

# Model Selection II



DATA SCIENCE BOOTCAMP

# Training and test sets

	Date	Title	Budget	DomesticTotalGross	Director	Rating	Runtime
0	2013-11-22	The Hunger Games: Catching Fire	130000000	424668047	Francis Lawrence	PG-13	146
1	2013-05-03	Iron Man 3	200000000	409013994	Shane Black	PG-13	129
2	2013-11-22	Frozen	150000000	400738009	Chris BuckJennifer Lee	PG	108
3	2013-07-03	Despicable Me 2	76000000	368061265	Pierre CoffinChris Renaud	PG	98
4	2013-06-14	Man of Steel	225000000	291045518	Zack Snyder	PG-13	143
5	2013-10-04	Gravity	100000000	274092705	Alfonso Cuaron	PG-13	91
6	2013-06-21	Monsters University	NaN	268492764	Dan Scanlon	G	107
7	2013-12-13	The Hobbit: The Desolation of Smaug	NaN	258366855	Peter Jackson	PG-13	161
8	2013-05-24	Fast & Furious 6	160000000	238679850	Justin Lin	PG-13	130
9	2013-03-08	Oz The Great and Powerful	215000000	234911825	Sam Raimi	PG	127
10	2013-05-16	Star Trek Into Darkness	190000000	228778661	J.J. Abrams	PG-13	123
11	2013-11-08	Thor: The Dark World	170000000	206362140	Alan Taylor	PG-13	120
12	2013-06-21	World War Z	190000000	202359711	Marc Forster	PG-13	116
13	2013-03-22	The Croods	135000000	187168425	Kirk De MiccoChris Sanders	PG	98
14	2013-06-28	The Heat	43000000	159582188	Paul Feig	R	117
15	2013-08-07	We're the Millers	37000000	150394119	Rawson Marshall Thurber	R	110
16	2013-12-13	American Hustle	40000000	150117807	David O. Russell	R	138
17	2013-05-10	The Great Gatsby	105000000	144840419	Baz Luhrmann	PG-13	143

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17	2013-05-10	The Great Gatsby	105000000	144840419	Baz Luhrmann	PG-13	143

Training  
set

Test set

# Training and test sets

Training set

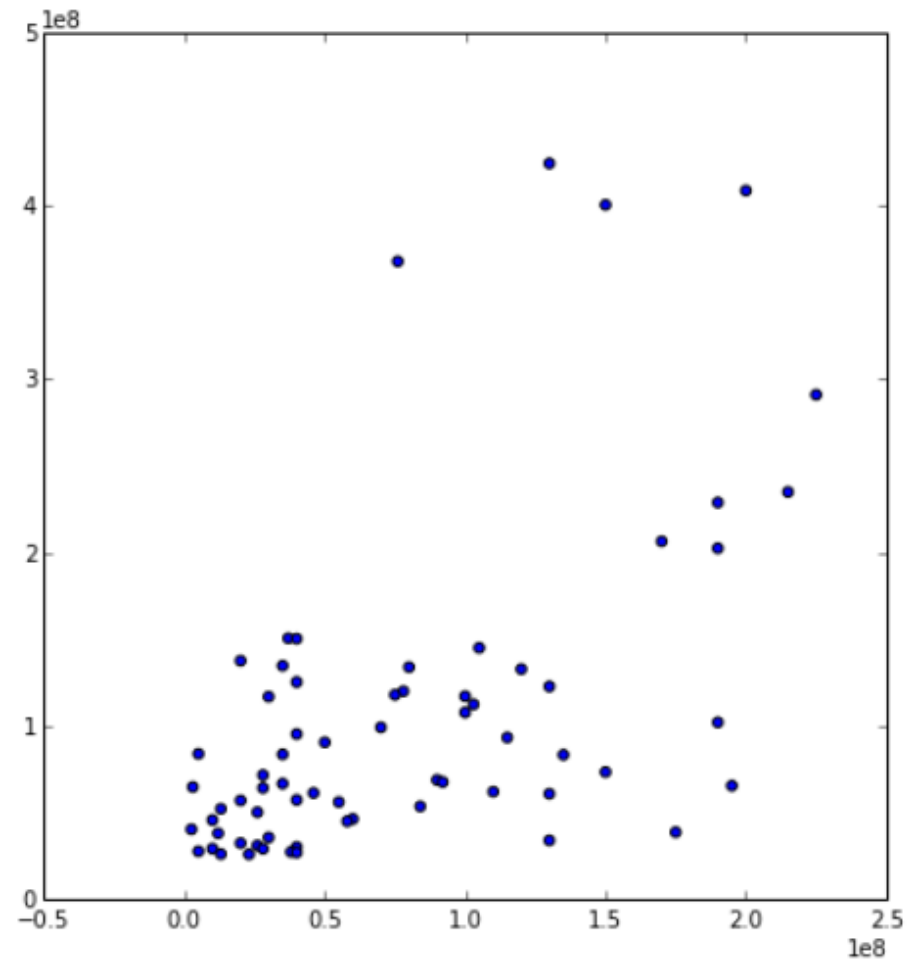
fit the model

Test set

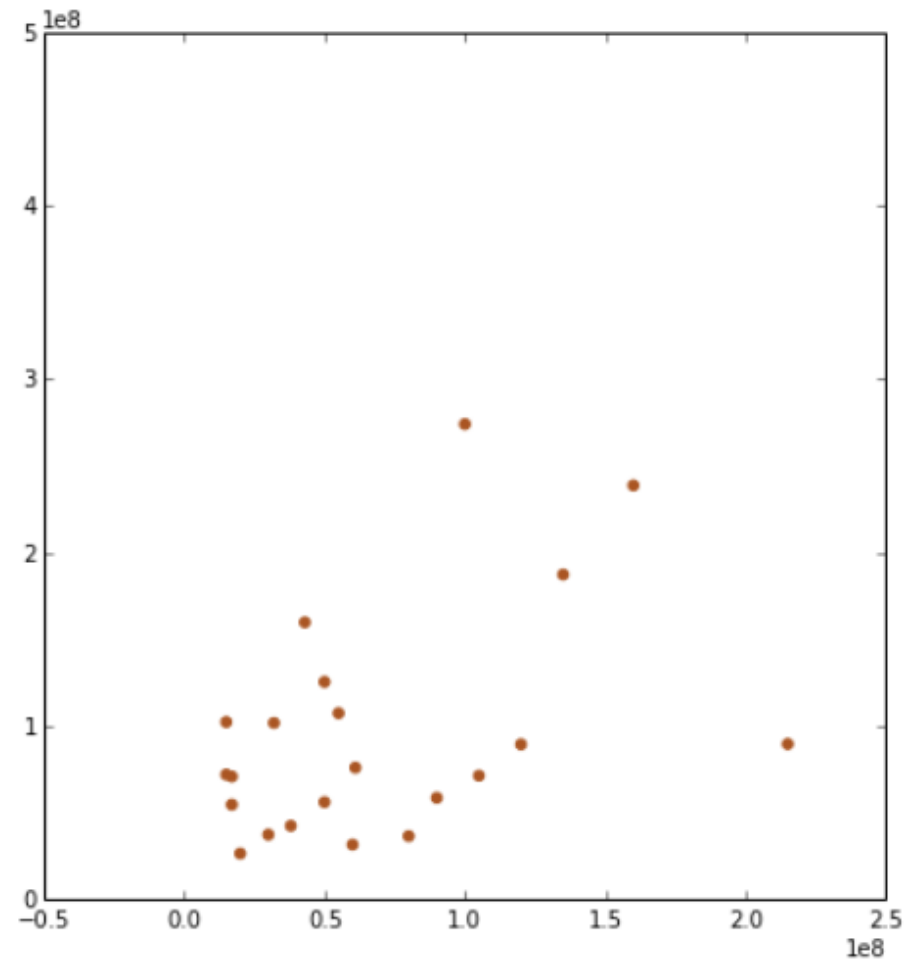
measure performance

- predict  $y$  with model
- compare with actual  $y$
- measure error

# Training set

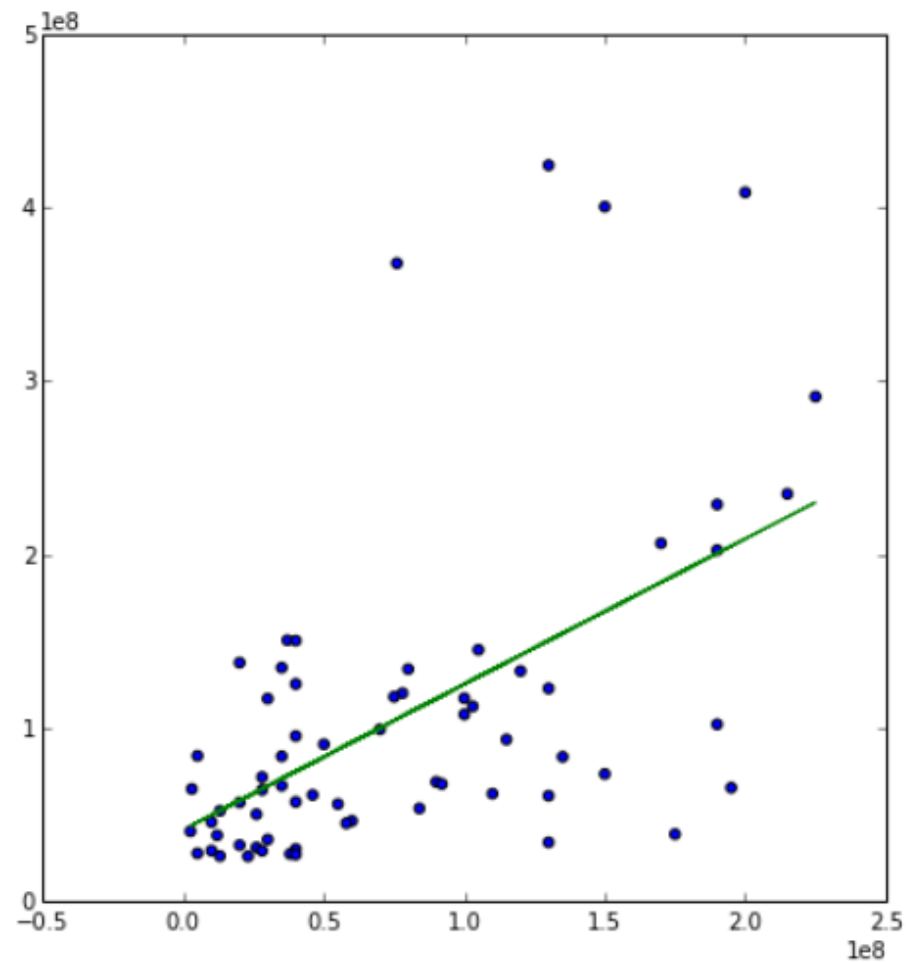


# Test set

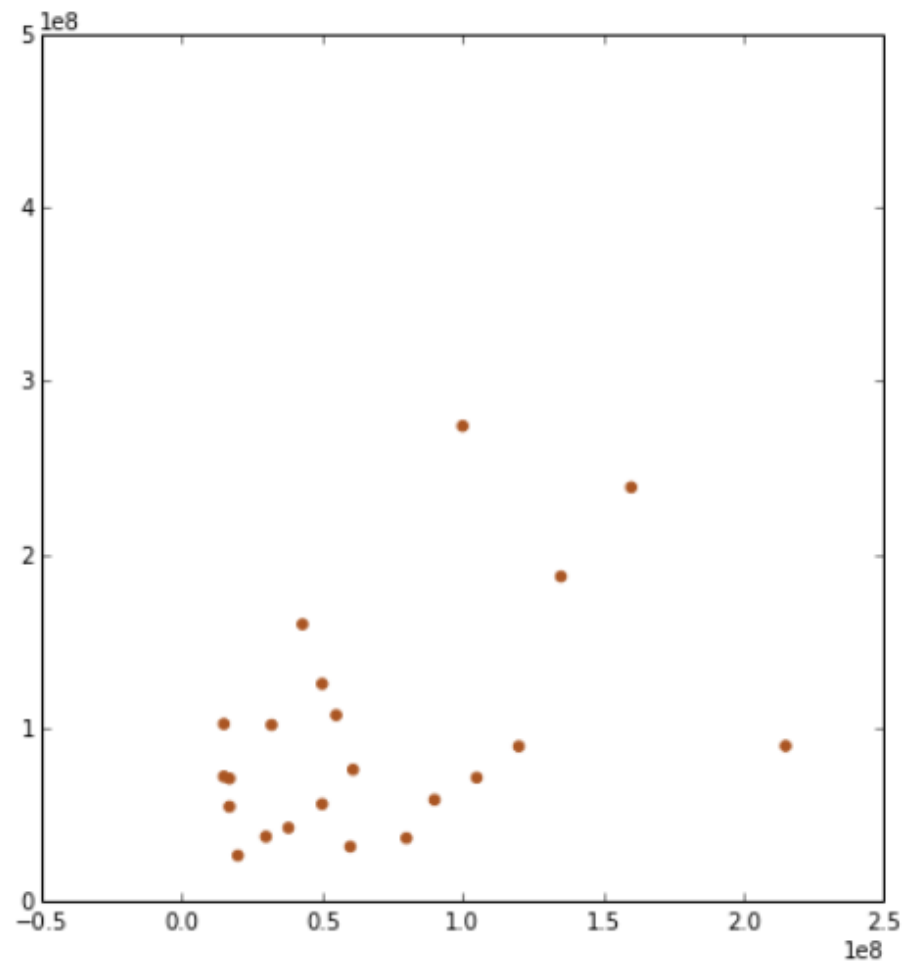


# Training set

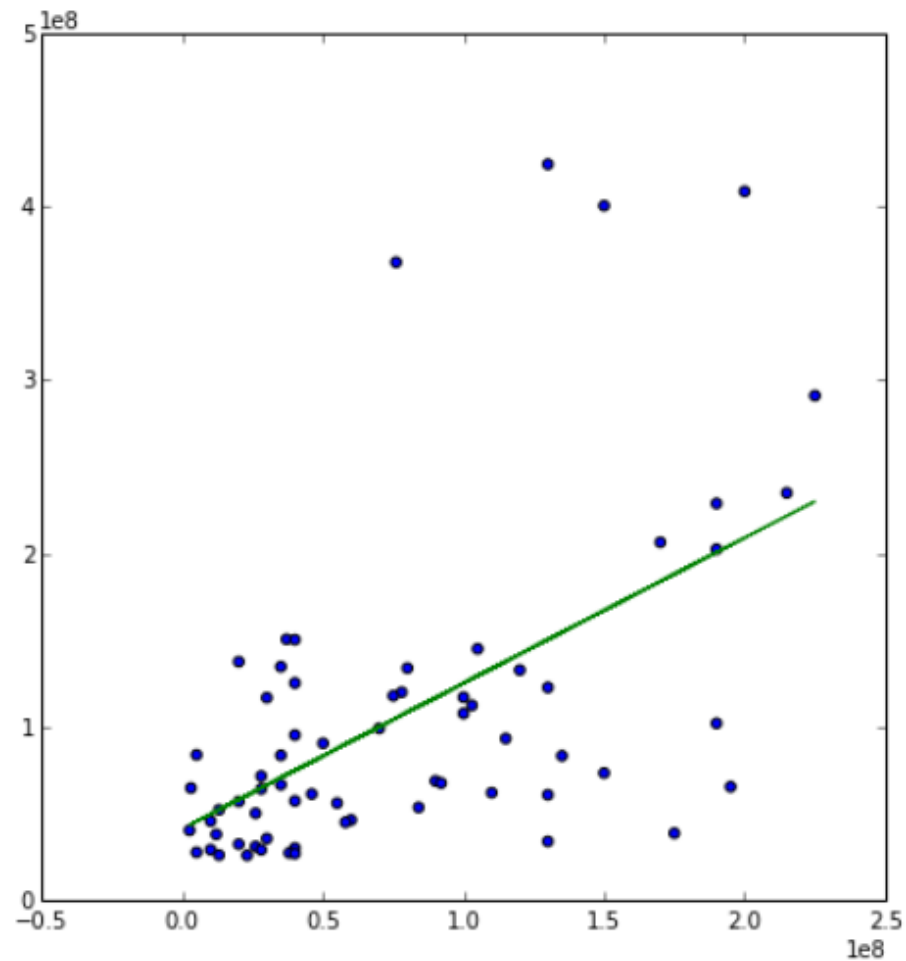
Fit the model



# Test set

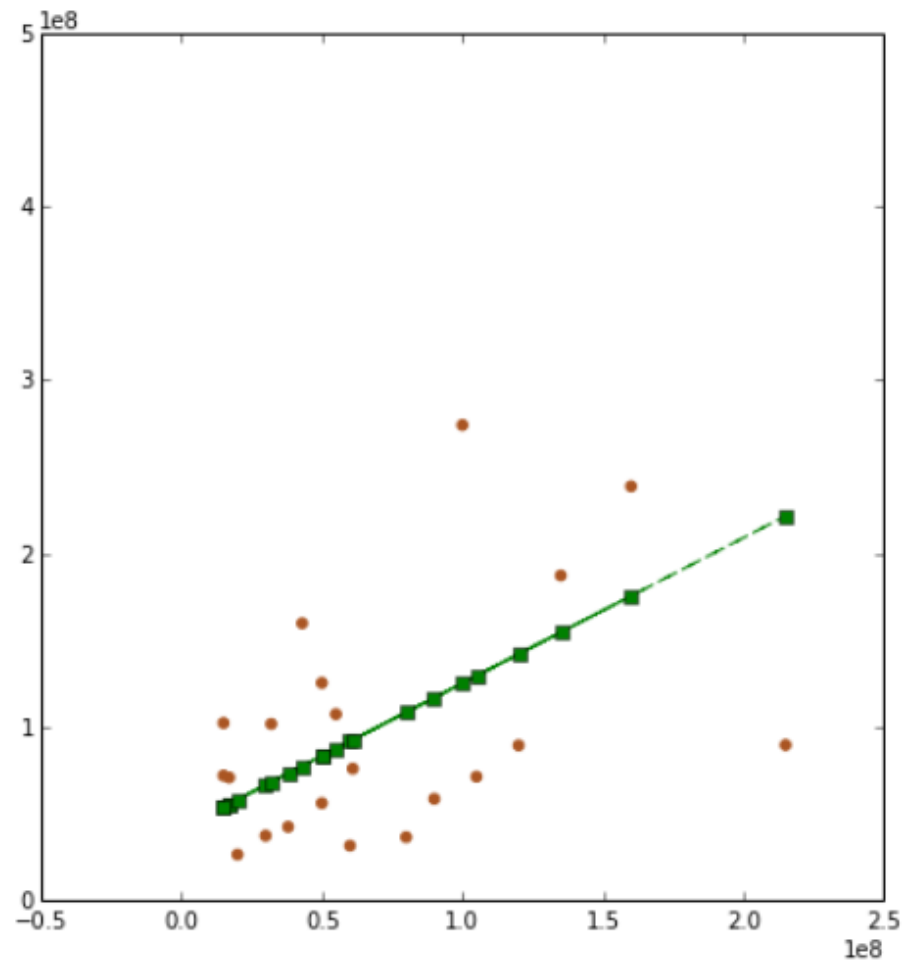


## Training set



## Test set

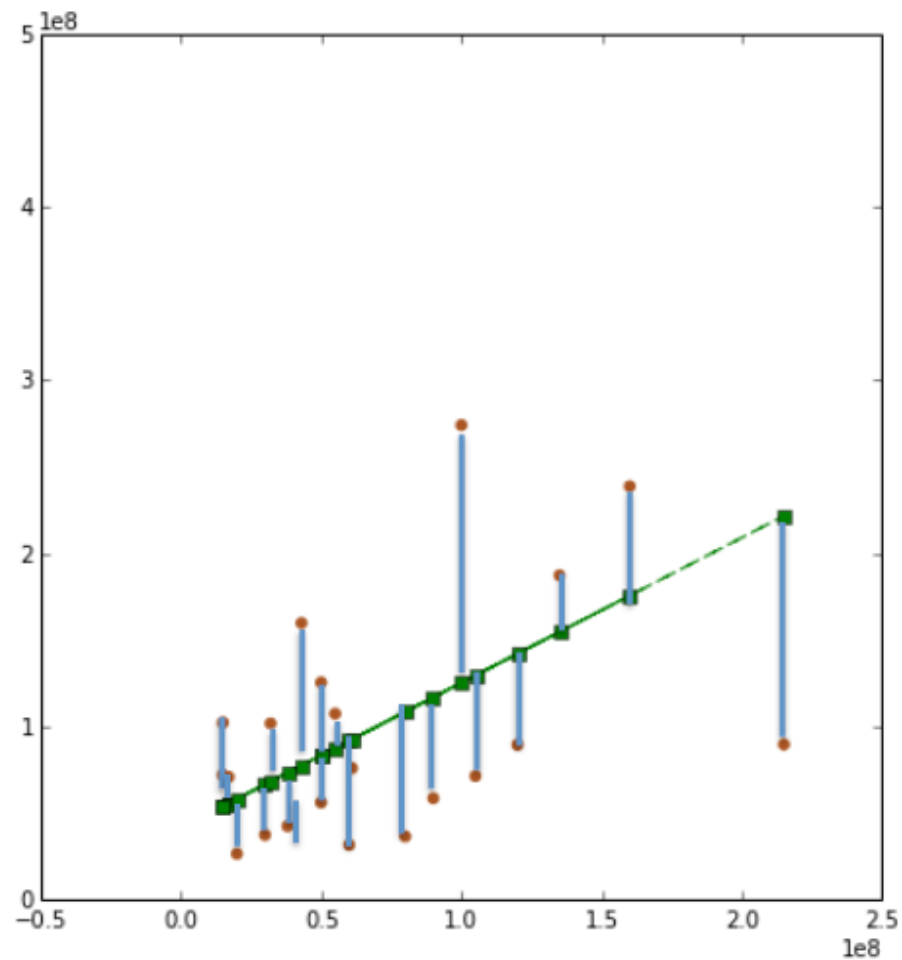
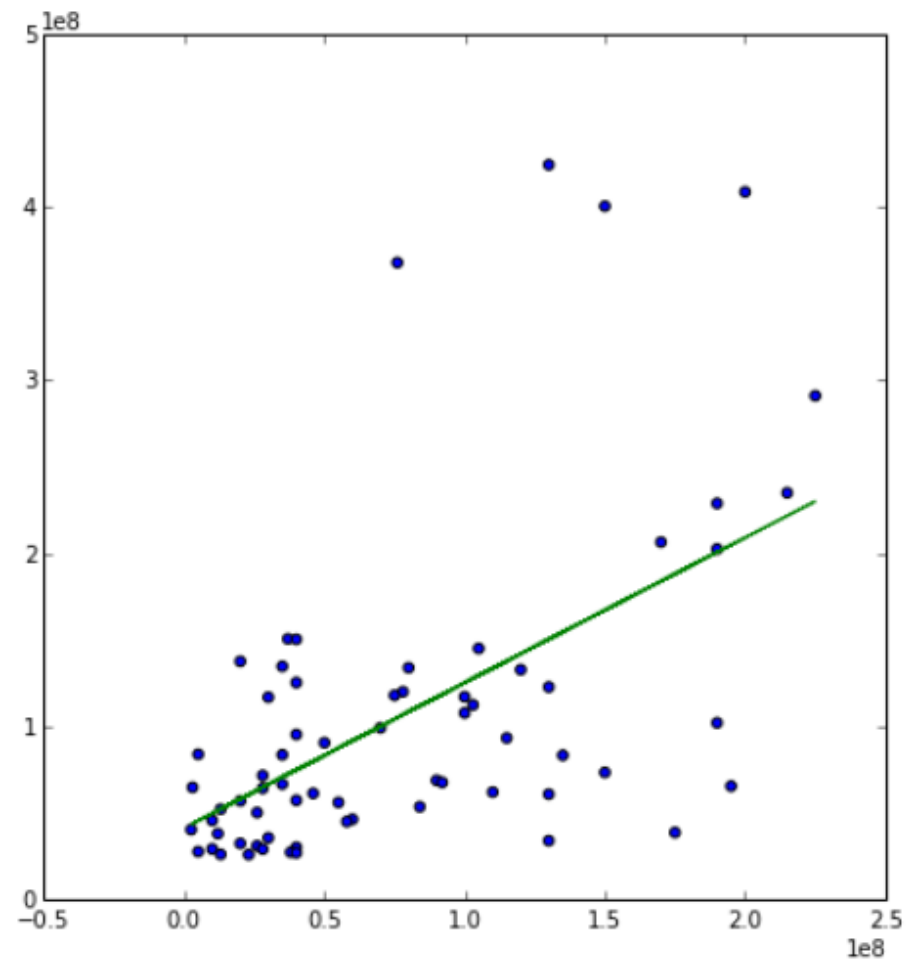
Use the model to predict y from x



Training set

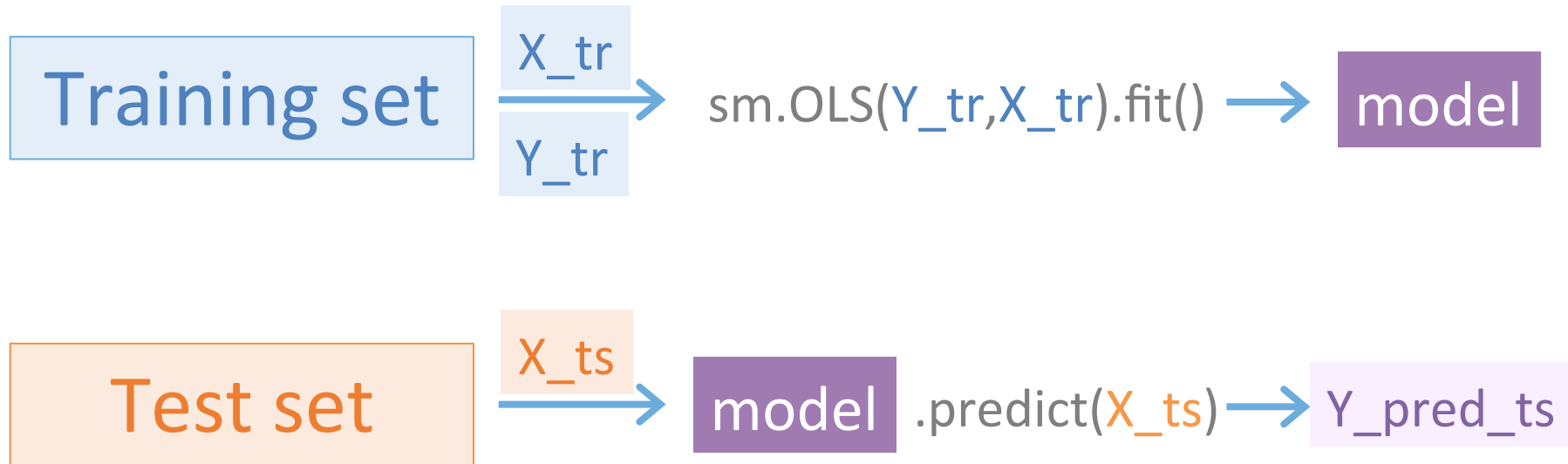
Test set

Measure the error

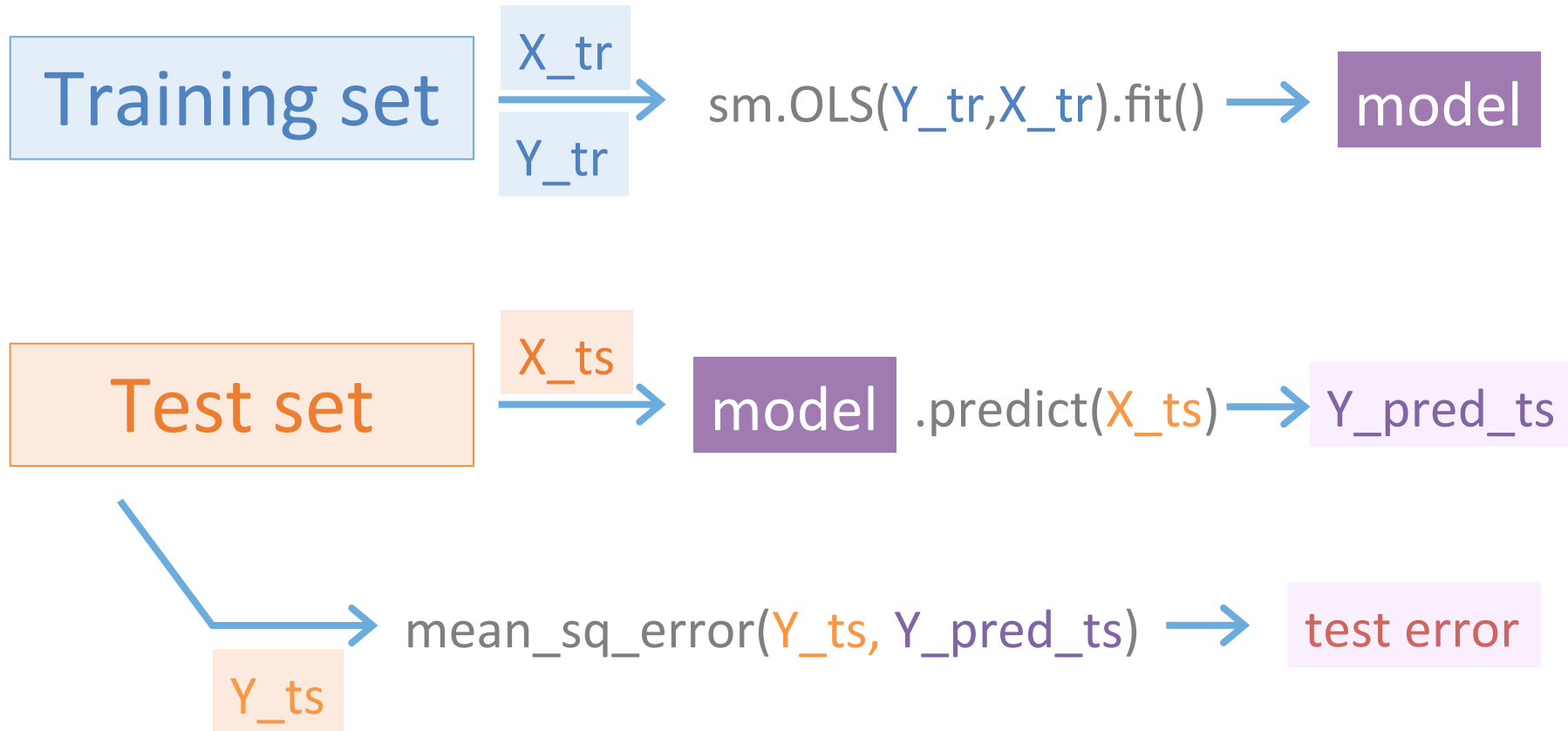




# Training and test sets



# Training and test sets



# Cross validation

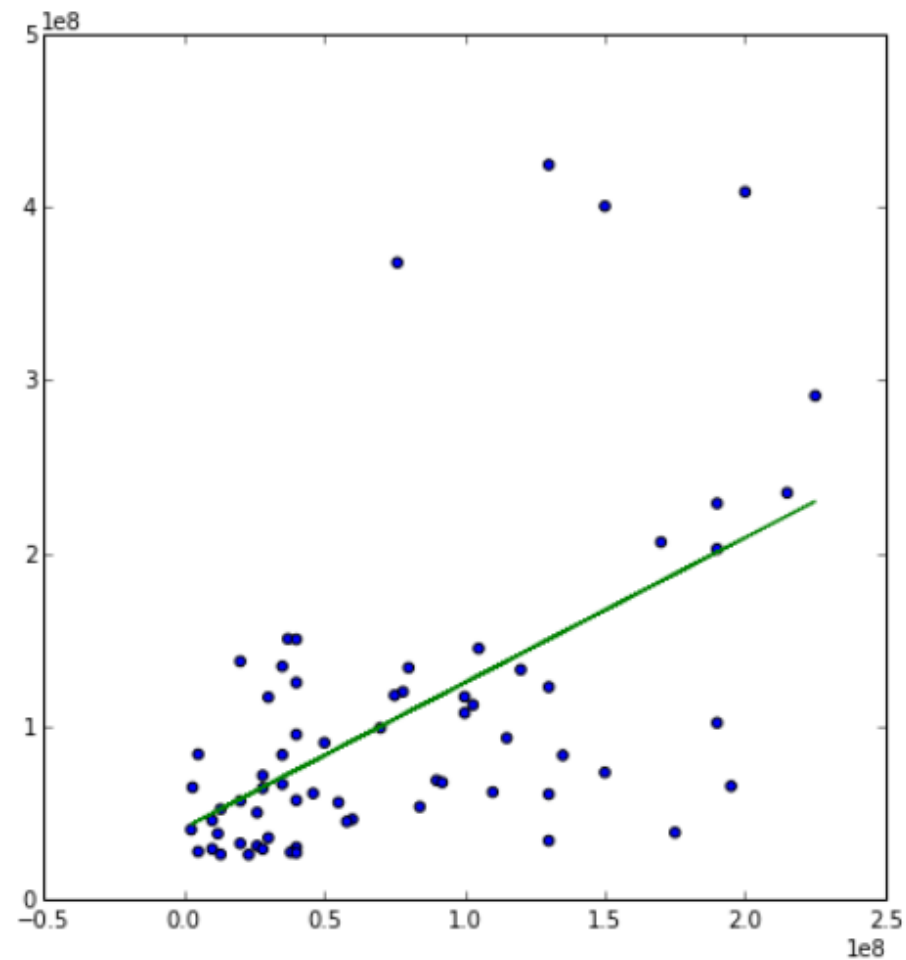
What's better than a single test set?

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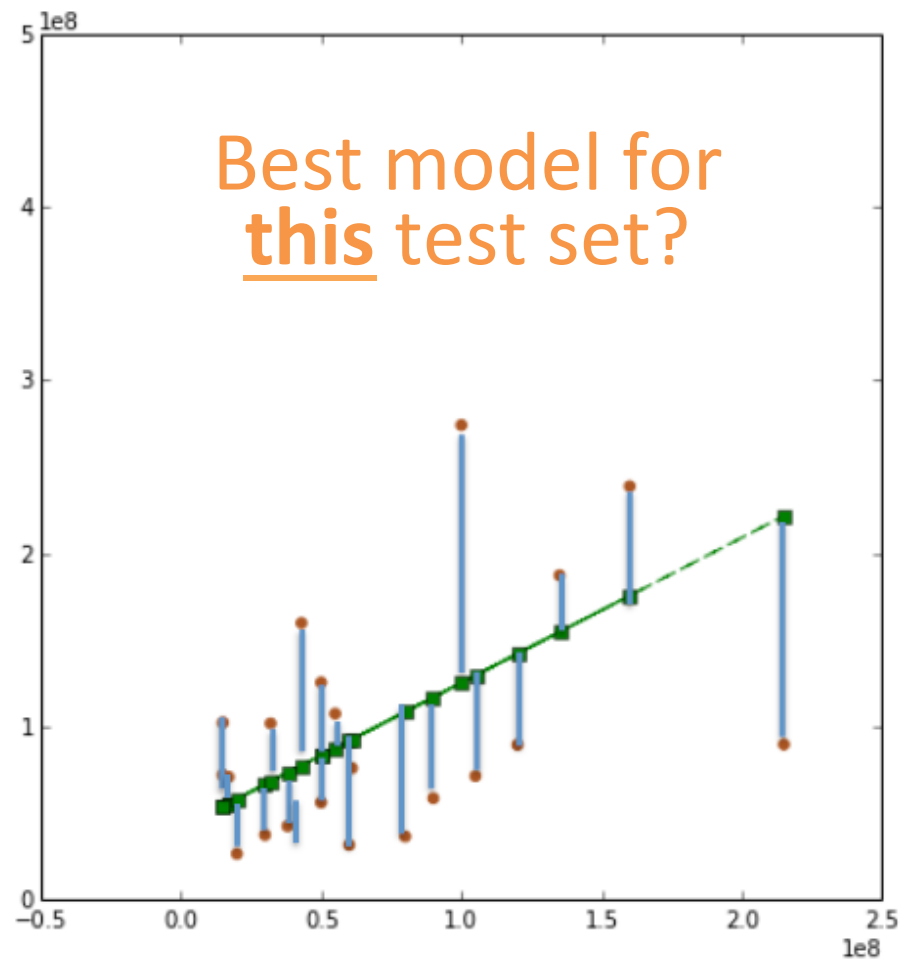
Training  
set

Test set

# Training set



# Test set



# Cross validation

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Training  
set

Test set

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Training  
set 2

Test set  
2

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Test set  
3

Training  
Set 3

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Test set  
4

Training  
Set 4

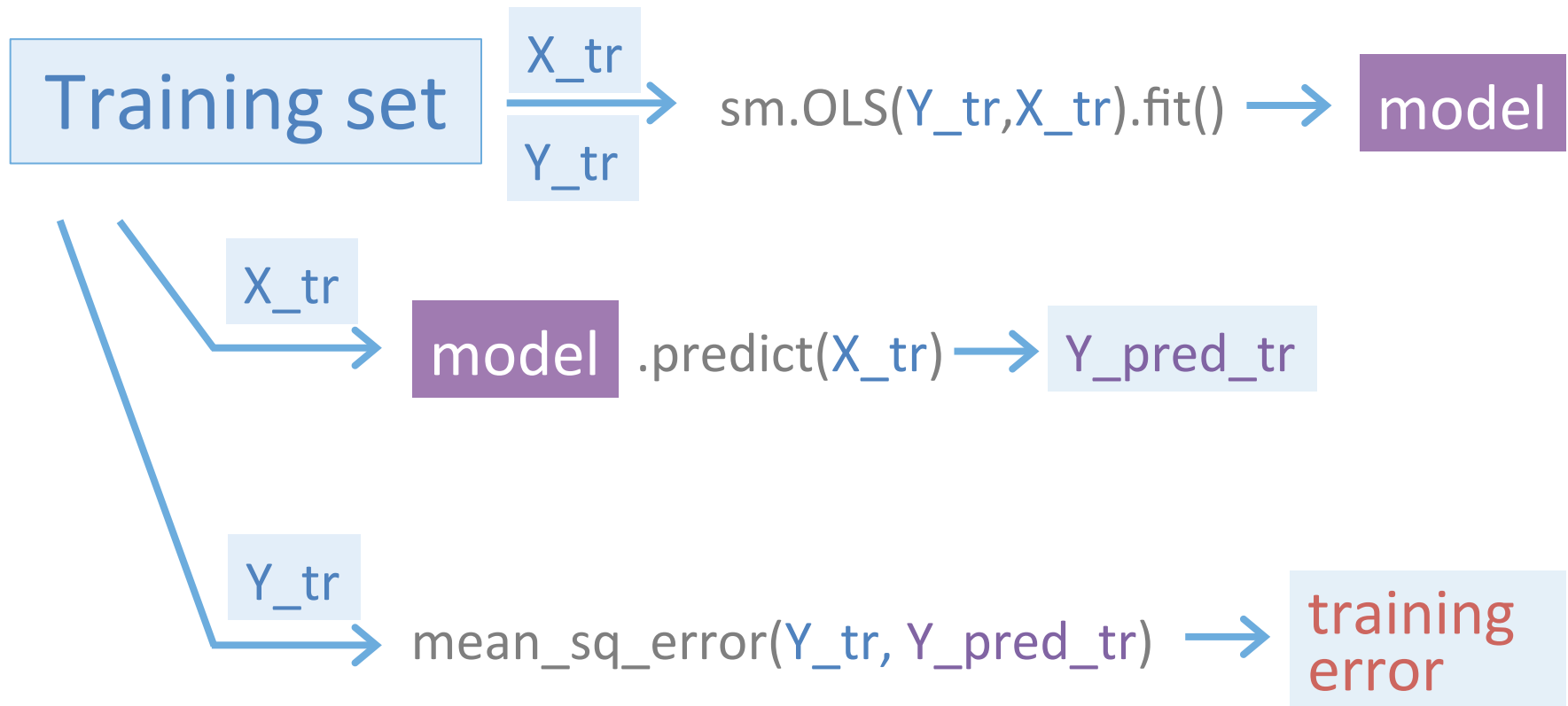


# Diagnostic tools with training and test errors

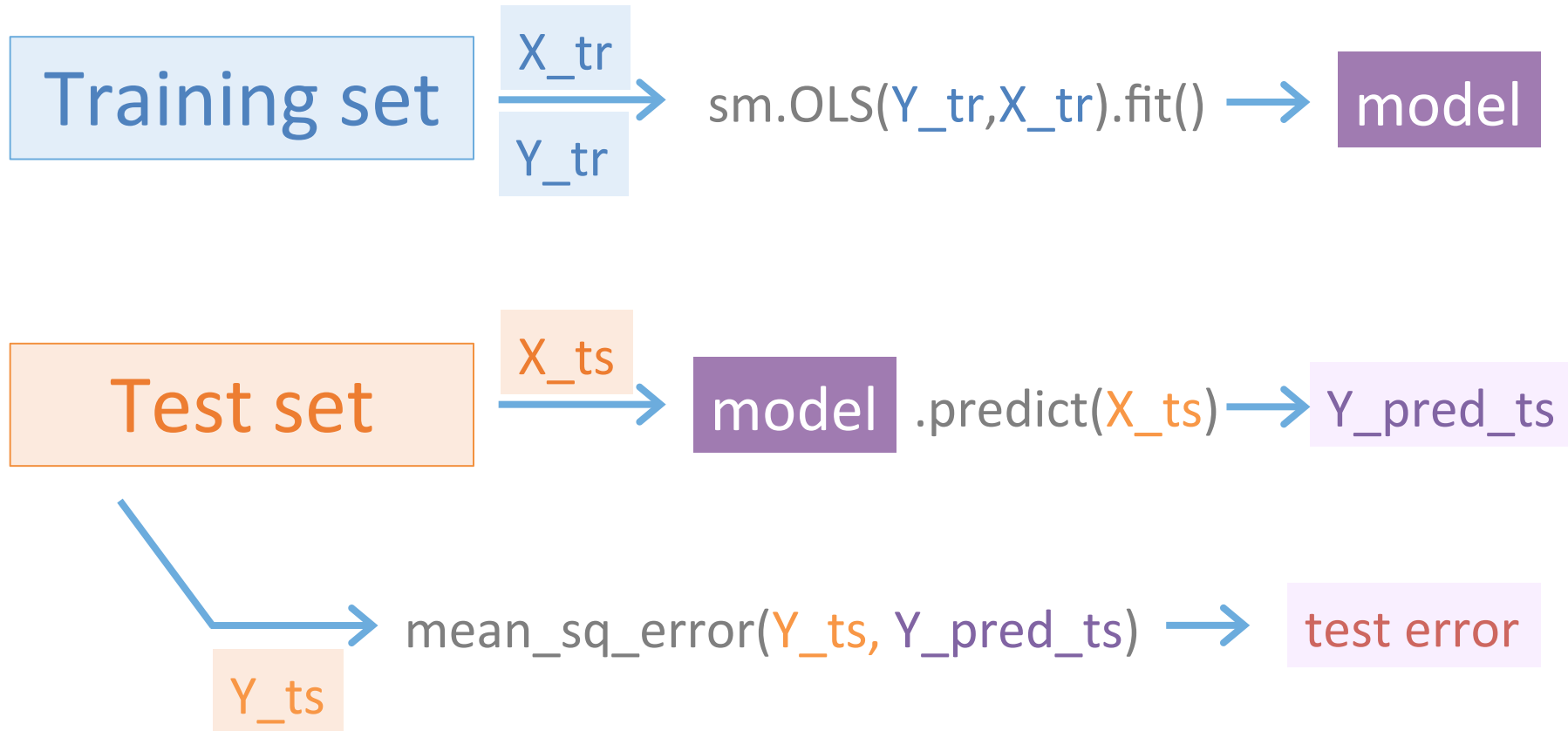


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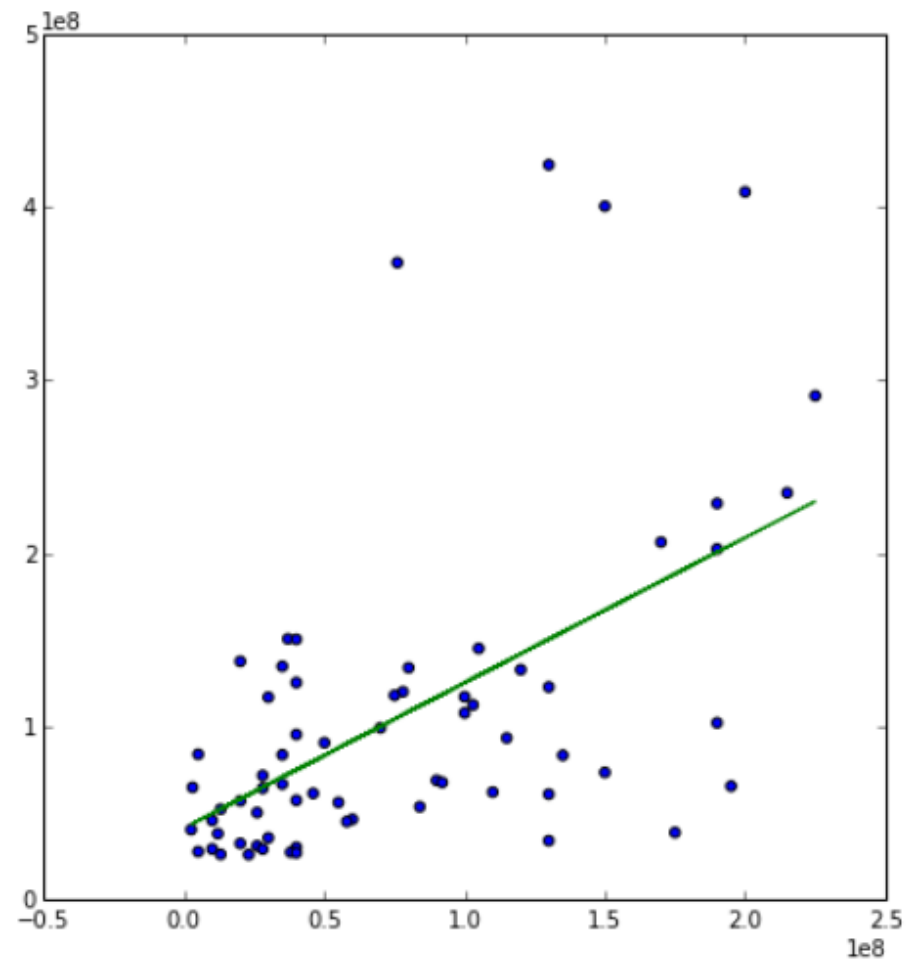
# Calculating Training error



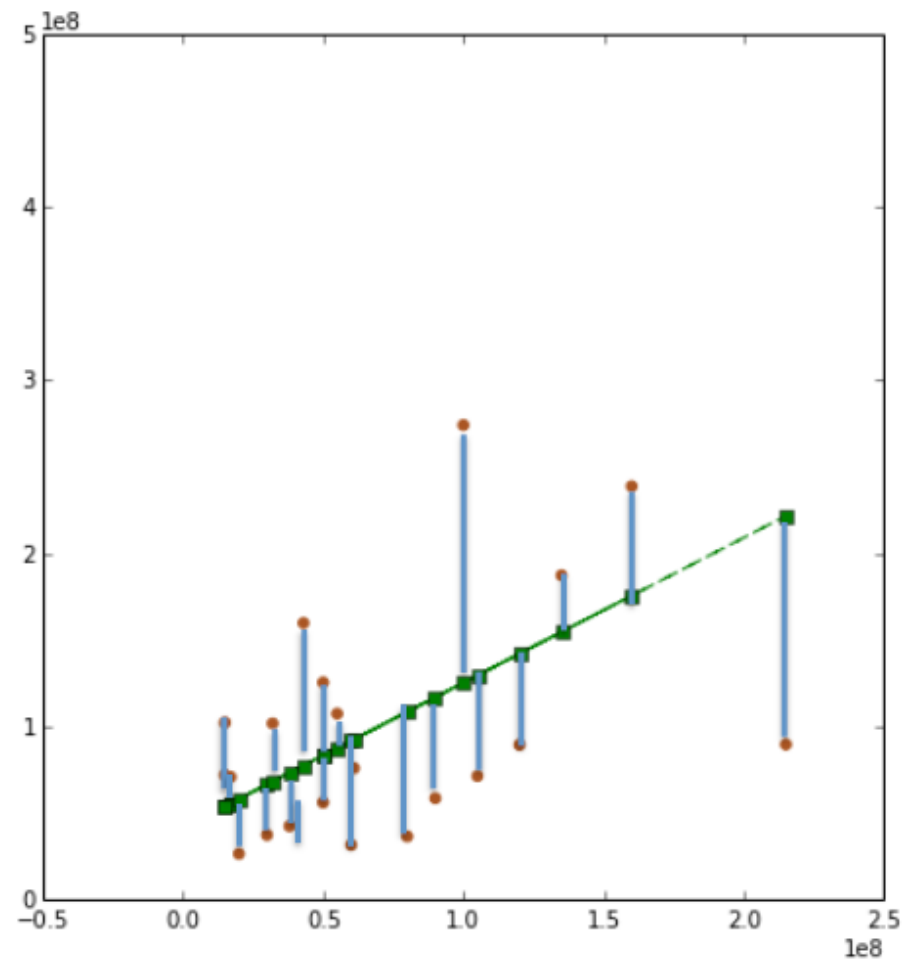
# Calculating test error



# Training set

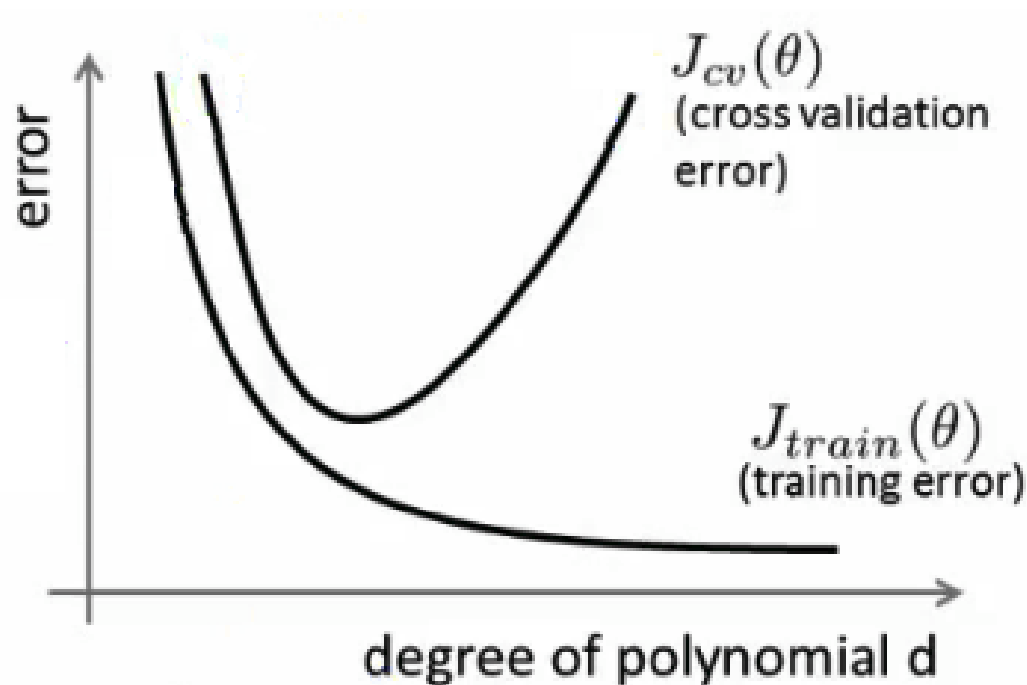


# Test set



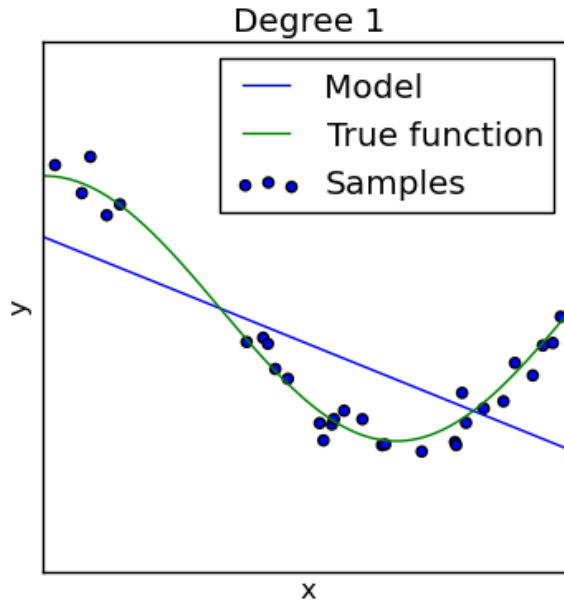
# Diagnostic tool I

## Errors vs. model complexity

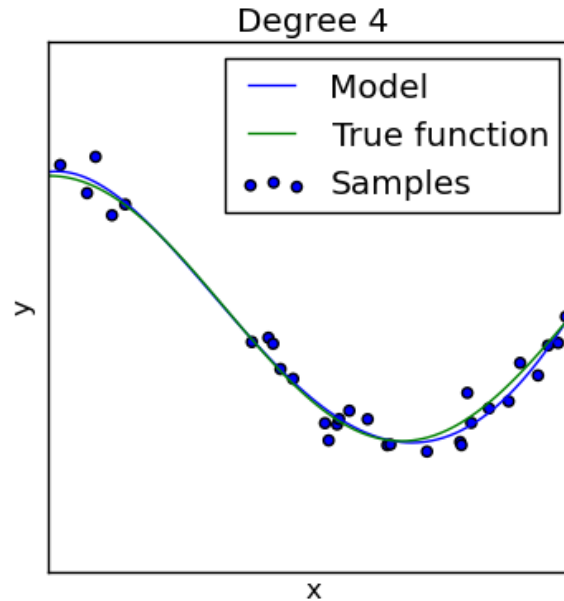


# Diagnostic tool to detect under/overfitting

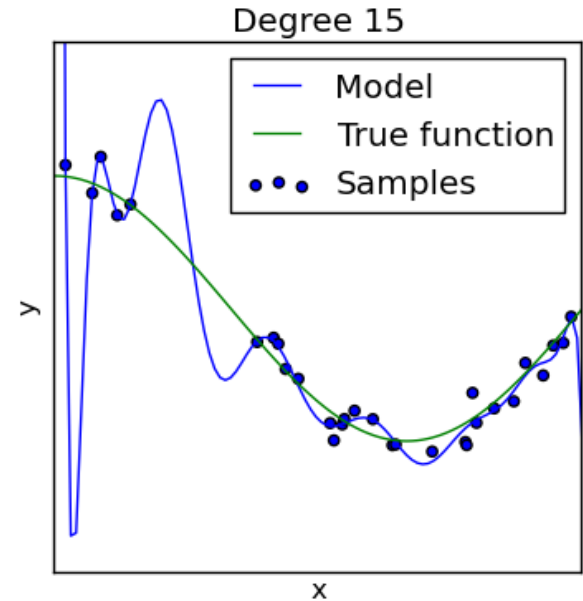
## Underfitting



## Just Right

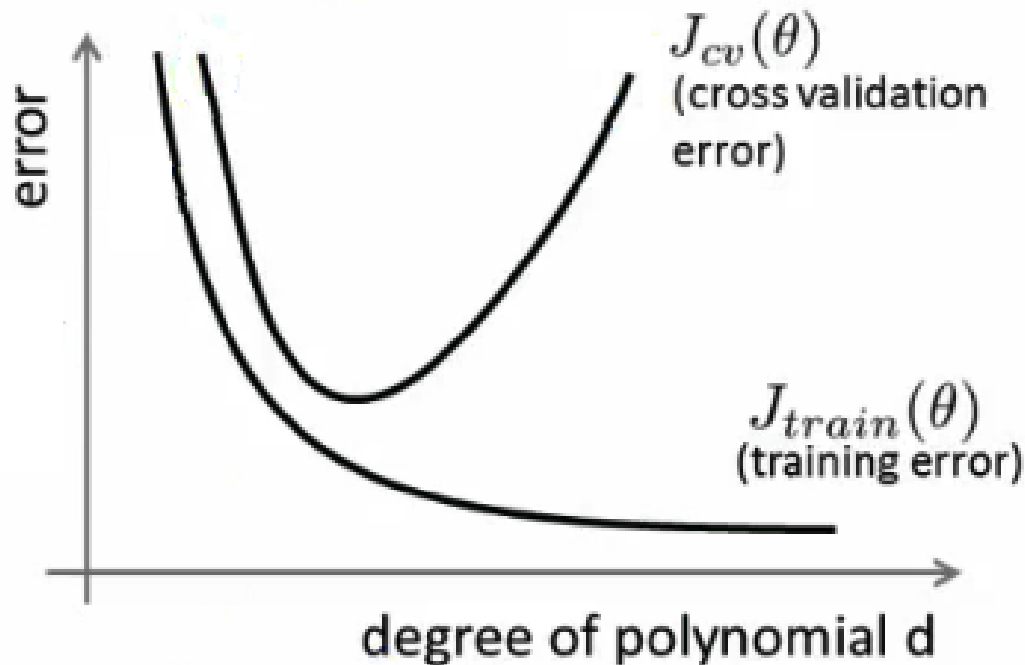


## Overfitting



# Diagnostic tool I

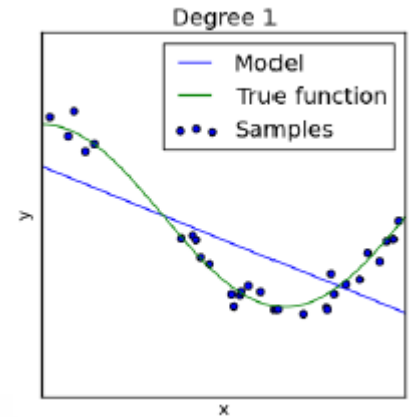
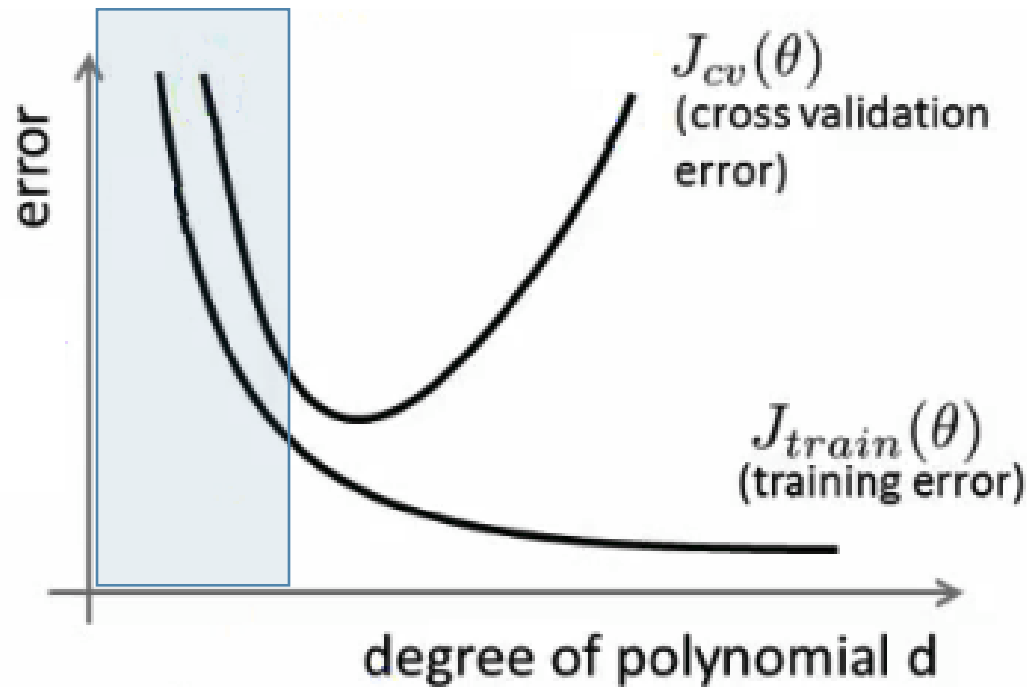
## Errors vs. model complexity



Evaluating MULTIPLE models

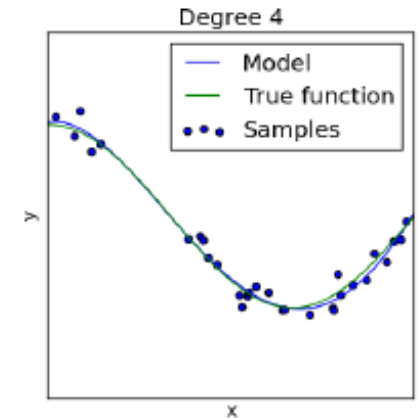
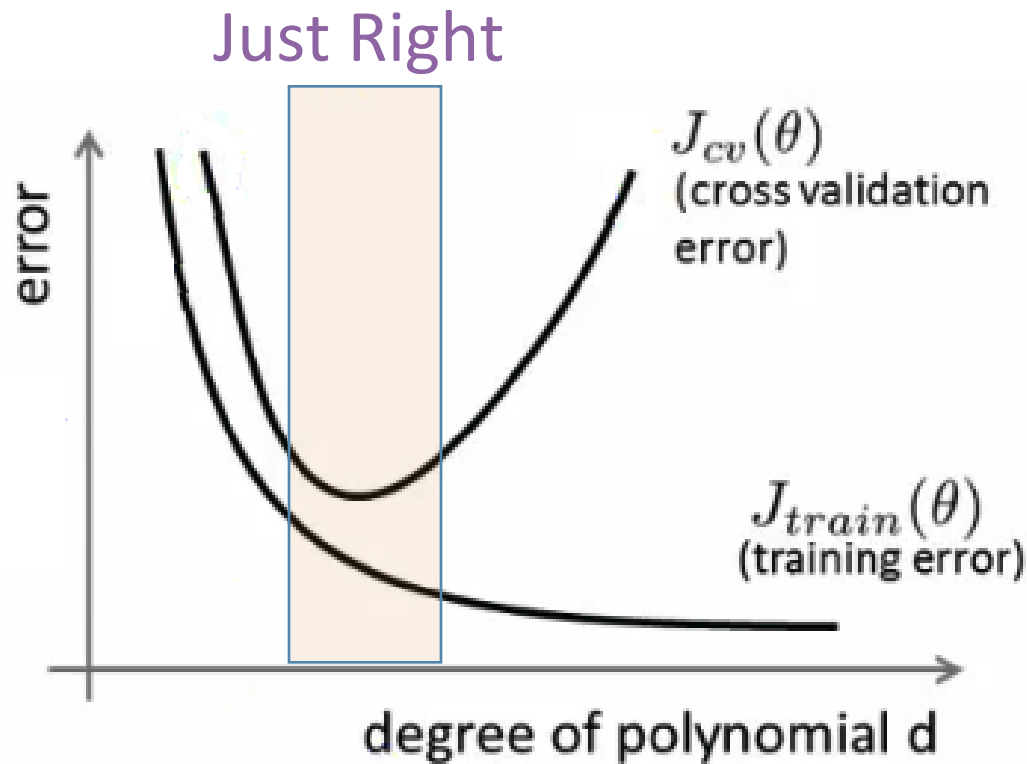
# Diagnostic tool I

## Underfitting

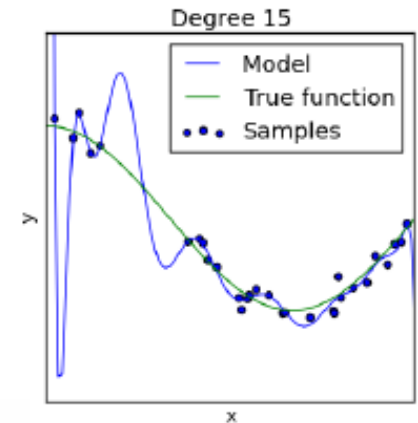
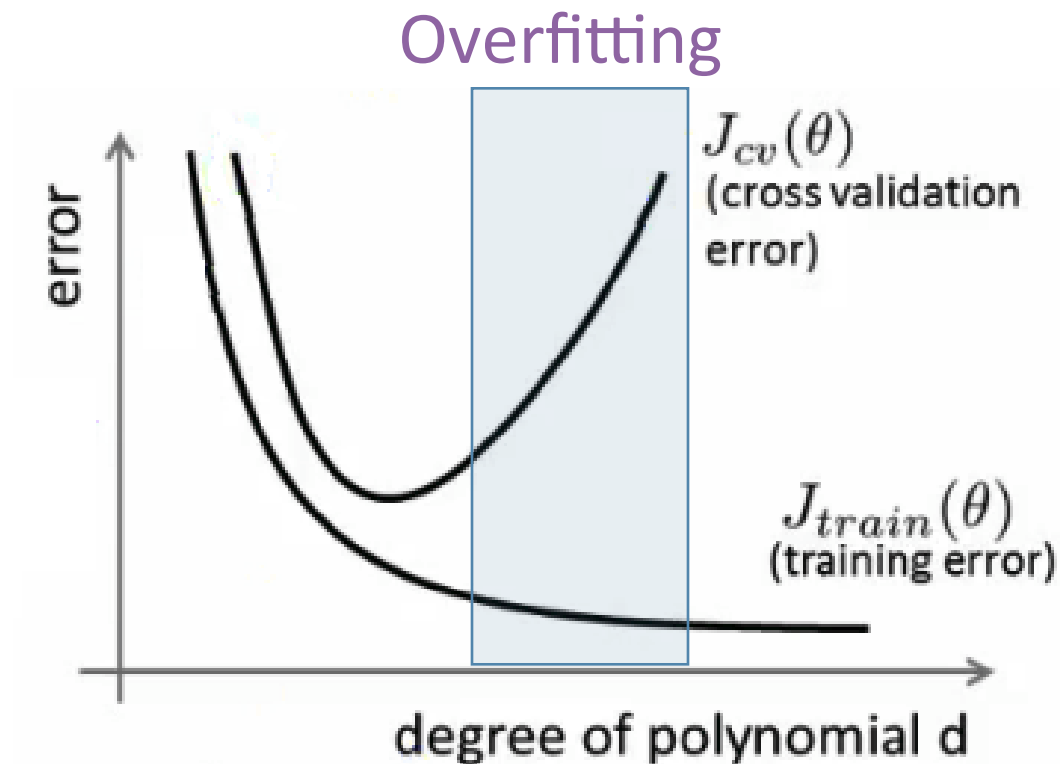




# Diagnostic tool I

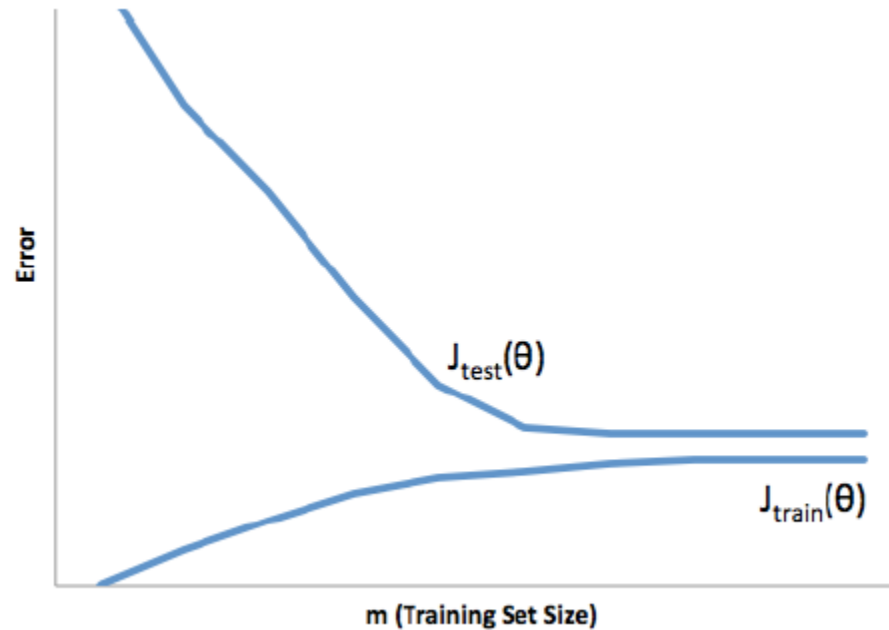


# Diagnostic tool I



# Diagnostic tool II

## Learning curve Errors vs size of training set

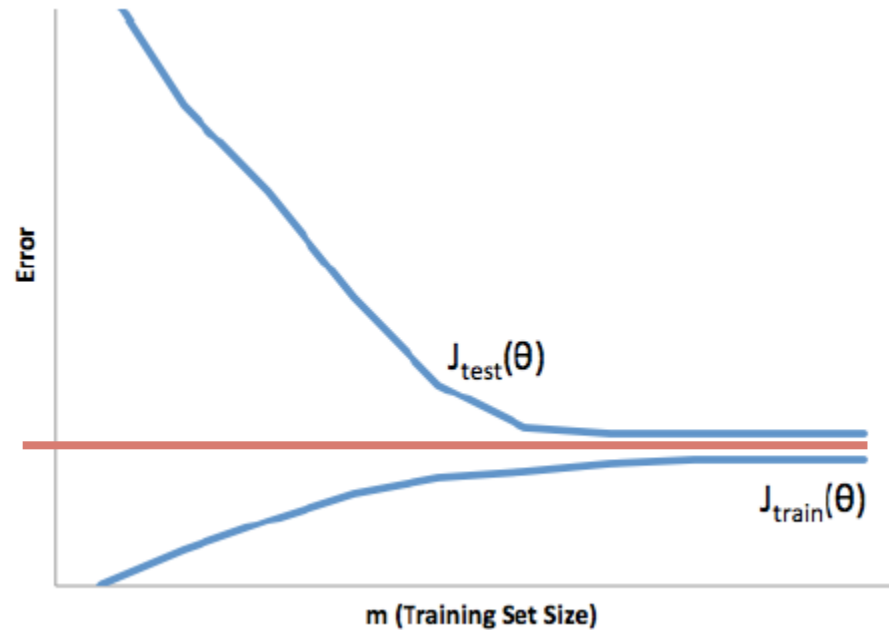


For a SINGLE model form

# Diagnostic tool II

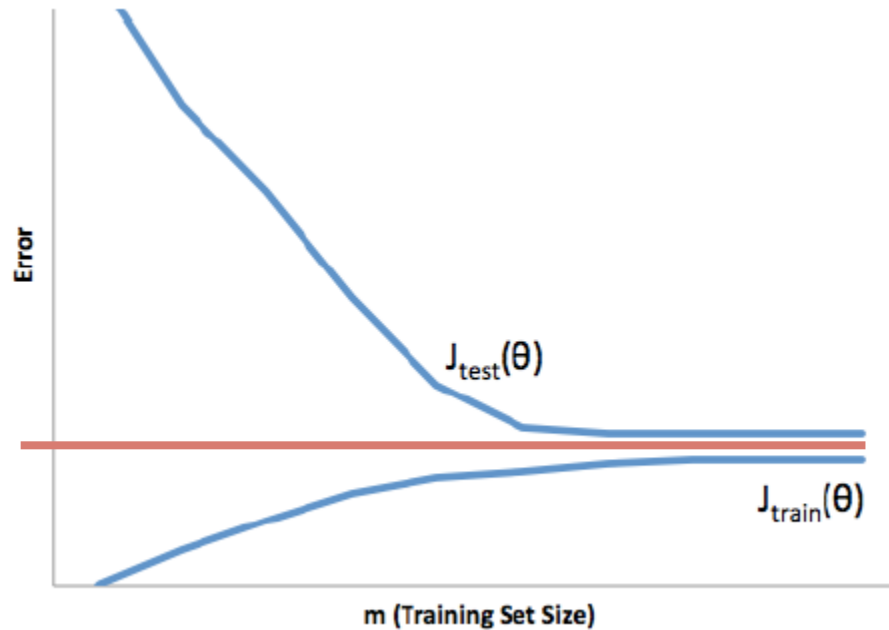
For a SINGLE model form

Is the converged  
error high/low?



# Diagnostic tool II

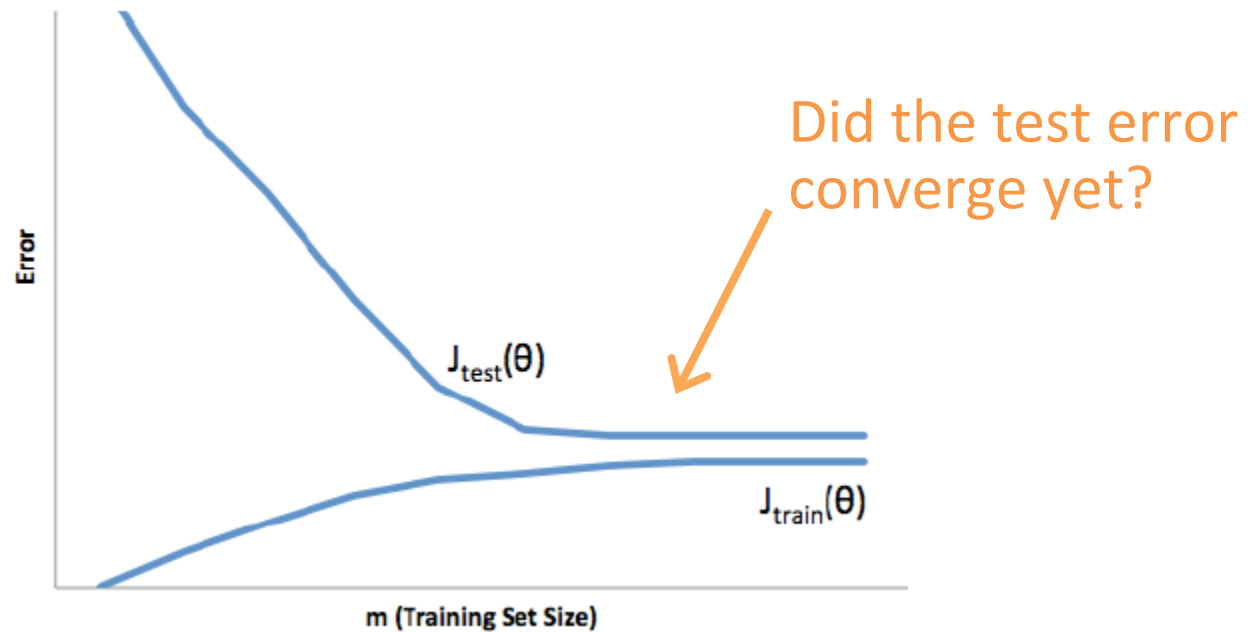
For a SINGLE model form



Is the converged error high/low?  
(compared to another model's learning curve)

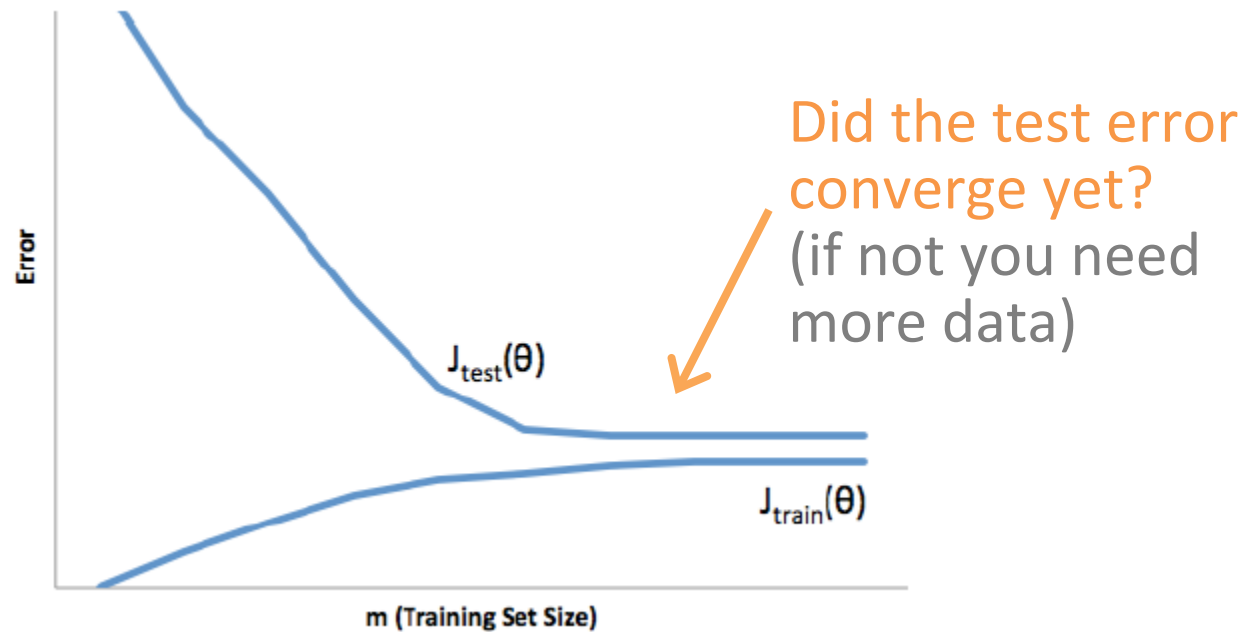
# Diagnostic tool II

For a SINGLE model form



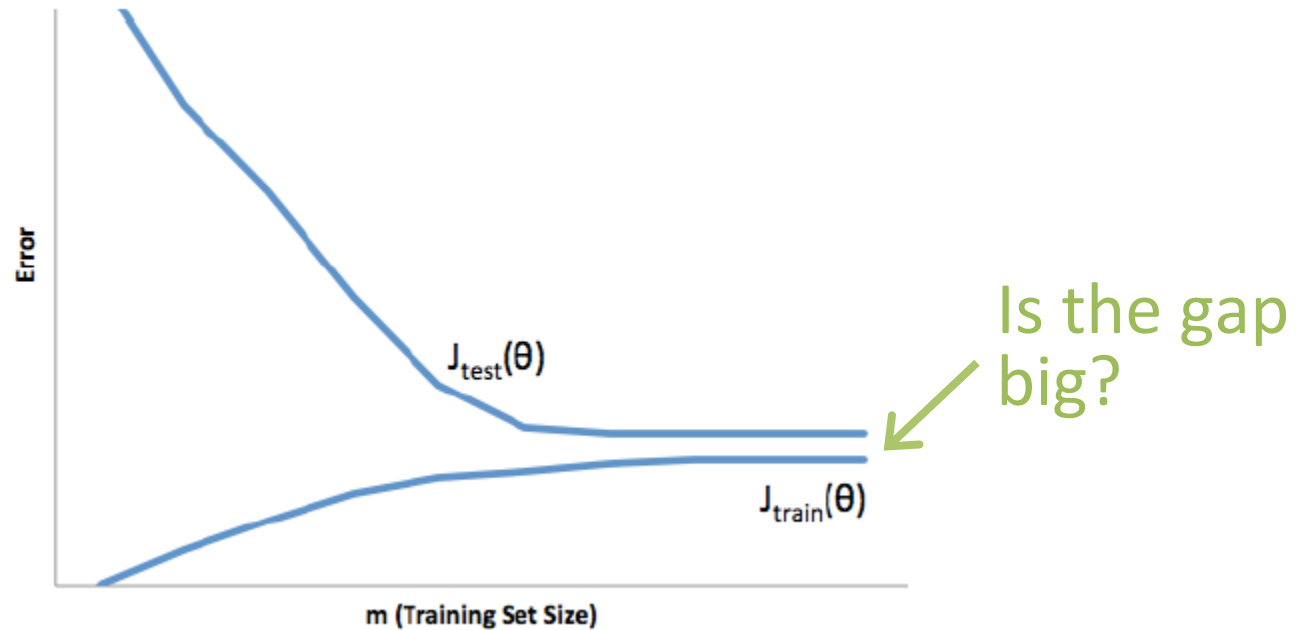
# Diagnostic tool II

For a SINGLE model form



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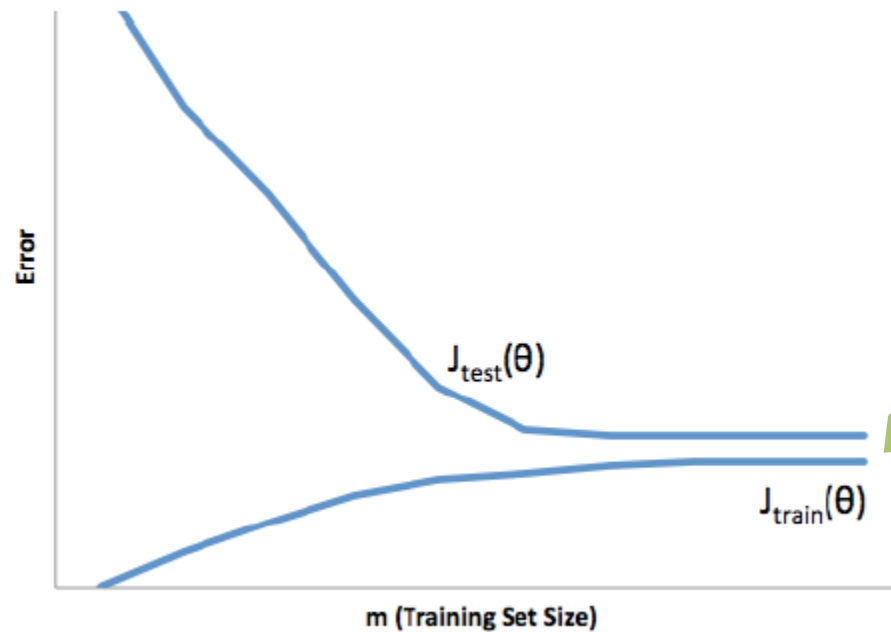
For a SINGLE model form





# Diagnostic tool II

For a SINGLE model form



Is the gap  
big?  
(big gap  
means  
overfit)

# Regularization



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### OLS Regression Results

<b>Dep. Variable:</b>	DomesticTotalGross	<b>R-squared:</b>	0.286
<b>Model:</b>	OLS	<b>Adj. R-squared:</b>	0.278
<b>Method:</b>	Least Squares	<b>F-statistic:</b>	34.82
<b>Date:</b>	Sun, 14 Sep 2014	<b>Prob (F-statistic):</b>	6.80e-08
<b>Time:</b>	21:59:46	<b>Log-Likelihood:</b>	-1738.1
<b>No. Observations:</b>	89	<b>AIC:</b>	3480.
<b>Df Residuals:</b>	87	<b>BIC:</b>	3485.
<b>Df Model:</b>	1		

	<b>coef</b>	<b>std err</b>	<b>t</b>	<b>P&gt; t </b>	<b>[95.0% Conf. Int.]</b>
<b>Budget</b>	0.7846	0.133	5.901	0.000	0.520 1.049
<b>Ones</b>	4.44e+07	1.27e+07	3.504	0.001	1.92e+07 6.96e+07

<b>Omnibus:</b>	39.749	<b>Durbin-Watson:</b>	0.674
<b>Prob(Omnibus):</b>	0.000	<b>Jarque-Bera (JB):</b>	99.441
<b>Skew:</b>	1.587	<b>Prob(JB):</b>	2.55e-22
<b>Kurtosis:</b>	7.091	<b>Cond. No.</b>	1.54e+08

$$AIC = 2k - 2\ln(L)$$



# parameters

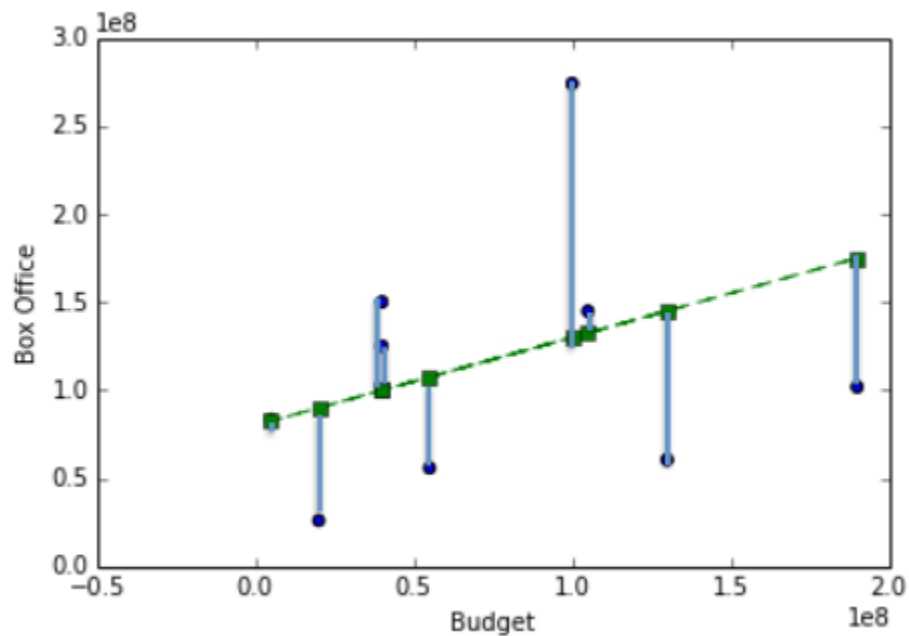


Log likelihood

While awarding **goodness of fit**, penalize **model complexity**

While awarding goodness of fit, penalize model complexity

Why not do that while we are fitting?

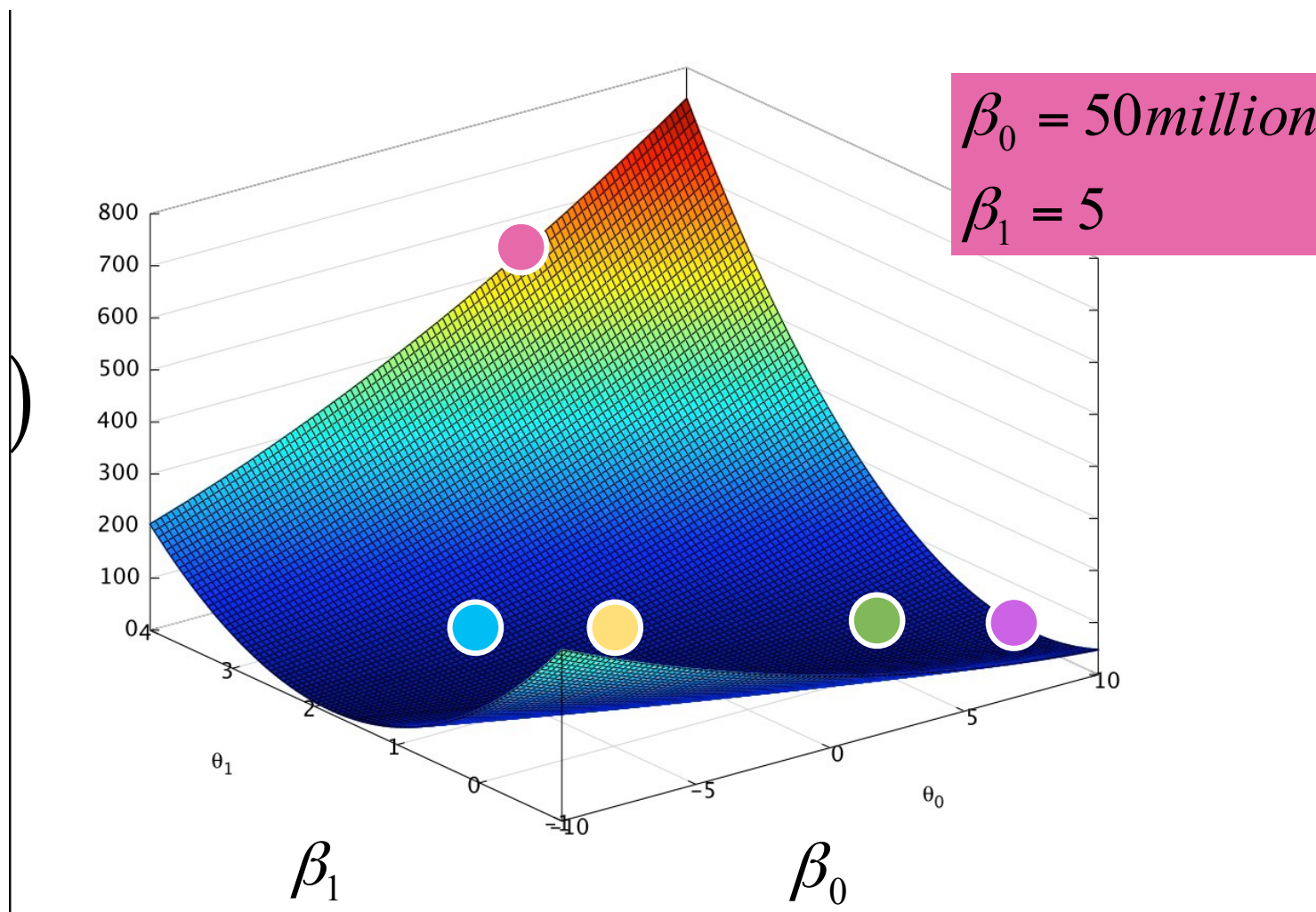


## Cost function

Takes a model (specific parameter values), returns a score

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( (\beta_0 + \beta_1 x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2$$

$$J(\beta_0, \beta_1)$$



$\beta_0 = 80\text{million}$   
 $\beta_1 = 0.5$

$\beta_0 = 0$   
 $\beta_1 = 1.5$

$\beta_0 = 120\text{million}$   
 $\beta_1 = 0.1$

$\beta_0 = 30\text{million}$   
 $\beta_1 = 2$

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( (\beta_0 + \beta_1 x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2$$



## Cost function

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( (\beta_0 + \beta_1 x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2$$

## Cost function

Add a penalty for the size of each parameter!

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( y_{\beta}(x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2 + \lambda \sum_{j=1}^k \beta_j^2$$

# Ridge Regression

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( y_{\beta}(x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2 + \lambda \sum_{j=1}^k \beta_j^2$$

$$\lambda=1$$

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( y_{\beta}(x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2 + \lambda \sum_{j=1}^k \beta_j^2$$

$$y_{\beta}(x) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_4 x_4 + \varepsilon$$

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( y_{\beta}(x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2 + \lambda \sum_{j=1}^k \beta_j^2$$

$\lambda=1$ 
↘

$$y_{\beta}(x) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_4 x_4 + \varepsilon$$

$\approx 0$ 
↓
 $\approx 0$ 
↓

VERY LARGE  
underfit

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( y_{\beta}(x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2 + \lambda \sum_{j=1}^k \beta_j^2$$

$\approx 0$



$\approx 0$



$\approx 0$



$\approx 0$



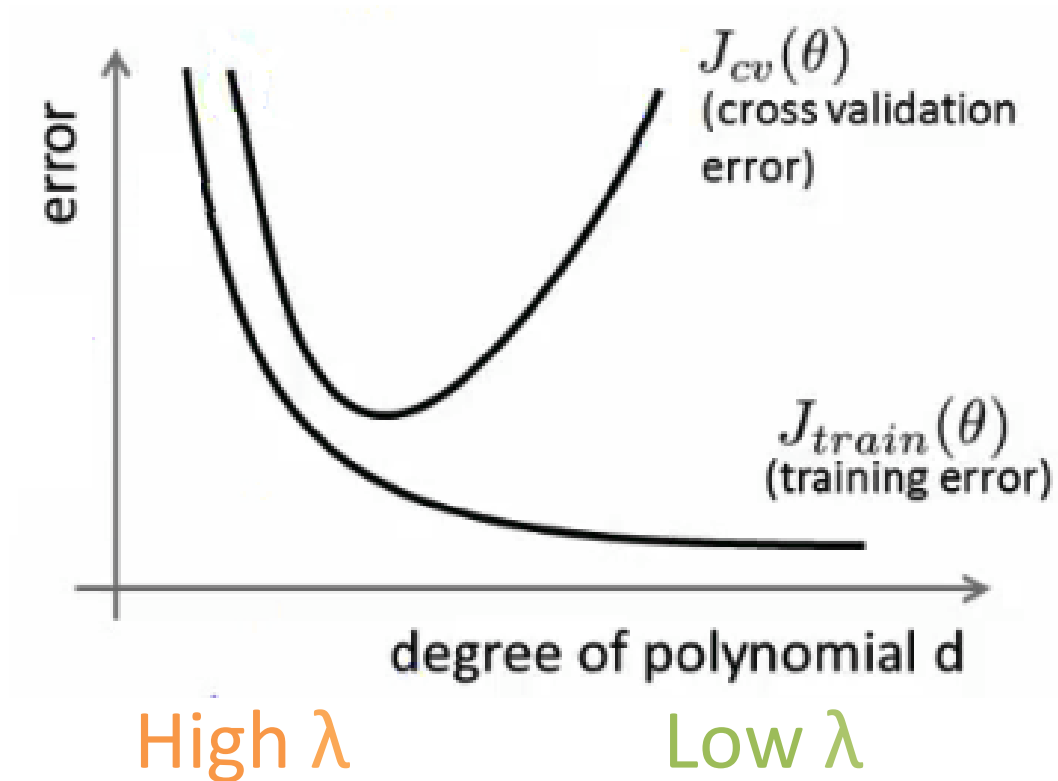
$$y_{\beta}(x) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_4 x_4 + \varepsilon$$

very small  
possible  
overfit

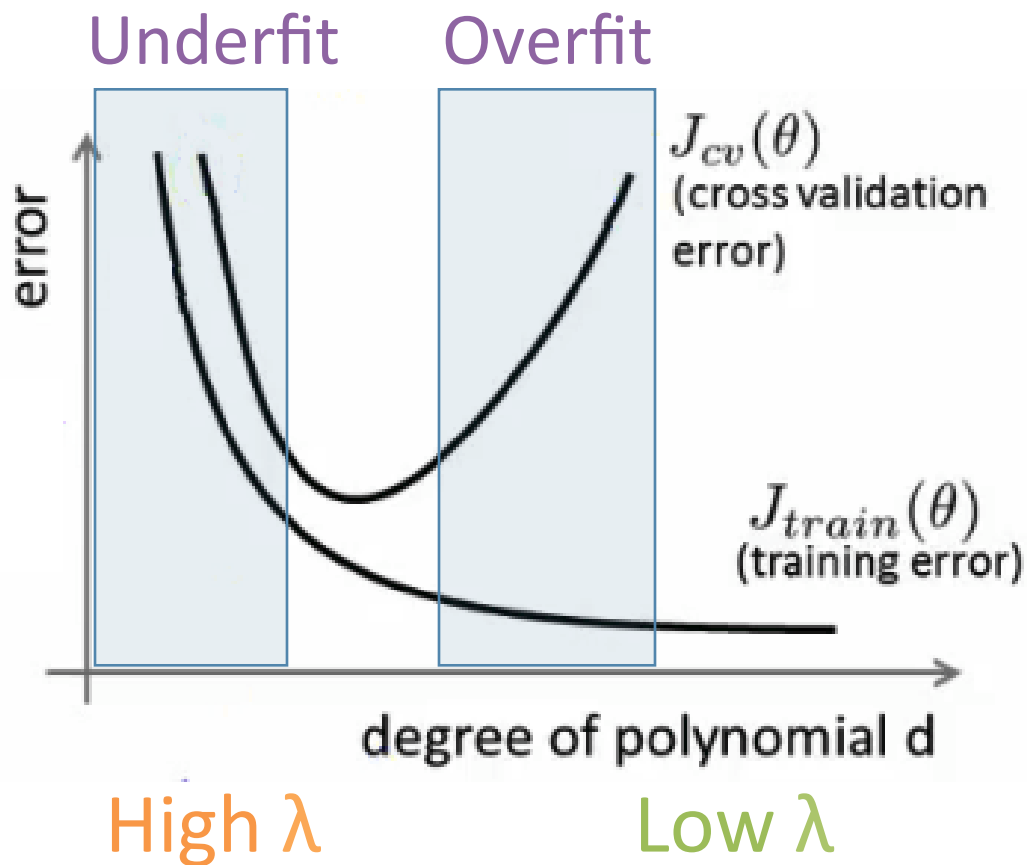
$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( y_{\beta}(x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2 + \lambda \sum_{j=1}^k \beta_j^2$$

$$y_{\beta}(x) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_4 x_4 + \varepsilon$$

# Error vs. regularization $\lambda$







## Ridge Regularization (L2)

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( y_{\beta}(x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2 + \lambda \sum_{j=1}^k \beta_j^2$$

## Ridge Regularization (L2)

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( y_{\beta}(x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2 + \lambda \sum_{j=1}^k \beta_j^2$$

## Lasso Regularization (L1)

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( y_{\beta}(x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2 + \lambda \sum_{j=1}^k |\beta_j|$$

## Ridge Regularization (L2)

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( y_{\beta}(x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2 + \lambda \sum_{j=1}^k \beta_j^2$$

## Lasso Regularization (L1)

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( y_{\beta}(x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2 + \lambda \sum_{j=1}^k |\beta_j|$$

## Elastic Net (L1 + L2)

$$J(\beta_0, \beta_1) = \frac{1}{2m} \sum_{i=1}^m \left( y_{\beta}(x_{obs}^{(i)}) - y_{obs}^{(i)} \right)^2 + \lambda_1 \sum_{j=1}^k |\beta_j| + \lambda_2 \sum_{j=1}^k \beta_j^2$$

# How can I use this?

We were doing:

```
from sklearn.linear_model import LinearRegression  
model = LinearRegression()  
model.fit(X,Y)
```

# How can I use this?

We were doing:

```
from sklearn.linear_model import LinearRegression  
model = LinearRegression()  
model.fit(X,Y)
```

To use Ridge Regularization:

```
from sklearn.linear_model import Ridge  
model = Ridge(1.0)  
model.fit(X,Y)
```

$\lambda$  (sklearn Calls It alpha)



# How can I use this?

We were doing:

```
from sklearn.linear_model import LinearRegression  
model = LinearRegression()  
model.fit(X,Y)
```

To use Lasso:

```
from sklearn.linear_model import Lasso  
model = Lasso(1.0)  
model.fit(X,Y)
```

$\lambda$  (sklearn Calls It alpha)



# How can I use this?

We were doing:

```
from sklearn.linear_model import LinearRegression
model = LinearRegression()
model.fit(X,Y)
```

To use Elastic Net:

```
from sklearn.linear_model import ElasticNet
model = ElasticNet(1.0, l1_ratio = 0.5)
model.fit(X,Y)
```



total weight for the full  
penalty term



ratio of l1/l2 penalty



My model is not  
awesome  
enough.

What do I do?

Try these and check test error  
(and AIC,BIC,etc.) again:

Use a smaller set of features

Try adding polynomials

Check functional forms for each feature

Try including other features

Use more data (bigger training set)

Regularization (tomorrow)

Try these and check test error  
(and AIC,BIC,etc.) again:

Use a smaller set of features

**Regularization: Increase/decrease  $\lambda$**

Try adding polynomials

Check functional forms for each feature

Try including other features

Use more data (bigger training set)