

Transformers for Time Series Forecasting

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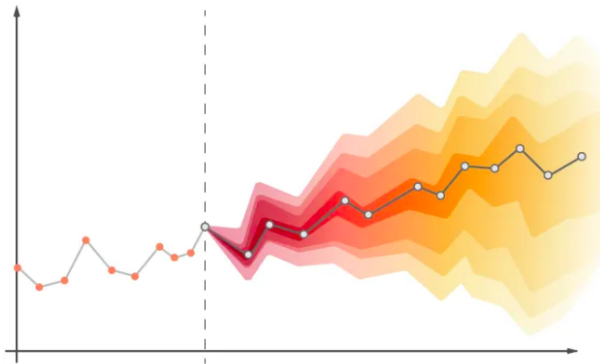


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1. The TSF Problem

Time series forecasting (TSF) is the task of predicting future values of a given sequence based on previously observed values.



The TSF problem may be essentially identified by the following aspects:

- ▶ **Prediction objective:** point forecasting vs probabilistic forecasting
- ▶ **Forecast horizon:** short-term vs long-term forecasting
- ▶ **Input-Output dimension:** univariate vs multivariate forecasting
- ▶ **Forecasting task:** single-step vs multi-step forecasting

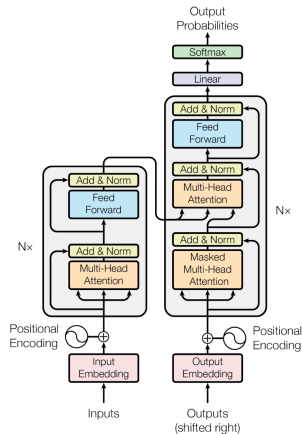
The TSF problem is usually faced with statistical models (ARIMA, ETS) or deep learning models (RNN, LSTM).

The main challenges of the TSF problem are:

- ▶ **uncertainty** increases as the forecast horizon increases
- ▶ difficulty in capturing **multiple complex patterns** over time
- ▶ difficulty in capturing **long-term dependencies** (critical for long-term forecasting)
- ▶ difficulty to handle **long input sequences**

2. Vanilla Transformer

- ▶ Based on Encoder-Decoder architecture
- ▶ Uses self-attention mechanism to access any part of the sequence history
- ▶ Positional encoding allows to account for element positions
- ▶ Residual connections and layer normalization help to stabilize the learning process
- ▶ Each encoder and decoder layer is composed of a self-attention layer and a feed-forward layer



Can vanilla Transformers be used for TSF?

The TSF problem can be seen as a sequence learning problem such as machine translation.

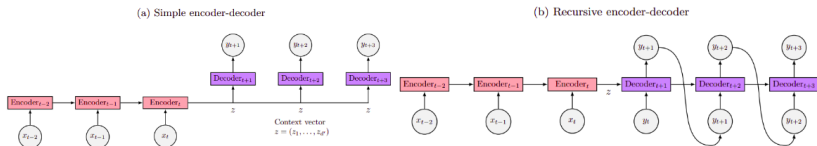
Main ingredients allowing to use vanilla Transformers for TSF:

- ▶ **Multi-head Self-attention** mechanism allows to access any part of the sequence history, capturing both short-term and long-term dependencies (but it is invariant to the order of elements in a sequence)
- ▶ **Positional encoding** allows to account for the sequence ordering
- ▶ **Masked self-attention** allows to avoid information leakage from future

Can vanilla Transformers be used for TSF?

Just few changes are needed to adapt Transformers to TSF:

- ▶ **Remove the final activation** function (softmax) from the output layer and set the dimension of the linear layer equal to the forecasting horizon
- ▶ **Adapt the structure** to the desired forecasting task (single-step or multi-step)



Problems with vanilla Transformers

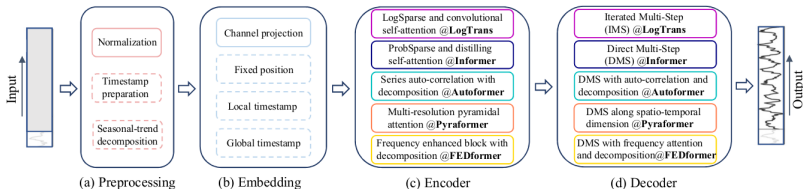
- ▶ **Locally agnostic:** the attention mechanism matches queries and keys without considering their local context being prone to temporal anomalies
- ▶ **Positional encoding:** only the order in which two elements occur is taken into account, but their temporal distance is not
- ▶ **Computational complexity:** given a sequence of length L , the time and memory burden is $O(L^2)$, making it difficult to learn patterns in long time series
- ▶ **Simple Architecture:** the architecture does not include any component of typical importance in TSF (e.g. autocorrelation, decomposition, recurrent layers, etc.)

3. TSF Transformers

Classification

Transformers are **very appealing for long-term TSF** due to their ability to learn long-range dependencies.

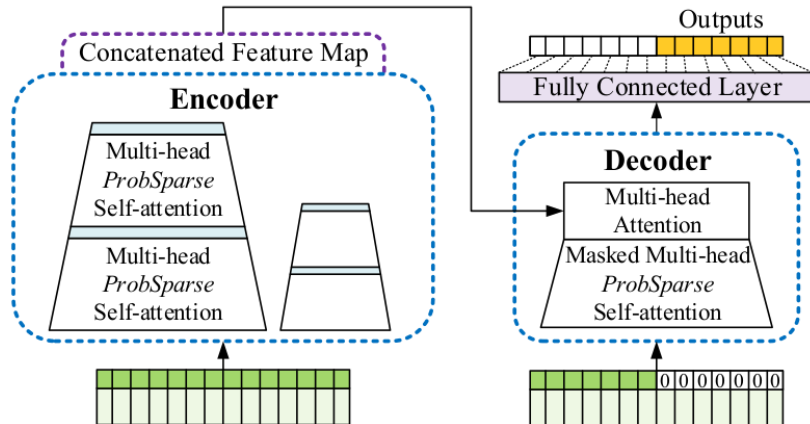
Many solutions have been proposed to adapt Transformers to TSF, mainly in the direction to improve the encoding, adopt more efficient attention and expand the architecture.



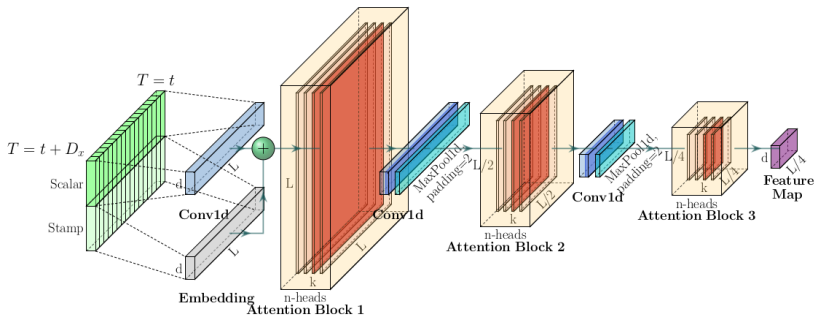
Informer

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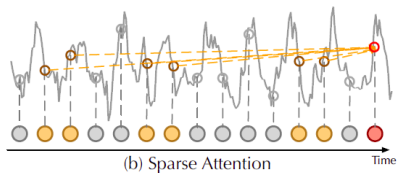
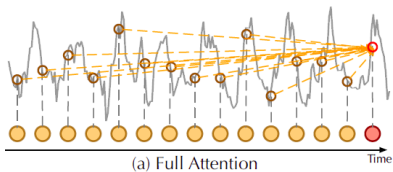
Informer - Architecture



Informer - Causal Convolution Layers



Informer - ProbSparse Attention

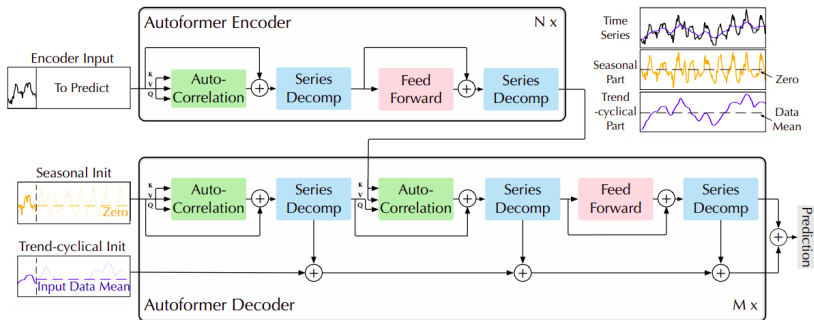


Autoformer

Autoformer builds upon two traditional time series analysis methods:

- ▶ **Decomposition Layer**, which allows to decompose the time series into seasonality and trend-cycle components, enhancing the model's ability to capture these components accurately
- ▶ **Attention (Autocorrelation) Mechanism**, which replaces the standard self-attention used in the vanilla transformer with an autocorrelation mechanism, allowing to capture the temporal dependencies in the frequency domain

Autoformer - Architecture



Autoformer - Decomposition Layer

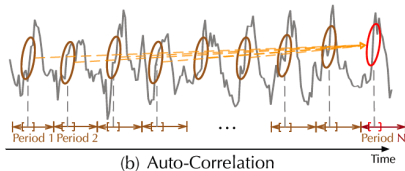
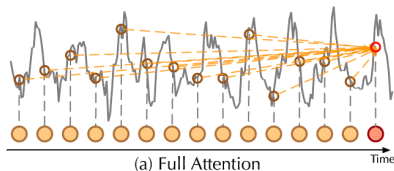
Autoformer incorporates **decomposition blocks** as an inner operation of the model.

Encoder and decoder use decomposition blocks to extract and aggregate the trend-cyclical and seasonal parts from the series progressively.

For an input series X_t with length L , the decomposition layer returns X_{trend} and $X_{seasonal}$, both of length L .

Autoformer - Attention Mechanism

Autoformer uses **autocorrelation within the self-attention** mechanism, extracting frequency-based dependencies from queries and keys (instead of the standard dot-product).



In practice, autocorrelation of the queries and keys for all lags is calculated at once by Fast Fourier Transform, so to achieve $O(L \log L)$ time complexity (similar to Informer's ProbSparse attention).

4. Conclusions

Conclusions



Bibliografy

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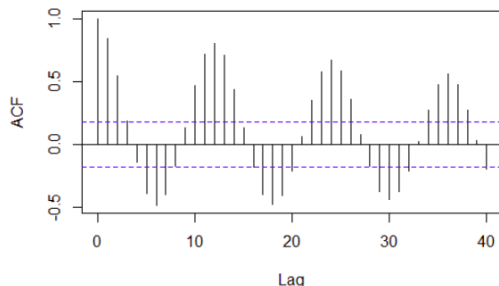
Thank you!

Appendix

Autocorrelation

In theory, given a time lag k , autocorrelation for a single discrete variable Y is used to measure the “relationship” (pearson correlation) between the variable’s current value at time t to its past value at time $t - k$.

$$\text{Autocorrelation}(k) = \text{Corr}(Y_t, Y_{t-k})$$



Time Series Decomposition

In time series analysis, decomposition is a method of breaking down a time series into three systematic components: trend-cycle, seasonal variation, and random fluctuations.

