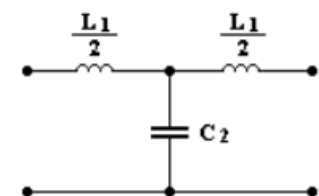


## pasa bajos



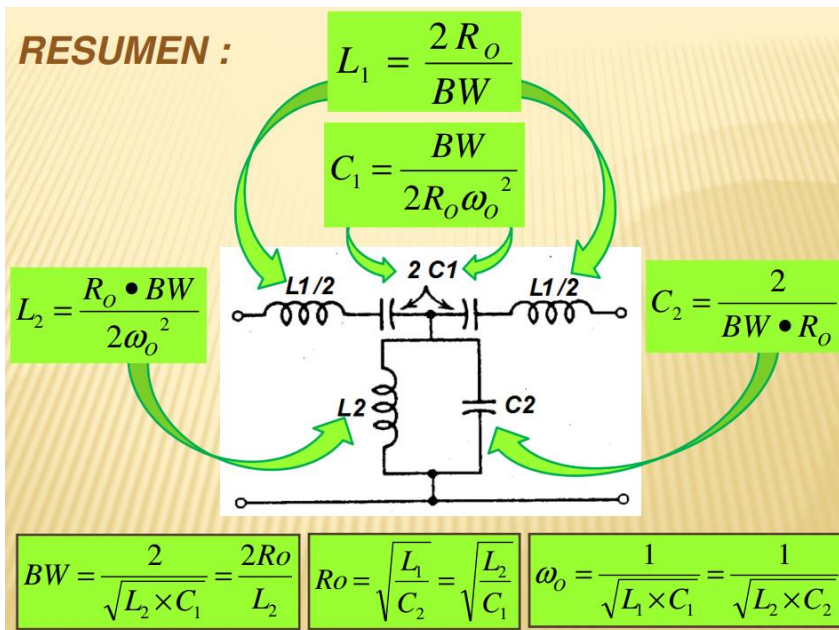
$$L_1 = \frac{2 * R_o}{\omega_c}$$

$$C_2 = \frac{2}{R_o * \omega_c}$$

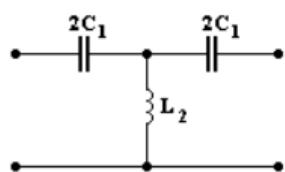
$$\omega_c = \frac{2}{\sqrt{L_1 * C_2}}$$

## PASA BANDA

### RESUMEN :



## pasa altos



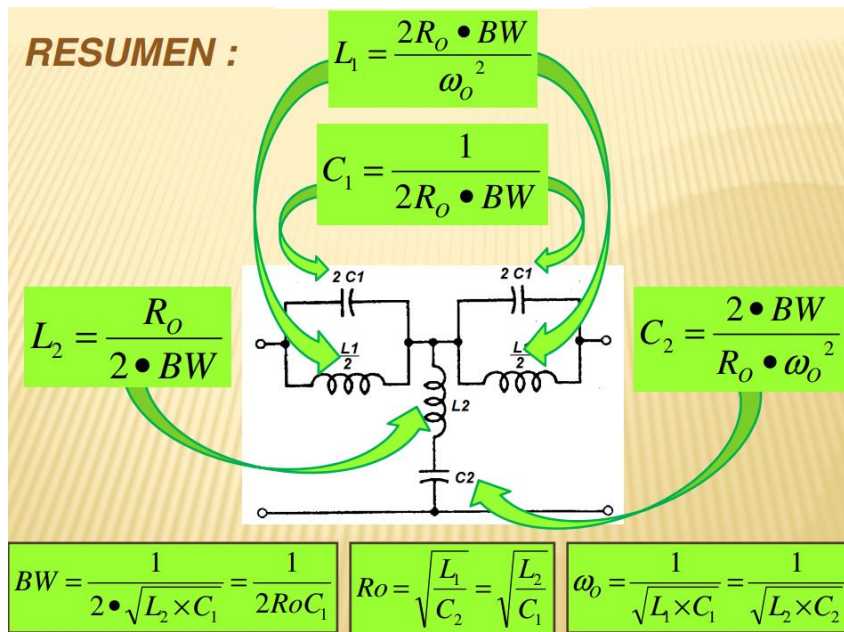
$$C_1 = \frac{1}{2 * R_o * \omega_c}$$

$$L_2 = \frac{R_o}{2 * \omega_c}$$

$$\omega_c = \frac{1}{2 * \sqrt{L_2 * C_1}}$$

## ELIMINA BANDA

### RESUMEN :



$R_o$  = Impedancia de carga;  $\omega_c$  = Pulsación de corte (pb y pa);  $\omega_1$  = Pulsación de corte inferior;  
 $\omega_2$  = Pulsación de corte superior;  $W$  = Ancho de banda =  $\omega_2 - \omega_1$  y  $\omega_o$  = Pulsación de Resonancia.

$$AB = W = \omega_{c2} - \omega_{c1}$$

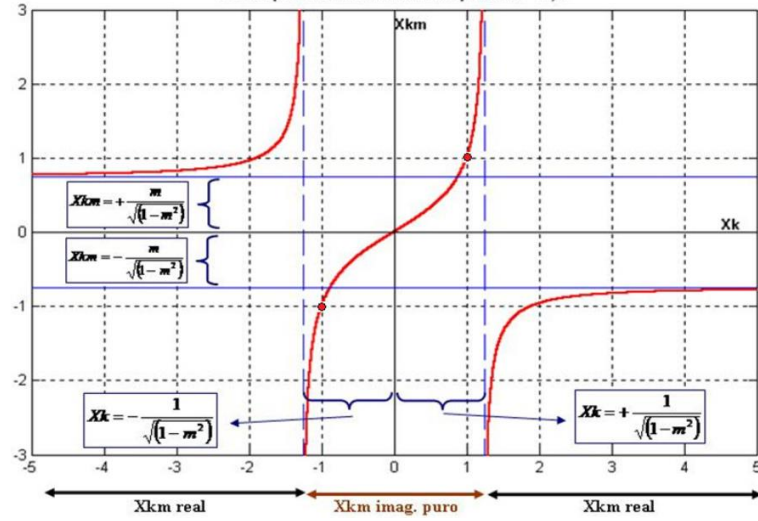
$$\omega_o = \sqrt{\omega_{c2} * \omega_{c1}}$$

# FILTRO M-DERIVADO GRÁFICOS

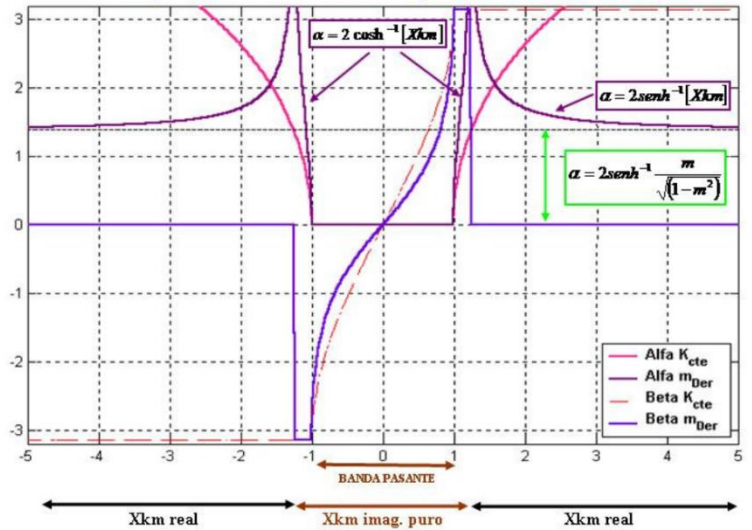
$$Z_{1Km} = m \bullet Z_{1K}$$

$$Z_{2Km} = \frac{Z_{2K}}{m} + Z_{1K} \left( \frac{1-m^2}{4m} \right)$$

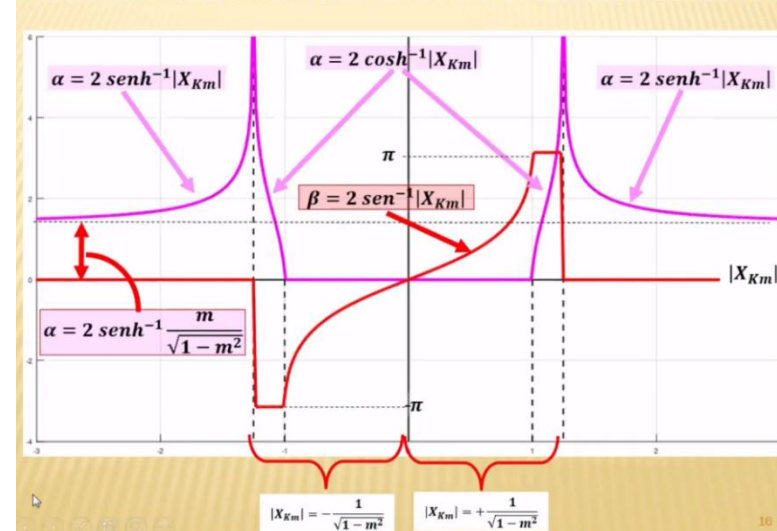
Correspondencia  $X_{Km}$  a  $X_K$  para  $m = 0,6$



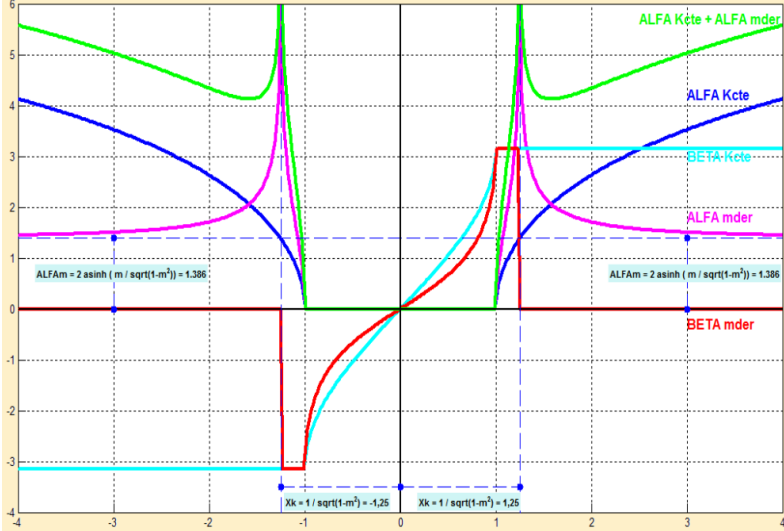
Comparación entre curvas de filtros Kcte y filtros m-Derivado con  $m = 0.6$



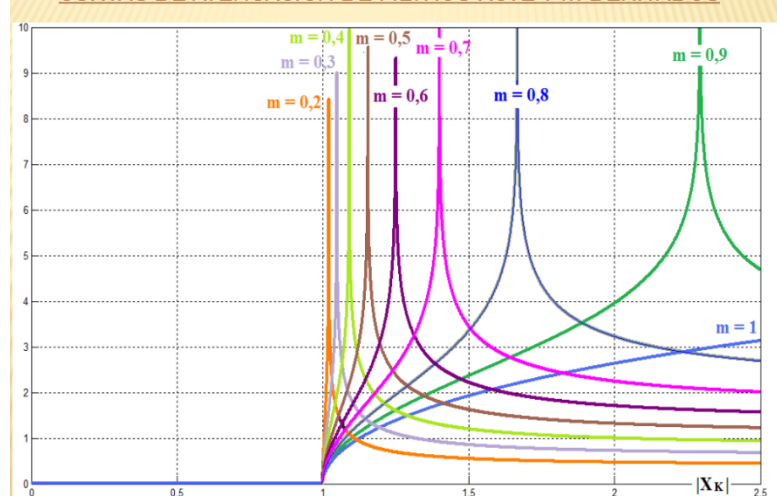
CURVA DE ATENUACION Y DE FASE DE FILTRO  $m$ -DERIVADO



CURVAS DE ATENUACION Y FASE DE FILTROS Kcte, M-DERIVADO Y COMPUESTO CON  $m = 0,6$

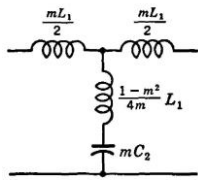


CURVAS DE ATENUACIÓN DE FILTROS Kcte Y  $m$ -DERIVADOS



# ANÁLISIS DE M-DERIVADO

pasa bajos



$$W_0 = \frac{2}{\sqrt{1-m^2}} \cdot \frac{1}{\sqrt{L_1 C_2}} \quad W_{\infty} = \frac{1}{\sqrt{L_{2m} C_{2m}}}$$

$$W_c = W_{\infty} \cdot \sqrt{1-m^2}$$

$$M = \sqrt{1 - \left(\frac{W_c}{W_{\infty}}\right)^2} \quad m = \sqrt{\frac{L_{1m}}{L_{1m} + 4L_{2m}}}$$

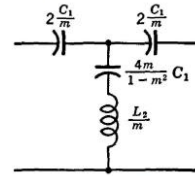
$$\frac{L_{1m}}{2} = \frac{L_1}{2} \cdot m \Rightarrow L_1 = \frac{2}{m} \left(\frac{L_{1m}}{2}\right)$$

$$C_{2m} = m C_2 \Rightarrow C_2 = \frac{C_{2m}}{m}$$

$$L_{2m} = L_1 \left(\frac{1-m^2}{4m}\right) \Rightarrow L_1 = \frac{L_{2m} \cdot 4m}{1-m^2}$$

$$R_0 = \sqrt{\frac{L_{1m}}{C_{2m}}}$$

pasa altos



$$W_0 = \frac{\sqrt{1-m^2}}{2} \cdot \frac{1}{\sqrt{C_1 L_2}} \quad W_{\infty} = \frac{1}{\sqrt{C_{2m} L_{2m}}}$$

$$W_c = \frac{W_{\infty}}{\sqrt{1-m^2}}$$

$$m = \sqrt{\frac{C_{2m}}{C_{2m} + 4C_{1m}}} \quad M = \sqrt{1 - \left(\frac{W_{\infty}}{W_c}\right)^2}$$

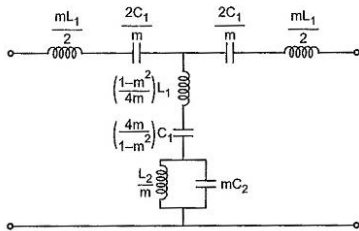
$$2C_{1m} = \frac{2C_1}{m} \Rightarrow C_1 = C_{1m} \cdot m$$

$$L_{2m} = \frac{L_2}{m} \Rightarrow L_2 = L_{2m} \cdot m$$

$$C_{2m} = C_1 \cdot \frac{4m}{1-m^2} \Rightarrow C_1 = \frac{C_{2m} \cdot 1-m^2}{4m}$$

$$R_0 = \sqrt{\frac{L_{2m}}{C_{1m}}}$$

PASA BANDA



$$m = \sqrt{1 - \left(\frac{BW_k}{BW_{\infty}}\right)^2} \quad L_{1m} C_{1m} = L_{3m} C_{3m}$$

$$M = \sqrt{\frac{L_{1m}}{L_{1m} + 4L_{3m}}} \quad M = \sqrt{\frac{C_{3m}}{C_{3m} + 4C_{1m}}}$$

$$BW_{\infty} = BW_k \cdot \sqrt{1-m^2} \quad L_{1m} C_{1m} = L_{3m} C_{3m}$$

$$\frac{2}{m} \sqrt{\frac{1}{L_{2m} C_{1m}}} = BW_{\infty} \quad (?)$$

$$W_{\infty}^2 - \frac{BW}{\sqrt{1-m^2}} W_{\infty} - W_0^2 = 0 \quad (?)$$

$$\frac{L_{1m}}{2} = m \frac{L_1}{2} \Rightarrow L_1 = \frac{L_{1m}}{m}$$

$$2C_{1m} = \frac{2C_1}{m} \Rightarrow C_1 = C_{1m} \cdot m$$

$$L_{2m} = \frac{L_2}{m} \Rightarrow L_2 = m \cdot L_{2m}$$

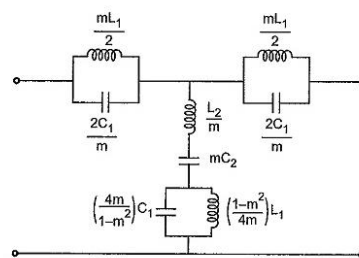
$$C_{2m} = m C_2 \Rightarrow C_2 = \frac{C_{2m}}{m}$$

$$L_{3m} = L_1 \cdot \frac{1-m^2}{4m} \Rightarrow L_1 = \frac{L_{3m} \cdot 4m}{1-m^2}$$

$$C_{3m} = C_1 \cdot \frac{4m}{1-m^2} \Rightarrow C_1 = \frac{C_{3m} \cdot 1-m^2}{4m}$$

$$R_0 = \sqrt{\frac{L_{1m}}{C_{2m}}} = \sqrt{\frac{L_{2m}}{C_{1m}}}$$

ELIMINA BANDA



$$M = \sqrt{1 - \left(\frac{BW_k}{BW_{\infty}}\right)^2} \quad M = \sqrt{\frac{L_{1m}}{L_{1m} + 4L_{3m}}} = \sqrt{\frac{C_{3m}}{C_{3m} + 4C_{1m}}}$$

$$BW_{\infty} = BW_k \cdot \sqrt{1-m^2} \quad BW_{\infty} = \frac{1}{2\sqrt{L_2 C_1}} \cdot \sqrt{1-m^2}$$

$$W_{\infty}^2 - \frac{BW}{\sqrt{1-m^2}} W_{\infty} - W_0^2 = 0 \quad BW_{\infty} = \frac{1}{2m} \cdot \frac{1}{\sqrt{L_{2m} C_{1m}}}$$

$$2C_{1m} = \frac{2C_1}{m} \Rightarrow C_1 = C_{1m} \cdot m$$

$$\frac{L_{1m}}{2} = \frac{L_1}{2} \cdot m \Rightarrow L_1 = \frac{L_{1m}}{m}$$

$$L_{2m} = \frac{L_2}{m} \Rightarrow L_2 = L_{2m} \cdot m$$

$$C_{2m} = C_2 \cdot m \Rightarrow C_2 = \frac{C_{2m}}{m}$$

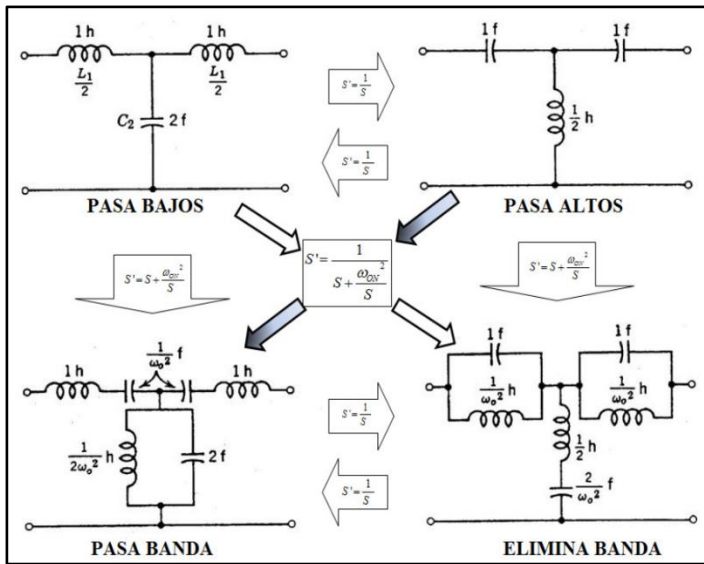
$$C_{3m} = C_1 \cdot \frac{4m}{1-m^2} \Rightarrow C_1 = \frac{C_{3m} \cdot 1-m^2}{4m}$$

$$L_{3m} = L_1 \cdot \frac{1-m^2}{4m} \Rightarrow L_1 = \frac{L_{3m} \cdot 4m}{1-m^2}$$

$$R_0 = \sqrt{\frac{L_{1m}}{C_{2m}}} = \sqrt{\frac{L_{2m}}{C_{1m}}}$$

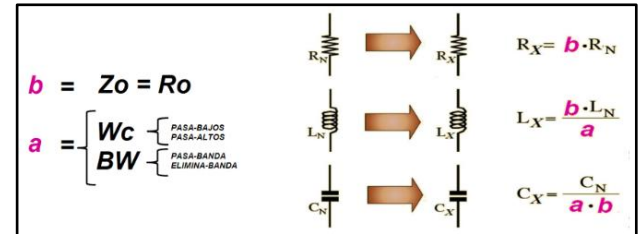


# DISEÑO DE FILTRO COMPUESTO



1. Cálculo del filtro k-cte prototipo partiendo de uno normalizado

2. Desnormalización del filtro k-cte prototipo



3. Cálculo de "m" (para atenuación alfa = infinito)

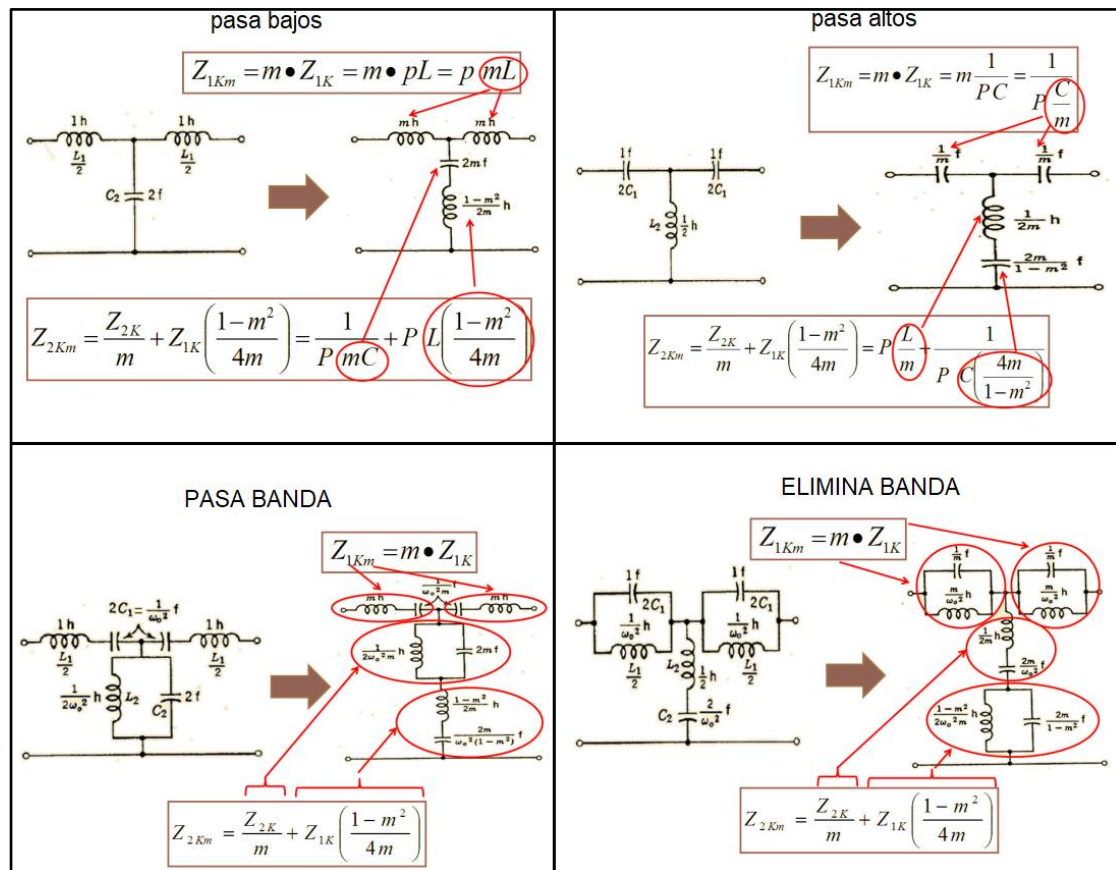
$$m = \sqrt{1 - \left(\frac{f_{sc}}{f_c}\right)^2} \rightarrow \text{En Filtros pasa - bajos}$$

$$m = \sqrt{1 - \left(\frac{f_c}{f_{sc}}\right)^2} \rightarrow \text{En Filtros pasa - altos}$$

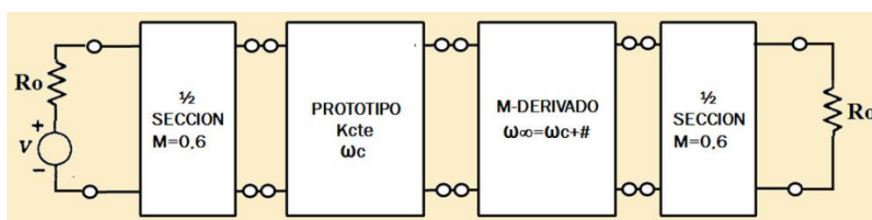
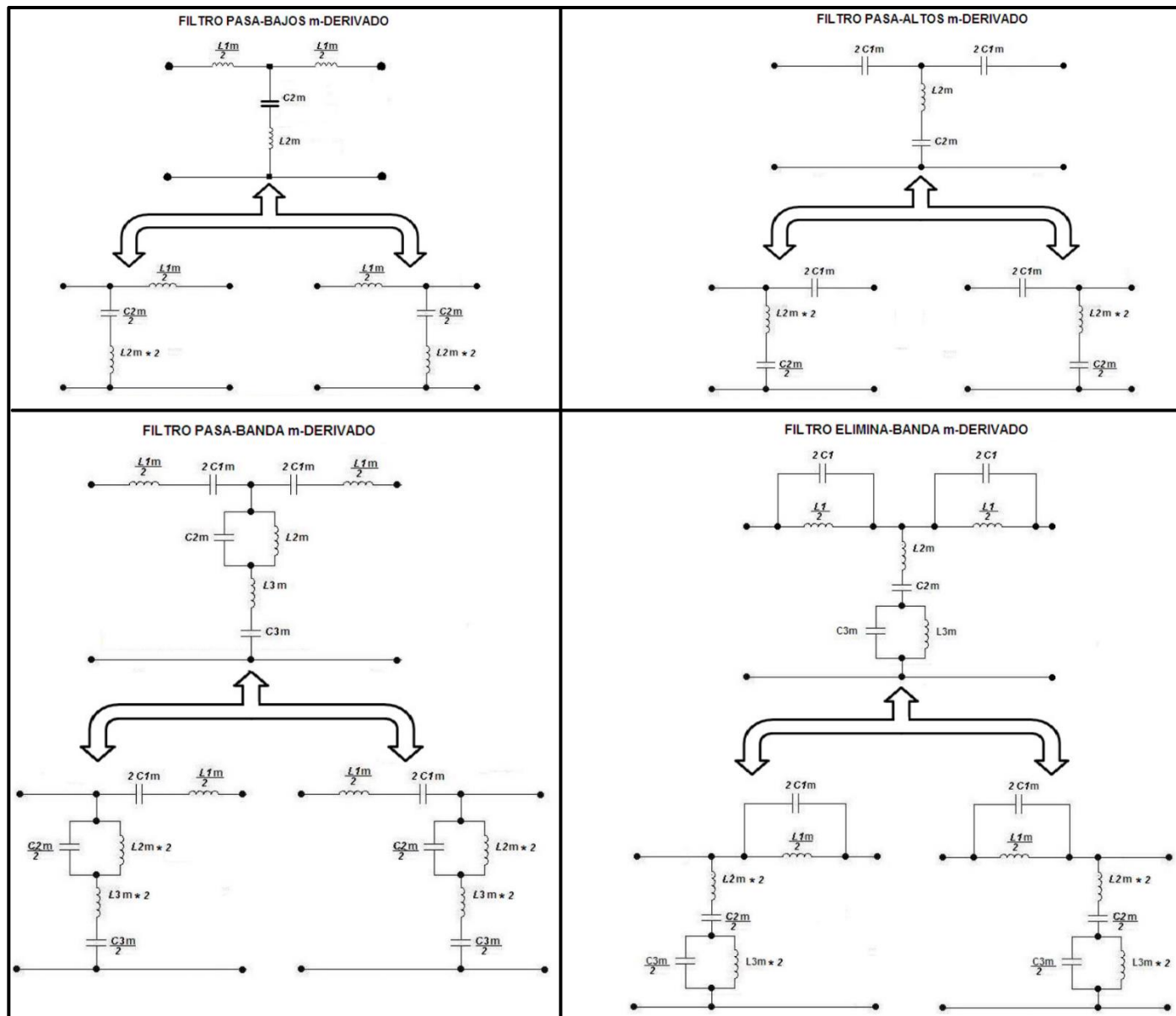
$$m = \sqrt{1 - \left(\frac{BW}{BW_{sc}}\right)^2} = \sqrt{1 - \left(\frac{\omega_{c2} - \omega_{c1}}{\omega_{c2} * \frac{\omega_{sc2} - \omega_{c1}}{\omega_{sc2}^2} - \frac{\omega_{c1}}{\omega_{c2}^2}}\right)^2} \rightarrow \text{En Filtros Pasa - Banda}$$

$$m = \sqrt{1 - \left(\frac{BW_{sc}}{BW}\right)^2} = \sqrt{1 - \left(\frac{\omega_{c2} * \frac{\omega_{sc2} - \omega_{c1}}{\omega_{sc2}^2} - \frac{\omega_{c1}}{\omega_{c2}^2}}{\omega_{c2} - \omega_{c1}}\right)^2} \rightarrow \text{En Filtros Elimina - Banda}$$

4. Cálculo del filtro m-derivado



## 5. Cálculo de las semisecciones adaptadoras m-derivadas



# BUTTERWORTH

Desnormalización:

$$\epsilon = \sqrt{10^{(0,1 \cdot A_{max_{dB}})} - 1}$$

$$R_X = R_{OUT}$$

$$L_X = R_{OUT} * \epsilon^{1/n} * \frac{1}{\omega_p} * L_N$$

$$C_X = \frac{1}{R_{OUT}} * \epsilon^{1/n} * \frac{1}{\omega_p} * C_N$$

Se calcula  $\epsilon$  para cualquier  $A_{max}$  y se multiplican todos los valores de esta tabla por  $\epsilon^{1/n}$

## VALORES DE COMPONENTES PARA $A_{max} = 3 \text{ dB}$

n	Epsilon <sup>^(1/n)</sup>	L1	C1	L2	C2	L3
1	1					1
2	1				0,70710678	1,41421356
3	1			0,5	1,33333333	1,5
4	1		0,382683	1,08239	1,57716	1,53073
5	1	0,309017	0,894427	1,38197	1,69443	1,54508

COMPONENTES ORIGINALES

$$R_X = R_O$$

$$L_X = L_N \frac{R_O * \epsilon^{1/n}}{\omega_p}$$

$$C_X = C_N \frac{\epsilon^{1/n}}{\omega_p * R_O}$$

COMPONENTES DE CIRCUITO RESONANTE

$$L_X\# = L_N \frac{R_O}{\omega_{on}^2 * BW}$$

$$C_X\# = C_N \frac{1}{\omega_{on}^2 * BW * R_O}$$

$$\omega_{on}^2 = \frac{\omega_o^2}{BW^2} = \frac{(\omega_{c2} * \omega_{c1})}{(\omega_{c2} - \omega_{c1})^2}$$

Se debe eliminar de la función de transferencia los componentes que no correspondan al grado del filtro:

$$G_5(S) = \frac{V_{OUT}}{V_{IN}} = \frac{1}{S^5 L_1 L_2 L_3 C_1 C_2 + S^4 L_2 L_3 C_1 C_2 + S^3 [L_1 (L_2 C_1 + L_3 C_1 + L_3 C_2) + L_2 L_3 C_2] + S^2 [C_1 (L_2 + L_3) + L_3 C_2] + S (L_1 + L_2 + L_3) + 1}$$

Otros cálculos de utilidad:

$$|H(j\omega)|_{dB} = A(\omega)_{dB} = 10 \cdot \log_{10} \left[ 1 + \epsilon^2 \left( \frac{\omega}{\omega_p} \right)^{2n} \right] [dB]$$

$$n = \frac{\log_{10} \left( \frac{10^{0,1 \cdot A_{min}} - 1}{\epsilon^2} \right)}{\log_{10} \left( \frac{\omega_s}{\omega_p} \right)^2}$$

$$\Omega = \epsilon^{1/n} \left( \frac{\omega}{\omega_p} \right) \Rightarrow A(\Omega) = 10 \cdot \log_{10} (1 + \Omega^{2n})$$

n	Polinomios de Butterworth Normalizados - H(S)
1	S + 1
2	S <sup>2</sup> + 1.414 S + 1
3	(S <sup>2</sup> + S + 1).(S + 1)
4	(S <sup>2</sup> + 0.765 S + 1).(S <sup>2</sup> + 1.848 S + 1)
5	(S + 1).(S <sup>2</sup> + 0.618 S + 1).(S <sup>2</sup> + 1.618 S + 1)
6	(S <sup>2</sup> + 0.517 S + 1).(S <sup>2</sup> + 1.414 S + 1).(S <sup>2</sup> + 1.932 S + 1)
7	(S + 1).(S <sup>2</sup> + 0.445 S + 1).(S <sup>2</sup> + 1.247 S + 1).(S <sup>2</sup> + 1.802 S + 1)
8	(S <sup>2</sup> + 0.39 S + 1).(S <sup>2</sup> + 1.111 S + 1).(S <sup>2</sup> + 1.663 S + 1).(S <sup>2</sup> + 1.962 S + 1)

n	Butterworth Polynomials
1	s + 1
2	s <sup>2</sup> + 1.414s + 1
3	s <sup>3</sup> + 2s <sup>2</sup> + 2s + 1
4	s <sup>4</sup> + 2.613s <sup>3</sup> + 3.414s <sup>2</sup> + 2.613s + 1
5	s <sup>5</sup> + 3.236s <sup>4</sup> + 5.236s <sup>3</sup> + 5.236s <sup>2</sup> + 3.236s + 1

## CHEBYSHEV

Coeficientes de los polinomios de Chebychev ( $\alpha_p = 1dB$ )  
( $\varepsilon = 0.5089$ )

n	a <sub>0</sub>	a <sub>1</sub>	a <sub>2</sub>	a <sub>3</sub>	a <sub>4</sub>
1	1.9652267				
2	1.1025103	1.0977343			
3	0.4913067	1.2384092	0.9883412		
4	0.2756276	0.7426194	1.4539248	0.9527114	
5	0.1228267	0.5805342	0.9743961	1.6888160	0.9368201

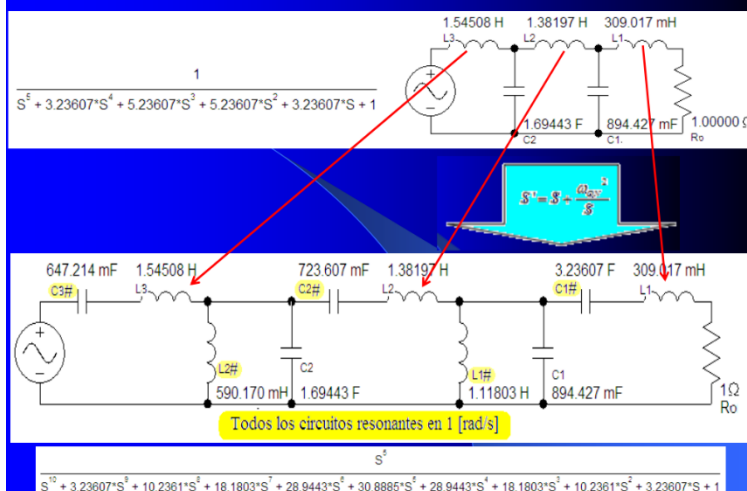
n	Chebyshev Polynomials
1	$s + 1.965$
2	$s^2 + 1.097s + 1.102$
3	$s^3 + 0.7378s^2 + 1.0222s + 0.3269$
4	$s^4 + 0.952s^3 + 1.453s^2 + 0.742s + 0.275$
5	$s^5 + 0.7064s^4 + 1.4995s^3 + 0.6935s^2 + 0.4594s + 0.0817$

## BESSEL

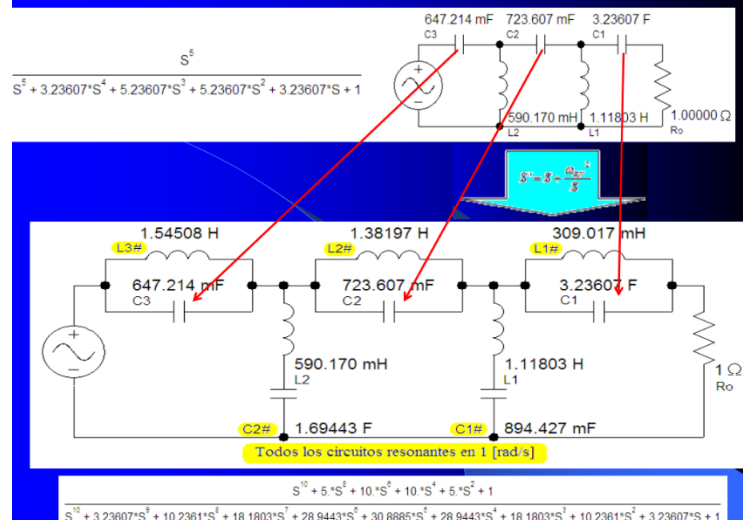
Polinomios de Bessel y ecuación de recurrencia

$$\begin{aligned}
 B_0(p) &= 1 \\
 B_1(p) &= p + 1 \quad \rightarrow \quad A_{\max} = 3 \text{ [dB]} \\
 B_2(p) &= p^2 + 3p + 3 \quad \rightarrow \quad A_{\max} = 1,597 \text{ [dB]} \\
 B_3(p) &= p^3 + 6p^2 + 15p + 15 \quad \rightarrow \quad A_{\max} = 0,903 \text{ [dB]} \\
 B_4(p) &= p^4 + 10p^3 + 45p^2 + 105p + 105 \quad \rightarrow \quad A_{\max} = 0,63 \text{ [dB]} \\
 B_5(p) &= p^5 + 15p^4 + 105p^3 + 420p^2 + 945p + 945 \quad \rightarrow \quad A_{\max} = 0,4865 \text{ [dB]} \\
 B_6(p) &= p^6 + 210p^4 + 1260p^3 + 4725p^2 + 10395p + 10395 \\
 &\vdots \\
 B_{N+1}(p) &= (2N+1)B_N(p) + p^2B_{N-1}(p)
 \end{aligned}$$

### TRANSFORMACIÓN PASA-BAJOS A PASA-BANDA :



### TRANSFORMACIÓN PASA-ALTOS A ELIMINA-BANDA :



# FILTROS ACTIVOS: SALLEN-KEY

$a_i$  y  $b_i$  definen el tipo de filtro (Butterworth, chebyshev, etc)

$$A(s) \Big|_{\text{pasa-bajos}} = \frac{A_o}{(1 + a_i s + b_i s^2)}$$

$$A(s) \Big|_{\text{pasa-altos}} = \frac{A_o s^2}{(1 + a_i s + b_i s^2)}$$

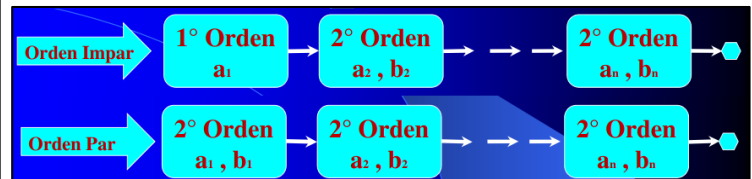
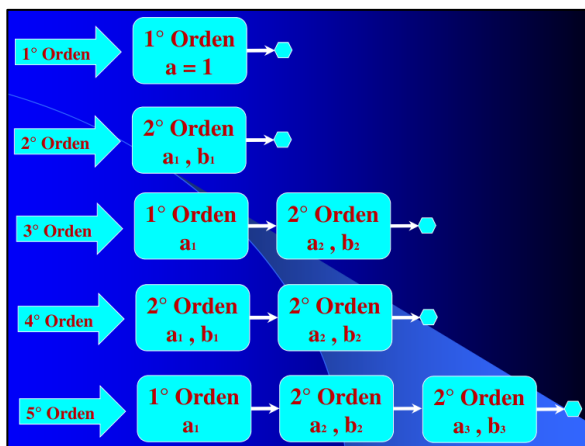
$$A(s) \Big|_{\text{Pasa-Banda}} = \frac{A_o s}{(1 + a_i s + b_i s^2)}$$

$$A(s) \Big|_{\text{Elimina-Banda}} = \frac{A_o (1 + c_i s + d_i s^2)}{(1 + a_i s + b_i s^2)}$$

$A_o \Rightarrow$  ganancia

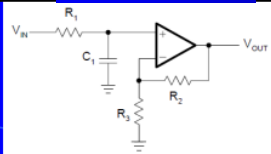
$b_i \Rightarrow \omega_o^2$

$a_i \Rightarrow \frac{\omega_o}{Q_o} \quad \text{ó} \quad Q_o = \frac{\sqrt{b_i}}{a_i}$



## PASA BAJOS 1º ORDEN

### NO INVERSOR



$$A(s) = \frac{1 + \frac{R_2}{R_3}}{1 + \omega_c R_1 C_1 s}$$

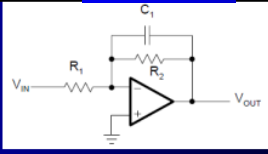
$$A_0 = 1 + \frac{R_2}{R_3}$$

$$a_1 = \omega_c R_1 C_1$$

$$R_1 = \frac{a_1}{2\pi f_c C_1}$$

$$R_2 = R_3(A_0 - 1)$$

### INVERSOR



$$A(s) = \frac{-\frac{R_2}{R_1}}{1 + \omega_c R_2 C_1 s}$$

$$A_0 = -\frac{R_2}{R_1}$$

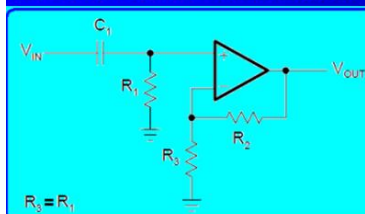
$$a_1 = \omega_c R_2 C_1$$

$$R_2 = \frac{a_1}{2\pi f_c C_1}$$

$$R_1 = -\frac{R_2}{A_0}$$

## PASA ALTOS 1º ORDEN

### PASA-ALTO NO INVERSOR

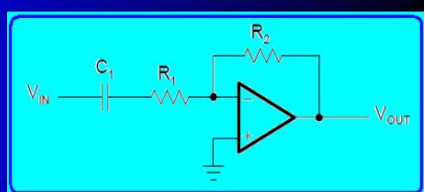


$$A(s) = \frac{1 + \frac{R_2}{R_3}}{1 + \frac{1}{\omega_c R_1 C_1} \cdot \frac{1}{s}}$$

$$A_\infty = 1 + \frac{R_2}{R_3}$$

$$R_2 = R_3(A_\infty - 1)$$

### PASA-ALTO INVERSOR



$$A(s) = -\frac{\frac{R_2}{R_1}}{1 + \frac{1}{\omega_c R_1 C_1} \cdot \frac{1}{s}}$$

$$A_\infty = -\frac{R_2}{R_1}$$

$$R_2 = -R_1 A_\infty$$

PARA AMBOS CIRCUITOS  $\rightarrow$

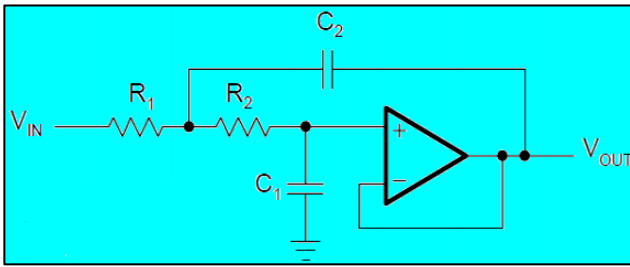
$$a_1 = \frac{1}{\omega_c R_1 C_1}$$

$$R_1 = \frac{1}{2\pi f_c a_1 C_1}$$

Para cualquier configuración, si la ganancia es unitaria, desaparecen R2 y R3.

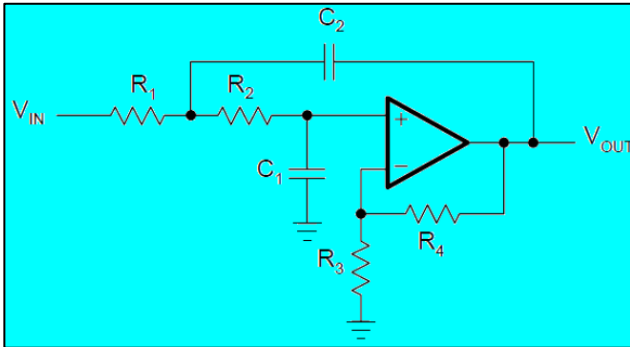


## SALLEN-KEY 2º ORDEN PASA BAJOS:



**$A_0=1$**

$$A(s) = \frac{1}{1 + \omega_c C_1 (R_1 + R_2) s + \omega_c^2 R_1 R_2 C_1 C_2 s^2}$$



**$A_0 \neq 1$**

$$A(s) = \frac{A_0}{1 + \omega_c [C_1 (R_1 + R_2) + (1 - A_0) R_1 C_2] s + \omega_c^2 R_1 R_2 C_1 C_2 s^2}$$

Método 1: Se fija  $C_1 < 100\text{pF}$ . Se calcula  $C_2$  y se toma su valor normalizado más próximo. Se calcula  $R_1$  y  $R_2$ .

$$A_0 = 1$$

$$a_1 = \omega_c C_1 (R_1 + R_2)$$

$$b_1 = \omega_c^2 R_1 R_2 C_1 C_2$$

$$R_{1,2} = \frac{a_1 C_2 \mp \sqrt{a_1^2 C_2^2 - 4b_1 C_1 C_2}}{4\pi f_c C_1 C_2}$$

$$C_2 \geq C_1 \frac{4b_1}{a_1^2}$$

Método 2: Se toma  $[R_1 = R_2 = R]$  y  $[C_1 = C_2 = C < 100\text{pF}]$

$$A(s) = \frac{A_0}{1 + \omega_c RC(3 - A_0)s + (\omega_c RC)^2 s^2}$$

$$A_0 = 1 + \frac{R_4}{R_3}$$

$$a_1 = \omega_c RC(3 - A_0)$$

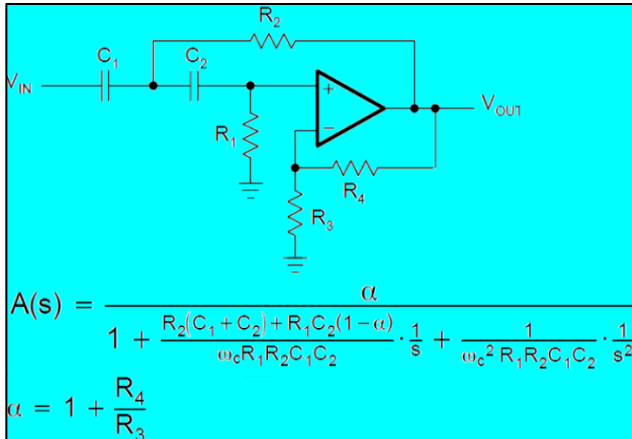
$$b_1 = (\omega_c RC)^2$$

$$R = \frac{\sqrt{b_1}}{2\pi f_c C}$$

$$Q = \frac{1}{3 - A_0} \quad A_0 = 3 - \frac{a_1}{\sqrt{b_1}}$$

## SALLEN-KEY 2º ORDEN PASA ALTOS:

Ganancia  $\neq 1$



Ganancia = 1

$$A(s) = \frac{1}{1 + \frac{2}{\omega_c R_1 C} \cdot \frac{1}{s} + \frac{1}{\omega_c^2 R_1 R_2 C^2} \cdot \frac{1}{s^2}}$$

$$A_{\infty} = 1$$

$$a_1 = \frac{2}{\omega_c R_1 C} \quad R_1 = \frac{1}{\pi f_c C a_1}$$

$$b_1 = \frac{1}{\omega_c^2 R_1 R_2 C^2} \quad R_2 = \frac{a_1}{4\pi f_c C b_1}$$

## SALLEN-KEY: cálculos de utilidad

Orden del filtro:

$$\varepsilon = \sqrt{10^{0,1 \cdot A_{\max}} - 1}$$

$$n \geq \frac{\log_{10} \left( \frac{\delta}{\varepsilon} \right)}{\log_{10} \Omega} \geq \frac{\log_{10} \left[ \sqrt{\frac{10^{(0,1 \cdot A_{\min})} - 1}{10^{(0,1 \cdot A_{\max})} - 1}} \right]}{\log_{10} \frac{\omega_s}{\omega_p}} = \frac{\log_{10} \left( \frac{10^{0,1 \cdot A_{\min}} - 1}{\varepsilon^2} \right)}{\log_{10} \left( \frac{\omega_s}{\omega_p} \right)^2}$$

Desnormalización de función de transferencia:

$$S = s \cdot \left( \frac{\varepsilon^{1/n}}{\omega_p} \right)$$

Valores normalizados de componentes:

### E-12 Resistor / Capacitor Values

1.0, 1.2, 1.5, 1.8, 2.2, 2.7, 3.3, 3.9, 4.7, 5.6, 6.8, and 8.2; multiplied by the decade value.

Normalización de componentes de un filtro S-K: ( $\omega_p=1$  rad/s |  $R_n=1 \Omega$  |  $Q_p=\sqrt{1/2}$ )

$$K = 1 \quad R1 = R2 = 1 \Omega$$

$$C_1 = \frac{2}{\omega_p} \frac{Q_p}{\omega_p} \quad C_2 = \frac{1}{2 Q_p \omega_p}$$

Desnormalización de componentes de un filtro S-K ya diseñado (datos:  $\omega_c=\omega_p$  y  $R=R_x$ )

$$R_x = R_n * R_{TABLA} \quad C_x = \frac{C_n}{\omega_p * R_x} = \frac{C_n}{2 * \pi * f_p * R_x}$$

# TABLAS DE COEFICIENTES

<i>Butterworth</i>					
n	i	a <sub>i</sub>	b <sub>i</sub>	k <sub>i</sub> = f <sub>ci</sub> / f <sub>c</sub>	Q <sub>i</sub>
1	1	1.0000	0.0000	1.000	—
2	1	1.4142	1.0000	1.000	0.71
3	1	1.0000	0.0000	1.000	—
	2	1.0000	1.0000	1.272	1.00
4	1	1.8478	1.0000	0.719	0.54
	2	0.7654	1.0000	1.390	1.31
5	1	1.0000	0.0000	1.000	—
	2	1.6180	1.0000	0.859	0.62
	3	0.6180	1.0000	1.448	1.62

<i>Tschebyscheff</i> 1-dB					
n	i	a <sub>i</sub>	b <sub>i</sub>	k <sub>i</sub> = f <sub>ci</sub> / f <sub>c</sub>	Q <sub>i</sub>
1	1	1.0000	0.0000	1.000	—
2	1	1.3022	1.5515	1.000	0.96
3	1	2.2156	0.0000	0.451	—
	2	0.5442	1.2057	1.353	2.02
4	1	2.5904	4.1301	0.540	0.78
	2	0.3039	1.1697	1.417	3.56
5	1	3.5711	0.0000	0.280	—
	2	1.1280	2.4896	0.894	1.40
	3	0.1872	1.0814	1.486	5.56

<i>Tschebyscheff</i> 2-dB					
n	i	a <sub>i</sub>	b <sub>i</sub>	k <sub>i</sub> = f <sub>ci</sub> / f <sub>c</sub>	Q <sub>i</sub>
1	1	1.0000	0.0000	1.000	—
2	1	1.1813	1.7775	1.000	1.13
3	1	2.7994	0.0000	0.357	—
	2	0.4300	1.2036	1.378	2.55
4	1	2.4025	4.9862	0.550	0.93
	2	0.2374	1.1896	1.413	4.59
5	1	4.6345	0.0000	0.216	—
	2	0.9090	2.6036	0.908	1.78
	3	0.1434	1.0750	1.493	7.23

<i>Tschebyscheff</i> 3-dB					
n	i	a <sub>i</sub>	b <sub>i</sub>	k <sub>i</sub> = f <sub>ci</sub> / f <sub>c</sub>	Q <sub>i</sub>
1	1	1.0000	0.0000	1.000	—
2	1	1.0650	1.9305	1.000	1.30
3	1	3.3496	0.0000	0.299	—
	2	0.3559	1.1923	1.396	3.07
4	1	2.1853	5.5339	0.557	1.08
	2	0.1964	1.2009	1.410	5.58
5	1	5.6334	0.0000	0.178	—
	2	0.7620	2.6530	0.917	2.14
	3	0.1172	1.0686	1.500	8.82

<i>Tschebyscheff</i> 0.5-dB					
n	i	a <sub>i</sub>	b <sub>i</sub>	k <sub>i</sub> = f <sub>ci</sub> / f <sub>c</sub>	Q <sub>i</sub>
1	1	1.0000	0.0000	1.000	—
2	1	1.3614	1.3827	1.000	0.86
3	1	1.8636	0.0000	0.537	—
	2	0.0640	1.1931	1.335	1.71
4	1	2.6282	3.4341	0.538	0.71
	2	0.3648	1.1509	1.419	2.94
5	1	2.9235	0.0000	0.342	—
	2	1.3025	2.3534	0.881	1.18
	3	0.2290	1.0833	1.480	4.54

<i>Bessel</i>					
n	i	a <sub>i</sub>	b <sub>i</sub>	k <sub>i</sub> = f <sub>ci</sub> / f <sub>c</sub>	Q <sub>i</sub>
1	1	1.0000	0.0000	1.000	—
2	1	1.3617	0.6180	1.000	0.58
3	1	0.7560	0.0000	1.323	—
	2	0.9996	0.4772	1.414	0.69
4	1	1.3397	0.4889	0.978	0.52
	2	0.7743	0.3890	1.797	0.81
5	1	0.6656	0.0000	1.502	—
	2	1.1402	0.4128	1.184	0.56
	3	0.6216	0.3245	2.138	0.92