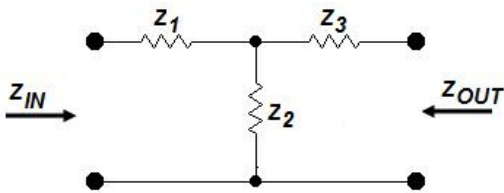


CALCULO DE CUADRIPOLOS – EJEMPLO FUNCIÓN DE PROPAGACIÓN

EJEMPLO 1:



Valor de Z1 [Ohms] ? 20

Valor de Z2 [Ohms] ? 16

Valor de Z3 [Ohms] ? 32

PARAMETROS IMPEDANCIA

$$Z_{11} = Z_1 + Z_2 = 36 \text{ [Ohms]}$$

$$Z_{12} = Z_{21} = Z_2 = 16 \text{ [Ohms]}$$

$$Z_{22} = Z_2 + Z_3 = 48 \text{ [Ohms]}$$

$$AZ = Z_{11}Z_{22} - Z_{12}Z_{21} = 1472 \text{ [Ohms}^2\text{]}$$

PARAMETROS TRANSMISION DIRECTA

$$A = Z_{11}/Z_{21} = 2.25 \text{ [Adim]}$$

$$B = AZ/Z_{21} = 92 \text{ [Ohms}^2\text{]}$$

$$C = 1/Z_{21} = 0.0625 \text{ [Mho]}$$

$$D = Z_{22}/Z_{21} = 3 \text{ [Adim]}$$

CALCULO DE LA IMPEDANCIA ITERATIVA

$$Z_{K1} = -(A-D)/(2*C) + \sqrt{((A-D)/(2*C))^2 + (B/C)} = 44.833 \text{ [Ohms]}$$

$$Z_{K2} = -(D-A)/(2*C) + \sqrt{((D-A)/(2*C))^2 + (B/C)} = 32.833 \text{ [Ohms]}$$

CALCULO DE LA IMPEDANCIA IMAGEN

$$Z_{IM1} = \sqrt{(A*B)/(C*D)} = 33.2265 \text{ [Ohms]}$$

$$Z_{IM2} = \sqrt{(B*D)/(A*C)} = 44.302 \text{ [Ohms]}$$

CALCULO DE LA FUNCION DE PROPAGACIÓN EN BASE ITERATIVA

$$\text{Fun_Prop_It} = ((A+D)/2) + \sqrt{((A+D)/2)^2 - 1}$$

$$\text{Fun_Prop_ZIt} = 5.0521 \text{ [Adim]}$$

CALCULO DE LA FUNCION DE PROPAGACIÓN EN BASE IMAGEN

$$\text{Fun_Prop_Im} = \sqrt{A/D} * ((\sqrt{A*D}) + \sqrt{(A*D) - 1})$$

$$\text{Fun_Prop_ZIm} = 4.3267 \text{ [Adim]}$$

RESUMEN

$$Z_{K1} = 44.8329756778952$$

$$Z_{K2} = 32.8329756778952$$

$$Z_{IM1} = 33.2264954516723$$

$$Z_{IM2} = 44.3019939355631$$

$$\text{Fun_Prop_It} = 5.05206097986845$$

$$\alpha_{\text{ITERATIVA}} = \log(\text{Fun_Prop_It}) = 1.6197962748565 \text{ [Np ó nepers]}$$

$$\text{Fun_Prop_Im} = 4.32665596572952$$

$$\text{Ein/Eout}_{\text{IMAGEN}} = \sqrt{Z_{IM1}/Z_{IM2}} * (\sqrt{A*D} + \sqrt{A*D - 1})$$

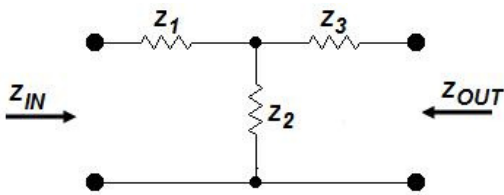
$$\text{ans} = 4.32665596572952$$

$$\text{lin/lout}_{\text{IMAGEN}} = \sqrt{Z_{IM2}/Z_{IM1}} * (\sqrt{A*D} + \sqrt{A*D - 1})$$

$$\text{ans} = 5.76887462097269$$

$$\alpha_{\text{IMAGEN}} = \log(\text{Fun_Prop_Im}) = 1.4647949493527 \text{ [Np ó nepers]}$$

EJEMPLO 2:



Valor de Z1 [Ohms] ? 3300

Valor de Z2 [Ohms] ? 1200

Valor de Z3 [Ohms] ? 6800

PARAMETROS IMPEDANCIA

$$Z_{11} = Z_1 + Z_2 = 4500 \text{ [Ohms]}$$

$$Z_{12} = Z_{21} = Z_2 = 1200 \text{ [Ohms]}$$

$$Z_{22} = Z_2 + Z_3 = 8000 \text{ [Ohms]}$$

$$AZ = Z_{11} \cdot Z_{22} - Z_{12} \cdot Z_{21} = 34560000 \text{ [Ohm]}$$

PARAMETROS TRANSMISION DIRECTA

$$A = Z_{11}/Z_{21} = 3.75 \text{ [Adim]}$$

$$B = AZ/Z_{21} = 28800 \text{ [Ohms}^2\text{]}$$

$$C = 1/Z_{21} = 0.00083333 \text{ [Mho]}$$

$$D = Z_{22}/Z_{21} = 6.6667 \text{ [Adim]}$$

CALCULO DE LA IMPEDANCIA ITERATIVA

$$ZK1 = \frac{-(A-D)}{(2 \cdot C)} + \sqrt{\left(\frac{(A-D)}{(2 \cdot C)}\right)^2 + (B/C)} = 7883.7183 \text{ [Ohms]}$$

$$ZK2 = \frac{-(D-A)}{(2 \cdot C)} + \sqrt{\left(\frac{(D-A)}{(2 \cdot C)}\right)^2 + (B/C)} = 4383.7183 \text{ [Ohms]}$$

CALCULO DE LA IMPEDANCIA IMAGEN

$$ZIM1 = \sqrt{(A \cdot B)/(C \cdot D)} = 4409.0815 \text{ [Ohms]}$$

$$ZIM2 = \sqrt{(B \cdot D)/(A \cdot C)} = 7838.3672 \text{ [Ohms]}$$

CALCULO DE LA FUNCION DE PROPAGACIÓN EN BASE ITERATIVA

$$\text{Fun_Prop_It} = ((A+D)/2) + \sqrt{\left(\frac{(A+D)}{2}\right)^2 - 1}$$

$$\text{Fun_Prop_ZIt} = 10.3198 \text{ [Adim]}$$

CALCULO DE LA FUNCION DE PROPAGACIÓN EN BASE IMAGEN

$$\text{Fun_Prop_Im} = \sqrt{A/D} \cdot (\sqrt{A \cdot D} + \sqrt{(A \cdot D) - 1})$$

$$\text{Fun_Prop_ZIm} = 7.4242 \text{ [Adim]}$$

RESUMEN

$$ZK1 = 7883.71828502092 \text{ [Ohms]}$$

$$ZK2 = 4383.71828502092 \text{ [Ohms]}$$

$$ZIM1 = 4409.08153700972 \text{ [Ohms]}$$

$$ZIM2 = 7838.36717690617 \text{ [Ohms]}$$

$$\text{Fun_Prop_It} = 10.3197652375174$$

$$\alpha_{\text{ITERATIVA}} = \log(\text{Fun_Prop_It}) = 2.3340610114921 \text{ [Np ó nepers]}$$

$$\text{Fun_Prop_Im} = 7.42423461417477$$

$$E_{in}/E_{out_IMAGEN} = \sqrt{ZIM1/ZIM2} \cdot (\sqrt{A \cdot D} + \sqrt{A \cdot D - 1})$$

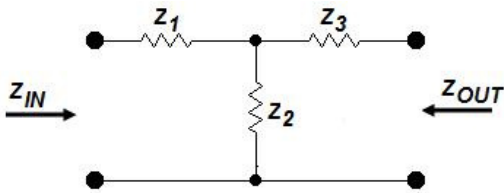
$$\text{ans} = 7.42423461417477$$

$$I_{in}/I_{out_IMAGEN} = \sqrt{ZIM2/ZIM1} \cdot (\sqrt{A \cdot D} + \sqrt{A \cdot D - 1})$$

$$\text{ans} = 13.1986393140885$$

$$\alpha_{\text{IMAGEN}} = \log(\text{Fun_Prop_Im}) = 1.4647949493527 \text{ [Np ó nepers]}$$

EJEMPLO 3: CUADRIPOLO SIMÉTRICO



Valor de Z1 [Ohms] ? 4700

Valor de Z2 [Ohms] ? 7500

Valor de Z3 [Ohms] ? 4700

PARAMETROS IMPEDANCIA

$$Z_{11} = Z_1 + Z_2 = 12200 \text{ [Ohms]}$$

$$Z_{12} = Z_{21} = Z_2 = 7500 \text{ [Ohms]}$$

$$Z_{22} = Z_2 + Z_3 = 12200 \text{ [Ohms]}$$

$$AZ = Z_{11} \cdot Z_{22} - Z_{12} \cdot Z_{21} = 92590000 \text{ } [\Omega^2]$$

PARAMETROS TRANSMISION DIRECTA

$$A = Z_{11}/Z_{21} = 1.6267 \text{ [Adim]}$$

$$B = AZ/Z_{21} = 12345.3333 \text{ [Ohms}^2\text{]}$$

$$C = 1/Z_{21} = 0.00013333 \text{ [Mhos]}$$

$$D = Z_{22}/Z_{21} = 1.6267 \text{ [Adim]}$$

CALCULO DE LA IMPEDANCIA ITERATIVA

$$Z_{K1} = -(A-D)/(2 \cdot C) + \sqrt{((A-D)/(2 \cdot C))^2 + (B/C)} = 9622.36977048793 \text{ [Ohms]}$$

$$Z_{K2} = -(D-A)/(2 \cdot C) + \sqrt{((D-A)/(2 \cdot C))^2 + (B/C)} = 9622.36977048793 \text{ [Ohms]}$$

CALCULO DE LA IMPEDANCIA IMAGEN

$$Z_{IM1} = \sqrt{(A \cdot B)/(C \cdot D)} = 9622.36977048793 \text{ [Ohms]}$$

$$Z_{IM2} = \sqrt{(B \cdot D)/(A \cdot C)} = 9622.36977048793 \text{ [Ohms]}$$

CALCULO DE LA IMPEDANCIA CARACTERISTICA

$$Z_o = \sqrt{B/C} = 9622.3698 \text{ [Ohms]}$$

CALCULO DE LA FUNCION DE PROPAGACIÓN EN BASE ITERATIVA

$$\text{Fun_Prop_It} = ((A+D)/2) + \sqrt{((A+D)/2)^2 - 1} = 2.90964930273172 \text{ [Adim]}$$

CALCULO DE LA FUNCION DE PROPAGACIÓN EN BASE IMAGEN

$$\text{Fun_Prop_Im} = \sqrt{A/D} \cdot ((\sqrt{A \cdot D}) + \sqrt{(A \cdot D) - 1}) = 2.90964930273172 \text{ [Adim]}$$

CALCULO DE LA FUNCION DE PROPAGACIÓN EN BASE CARACTERISTICA

$$\text{Fun_Prop_Zo} = A + \sqrt{A^2 - 1} = 2.90964930273172 \text{ [Adim]}$$

RESUMEN

$$Z_{K1} = 9622.36977048793 \text{ [Ohms]}$$

$$Z_{K2} = 9622.36977048793 \text{ [Ohms]}$$

$$Z_{IM1} = 9622.36977048793 \text{ [Ohms]}$$

$$Z_{IM2} = 9622.36977048793 \text{ [Ohms]}$$

$$Z_o = 9622.36977048793 \text{ [Ohms]}$$

$$\text{Fun_Prop_It} = 2.90964930273172$$

$$\alpha_{\text{ITERATIVA}} = \log(\text{Fun_Prop_It}) = 1.0680325593957 \text{ [Np ó nepers]}$$

$$\text{Fun_Prop_Im} = 2.90964930273172$$

$$E_{in}/E_{out_IMAGEN} = \sqrt{Z_{IM1}/Z_{IM2}} \cdot (\sqrt{A \cdot D} + \sqrt{A \cdot D - 1})$$

$$\text{ans} = 2.90964930273172$$

$$I_{in}/I_{out_IMAGEN} = \sqrt{Z_{IM2}/Z_{IM1}} \cdot (\sqrt{A \cdot D} + \sqrt{A \cdot D - 1})$$

$$\text{ans} = 2.90964930273172$$

$$\text{Fun_Prop_Zo} = A + \sqrt{A^2 - 1} = 2.90964930273172$$

$$\alpha_{\text{CARACTERÍSTICA}} = \log(\text{Fun_Prop_Zo}) = 1.06803255939576 \text{ [Np]}$$