

# EJEMPLO 1-11

Sea el sistema que aparece en la figura 1-27. Se desea hallar la función de transferencia de lazo cerrado  $C(s)/R(s)$  utilizando la fórmula de Mason.

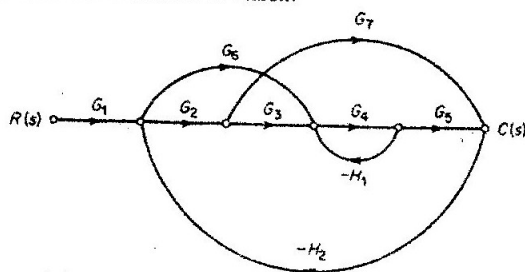


Figura 1-27  
Gráfico de flujo de  
señal de un sistema.

Trayectorias directas:

$$P_1 = G_1 G_2 G_3 G_4 G_5; \quad P_2 = G_1 G_6 G_4 G_5; \quad P_3 = G_1 G_2 G_7$$

Lazos cerrados:

$$L_1 = -G_2 G_3 G_4 G_5 H_2; \quad L_2 = -G_6 G_4 G_5 H_2; \quad L_3 = -G_7 H_2 G_2$$

$$L_4 = -G_4 H_1$$

$$\Delta = 1 - (L_1 + L_2 + L_3 + L_4) + L_3 L_4 \quad (L_3 \text{ y } L_4 \text{ disjuntas})$$

$$\Delta_1 = 1; \quad \Delta_2 = 1; \quad \Delta_3 = 1 - L_4 \quad (\text{la trayectoria } P_3 \text{ es disjunta respecto } L_4)$$

$$\Delta = 1 - L_1 - L_2 - L_3 - L_4 + L_3 L_4$$

$$\frac{C(s)}{R(s)} = \frac{1}{\Delta} (P_1 \Delta_1 + P_2 \Delta_2 + P_3 \Delta_3) = \frac{1}{\Delta} [P_1 + P_2 + P_3 (1 - L_4)] = \frac{C(s)}{R(s)}$$

$$\Delta = 1 + G_2 G_3 G_4 G_5 H_2 + G_4 G_5 G_6 H_2 + G_2 G_7 H_2 + G_4 H_1 + (G_2 G_7 H_2 \cdot G_4 H_1)$$

$$\Delta = 1 + G_2 G_3 G_4 G_5 H_2 + G_4 G_5 G_6 H_2 + G_2 G_7 H_2 + G_4 H_1 + G_2 G_4 G_7 H_1 H_2$$

$$P_1 + P_2 + P_3 - P_3 L_4 = G_1 G_2 G_3 G_4 G_5 + G_1 G_4 G_5 G_6 + G_1 G_2 G_7 + G_1 G_2 G_7 G_4 H_1$$

$$\frac{C(s)}{R(s)} = \frac{G_1 G_2 G_3 G_4 G_5 + G_1 G_4 G_5 G_6 + G_1 G_2 G_7 (1 + G_4 H_1)}{1 + G_4 H_1 + G_2 G_7 H_2 + G_4 G_5 G_6 H_2 + G_2 G_3 G_4 G_5 H_2 + G_2 G_4 G_7 H_1 H_2}$$