Tabla de propiedades de la Transformada de Laplace

Dominio del tiempo, $x(t)$	Dominio de la variable $s, X(s)$	ROC
$\frac{ax_1(t) + bx_2(t)}{ax_1(t) + bx_2(t)}$	$\frac{aX_1(s) + bX_2(s)}{aX_1(s) + bX_2(s)}$	$R' = R_1 \cap R_2$
$x(t-t_0)$	$e^{-st_0}X(s)$	R' = R
$e^{s_0t}x(t)$	$X(s-s_0)$	$R' = R + \Re\{s_0\}$
x(at)	$\frac{1}{ a }X\left(\frac{s}{a}\right)$	R' = aR
x(-t)	X(-s)	R' = -R
$\frac{\mathrm{d}x(t)}{\mathrm{d}t}$	$sX\left(s\right) -x(0^{-})$	$R'\supset R$
$-tx\left(t\right)$	$\frac{\mathrm{d}X(s)}{\mathrm{d}s}$	$R'\supset R$
$\int_{-\infty}^{t} x(\tau) \mathrm{d}\tau$	$\frac{X(s)}{s}$	$R'=R\cap\{\mathbb{R}\{s\}>0\}$
$\frac{x(t)}{t}$	$\int\limits_{s}^{\infty}X(s)\mathrm{d}s$	$R' = R \cap \{\mathbb{R}\{s\} > 0\}$
$x_1(t) * x_2(t)$	$X_1(s) \cdot X_2(s)$	$R'\supset R_1\cap R_2$

Tabla 1. Propiedades de la Transformada de Laplace

Tabla de Transformadas de Laplace

$$f(t)$$
 $\mathcal{L}[f(t)] = F(s)$ $f(t)$ $\mathcal{L}[f(t)] = F(s)$

1
$$\frac{1}{s}$$
 (1) $e^{at}\sin kt$ $\frac{k}{(s-a)^2 + k^2}$ (15)

$$u(t-a)$$
 $\frac{e^{-as}}{s}$ (2) $e^{at}\cos kt$ $\frac{s-a}{(s-a)^2+k^2}$ (16)

$$\delta(t) \qquad 1 \qquad (3) \qquad e^{at} \sinh kt \qquad \frac{k}{(s-a)^2 - k^2} \qquad (17)$$

$$t^{n} (n = 0, 1, 2, ...) \frac{n!}{s^{n+1}}$$
 (4)
$$e^{at} \cosh kt \qquad \frac{s - a}{(s - a)^{2} - k^{2}}$$
 (18)

$$t^{x} (x \ge -1 \in \mathbb{R}) \qquad \frac{\Gamma(x+1)}{s^{x+1}} \tag{5}$$

$$t \sin kt \qquad \frac{2ks}{(s^{2}+k^{2})^{2}} \tag{19}$$

$$\frac{k}{s^2 + k^2} \tag{6}$$

$$t \cos kt$$

$$\frac{k}{s^2 + k^2} \tag{20}$$

$$\cos kt$$
 $\frac{s}{s^2 + k^2}$
 $t \cos kt$
 $\frac{s}{(s^2 + k^2)^2}$
(20)

$$e^{at} \qquad \frac{1}{s-a} \qquad (8) \qquad t \sinh kt \qquad \frac{2ks}{(s^2-k^2)^2} \qquad (21)$$

$$\frac{k}{s^2 - k^2}$$
(9) $t \cosh kt$ $\frac{s^2 + k^2}{(s^2 - k^2)^2}$ (22)

$$\frac{s}{s^2 - k^2} \qquad (10) \quad \frac{\sin at}{t} \qquad \arctan \frac{a}{s} \qquad (23)$$

$$\frac{e^{at} - e^{bt}}{a - b} \qquad \frac{1}{(s - a)(s - b)} \qquad (11) \quad \frac{1}{\sqrt{\pi t}} e^{-a^2/4t} \qquad \frac{e^{-a\sqrt{s}}}{\sqrt{s}}$$
 (24)

$$\frac{ae^{at} - be^{bt}}{a - b} \qquad \frac{s}{(s - a)(s - b)} \qquad (12) \quad \frac{a}{2\sqrt{\pi t^3}}e^{-a^2/4t} \qquad e^{-a\sqrt{s}}$$

$$te^{at}$$

$$\frac{1}{(s-a)^2}$$
 (13) $\operatorname{erfc}\left(\frac{a}{2\sqrt{t}}\right)$
$$\frac{e^{-a\sqrt{s}}}{s}$$
 (26)

$$t^n e^{at} \qquad \frac{n!}{(s-a)^{n+1}} \tag{14}$$