# A fast dynamic programming multi-objective knapsack problem

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#### Abstract

This work addresses... The Multidi Objective knapsack programming. The dynamic programming method... The data structure...

- 1 Introduction
- 2 The Multidimensional Knapsack Problem
- 3 The Dynamic Programing Algorithm

[1]

## 4 The use of data structure

The k-d tree is a type of binary search tree for indexing multidimensional data with simple construction and low space usage. Despite its simplicity it efficiently supports operations like nearest neighbour search and range search [2]. For those reasons k-d tree is widely used on spacial geometry algorithms [7, 3], clustering [5, 4] and graphic rendering algorithms [6].

Like a standard binary search tree, the k-d tree subdivides data at each recursive level of the tree. Unlike a standard binary tree, that users only one key for all levels of the tree, the k-d tree uses k keys and cycles through these keys for successive levels of the tree.

Concerning it's efficiency, it is important to consider the number of dimensions k-d tree is indexing. As a general rule, a k-d tree is suitable for efficiently indexing of n elements if n is much greater than  $2^k$ . Otherwise, when k-d tree are used with high-dimensional data, most of the elements in the tree will be evaluated and the efficiency is no better than exhaustive search [8].

Its operations...

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Use on the algorithm.

Indexing the solutions and range operations.

Tends to increase the feasibility on problems with higher dimensions.

## 5 Computational experiments

- Base de dados utilizaca
- Parametros dos algoritmos
- Anlise dos resultados (comparao)

## 6 Conclusions and future remarks

- Concluses dos resultados
- Trabalhos futuros

### References

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