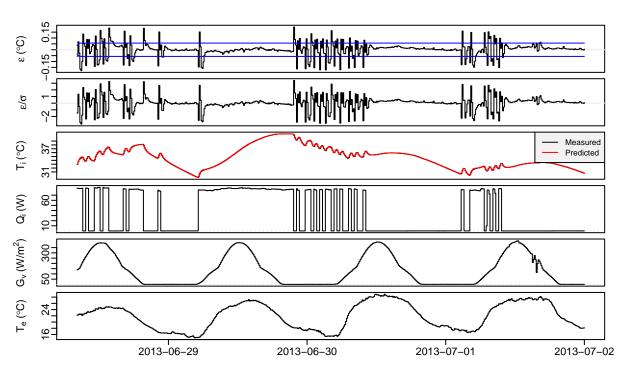
(1 + (stepQi * sigmalevel))

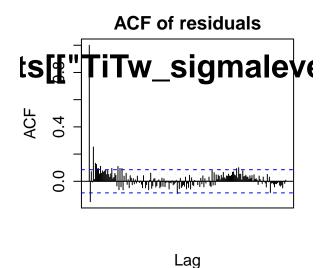
in the error term allowing to account for the noise of turning ON and OFF the heater.

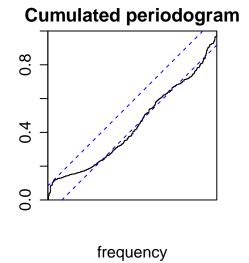
Now go to the script and fit the two models. Compare the results:

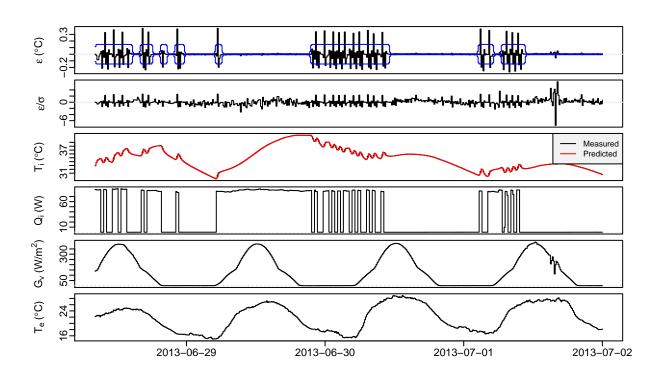












What is plotted in the upper two plots? (You maybe have to look into the analyzeFit() function).

The upper plot is the residuals of the predicted variable yTi. The lower plot is the standarized residuals (residuals / sd(yTi)), the y-axis changes as the errors are now divided by the standard deviation (sigma)

What is indicated by the blue lines in the upper plot? Step back in the plots and compare the results, and look at the summary output.

The blue lines in the upper plot are the standard deviation of the predicted variable (**yTi**) by which the residuals are divided to be standarized in the second graph below.

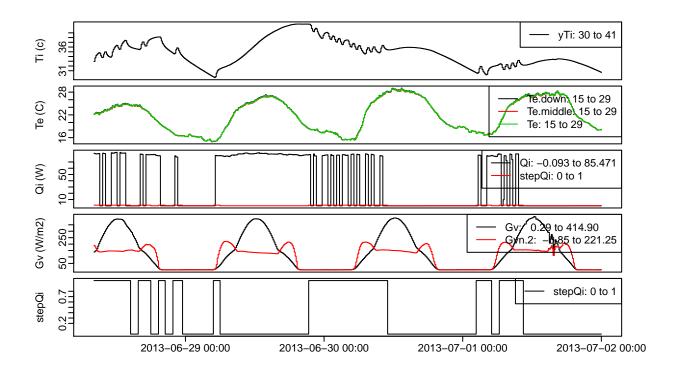
Step back in the plots and compare the results, and look at the summary output. Which of the two models will you prefer and why? The one with sigma level because it allows the variance to change with time and captures better the variability of the process and that is shown in its residuals. When comparing their Log-Likelihood, also the model with sigma-levels has a larger likelihood.

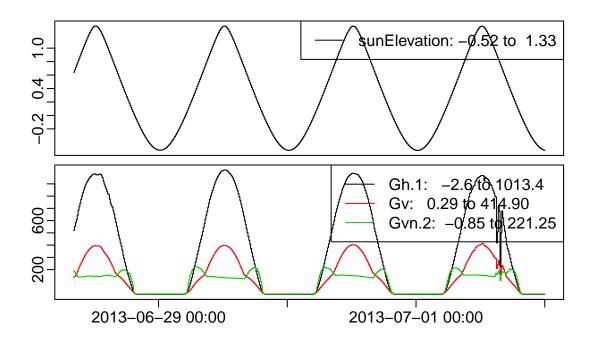
So it becomes clear that we have some (possible non-linear) dynamics when the heating turns on and off, which our models doesn't predict so well. But instead of adding a more detailed description to the deterministic part of the model, we simply vary the system noise, or in other words, change the uncertainty level of our states under under different conditions. This is a very useful thing, since there will be many phenomena in buildings, especially occupied buildings, which will lead different to levels of noise, e.g., solar radiation and occupants doing funny things.

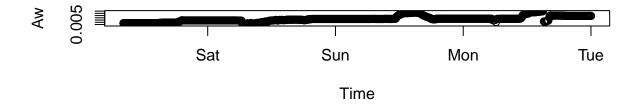
Question 2

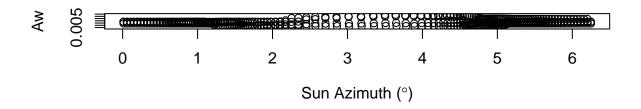
So far we have assumed that the solar gain is proportional to the radiation outside the test box. In reality, the heat gain from the sun depends highly on building geometry, surroundings, window properties, etc. In this part of the exercise, we will apply splines to estimate the solar heat gain as a function of solar position.

First we make a hidden state for Aw (also called the gA-value) to investigate if it changes over time and as the function of the sun position.







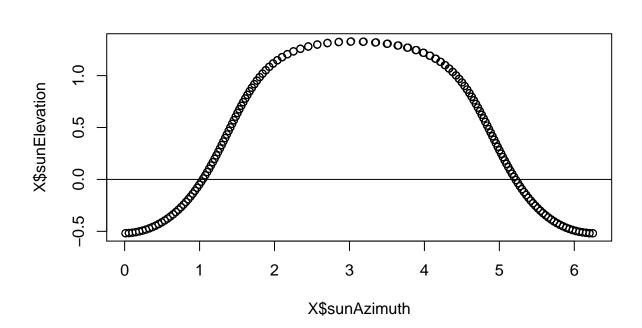


It is clear that the state of Aw is not constant, but changes. Furthermore, it seems like there could be a relation to the sun azimuth.

Now, answer the questions below as you progress in modelling the solar radiation with use of splines. The

spline function we want to estimate is the **gA value** (e.g. the percentage of solar heat that enters through the window, multiplied with the window area) as a function of the sun azimuth.

First, plot the sun elevation as a function of the sun azimuth, as well as a horizontal line through 0 (notice that the angles is in radians).

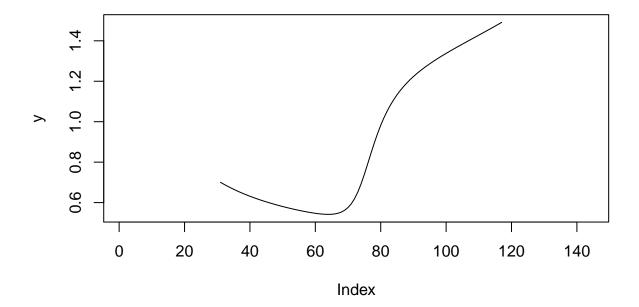


Find the azimuth angles (in radians) that corresponds to the sunrise and sunset, and assign them to azumith_bound <- c(..., ...) below. These two angles will in a moment be our boundary azimuth angles. Outside the boundaries the gA value is 0, as the sun is below the horizon and the radiation is zero. Thus, we are only interested in the gA values from sunrise to sunset.

Define the base splines in the following lines of the script and stop after you have assigned the base splines to the data frame with the command $X \leftarrow \operatorname{cbind}(X, Xbs)$. Now play around with the four parameters in in

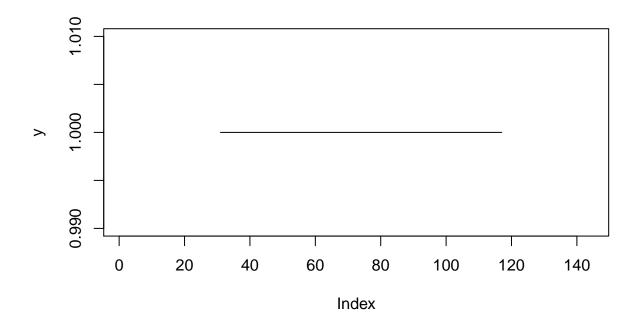
the vector Aw, and plot the resulting spline function to get an understanding of how the base splines and the resulting spline function work.

(Pro tip: the package lubridate is very useful when working with dates and time. Which often is the case for when dealing with time series!)

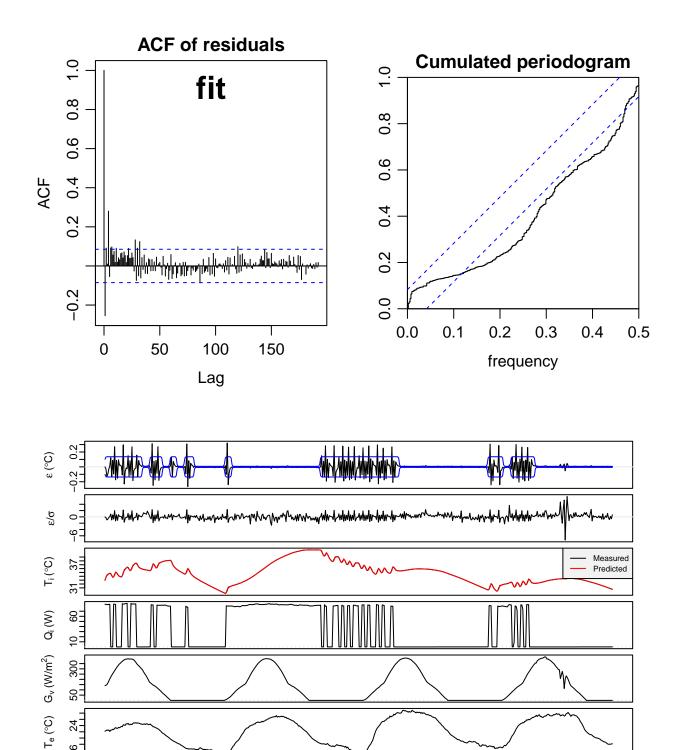


What happens if Aw only consists of 1's?

The result is just a straight line. These parameters determine how the spline function will look like. By multiplying the base splines to a solar radiation series and using this as input to an ARX model, the soalr absorption coefficient (gA-value) can vary as a smooth funiton of the sun azimuth angle.



Fit the model and investigate the estimated parameters. Is the parameters Aw1, Aw2, Aw3 and Aw4 significant, and is the magnitude reasonable when the actual glazed area is 52×52 cm? The parameters Aw2 nad Aw4 are highly significant. Aw3 is significant but its value is very low and Aw1 is not significant. For the significant values of Aw2 and Aw4, the coefficient of 0.1 to 0.13 is close to the constant gA estimated previously and since this is the time where most solar radiation is entering the box through the window, the estimated levels are found to be very reasonable.



Plot the gA curve and the 95 % confidence interval. The window in the test box is facing south towards an open area, and should therefore be rather unobstructed. Why do the gA curve then have a shape which is asymmetrical around the south (180 degrees)?

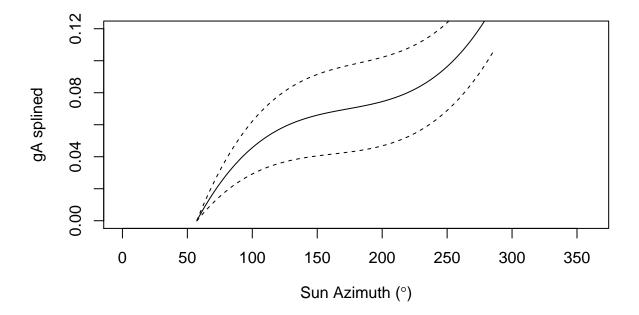
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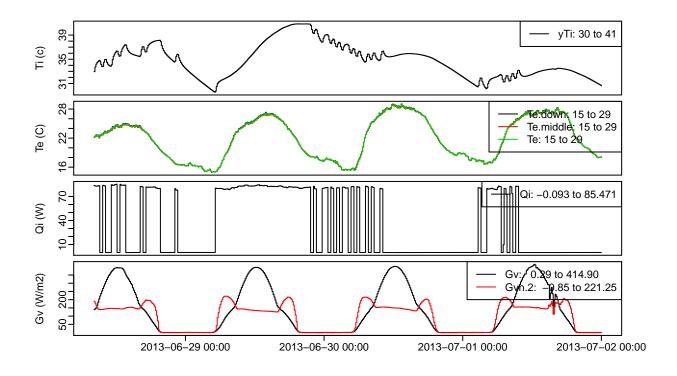
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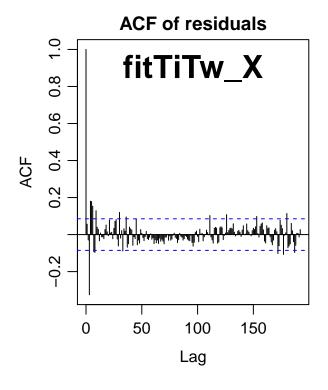
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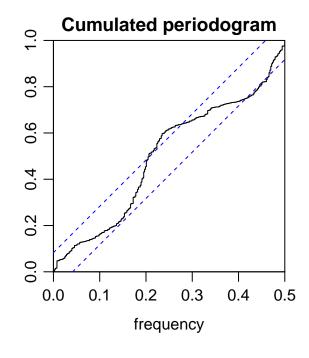
This could be due to the position of the vertical irradiance sensor which is on the east side of the box. This means that it would receive radiation in the morning but in the afternoon the box itself would block some of the diffuse light since the Sun is not going down exactly at the West.

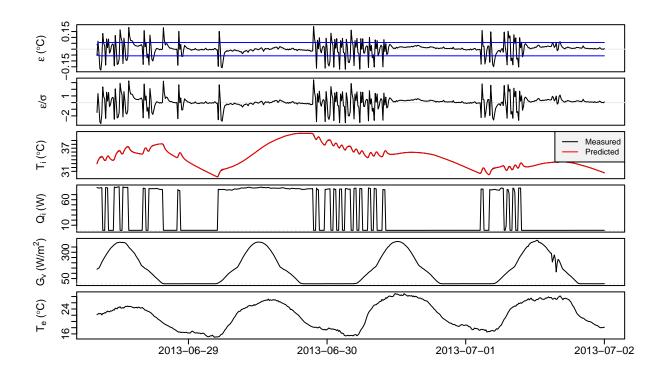


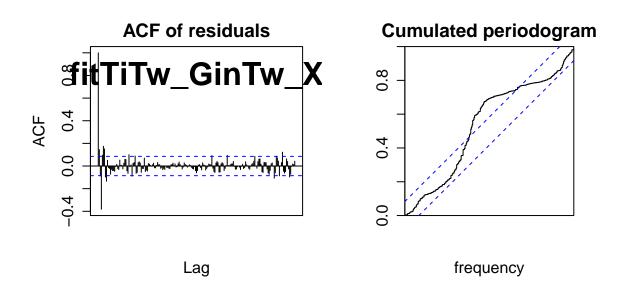
Question 3

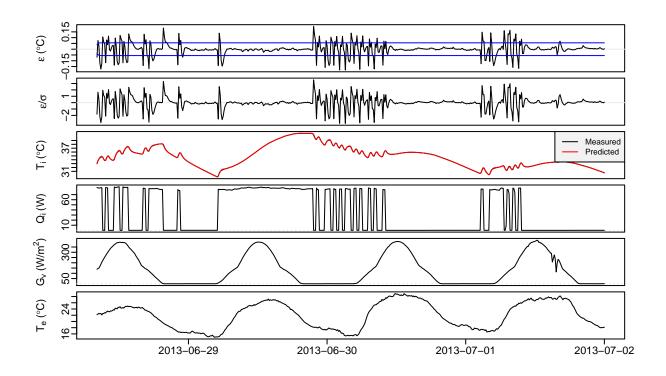


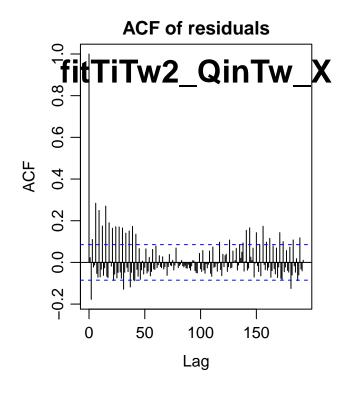


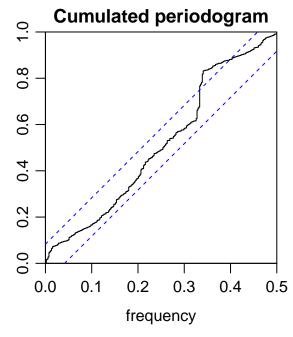


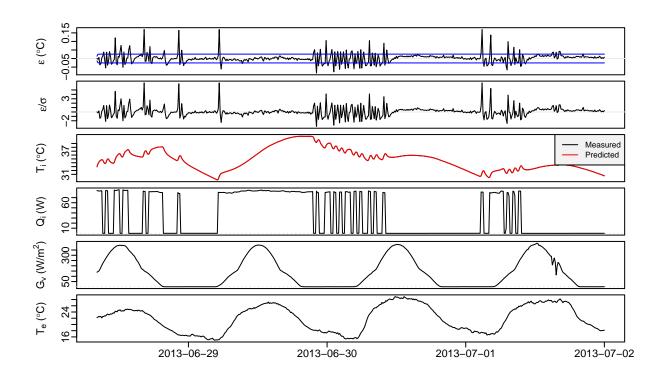


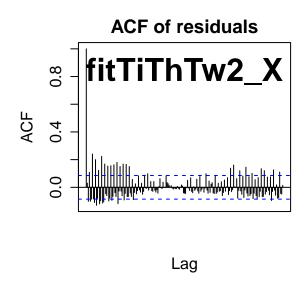


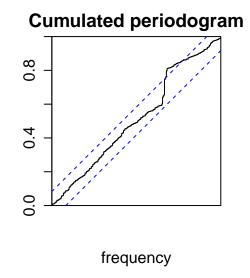


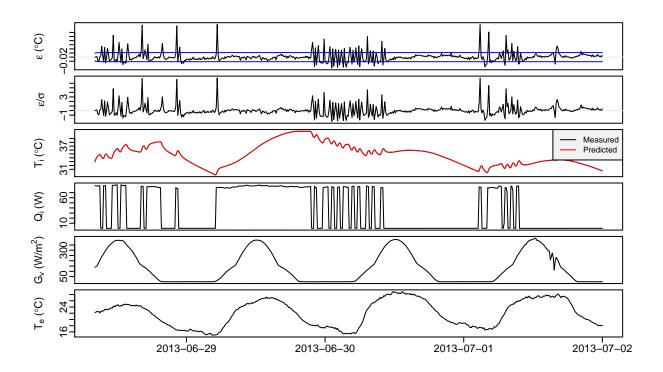












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