

# Homework 4 - Results

October 16, 2018

# Likelihood Function

$$l_i^1 = \int [\Pi_t \frac{1}{\sigma_{1t}} \phi(\frac{y_{it1} - X_{it1}\beta_1 - \theta_i}{\sigma_{1t}})] \Phi(\frac{\sum_t (X_{it1} - X_{it0}\tilde{\beta}) - Z_i\delta - \theta_i\gamma}{\sigma_w}) d\theta_i \quad (1)$$

$$\frac{1}{\sqrt{2\pi}\sigma_\theta} \exp(-(\frac{\theta_i}{\sqrt{2}\sigma_\theta})^2) d\theta \quad (2)$$

- Use Gauss-Hermite to approximate integral. Change of variables necessary.

# Test on fake data first

| $\beta_0$ | stde  |      | TRUE  |
|-----------|-------|------|-------|
|           | 0.65  | 0.86 | 1.00  |
|           | 2.08  | 0.18 | 2.00  |
|           | -0.02 | 0.01 | -0.02 |
|           | 0.52  | 0.02 | 0.50  |

| $\beta_1$ | stde |      | TRUE  |
|-----------|------|------|-------|
|           | 1.51 | 0.54 | 0.85  |
|           | 3.23 | 0.20 | 3.50  |
|           | 0.00 | 0.02 | -0.03 |
|           | 1.02 | 0.04 | 1.00  |

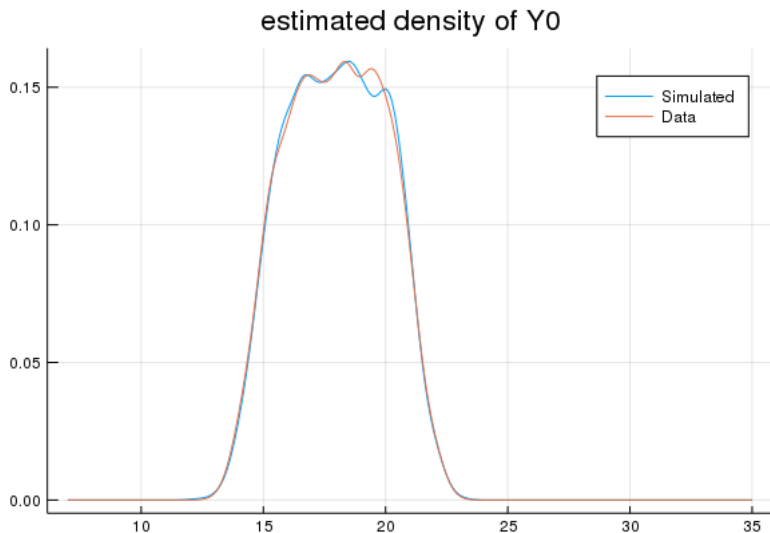
| $\sigma$ | stde |      | TRUE |
|----------|------|------|------|
|          | 0.53 | 0.24 | 0.50 |
|          | 0.50 | 0.31 | 0.50 |
|          | 0.49 | 0.25 | 0.50 |
|          | 0.50 | 0.05 | 0.50 |
|          | 0.70 | 0.03 | 0.71 |
|          | 0.73 | 0.04 | 0.71 |
|          | 0.69 | 0.04 | 0.71 |
|          | 0.70 | 0.04 | 0.71 |
|          | 0.97 | 0.05 | 1.00 |
|          | 0.64 | 0.05 | 0.63 |

| $\delta z$ | stde |      | TRUE |
|------------|------|------|------|
|            | 4.95 | 0.05 | 5.00 |
|            | 2.94 | 0.05 | 3.00 |

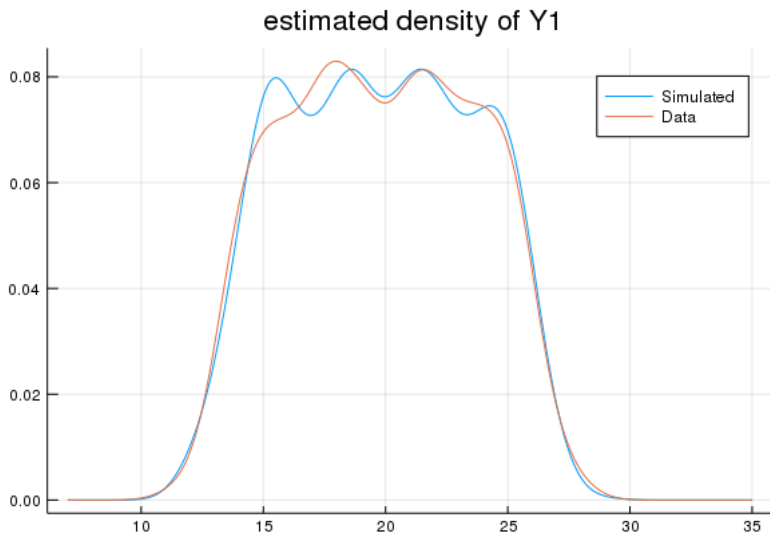
| $\delta t$ | stde |      | TRUE |
|------------|------|------|------|
|            | 0.71 | 0.12 | 0.50 |

| $\rho$ | stde |      | TRUE |
|--------|------|------|------|
|        | 0.76 | 0.05 | 0.80 |

## Test on fake data first



# Test on fake data first



# Test on fake data first

- ▶ Mean school choice: Data = 0.367; Simulated = 0.366

## Summary stats of zb

Mean: 0.020392  
Minimum: -2.929359  
1st Quartile: -0.628405  
Median: 0.002442  
3rd Quartile: 0.619182  
Maximum: 2.957066

## Test on fake data first

- ▶ New Mean school choice: 0.217



## Estimates in log-units

- ▶  $ATE = 11.49$
- ▶  $ATT = 8.12$
- ▶  $LATE = 8.46$

## NLSY data

- ▶  $X$  = experience, experience2 and family income
- ▶  $Z$  = tuition, family income, numsibs, scores, mother and father education

## NLSY data

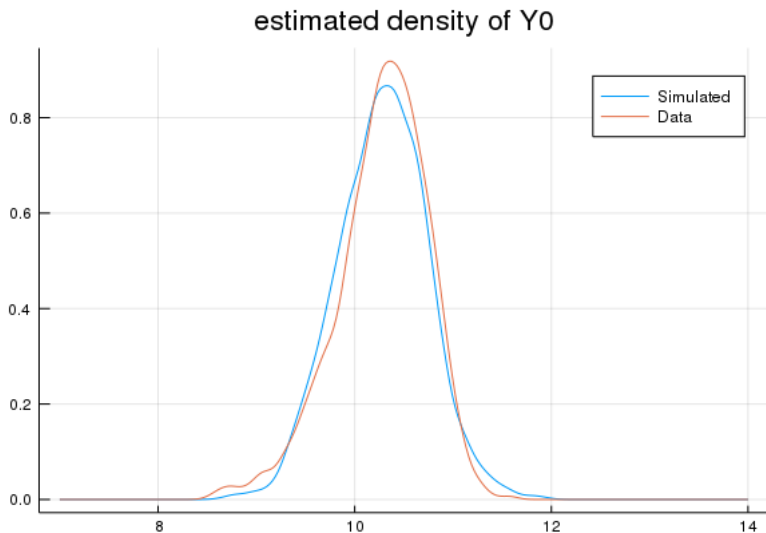
- ▶ Initial guesses:
- ▶ OLS on each wage equation, probit on  $Z$ s, standard errors from OLS

# NLSY Estimates

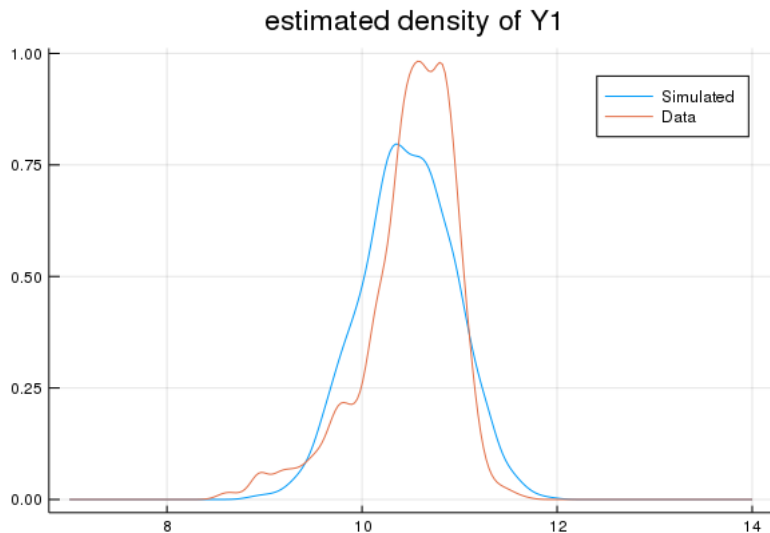
| $\beta_0$  |       | $\sigma$   |      | $\delta z$ |           | $\delta t$     |
|------------|-------|------------|------|------------|-----------|----------------|
| Constant   | 9.58  | $\sigma_0$ | 0.30 | constant   | -1.09     | -0.57          |
| Exp        | 0.18  | $\sigma_0$ | 0.20 | tuition    | -0.27     | $\rho$<br>1.02 |
| Exp^2      | -0.01 | $\sigma_0$ | 0.19 | family inc | -0.27     |                |
| Family Inc | 0.06  | $\sigma_0$ | 0.25 | numsibs    | -0.005168 |                |
|            |       | $\sigma_1$ | 0.34 | scores     | 0.24      |                |
|            |       | $\sigma_1$ | 0.22 | mother     | 0.05      |                |
|            |       | $\sigma_1$ | 0.26 | father     | 0.183375  |                |
|            |       | $\sigma_1$ | 0.31 |            |           |                |
|            |       | $\sigma_w$ | 0.33 |            |           |                |
|            |       | $\sigma_t$ | 0.38 |            |           |                |
| $\beta_1$  |       |            |      |            |           |                |
| Constant   | 8.72  |            |      |            |           |                |
| Exp        | 0.29  |            |      |            |           |                |
| Exp^2      | -0.01 |            |      |            |           |                |
| Family Inc | 0.00  |            |      |            |           |                |

No standard errors :(

## NLSY fit



## NLSY fit



## NLSY fit

- ▶ Mean school choice: Data = 0.372; Simulated = 0.372!

## Summary stats of tuition

Mean: 0.214001

Minimum: 0.000000

1st Quartile: 0.159418

Median: 0.207967

3rd Quartile: 0.257659

Maximum: 0.522191



# Estimates

- ▶ So, I will zero tuition for those below the mean
- ▶ New mean school choice: 0.372!

## Summary stats sim y0

Mean: 31,645.128

Minimum: 4,904.970

1st Quartile: 20,792.095

Median: 28,934.711

3rd Quartile: 39,456.350

Maximum: 155,488.773

# Summary stats sim y1

Mean: 29,664.918

Minimum: 3,547.429

1st Quartile: 17,553.850

Median: 25,781.921

3rd Quartile: 37,211.698

Maximum: 152,681.450

# Estimates

- ▶  $ATE = -1,980.21$
- ▶  $ATT = 8,623.56$
- ▶  $LATE = ?$