# EFFICIENT SIMULATION OF THERMAL ENHANCED OIL RECOVERY PROCESSES

# A DISSERTATION SUBMITTED TO THE DEPARTMENT OF ENERGY RESOURCES ENGINEERING AND THE COMMITTEE ON GRADUATE STUDIES OF STANFORD UNIVERSITY IN PARTIAL FULFILLMENT OF THE REQUIREMENTS FOR THE DEGREE OF DOCTOR OF PHILOSOPHY

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### **Abstract**

Simulating thermal processes is usually computationally expensive because of the complexity of the problem and strong nonlinearities encountered. In this work, we explore novel and efficient simulation techniques to solve thermal enhanced oil recovery problems. We focus on two major topics: the extension of streamline simulation for thermal enhanced oil recovery and the efficient simulation of chemical reaction kinetics as applied to the in-situ combustion process.

For thermal streamline simulation, we first study the extension to hot water flood processes, in which we have temperature induced viscosity changes and thermal volume changes. We first compute the pressure field on an Eulerian grid. We then solve for the advective parts of the mass balance and energy equations along the individual streamlines, accounting for the compressibility effects. At the end of each global time step, we account for the nonadvective terms on the Eulerian grid along with gravity using operator splitting. We test our streamline simulator and compare the results with a commercial thermal simulator. Sensitivity studies for compressibility, gravity and thermal conduction effects are presented.

We further extended our thermal streamline simulation to steam flooding. Steam flooding exhibits large volume changes and compressibility associated with the phase behavior of steam, strong gravity segregation and override, and highly coupled energy and mass transport. To overcome these challenges we implement a novel pressure update along the streamlines, a Glowinski  $\theta$ -scheme operator splitting and a preliminary streamline/finite volume hybrid approach. We tested our streamline simulator on a series of test cases. We compared our thermal streamline results with those computed by a commercial thermal simulator for both accuracy and efficiency. For the cases

investigated, we are able to retain solution accuracy, while reducing computational cost and gaining connectivity information from the streamlines. These aspects are useful for reservoir engineering purposes.

In traditional thermal reactive reservoir simulation, mass and energy balance equations are solved numerically on discretized reservoir grid blocks. The reaction terms are calculated through Arrhenius kinetics using cell-averaged properties, such as averaged temperature and reactant concentrations. For the in-situ combustion process, the chemical reaction front is physically very narrow, typically a few inches thick. To capture accurately this front, centimeter-sized grids are required that are orders of magnitude smaller than the affordable grid block sizes for full field reservoir models.

To solve this grid size effect problem, we propose a new method based on a non-Arrhenius reaction upscaling approach. We do not resolve the combustion front on the grid, but instead use a subgrid-scale model that captures the overall effects of the combustion reactions on flow and transport, i.e. the amount of heat released, the amount of oil burned and the reaction products generated. The subgrid-scale model is calibrated using fine-scale highly accurate numerical simulation and laboratory experiments. This approach significantly improves the computational speed of in-situ combustion simulation as compared to traditional methods. We propose the detailed procedures to implement this methodology in a field-scale simulator. Test cases illustrate the solution consistency when scaling up the grid sizes in multidimensional heterogeneous problems. The methodology is also applicable to other subsurface reactive flow modeling problems with fast chemical reactions and sharp fronts.

Displacement front stability is a major concern in the design of all the EOR processes. Historically, premature combustion front break through has been an issue for field operations of in-situ combustion. In this work, we perform detailed analysis based on both analytical methods and numerical simulation. We identify the different flow regimes and several driving fronts in a typical 1D ISC process. For the ISC process in a conventional mobile heavy oil reservoir, we identify the most critical front as the front of steam plateau driving the cold oil bank. We discuss the five main contributors for this front stability/instability: viscous force, condensation, heat conduction, coke plugging and gravity. Detailed numerical tests are performed to test

and rank the relative importance of all these different effects.  $\,$ 



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# Contents

A	bstra	ct		iv
A	ckno	wledge	ements	vi
1	Intr	oducti	ion	1
	1.1	Heavy	Oil and Thermal Enhanced Recovery	1
	1.2	Motiv	ations and Objectives	2
	1.3	Thesis	s Outline	Ş
<b>2</b>	${ m Lit}\epsilon$	erature	e Review	5
	2.1	Stream	nline Simulation	۶
		2.1.1	Streamline Simulation Concept and Basics	5
		2.1.2	Advantages and Disadvantages of Streamline Simulation	6
		2.1.3	Streamline Simulation for Complex Physics Processes	E
	2.2	In-situ	a Combustion	11
		2.2.1	In-situ Combustion Process	11
		2.2.2	Field Applications of ISC	12
		2.2.3	Numerical Simulation of In-situ Combustion	15
		2.2.4	Challenges in Combustion Reaction Modeling	16
		2.2.5	Alternative Approaches	16
		2.2.6	Thermal Front Stability for ISC	18
3	Gov	erning	g Equations	21
	3.1	Gener	al Conservation Equations	21

	3.2	Phase	Equilibrium	22
	3.3	Fluid	Property Calculations	24
	3.4	Chem	ical Reactions	25
	3.5	Prima	ry Equations and Variables	26
4	$\operatorname{Th}\epsilon$	ermal S	Streamline Simulation for Hot Water Flood	28
	4.1	Stream	nline Simulation Framework	28
	4.2	Stream	nline Formulation for Hot Water Flood	29
	4.3	Specif	ic Techniques	31
		4.3.1	Mappings	31
		4.3.2	Operator Splitting for Non-advective Processes	32
		4.3.3	Treatment of Compressibility	33
	4.4	Hot W	Vater Flood Results	33
		4.4.1	Incompressible Hot Water Flood	34
		4.4.2	Compressible Hot Water Flood	39
		4.4.3	Gravity Effects	42
		4.4.4	Heat Conduction Effects	43
	4.5	Concl	uding Remarks	44
5	$\operatorname{Th}\epsilon$	ermal S	Streamline for Steam Flood	45
	5.1	Stream	nline Simulation Framework	45
	5.2	Stream	nline Formulation for Steam Flood	46
	5.3	Specif	ic Techniques	49
		5.3.1	1D Pressure and Volumetric Flux Update Approach for Large	
			Compressibility	49
		5.3.2	Glowinski $\theta\text{-Scheme}$ Operator Splitting Approach for Non-advecti	ve
			Processes	55
		5.3.3	Preliminary Hybrid Simulation	56
	5.4	Steam	Flood Results	58
		5.4.1	Heterogeneous Quarter-Five Spot Steam Flood	58
		5.4.2	Cyclic Steam Stimulation	62
		5/13	Heterogeneous Multi-well Pattern Steam Flood	64

		5.4.4	Vertical Cross Section Steam Flood	69
	5.5	Discus	ssion and Applications	72
		5.5.1	Streamline Simulation as Fast Proxy: Cost Comparison	72
		5.5.2	Optimization and Flux Patterns	73
	5.6	Concl	uding Remarks	74
6	In-s	itu Co	ombustion Simulation	76
	6.1	Kineti	ic Reaction Models	76
	6.2	1D Co	ombustion Tube Simulation	79
	6.3	Sensit	ivity Studies on 1D ISC Problem	85
	6.4	Grid S	Size Effects and their Cause	89
		6.4.1	Grid Size Effects	89
		6.4.2	The Cause of Grid Size Effects	91
		6.4.3	Why not Adaptive Mesh Refinement?	92
		6.4.4	The Need for Upscaling	93
	6.5	Concl	uding Remarks	94
7	Ups	scaling	for In-situ Combustion Reactions	95
	7.1	Non-A	Arrhenius Reaction Modeling	96
	7.2	Imple	mentation	99
		7.2.1	Pseudo Code	99
		7.2.2	Implementation in Commercial Software	100
	7.3	Upsca	ling Test Cases	102
		7.3.1	1D Tests	102
		7.3.2	2D Tests	104
		7.3.3	3D Tests	107
	7.4	Discus	ssion and Applications	108
		7.4.1	Valid Range	108
		7.4.2	Sub-grid Scale Heterogeneity and its Effects on Reaction Up-	
			scaling	111
	7.5	Concl	uding Remarks	119

8	Fro	nt Stal	bility Study for In-situ Combustion	121		
	8.1	1D Flo	ow Regimes	121		
	8.2	Contri	ibutors for Front Stability/Instability	123		
	8.3	Numer	rical Tests	126		
		8.3.1	Minimizing Numerical Errors	126		
		8.3.2	Small Sub-grid Scale Front Stability	131		
		8.3.3	Large Field-scale Front Stability	136		
	8.4	Conclu	uding Remarks	136		
9	Fut	ure Di	rections	139		
	9.1	Therm	nal Streamline Simulation	139		
		9.1.1	Non-advective Forces	139		
		9.1.2	Guidelines for Commercial Code Development	139		
		9.1.3	Thermal Streamline Simulation for SAGD?	140		
	9.2	In-situ	Combustion	142		
		9.2.1	History Matching of Field-scale ISC process	142		
		9.2.2	Calibrating the Operational Range for Sustaining ISC Combus-			
		9.2.3	tion	143		
		9.2.4	cesses	144		
		0.2.1	in Fractured Carbonate Reservoir?	145		
10	Cor	nclusio	ns	150		
$\mathbf{A}$	Sim	ulation	n Inputs	154		
В	STA	ARS In	aput File for Three Reaction Model	158		
$\mathbf{C}$	Ecli	pse In	put File for Three Reaction Model	166		
D	STA	ARS In	aput File for Upscaled Three Reaction Model	179		
$\mathbf{E}$	SAGD Input File 18'					

$\mathbf{F}$	SAGD	Input	File for	Grid S	Size	Effects	Study	$\mathbf{y}$		193
Bi	bliograp	ohy								203



# List of Tables

4.1	Errors of different viscosity properties compared with reference result	
	$(400 \times 400 \text{ STARS result}) \text{ using L2 norm } \dots \dots \dots \dots$	37
4.2	Effects of thermal compressibility on the production (surface condition)	41
4.3	Heat Pe number and its influence on the simulation result	44
5.1	Errors of thermal streamline and STARS compared to reference (360 $\times$	
	180 STARS result) using the relative L2 norm	61
5.2	Sensitivity study on choice of $\theta$ . The simulation results close to each	
	other by using different $\theta$	62
5.3	Errors of thermal streamline and STARS compared to reference (200 $\times$	
	200 STARS result) using L2 norm	69
7.1	Explanation of major variables in the upscaling pseudo code	101
7.2	Explanation of major functions in the upscaling pseudo code	102
7.3	Summary of Sub-grid Scale Heterogeneity ISC Tests	118
A.1	Reservoir properties for hot water flood	154
A.2	Viscosity relationships for hot water flood	155
A.3	Fluid parameters for incompressible hot water flooding	155
A.4	Coefficients of density calculations in compressible hot water flood	155
A.5	Reservoir properties for steam flood	155
A.6	Well control for steam flood	156
A.7	Fluid parameters for steam flood	156
A.8	Reservoir properties for cyclic steam stimulation	156

A.9 Fluid properties in three reaction ISC model	157
A.10 Rock properties in ISC simulation	157
A.11 Kinetics parameters for three reaction ISC model	157
A.12 Reaction stoichiometry for three reaction ISC model	157



# List of Figures

2.1	Streamline simulation framework, with the four major steps in a global	
	time step	7
2.2	Different zones in the field in-situ combustion process, courtesy of US	
	Department of Energy, Bartlesville, Oklahoma	13
2.3	Different zones in 1D in-situ combustion process	13
4.1	The permeability field in quarter five-spot hot water flood test case	34
4.2	The water saturation results in quarter five-spot hot water flood test	
	case	34
4.3	The temperature results in quarter five-spot hot water flood test case.	35
4.4	The pressure results in quarter five-spot hot water flood test case	35
4.5	The comparison between 1D fully implicit (FIM) transport solver and	
	1D single point upwind explicit (SPU) transport solver for thermal SL	
	simulation (50X50)	36
4.6	The surface cumulative production results for M=10 quarter five-spot	
	hot water flood test case	38
4.7	The surface cumulative production results for $M=100$ quarter five-spot	
	hot water flood test case	38
4.8	The surface cumulative production results for $M=1000$ quarter five-	
	spot hot water flood test case	39
4.9	The saturation results in compressible quarter five-spot hot water flood	
	test case	40
4.10	The temperature results in compressible quarter five-spot hot water	
	flood test case	40

4.11	The surface cumulative production comparison results in compressible	
	quarter five-spot hot water flood test case	41
4.12	Saturation results in gravity test case 1 (quarter five-spot hot water	
	flood with dipping)	42
4.13	Saturation results in gravity test case 2 (quarter five-spot hot water	
	flood with dipping)	42
5.1	Steam condensation causes volume change and flux reduction right at	
	the steam front	49
5.2	Streamline segments constructed from the injector to the producer	50
5.3	1D streamline pressure and volumetric flux update approach. Trans-	
	missibility and block volume of each segment is calculated for the 1D	
	transport	50
5.4	Streamline $(s, n, m)$ coordinates and cross sectional area along the	
	streamline	51
5.5	1D pressure update improvements in capturing transient pressure change	
	within a global time step, (M=1000 quarter five spot hot water flood	
	test case). With two BHP controlled wells, classical SL underestimates	
	the breakthrough. Both SL predict-correct [71] and SL with pressure	
	update improves the hot water breakthrough results, compared to fine-	
	scale reference.	54
5.6	Pressure transient behavior inside a global time step (M=1000 quarter	
	five spot hot water flood test case). The pressure stitched together	
	from all the 1D pressure solves (B) is similar to the pressure we get at	
	the beginning of the next global time step (C). $\dots$	54
5.7	Schematic of coupled energy-mass transport. Changing the total en-	
	ergy of a grid block changes the fluid volume inside, thus causing fluid	
	transport to adjacent cells	55
5.8	Glowinski $\theta\text{-scheme}$ operator splitting. Most of the transport is solved	
	along 1D streamlines $[0 \sim (1-\theta)\Delta t]$ . Small amount of advective flux	
	is used to correct the volume changes in heat conduction/gravity step.	56

5.9	An equivalent representation of Glowinski $\theta$ -scheme operator splitting.
	Most of the transport is solved along 1D streamlines. Small amount
	of advective flux is used to correct the volume changes in heat conduc-
	tion/gravity step.
5.10	Quarter five spot steam flood permeability field and initial streamline
	shape
5.11	Viscosity curve for water and oil
5.12	Quarter five spot temperature and gas saturation at 3000 days (pre
	breakthrough)
5.13	Quarter five spot water and oil saturation at 3000 days (pre break-
	through)
5.14	Sensitivity study on the choice of $\theta$ . The simulation results are close
	to each other by using different $\theta$
5.15	Hybrid procedures in cyclic steam stimulation $(SL \to FV \to SL)$ and
	the initial streamline shape
5.16	Cyclic steam stimulation temperature result
5.17	Cyclic steam stimulation oil saturation result
5.18	Cyclic steam stimulation production profile (SL and FV)
5.19	2D multiple well test case permeability field
5.20	2D multiple well test case initial streamline shape
5.21	Multiple well test case temperature and oil saturation at 1500 days
	(pre breakthrough)
5.22	Multiple well test case field production history (pre breakthrough)
5.23	Multiple well test case temperature and oil saturation at 2100 days
	(post breakthrough)
5.24	Multiple well test case field production history (post breakthrough)
5.25	2D vertical cross section steam flood test case 1 (homogeneous perme-
	ability field)
5.26	2D vertical cross section steam flood case 2 (heterogeneous permeabil-
	ity field)
5.27	Flux pattern map, by Thiele and Batycky [106]

6.1	Gas composition from ramped temperature oxidation experiments	77
6.2	Relative permeability (water-oil and liquid-gas, respectively) and oil	
	viscosity curve used in the simulation of Hamaca oil 1D combustion	
	tube experiment	80
6.3	Temperature, oil saturation and pressure profiles in 1D combustion	
	tube simulation after 498 min of air injection	81
6.4	Typical temperature profile history from a 1D combustion tube exper-	
	iment, from Lapene et al., [66]	81
6.5	Water, oil and gas production rates in 1D combustion tube simulation.	83
6.6	Produced gas composition analysis in 1D combustion tube simulation.	84
6.7	Oil bank and combustion front distance-time diagram from 1D com-	
	bustion tube simulation	84
6.8	1D ISC simulation: peak temperature and combustion front velocity	
	as a function of the injection air flux	85
6.9	1D ISC simulation: oil saturation profile as a function of the initial oil	
	saturation $S_{oi}$	86
6.10	Temperature profiles as a function of the initial water saturation $S_{wi}$	
	of $0.10$ , $0.24$ and $0.50$ from left to right	88
6.11	Combustion tube simulation of a mobile heavy oil with high initial oil	
	saturation $S_{oi}$ at $378min$	89
6.12	Characteristics of different fronts in 1D ISC problem: scenario 1 (bi-	
	tumen like oil viscosity and oil bank stays inside the steam plateau)	90
6.13	Characteristics of different fronts in 1D ISC problem: scenario 2 (mo-	
	bile heavy oil viscosity and leading edge of steam plateau follows behind	
	the oil bank)	90
6.14	Basic assumption for thermal reservoir simulation: instantaneous mix-	
	ing in each cell	91
6.15	Grid-size effects in 1D combustion tube simulation. We require at	
	least 200 grid blocks to achieve convergent solution in this $0.8m$ long	
	combustion tube simulation	92

7.1	The critical physics for 1D ISC. When the reaction front sweeps through	
	the reservoir, a certain amount of oil becomes fuel and burns (usually	
	$x=5\sim 10\%~S_o$ ). The rest of the mobile oil is displaced further	
	downstream	95
7.2	ISC upscaling work flow	98
7.3	1D ISC upscaling tests: kinetic and upscaled model using different grid	
	resolutions. The coarse scale upscaled model matches the fine-scale	
	kinetics based reference, while the coarse scale kinetic model fails	103
7.4	1D ISC upscaled model with different equivalent fuel amount $S_{ofuel}$ .	
	The front location has a direct relationship with the fuel amount $S_{ofuel}$ .	103
7.5	ISC upscaling in horizontal 2D $1/4$ five spot case: $O_2$ fraction in gas	
	phase with different grid resolution and both kinetic and upscaled model.	105
7.6	ISC upscaling in horizontal 2D multi well case: coarse grid upscaled	
	model and fine grid kinetic model	105
7.7	ISC upscaling in horizontal 2D heterogeneous case: coarse grid up-	
	scaled model and fine grid kinetic model	106
7.8	ISC upscaling in 2D vertical case: coarse grid upscaled model and	
	fine-grid kinetic model	107
7.9	3D field-scale case using the upscaled reaction model. Consistency is	
	achieved between different grid resolutions	109
7.10	Permeability and oil saturation results for 2D case with uncorrelated	
	white noise permeability field. The combustion front propagates stably.	112
7.11	2D case with correlated heterogeneity (low perm in the middle). We	
	observe some oxygen by pass and change in equivalent fuel amount. $\ \ .$	113
7.12	2D case with correlated low permeability squares. We calculate oxygen	
	efficiency $E_u = 0.90$ and fuel amount $S_{ofuel} = 9.7\%$	114
7.13	2D case with horizontal layered permeability. We observe oxygen by-	
	pass and change in equivalent fuel amount	115
7.14	2D case with heterogeneity (layer 1 of SPE 10 [23]). The oxygen effi-	
	ciency is $E_{n} = 0.91$ and fuel amount $S_{ofuel} = 8.6\%$	116

7.15	2D case with channelized heterogeneity (layer 51 of SPE 10 [23]). The	
	oxygen efficiency is $E_u = 0.85$ and fuel amount $S_{ofuel} = 13\%$	117
7.16	Different scales in measurements, geomodeling and reservoir simula-	
	tion, lecture notes of ERE 241 Seismic Reservoir Characterization	120
8.1	Different fronts and flow regimes in 1D ISC process	123
8.2	Perturbation length $\lambda$ at leading edge of steam plateau, from [50]	125
8.3	Trigger instability by changing the initial oil saturation at the boundary	127
8.4	Test of numerical errors with triggered instability. The effect of grid	
	size and 5-point versus 9-point scheme is illustrated	129
8.5	Test of temporal numerical errors with automatic time-step selection	
	and restricted time step sizes	130
8.6	Sensitivity to thermal conductivity. Heat conduction stabilizes the dis-	
	placement front in small lab-scale tests. Reduced thermal conductivity	
	cases show greater instability	132
8.7	Nusselt number characterizes the heat conduction stabilizing effect,	
	compared to Fig. 8.6	133
8.8	Pore blocking with the Kozeny-Carman correlation. Very small changes	
	are observed compared to base case	134
8.9	Pore blocking with an exaggerated permeability reduction. The com-	
	bustion front slows down only when implementing pore blocking of	
	more than one order of magnitude reduction in permeability. $$	135
8.10	Unstable displacement in 2D larger scale ISC process. Heat conduction	
	is incapable of dissipating the energy of large wavelength perturbations.	137
9.1	Total phase velocity vectors in 2D SAGD process. Convection cell/loop	
	current occur when tracing streamlines	141
9.2	Grid size effects in 2D SAGD simulation (early time 360 days). The	
	simulation achieves convergent solution when using grid size $0.5m \times$	
	0.5m in this case	145

9.3	Grid size effects in 2D SAGD simulation (late time 1100 days). The	
	simulation achieves convergent solution when using grid size $0.5m \times$	
	0.5m in this case	146
9.4	Concept of ISC assisted gas oil gravity drainage in fractured media.	
	Vent well is added to achieve hydrostatic gravity drainage condition in	
	the reservoir	148
9.5	Gravity stable ISC process for a single block of fractured media. Be-	
	cause of the gas diffusion, we are able to combust into the matrix.	
	Most of the flue gas is produced from upper right corner	140

## Chapter 1

### Introduction

### 1.1 Heavy Oil and Thermal Enhanced Recovery

A large part of the world oil resource exists in the form of heavy oil, which is usually defined as oil with API gravity less than 22 and viscosity typically larger than 100cp. Estimated original oil in place of more than 1.8 trillion barrels is present in Venezuela, 1.7 trillion barrels in Alberta, Canada, and 20- 25 billion barrels on the North Slope of Alaska. The development of such resources by traditional methods (primary depletion, waterflood) is often inefficient due to the high viscosity of the heavy oil. At such high viscosities, the oil flows extremely slowly or not at all. For example, the bitumen resources in Athabasca oil sands typically have an extremely large viscosity of about  $10^6 cp$ .

Thermal recovery processes rely on viscosity reduction of the oil through heat that is injected (steam or hot water injection) or generated in-situ (in-situ combustion), and are well suited for efficiently unlocking these heavy oil resources. Accordingly to current U.S. Department of Energy data, thermal enhanced recovery techniques account for about 50% of the domestic Enhanced Oil Recovery (EOR) production. Steam flooding, cyclic steam stimulation and hot water flooding are widely used, but other processes, such as in-situ combustion (ISC) and increasingly steam-assisted gravity drainage (SAGD) are applied and are attractive to recover heavy oil resources.

### 1.2 Motivations and Objectives

Planning and management of thermal EOR processes generally make extensive use of reservoir simulation. Nearly all the commercial and academic thermal simulators are traditional finite volume (FV) based codes that use either a fully implicit (FIM) time stepping method or an adaptive implicit (AIM) method [6, 37, 101]. The computational costs for simulating thermal processes are usually high because of the complexity of the problem and strong nonlinearity encountered. As a result, it is time consuming to run optimization and/or sensitivity studies on grids with desirable numerical resolution. For problems such as ISC and SAGD, the simulations show extremely large computational costs with very strict requirements on the sizes of grid blocks, due to the need to capture/resolve accurately the narrow thermal fronts existing in these processes. Field-scale ISC simulation is still impractical, due to large computational costs associated with accurately resolving the inch-sized reactive combustion fronts. There is, therefore, an urgent need to develop fast and efficient numerical simulation methodologies for thermal EOR problems. Predictive mathematical models and efficient simulators are needed to improve our understanding of these thermal EOR processes and enable cost-effective design of these projects.

In this work, we focus on three major problems: the extension of streamline simulation (SL) to thermal problems (hot water flood and steam flood), the efficient simulation of field-scale ISC process through reaction upscaling, and the analysis of thermal front stability in ISC. The detailed objectives are as follows:

- 1. For the thermal streamline simulation, we are seeking a fast and effective reservoir simulator that gives sufficient accuracy for use in reservoir simulation studies, such as ranking, optimization and history matching. This is a first time that streamline simulation is extended to complex thermal problems such as steam flood. Problems such as fluid compressibility, strong coupling and gravity effects need to be addressed.
- 2. For the ISC simulation, our main objective is to find an efficient simulation technique to upscale the reaction kinetics for full field-scale ISC simulation. To