

Supervised Learning



DATA SCIENCE BOOTCAMP

What is Supervised Learning?

Data with
correct answers



model

New Data
without
answers



model



Predicted
answers

Regression: “answers” are numeric

Movie data
including gross



model

Movie data
without gross



model



Predicted
gross

Classification: “answers” are categories

Movie data
including Oscar
wins or lack
thereof



model

Movie data
without
Oscar results



model



Predict
winning oscar

Classification: “answers” are categories

Breast cancer
surgery patient
data including
(survived/not)



model

Patient data
without
survival result



model



Predict survival

Classification: “answers” are categories

Color, shape, weight,
sweetness, sourness
for a bunch of
apples, bananas &
peaches



model

Color, shape, weight,
sweetness, sourness
(without fruit type)



model



Predict apple,
banana or
peach

Classification: “answers” are categories



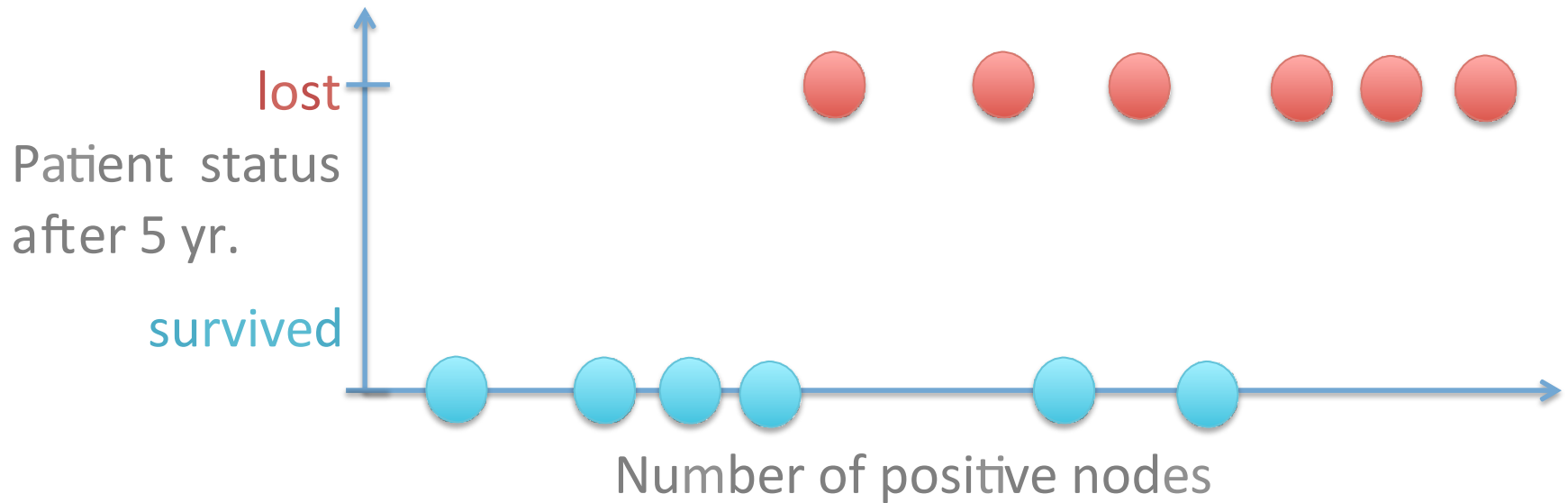
Example: each data point (row)

Label: each category to be predicted

Feature: each property (column) used in predicting

1 Feature: Number of + nodes

2 Labels: Survived / Lost



1 Feature: Number of + nodes

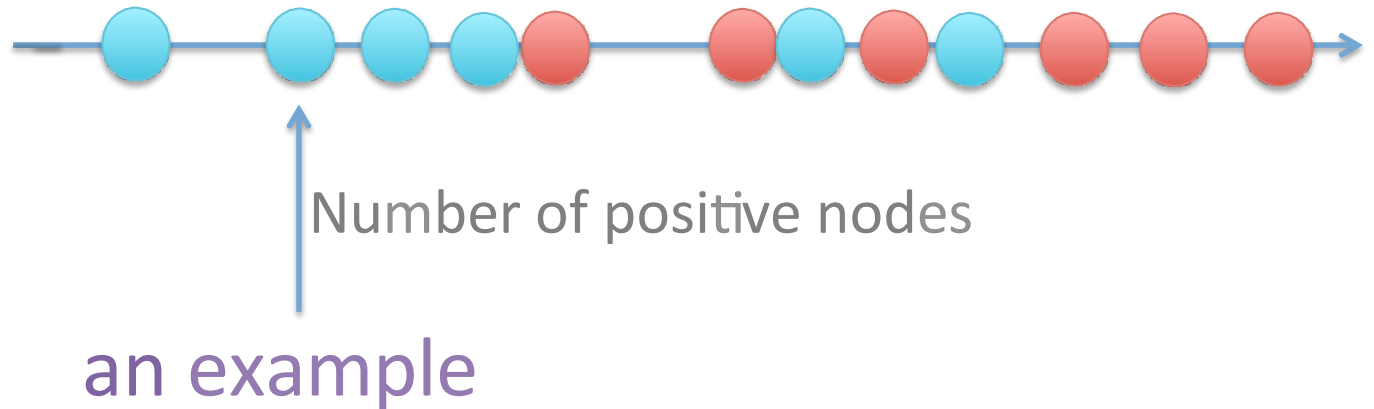
2 Labels: Survived / Lost



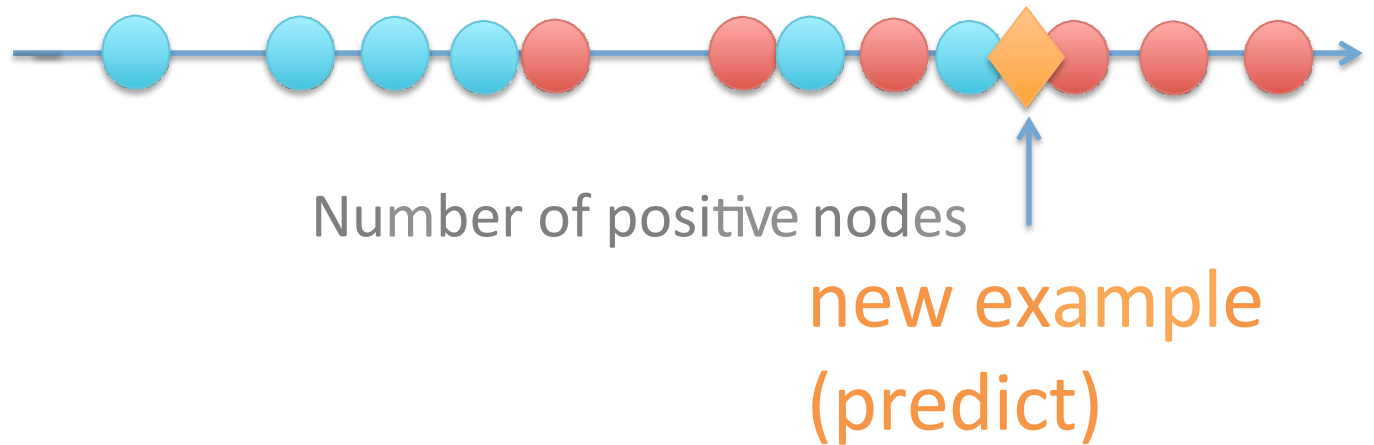
Number of positive nodes

1 Feature: Number of + nodes

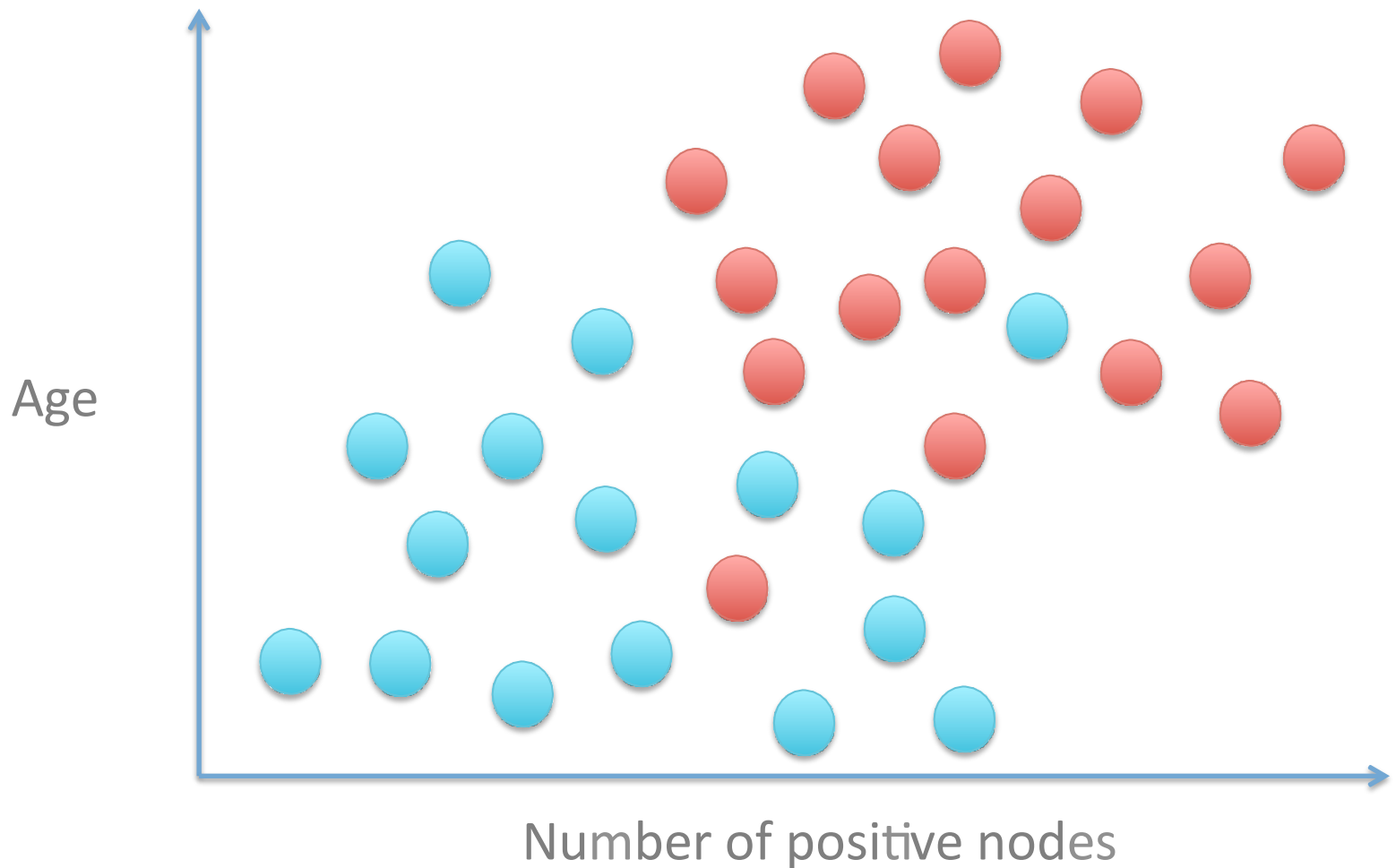
2 Labels: Survived / Lost



- 1 Feature: Number of + nodes
- 2 Labels: Survived / Lost

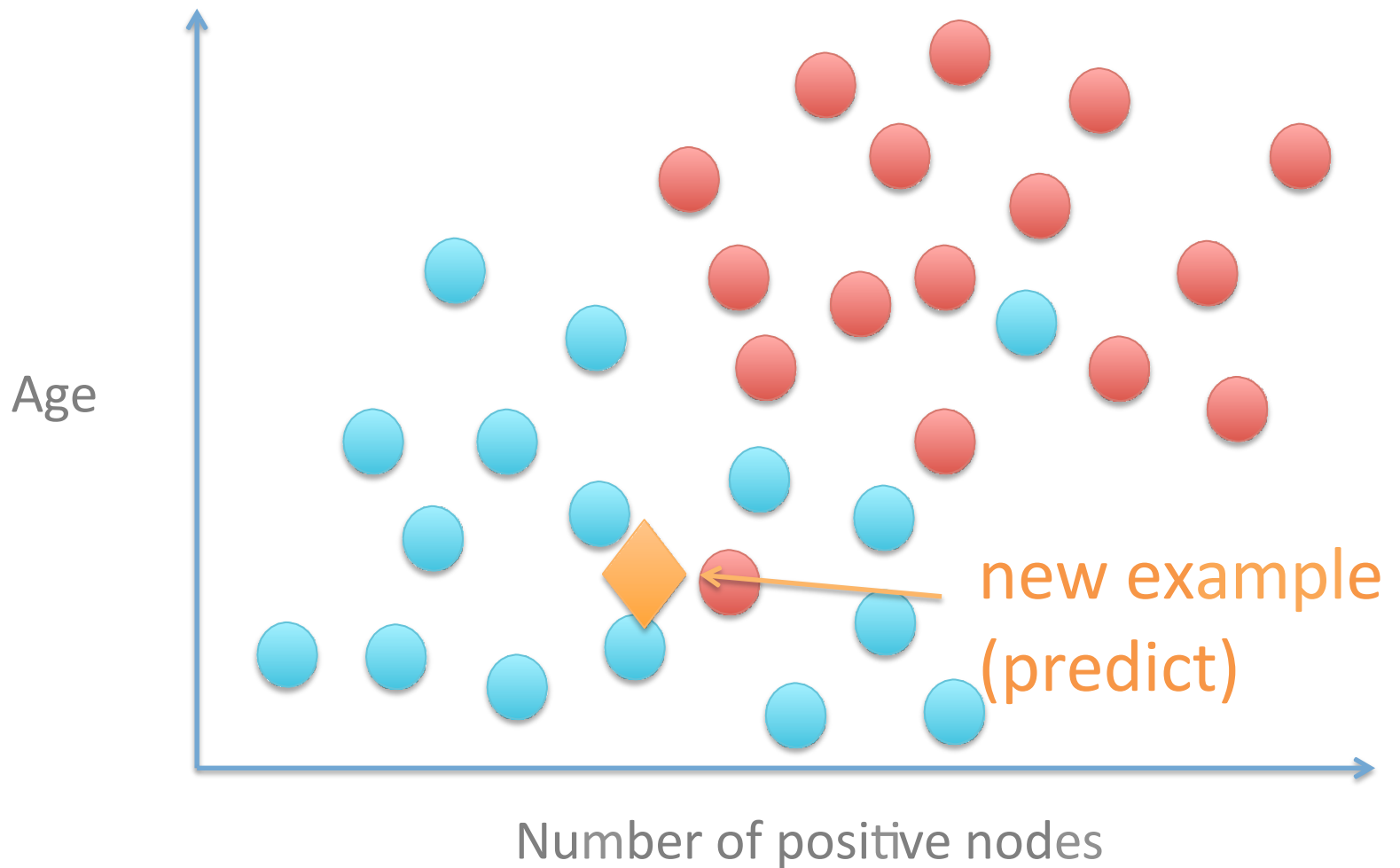


2 Labels: Survived / Lost

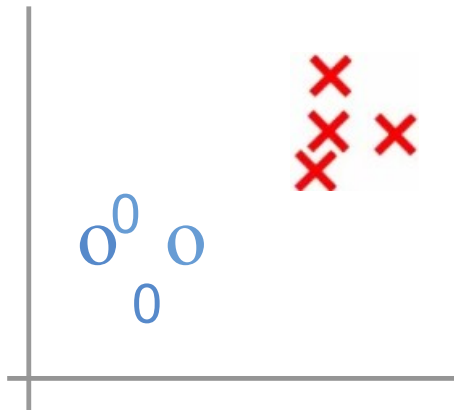


2 Features: Number of + nodes, Age

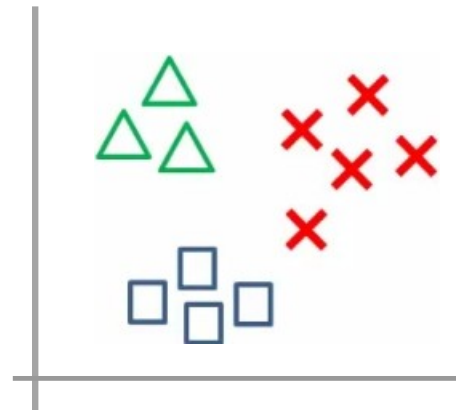
2 Labels: Survived / Lost



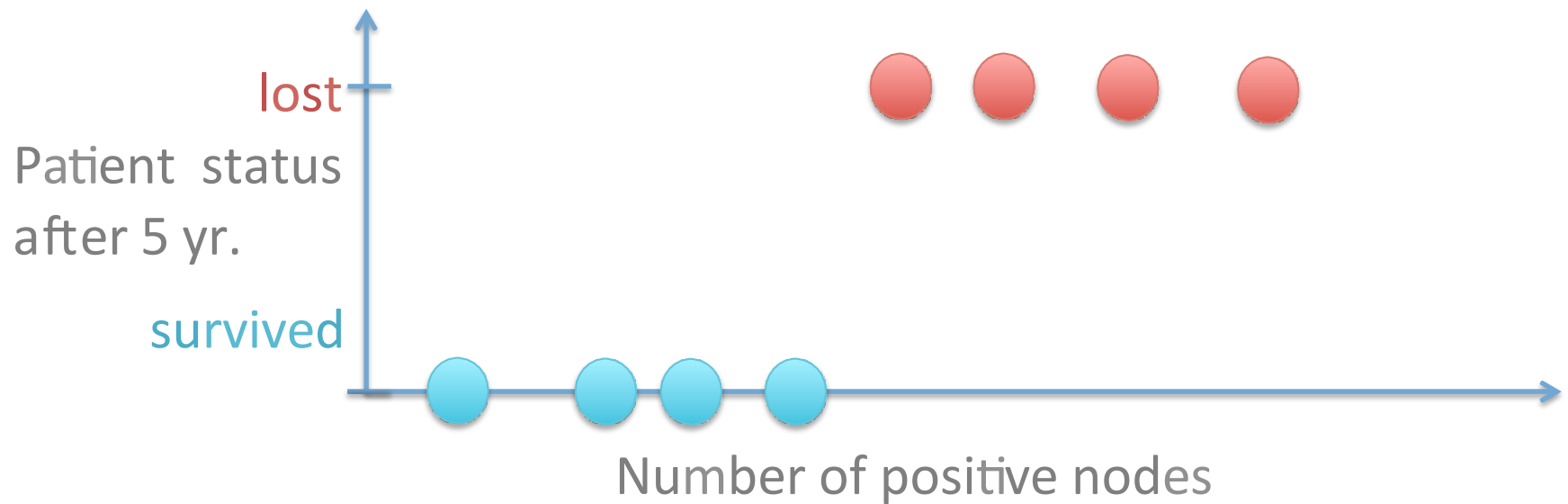
Binary classification:



Multi-class classification:



Linear regression for classification?

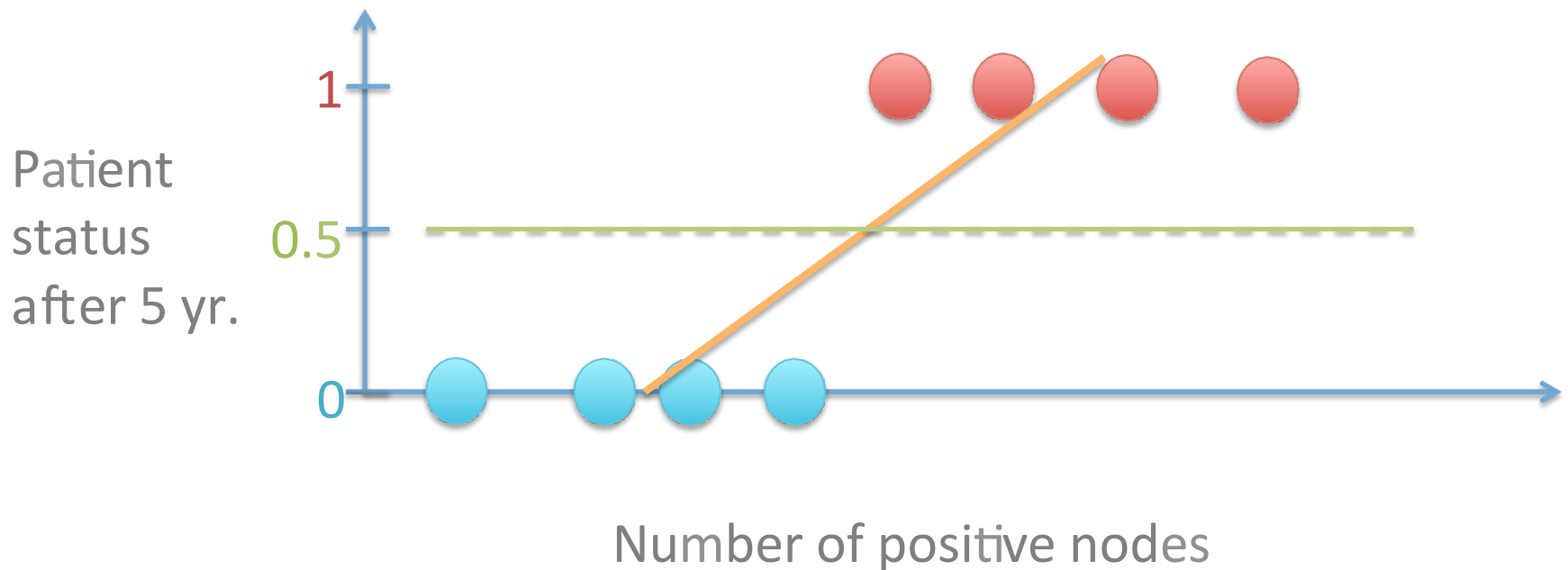


Linear regression for classification?



$$y_{\beta}(x) = \beta_0 + \beta_1 x + \varepsilon$$

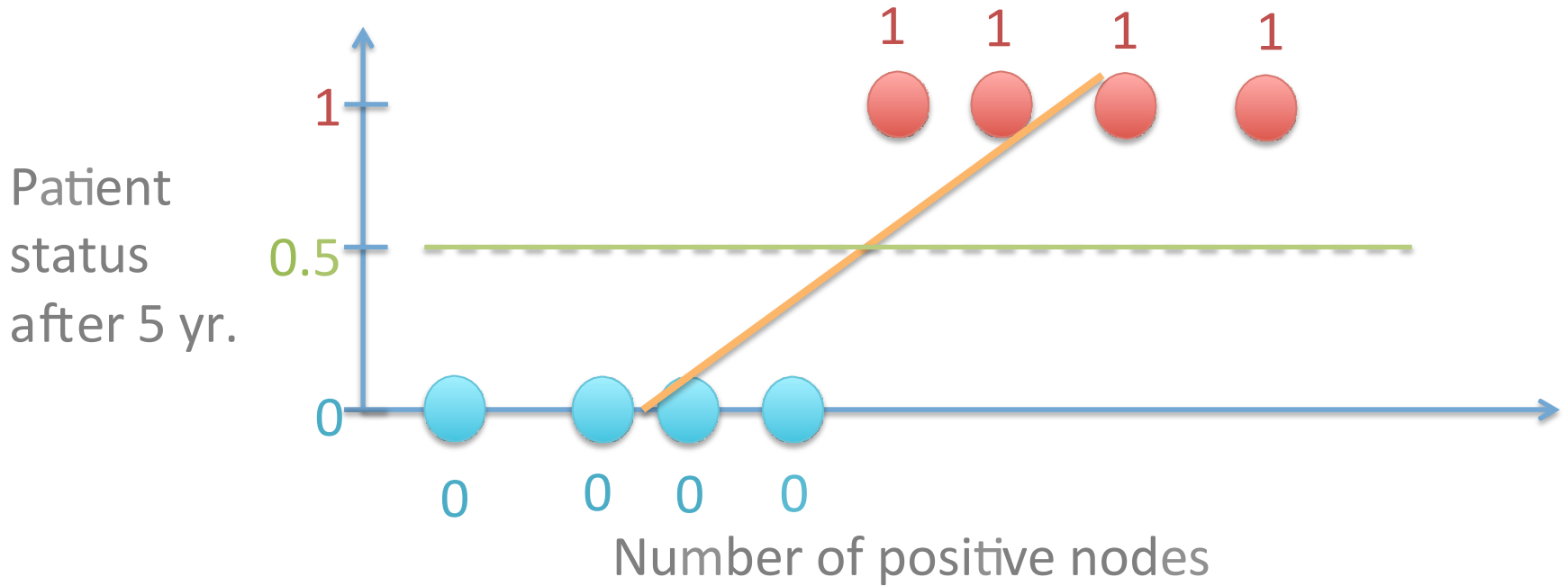
Linear regression for classification?



If $y_{\text{pred}} > 0.5$ predict label 1 (lost)

If $y_{\text{pred}} < 0.5$ predict label 0 (survived)

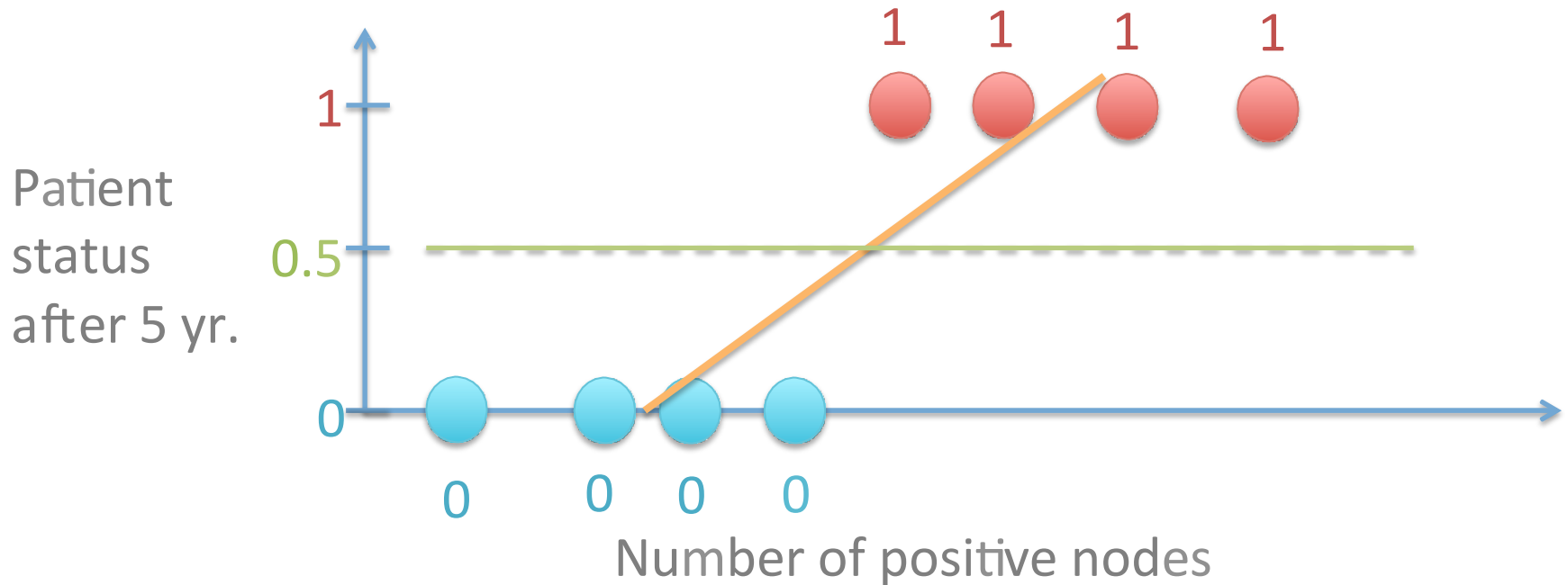
Linear regression for classification?



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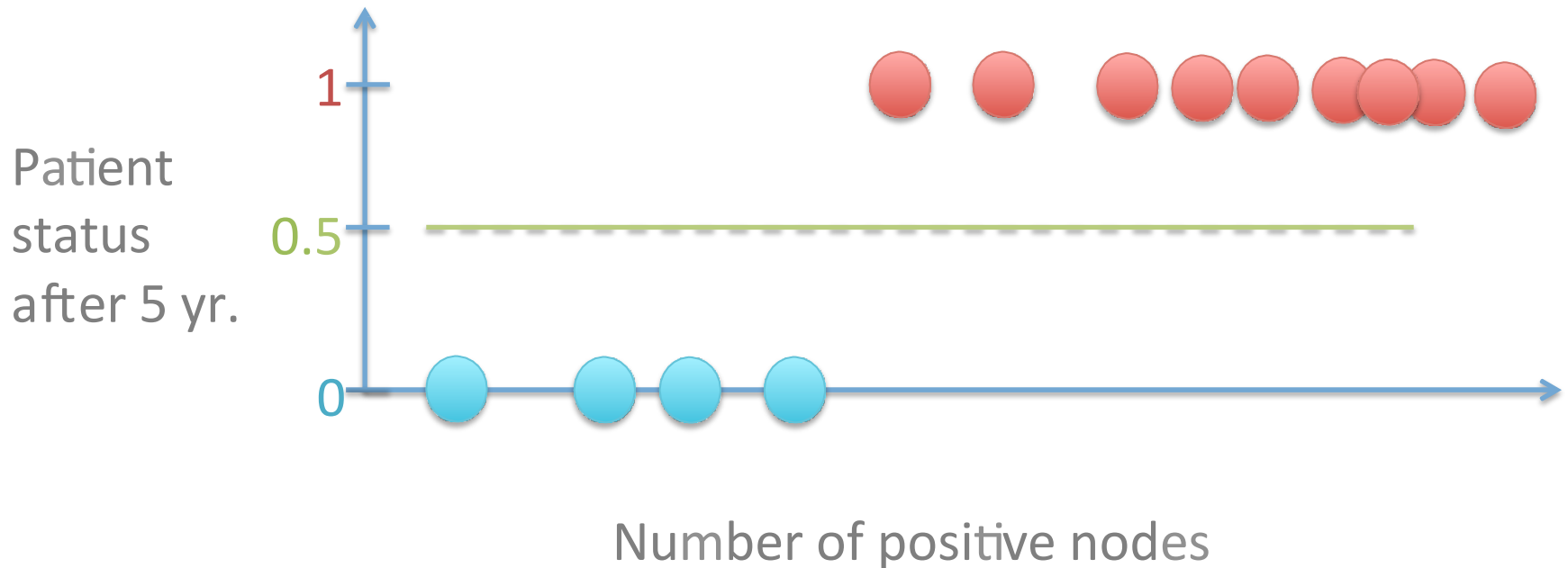
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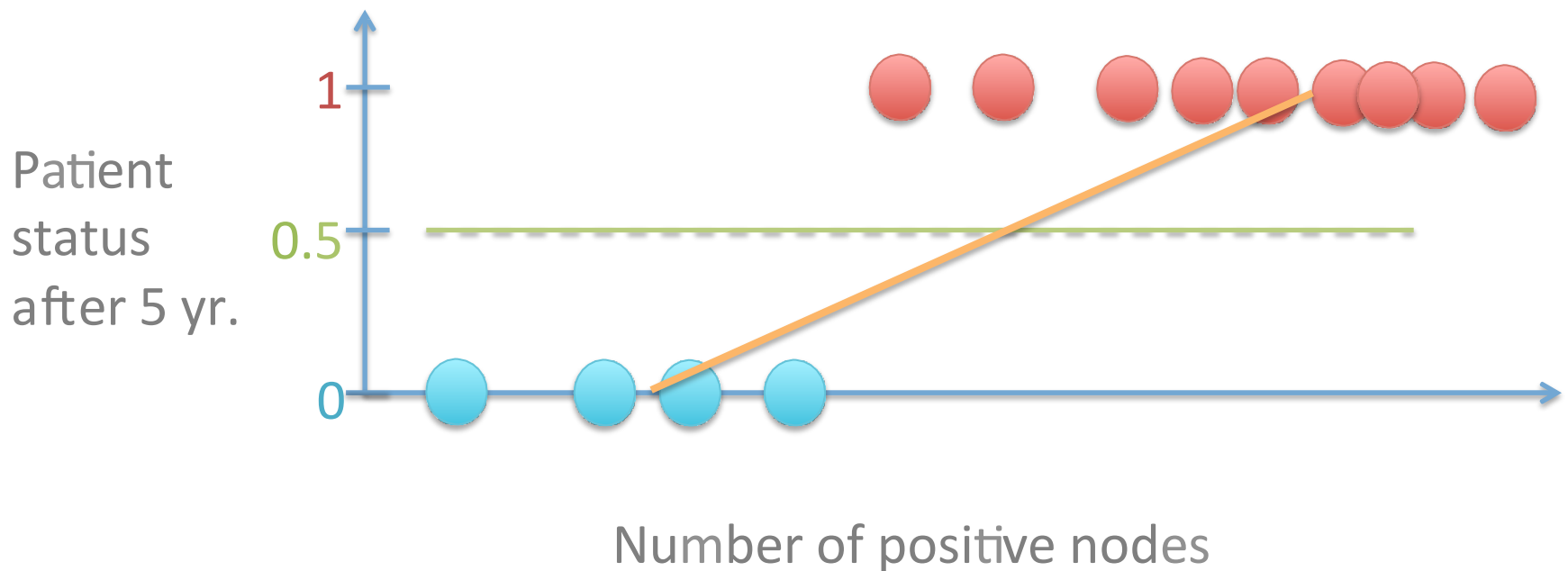
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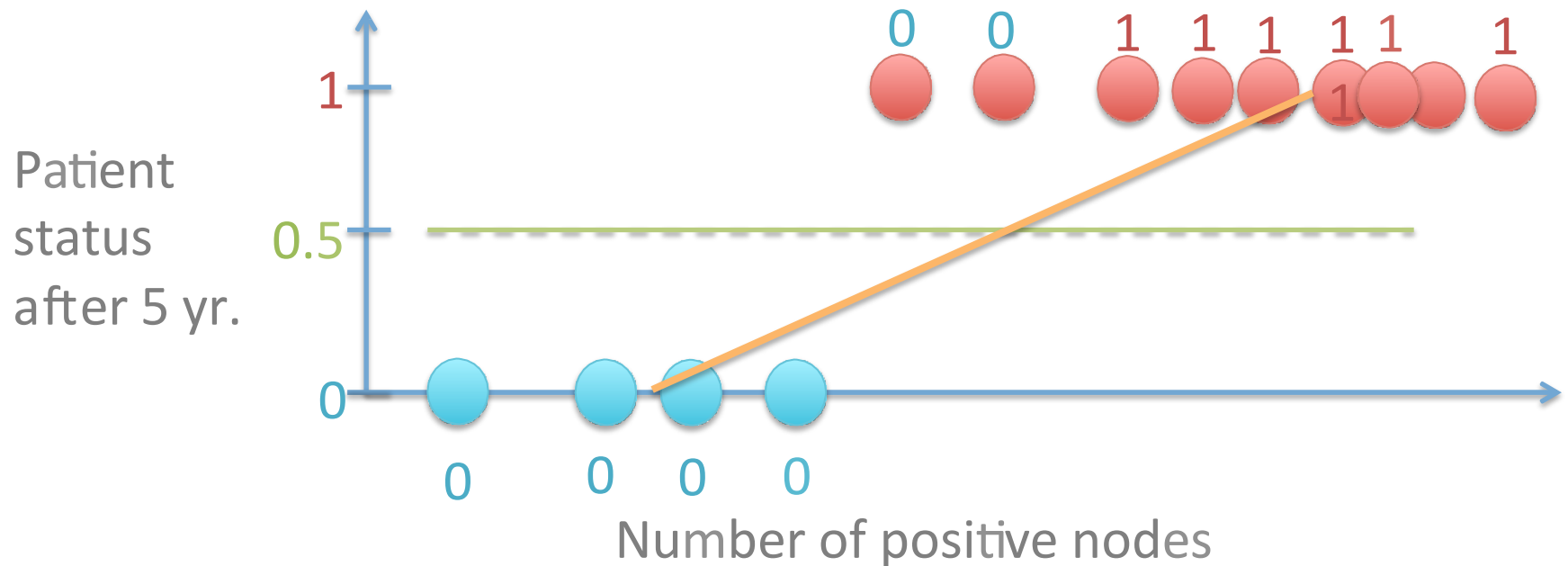
Linear regression for classification?



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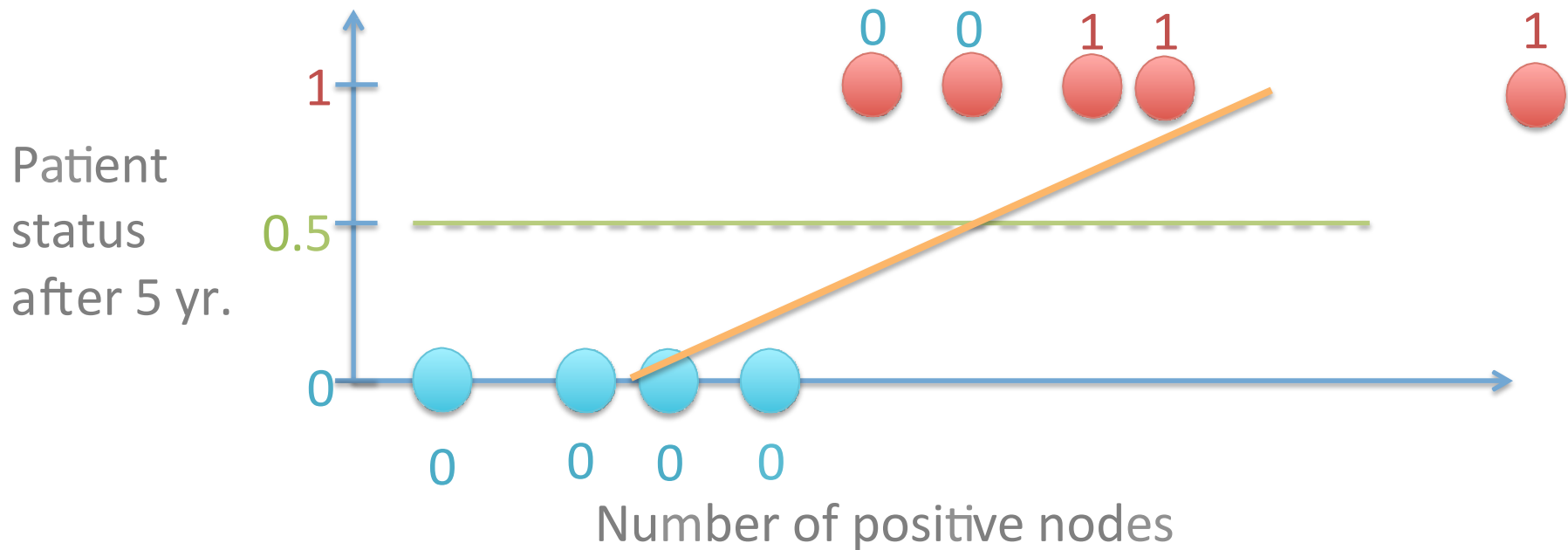
Linear regression for classification?



If $y_{\text{pred}} > 0.5$ predict label 1 (lost)

If $y_{\text{pred}} < 0.5$ predict label 0 (survived)

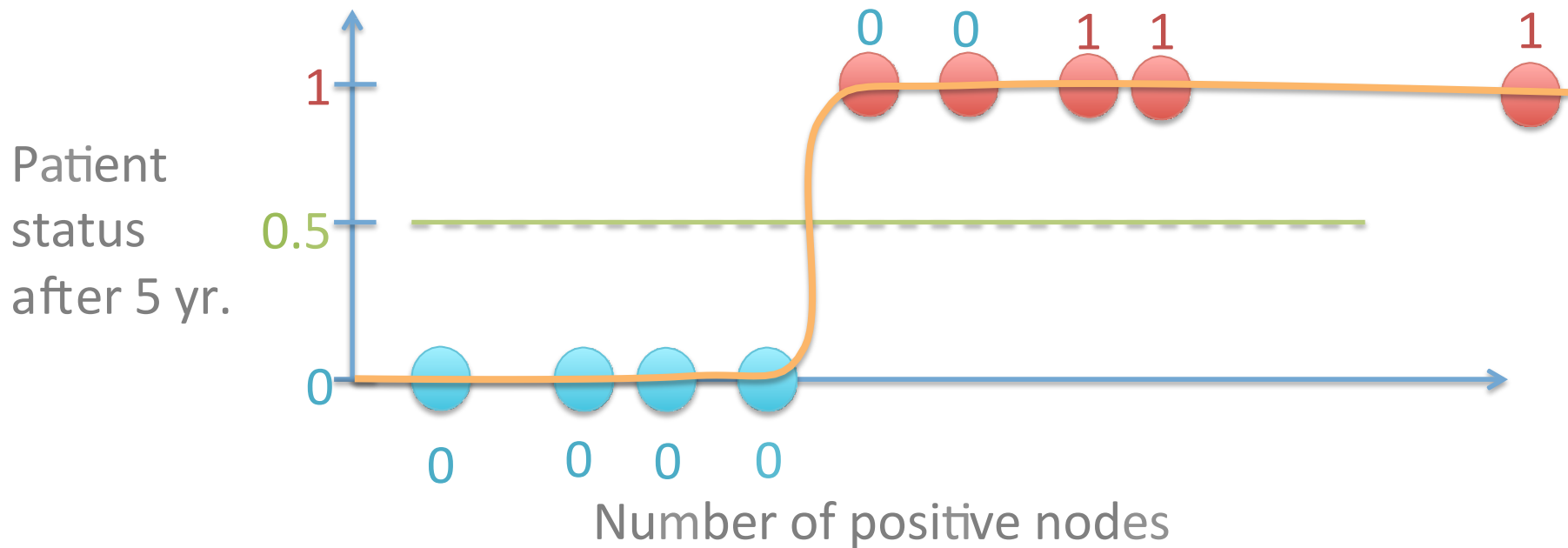
Linear regression for classification?



If $y_{\text{pred}} > 0.5$ predict label 1 (lost)

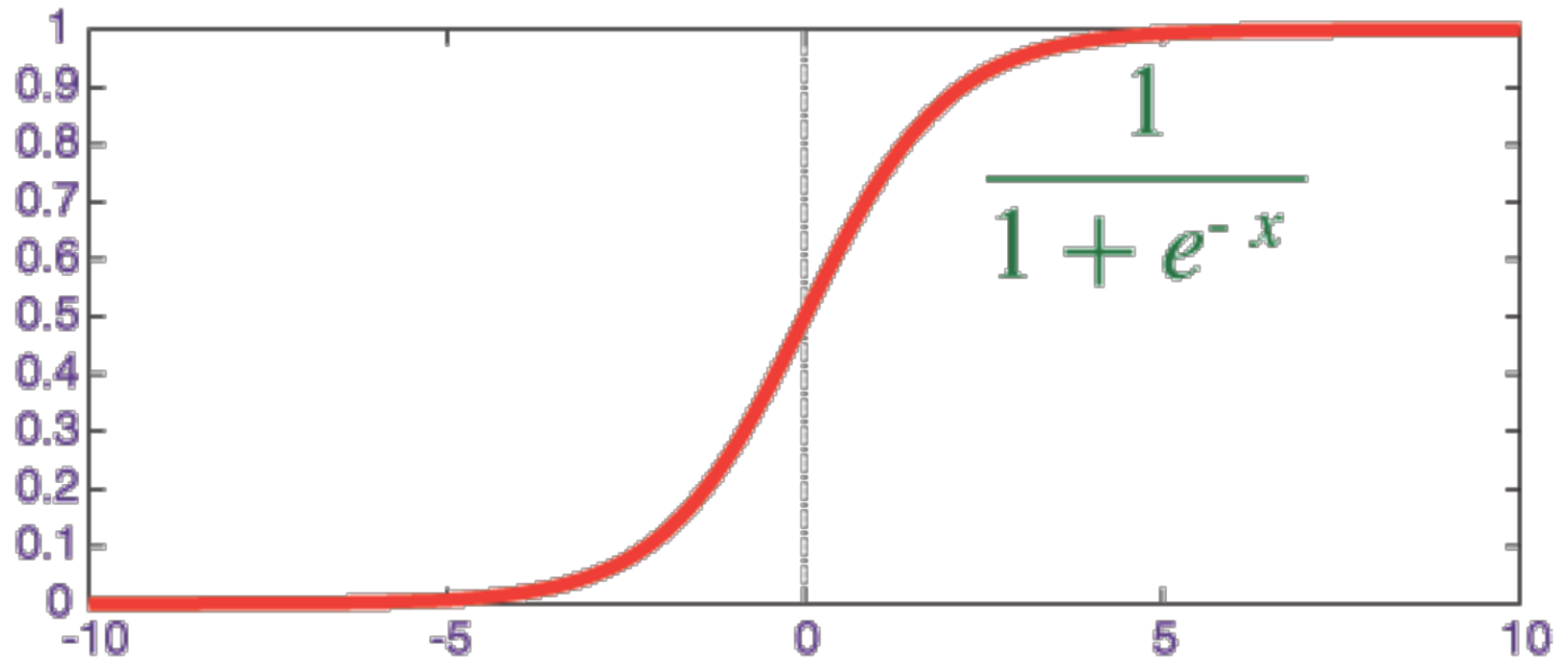
If $y_{\text{pred}} < 0.5$ predict label 0 (survived)

Logistic regression to the rescue

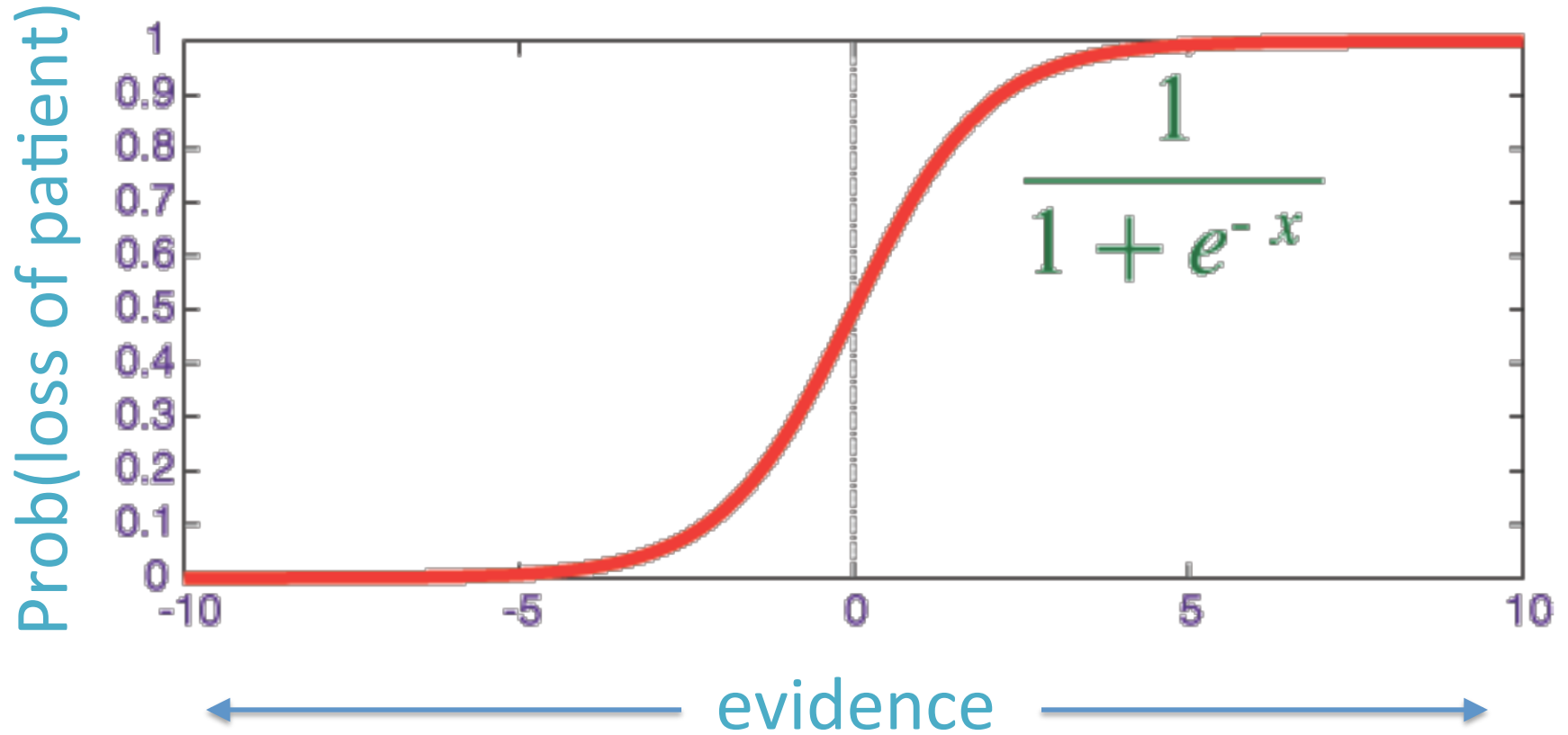


$$y_{\beta}(x) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x + \varepsilon)}}$$

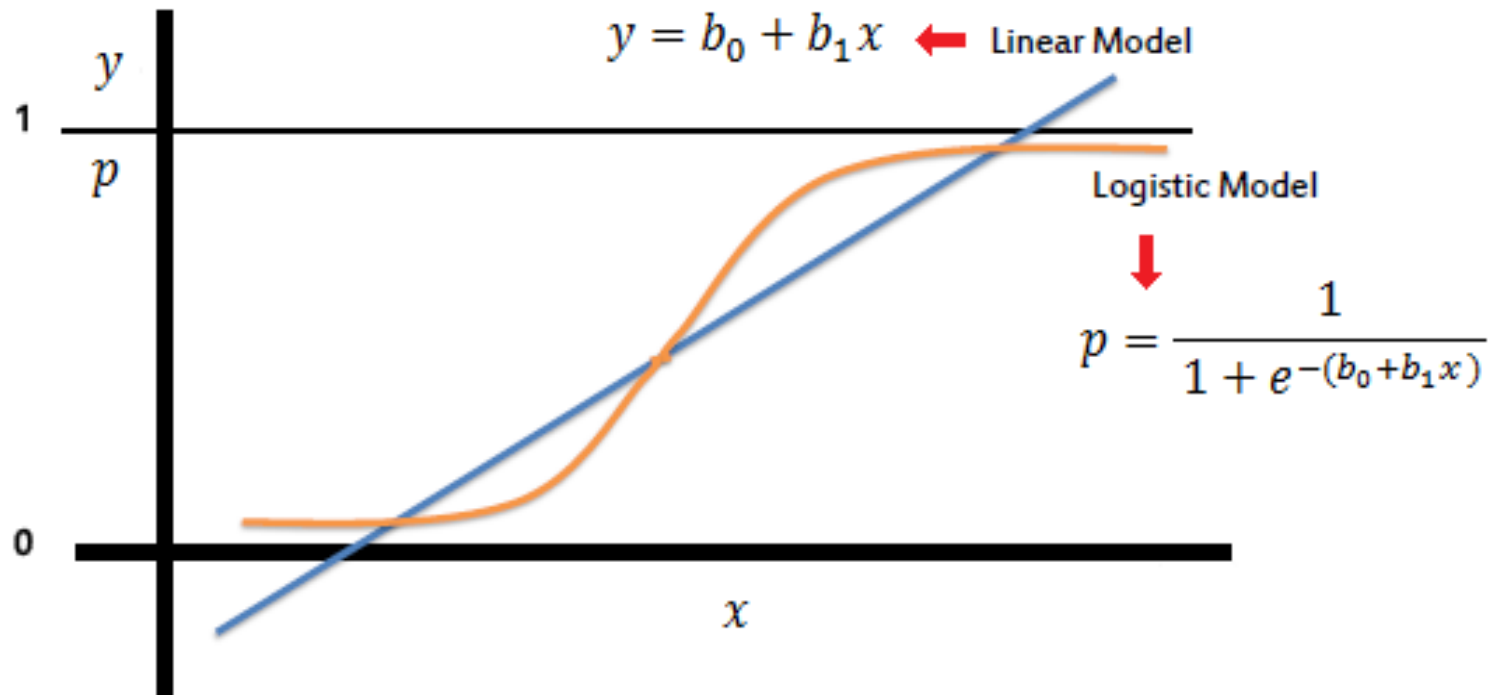
What is this function?



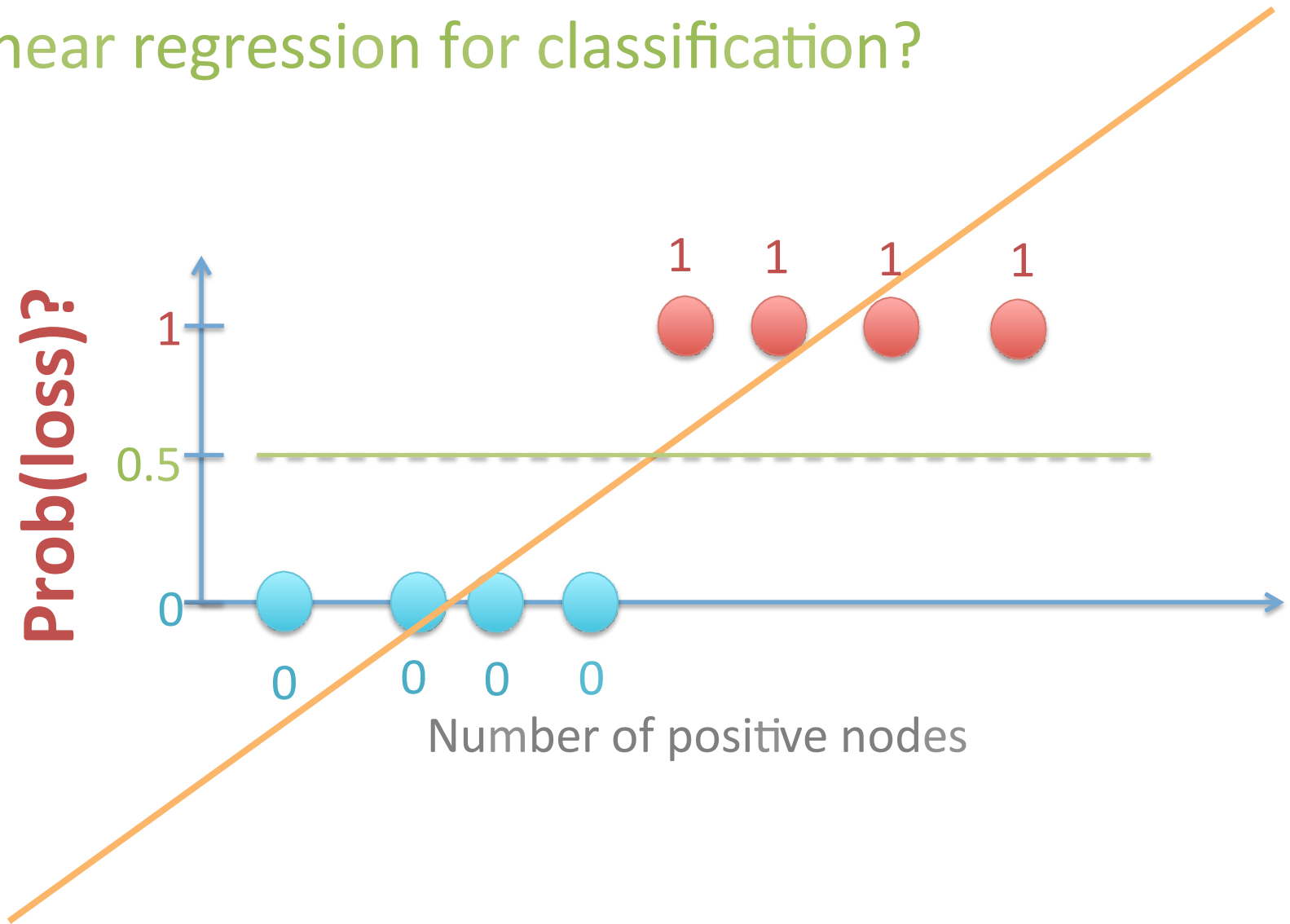
What is this function?



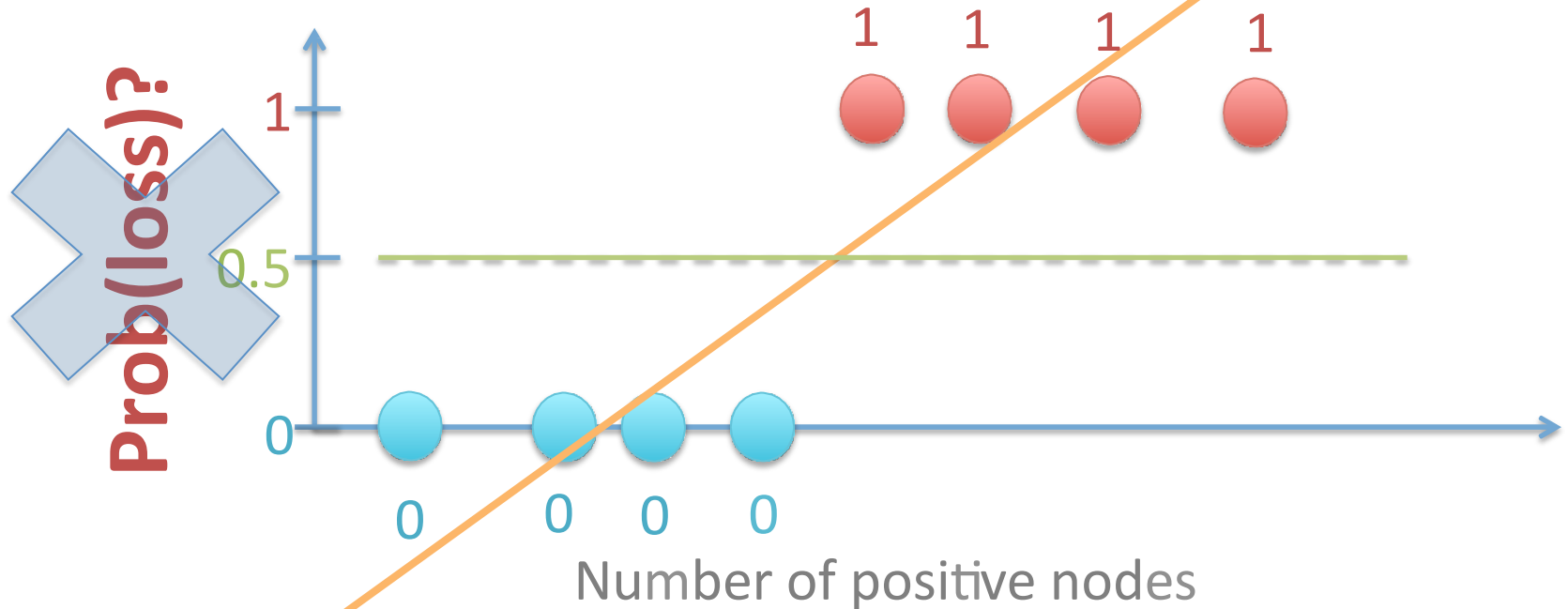
What is this function?



Linear regression for classification?



Linear regression for classification?



Y between $-\infty$ and ∞ ,
Not 0 and 1

What metric would express the chances of loss/survival, but not constrained to $[0, 1]$?

$$P(\textit{loss}) = 0.8$$

$$P(\textit{survival}) = 0.2$$

Probability

What metric would express the chances of loss/survival, but not constrained to $[0, 1]$?

$$P(loss) = 0.8$$

$$P(survival) = 0.2$$

$$\frac{P(loss)}{P(survival)} = 4$$

Probability

Odds

What metric would express the chances of loss/survival, but not constrained to $[0, 1]$?

$$\begin{array}{ll} P(\textit{loss}) = 0.05 & \frac{P(\textit{loss})}{P(\textit{survival})} = 0.053 \\ P(\textit{survival}) = 0.95 & \end{array}$$

Probability

Odds

What metric would express the chances of loss/survival, but not constrained to $[0, 1]$?

$$P(loss) = 0.5$$

$$P(survival) = 0.5$$

Probability

$$\frac{P(loss)}{P(survival)} = 1$$

Odds

What metric would express the chances of loss/survival, but not constrained to $[0, 1]$?

$$P(\textit{loss}) = 0.5$$

$$P(\textit{survival}) = 0.5$$

$$\frac{P(\textit{loss})}{P(\textit{survival})} = 1$$

Probability

Odds

between 0 and inf

What metric would express the chances of loss/survival, but not constrained to $[0, 1]$?

$$P(loss) = 0.5$$

$$P(survival) = 0.5$$

$$\log\left(\frac{P(loss)}{P(survival)}\right) = 0$$

Probability

Log Odds

between $-\infty$ and ∞

What metric would express the chances of loss/survival, but not constrained to $[0, 1]$?

$$\begin{aligned} P(\textit{loss}) &= 0.05 \\ P(\textit{survival}) &= 0.95 \end{aligned} \quad \log \left(\frac{P(\textit{loss})}{P(\textit{survival})} \right) = -2.94$$

Probability

Log Odds

between $-\infty$ and ∞

What metric would express the chances of loss/survival, but not constrained to $[0, 1]$?

$$P(\textit{loss}) = 0.8$$

$$P(\textit{survival}) = 0.2$$

$$\log\left(\frac{P(\textit{loss})}{P(\textit{survival})}\right) = 1.39$$

Probability

Log Odds

between $-\infty$ and ∞

What metric would express the chances of loss/survival, but not constrained to $[0, 1]$?

$$\begin{array}{l} P(\textit{loss}) = 0.999 \\ P(\textit{survival}) = 0.001 \end{array} \quad \log \left(\frac{P(\textit{loss})}{P(\textit{survival})} \right) = 6.9$$

Probability

Log Odds

between $-\infty$ and ∞

What metric would express the chances of loss/survival, but not constrained to $[0, 1]$?

$$P(loss) = 0.999$$

$$1 - P(loss) = 0.001$$

$$\log\left(\frac{P(loss)}{1 - P(loss)}\right) = 6.9$$

Probability

Log Odds

logit function

What metric would express the chances of loss/survival, but not constrained to $[0, 1]$?

$$P(loss) = 0.999$$

$$1 - P(loss) = 0.001$$

$$\log\left(\frac{P(loss)}{1 - P(loss)}\right) = 6.9$$

Probability

Log Odds

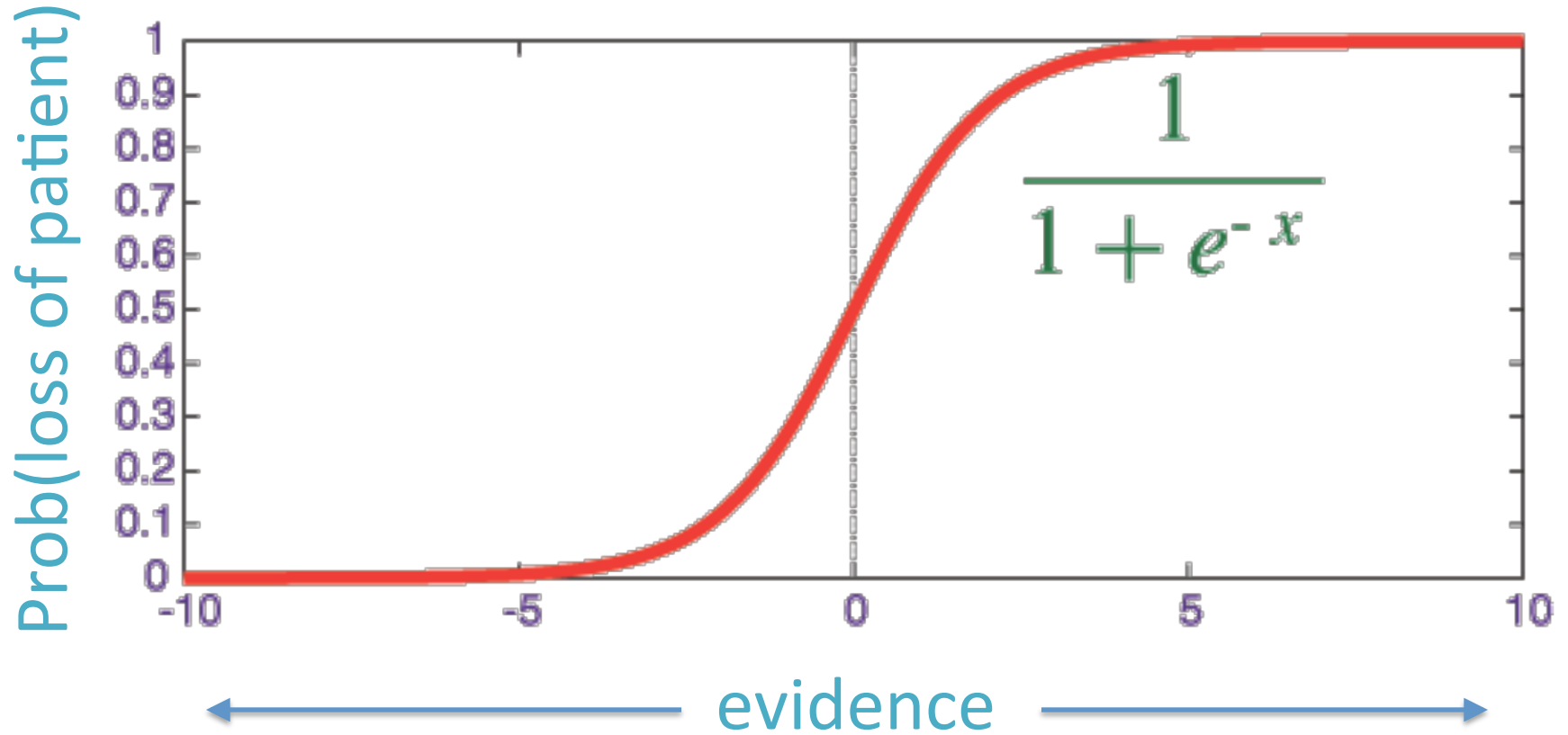
logit function

$$\frac{1}{1 - e^{\log\left(\frac{P(loss)}{1 - P(loss)}\right)}} = P(loss)$$

Logistic Function

Log Odds \rightarrow Prob

What is this function?



“Logistic regression” is a classification algorithm

$$y_{\beta}(x) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x + \varepsilon)}}$$

```
from sklearn.linear_model import LogisticRegression  
#(just like LinearRegression)
```

```
from statsmodels.formula.api import Logit  
#(just like OLS)
```

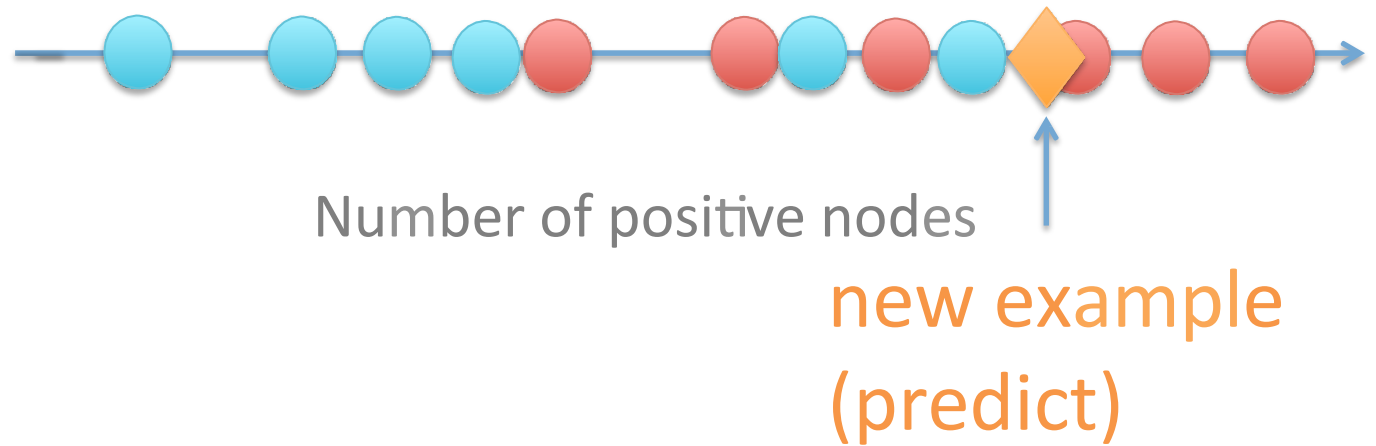
K Nearest Neighbors

K Nearest Neighbors



Number of positive nodes

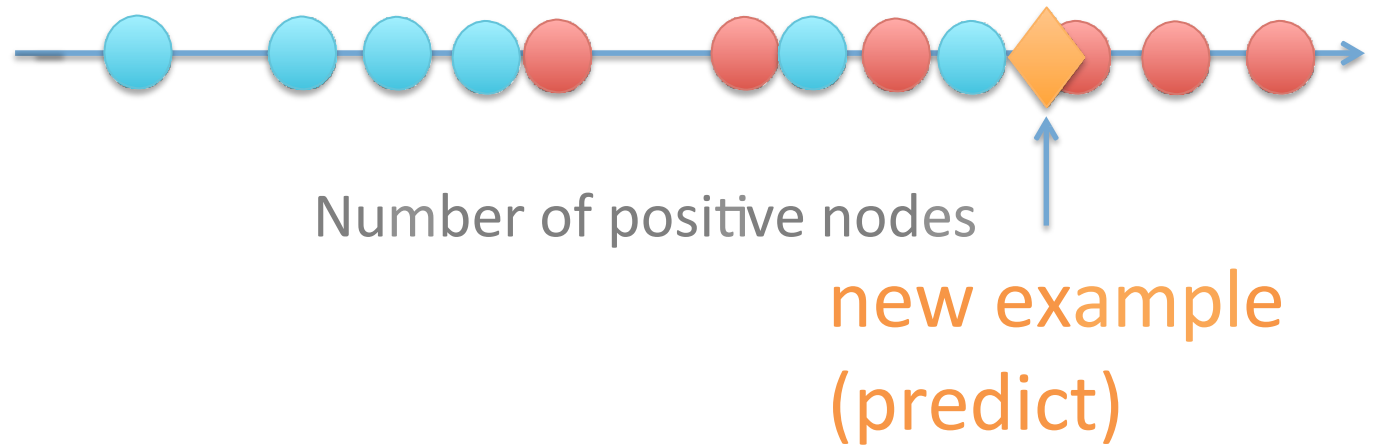
K Nearest Neighbors



K Nearest Neighbors

K=1:

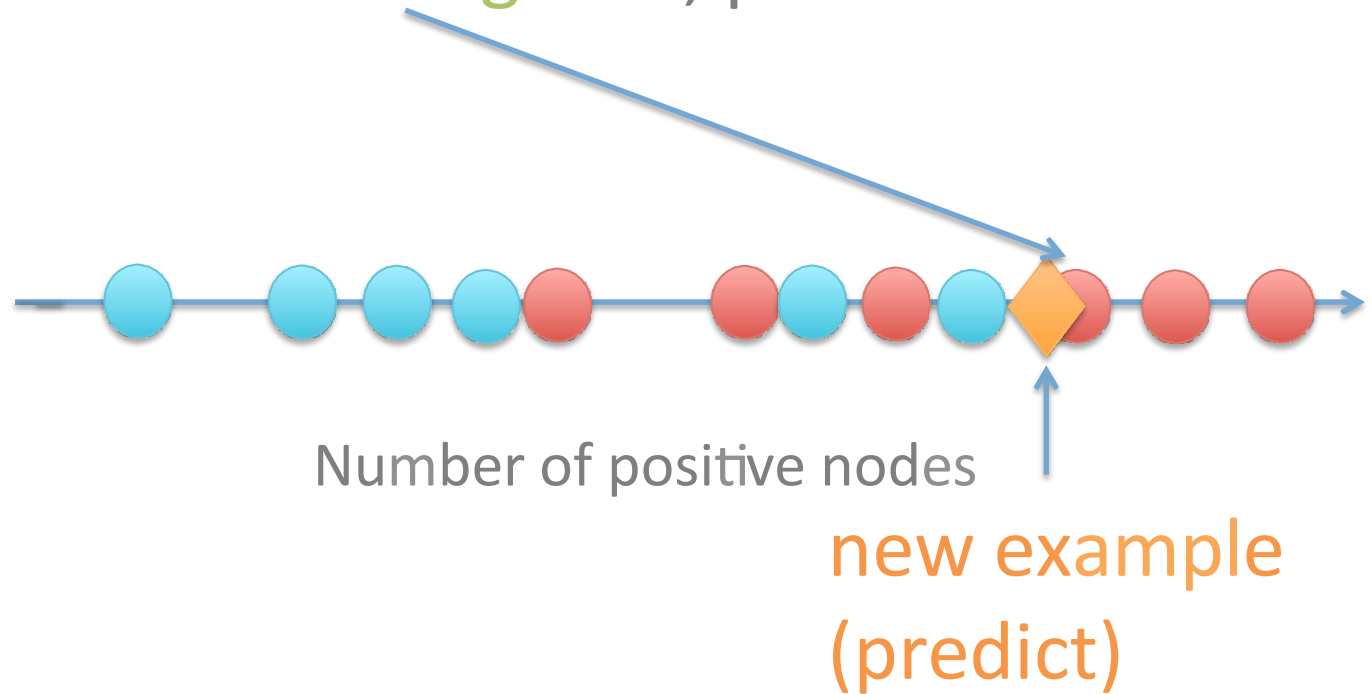
Look at the nearest neighbor, predict their label



K Nearest Neighbors

K=1:

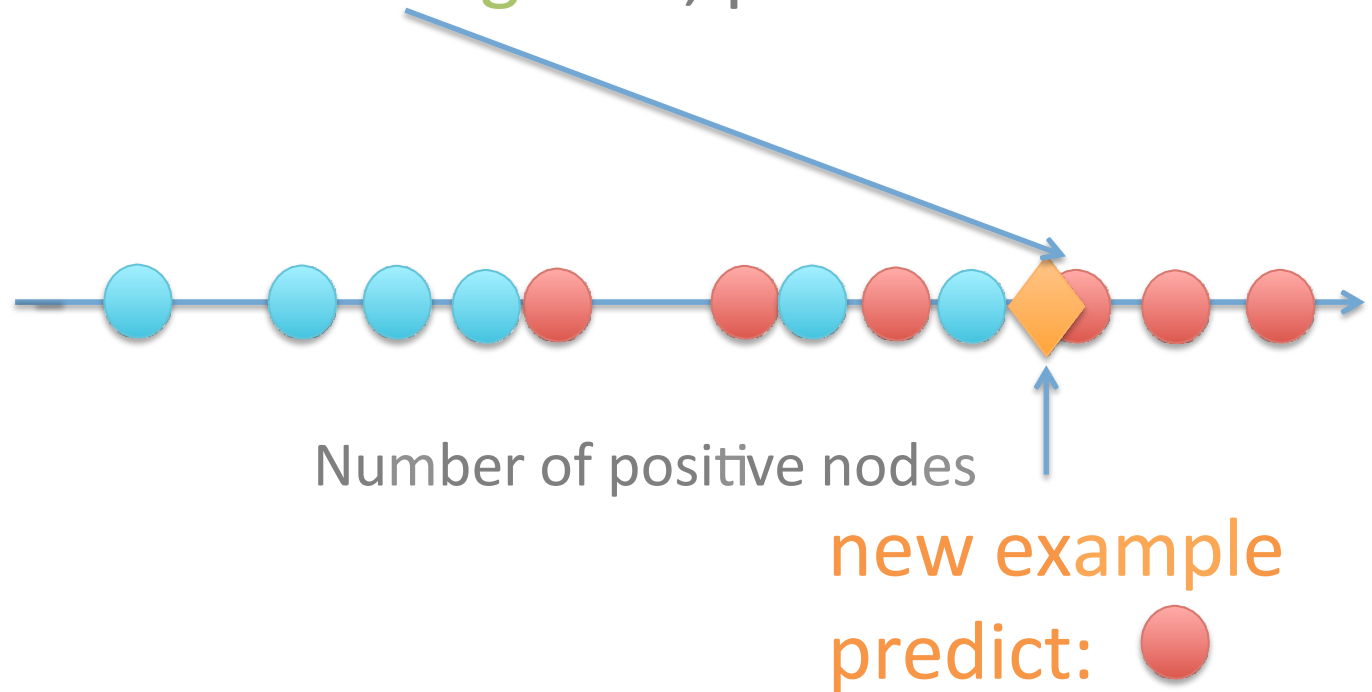
Look at the nearest neighbor, predict their label



K Nearest Neighbors

K=1:

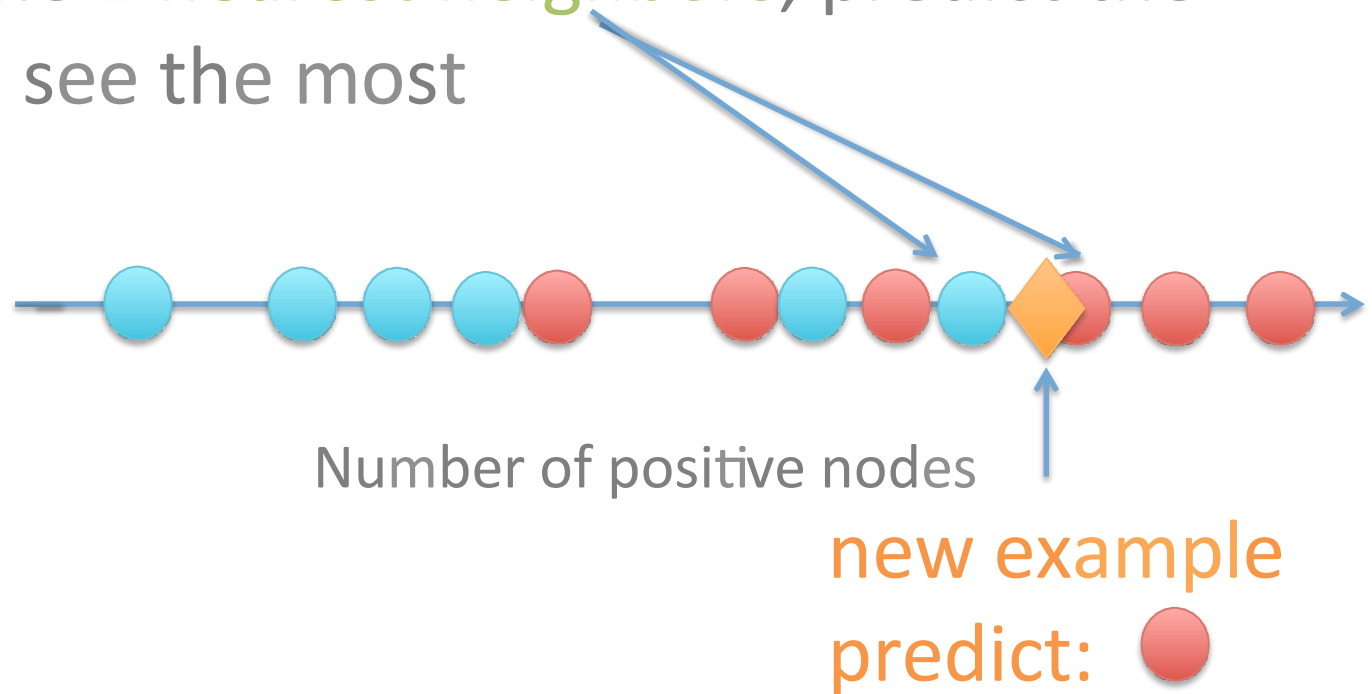
Look at the nearest neighbor, predict their label



K Nearest Neighbors

K=2:

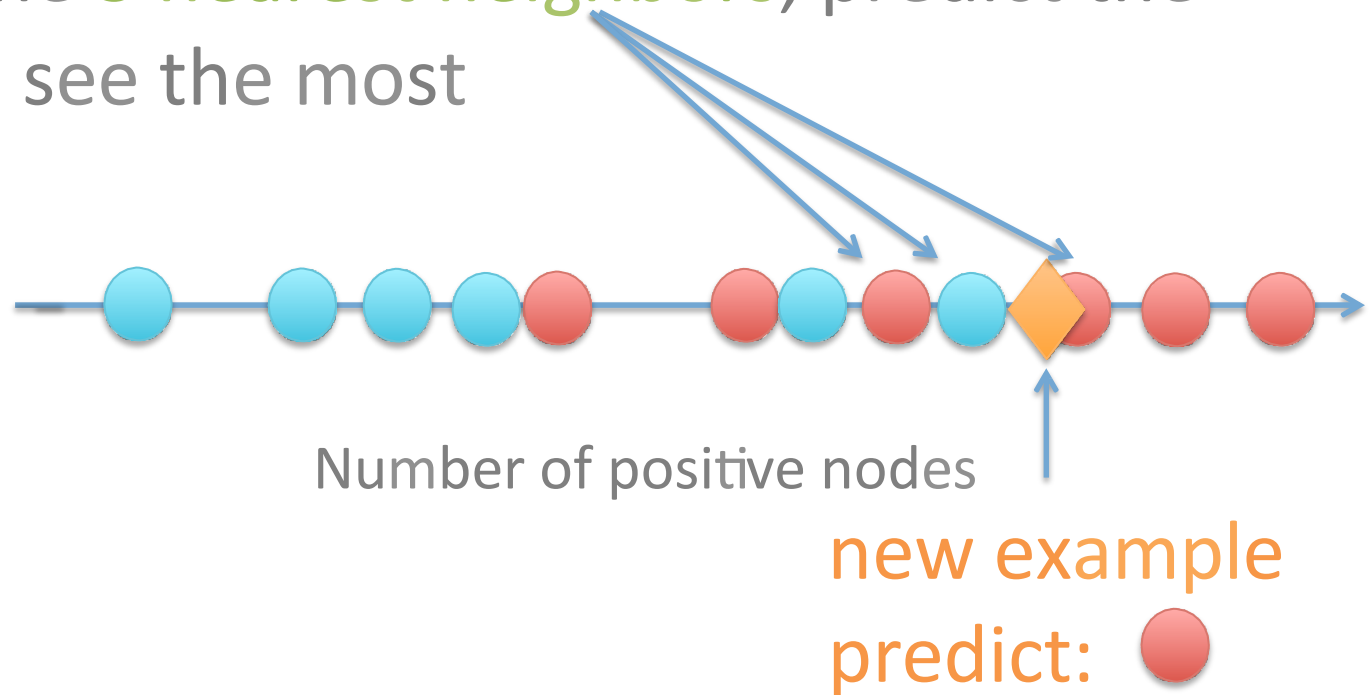
Look at the **2 nearest neighbors**, predict the label you see the most



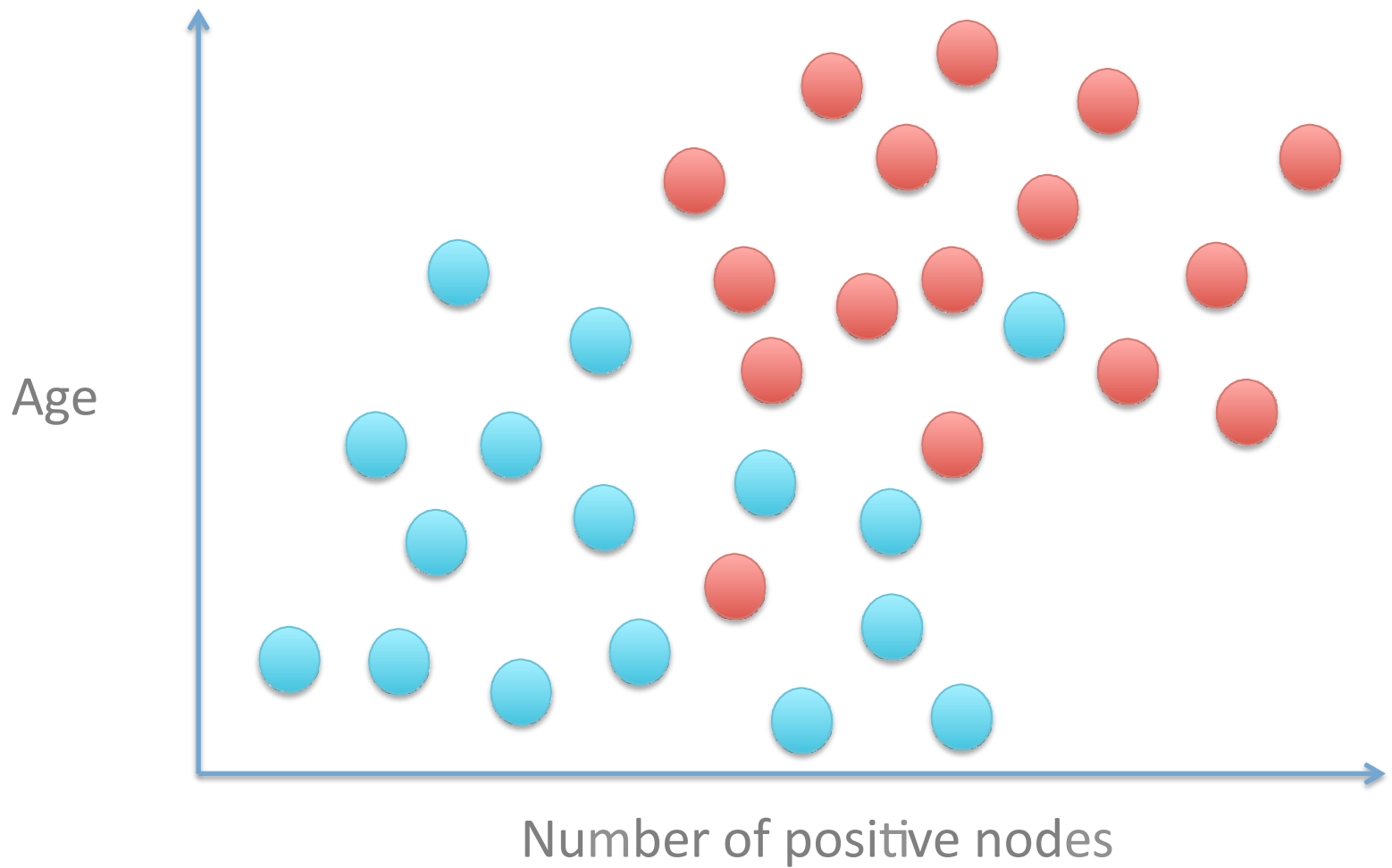
K Nearest Neighbors

K=3:

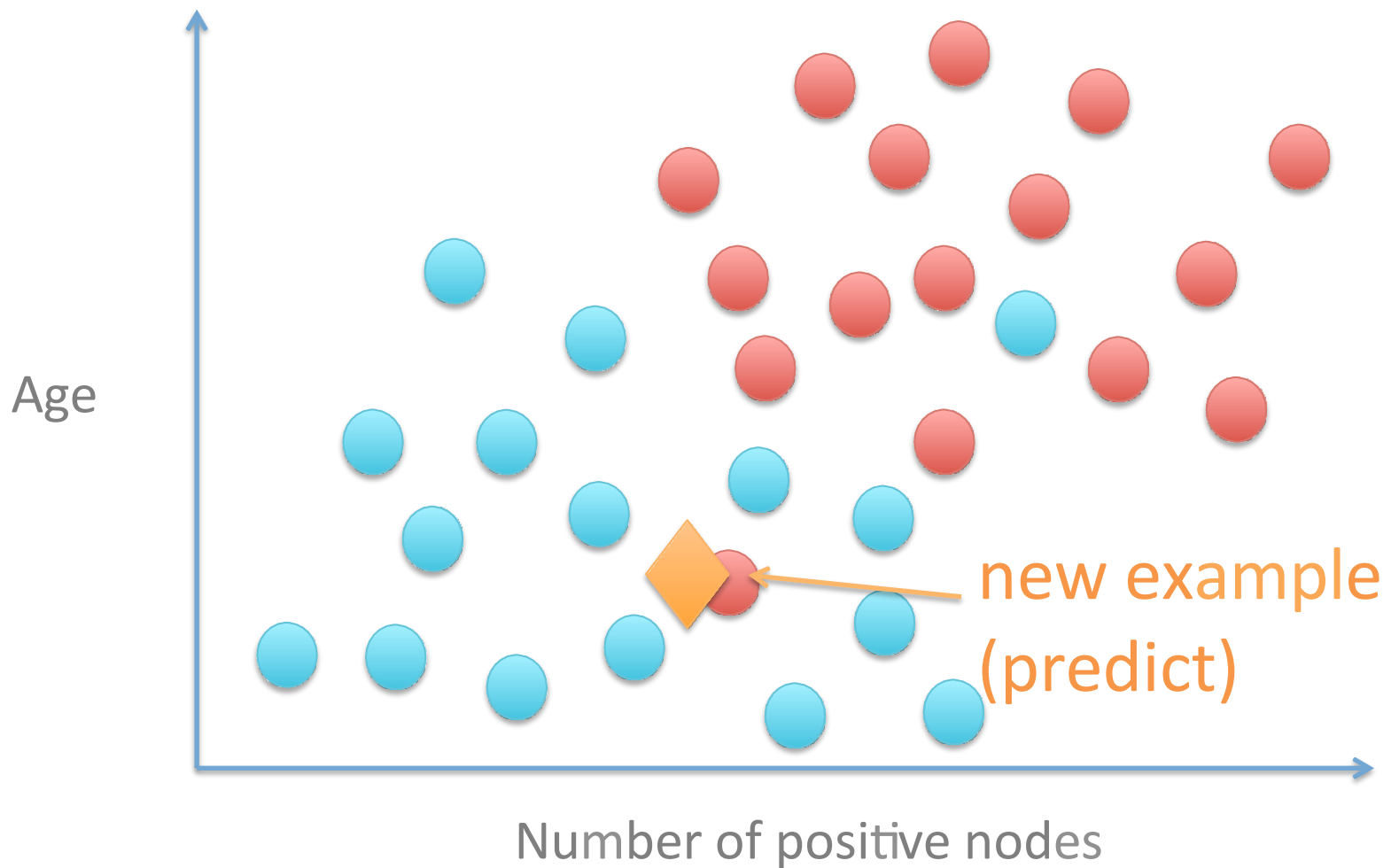
Look at the 3 nearest neighbors, predict the label you see the most



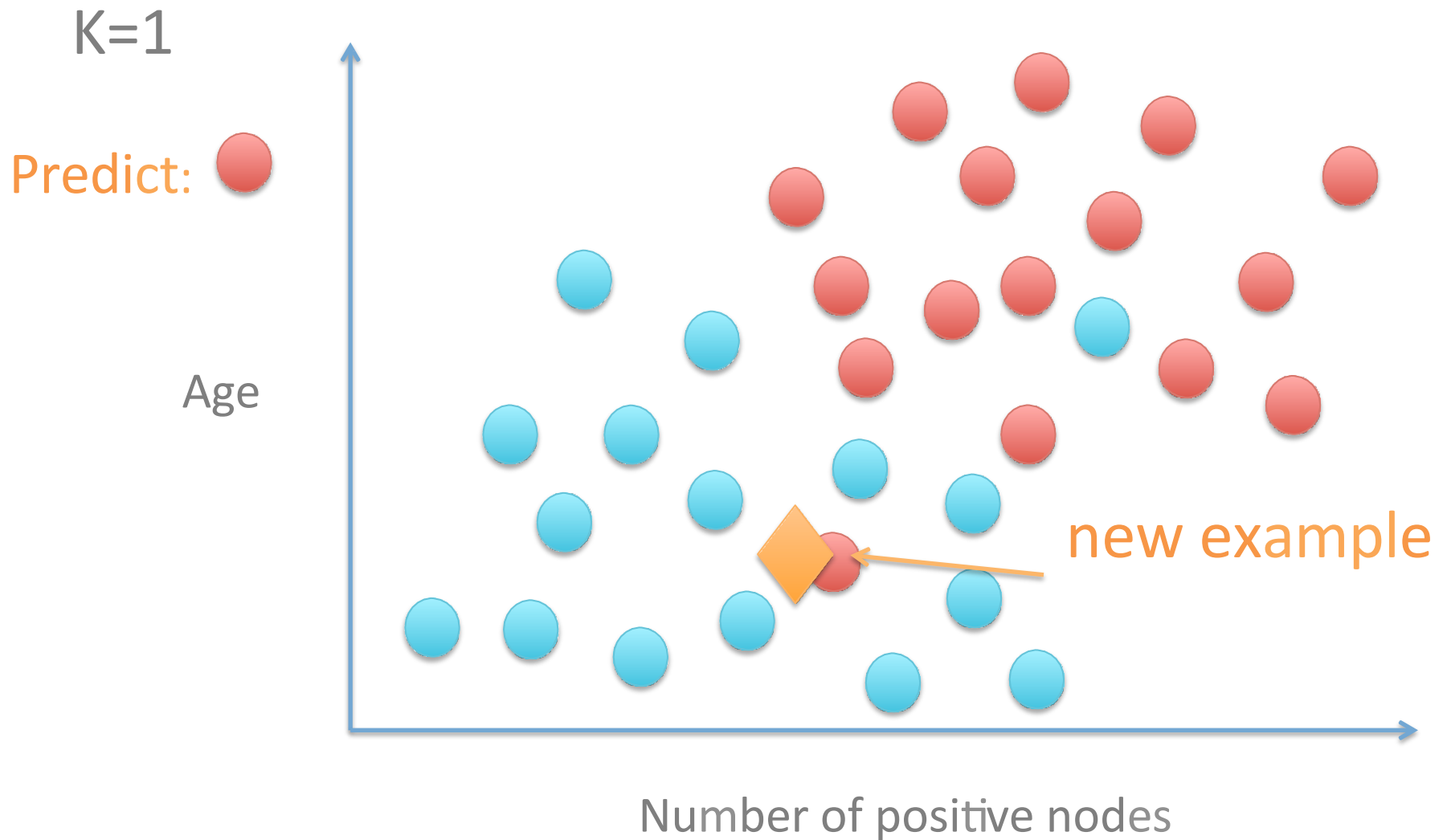
K Nearest Neighbors



K Nearest Neighbors



K Nearest Neighbors



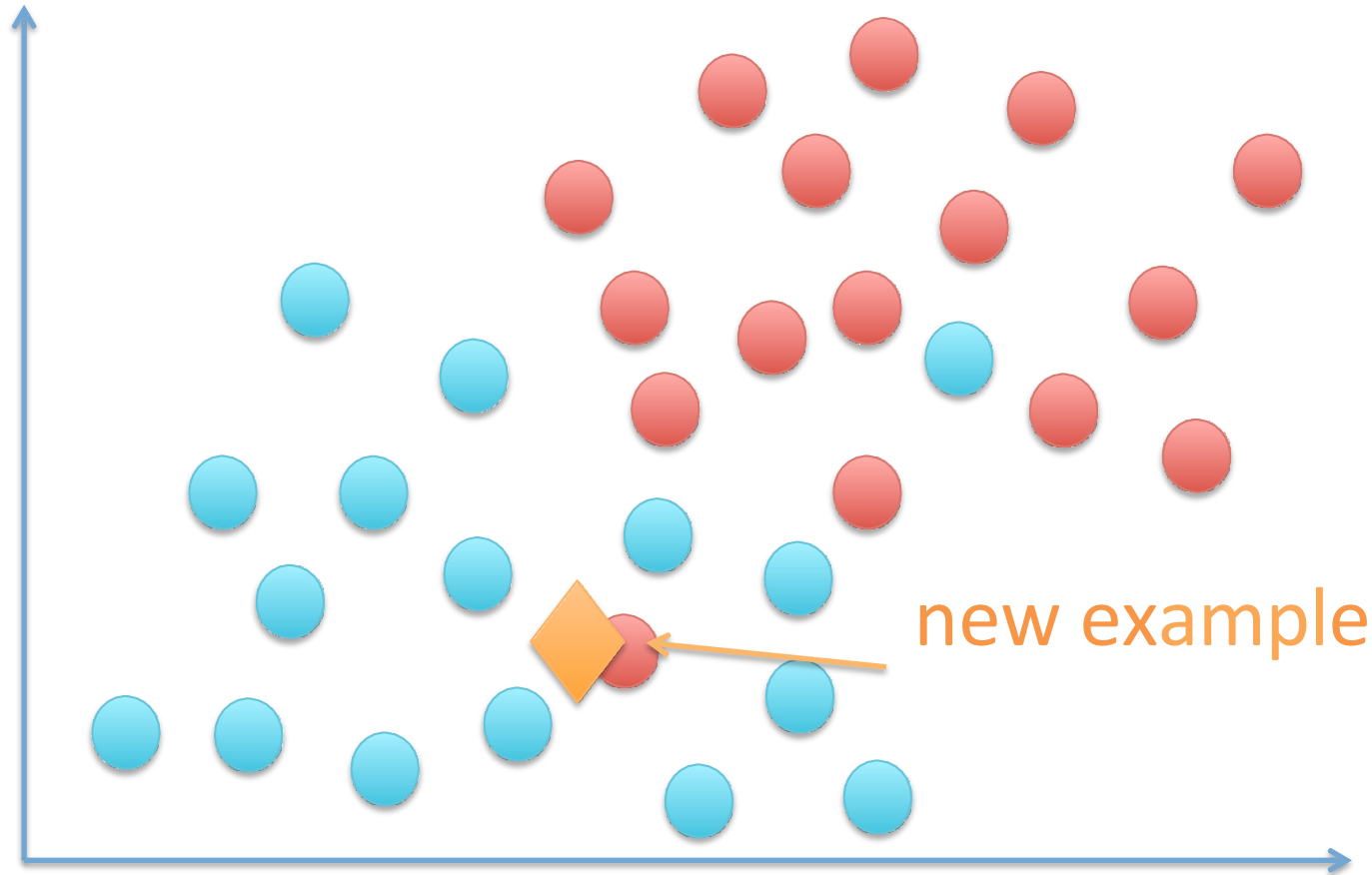
K Nearest Neighbors

K=2

Predict:



Age



new example

Number of positive nodes

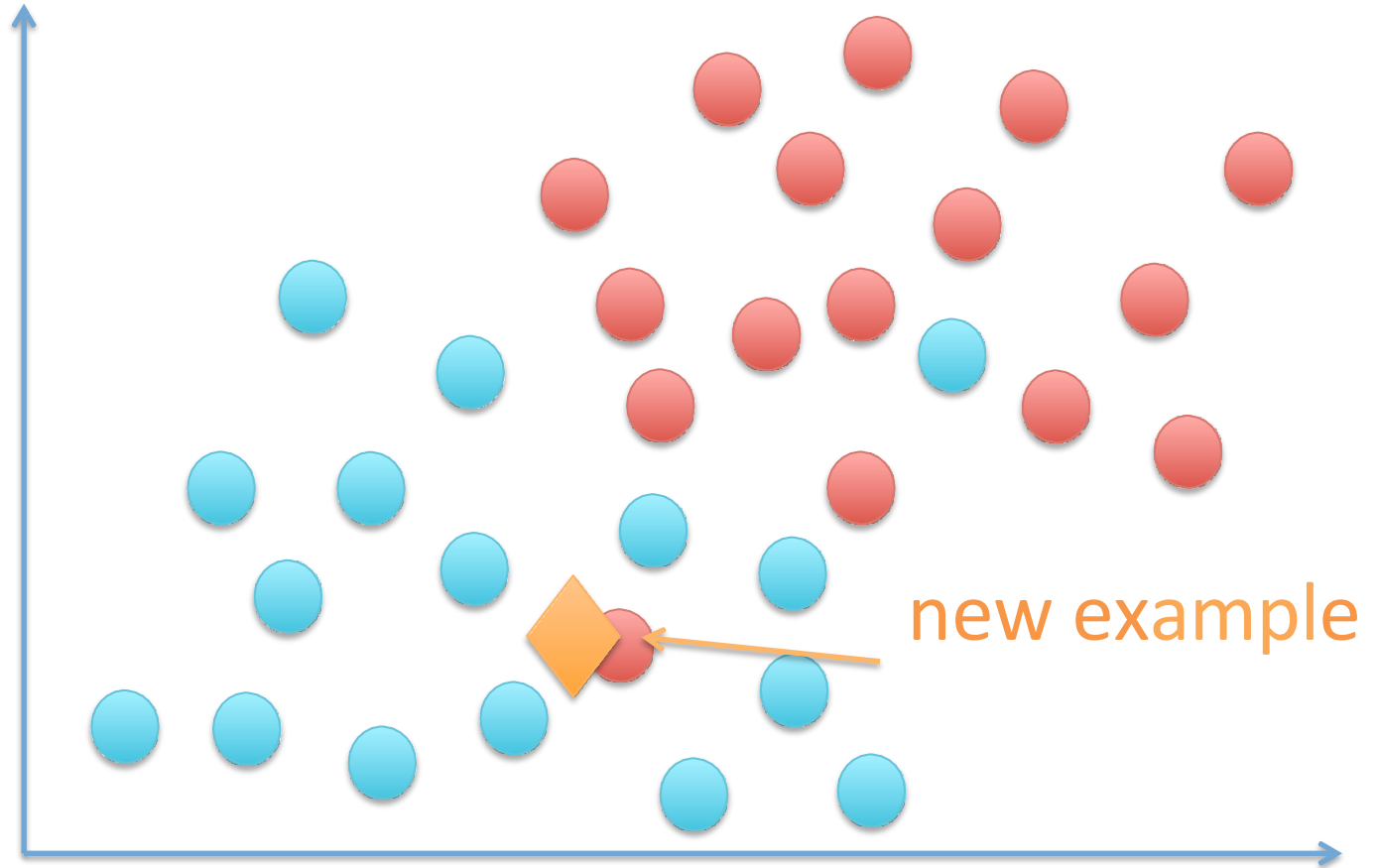
K Nearest Neighbors

K=3

Predict:

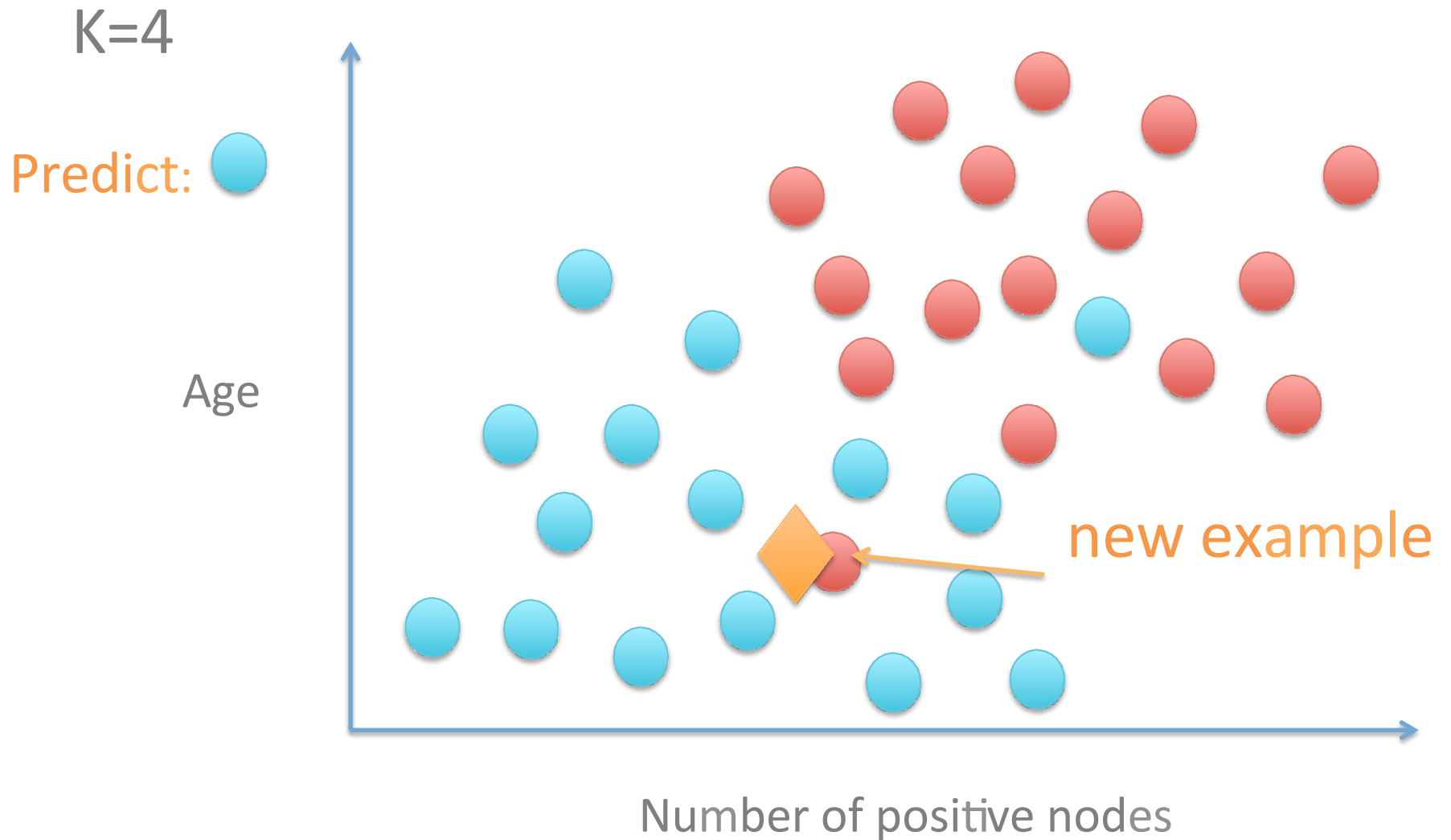


Age



Number of positive nodes

K Nearest Neighbors



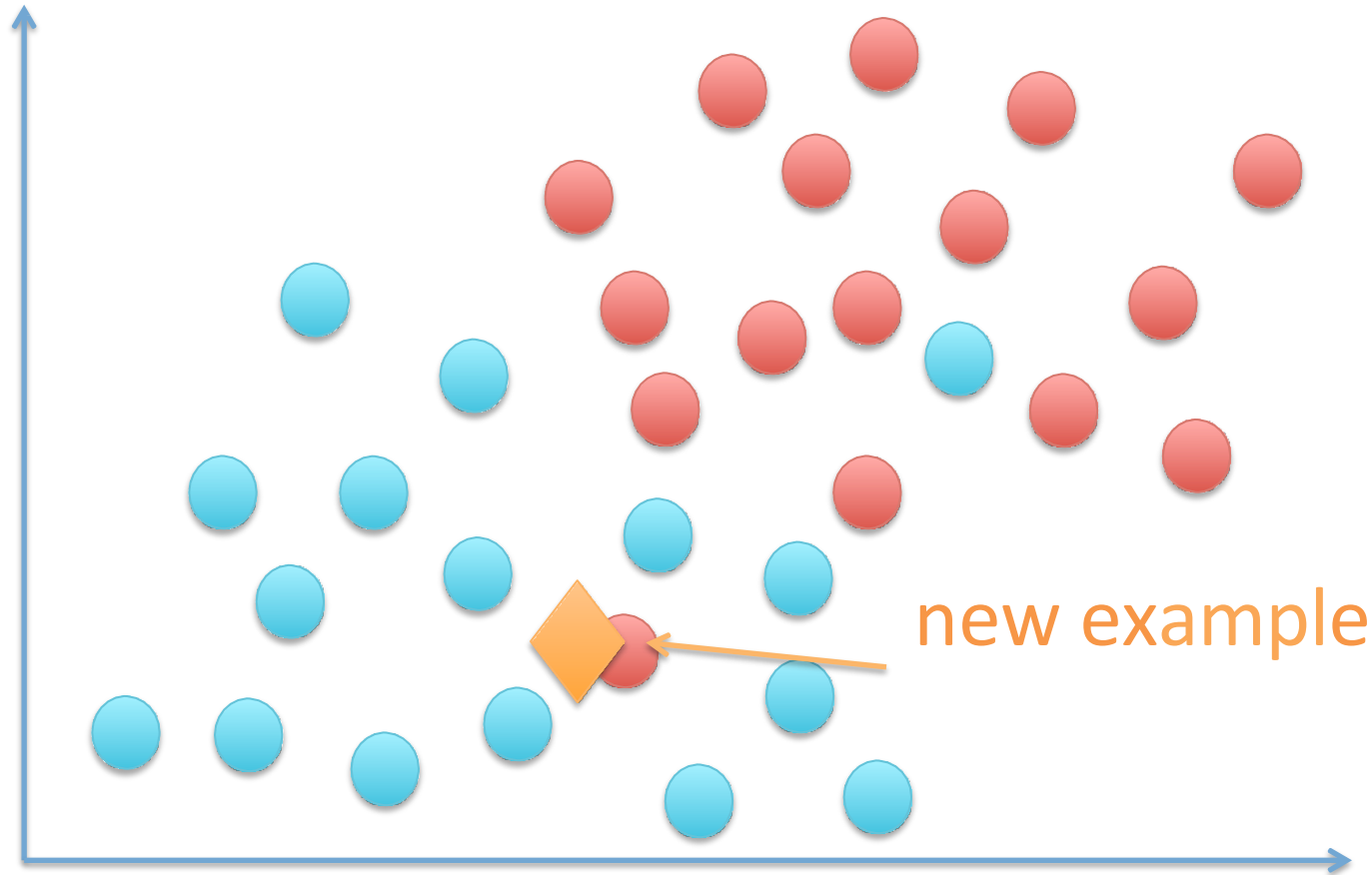
K Nearest Neighbors

K=5

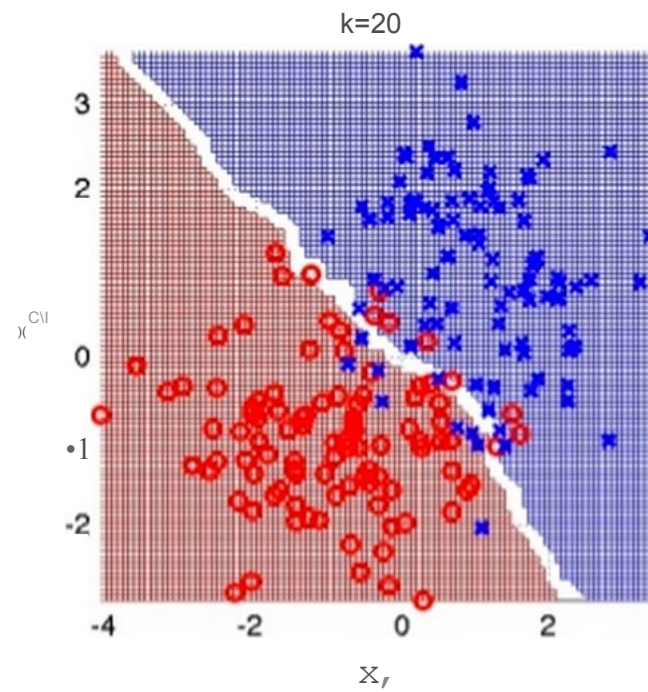
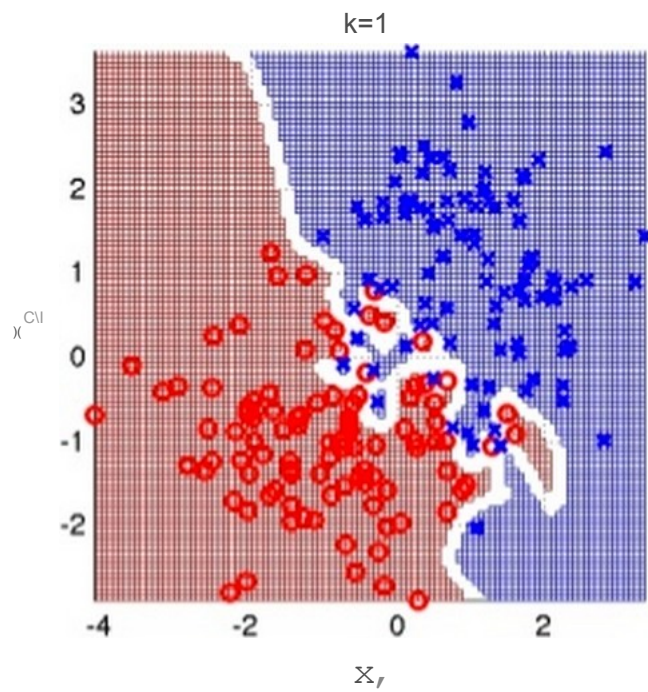
Predict:



Age



Number of positive nodes



```
from sklearn.neighbors import KNeighborsClassifier
```