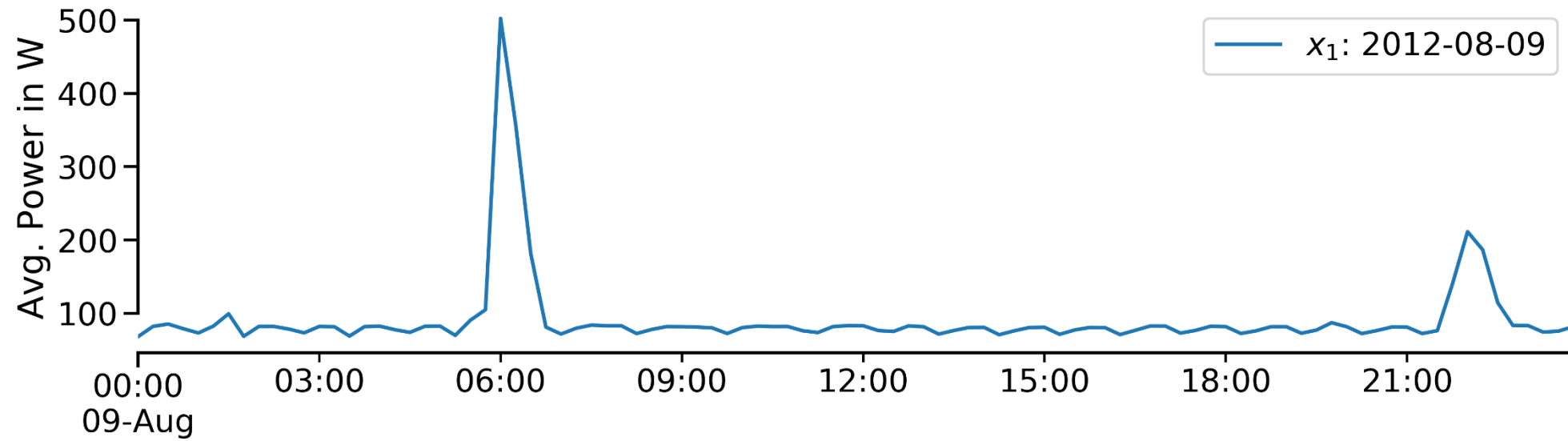




# Permutation-Based Residential Short-term Load Forecasting in the Context of Energy Management Optimization Objectives

Marcus Voß, Technische Universität Berlin (DAI-Labor)

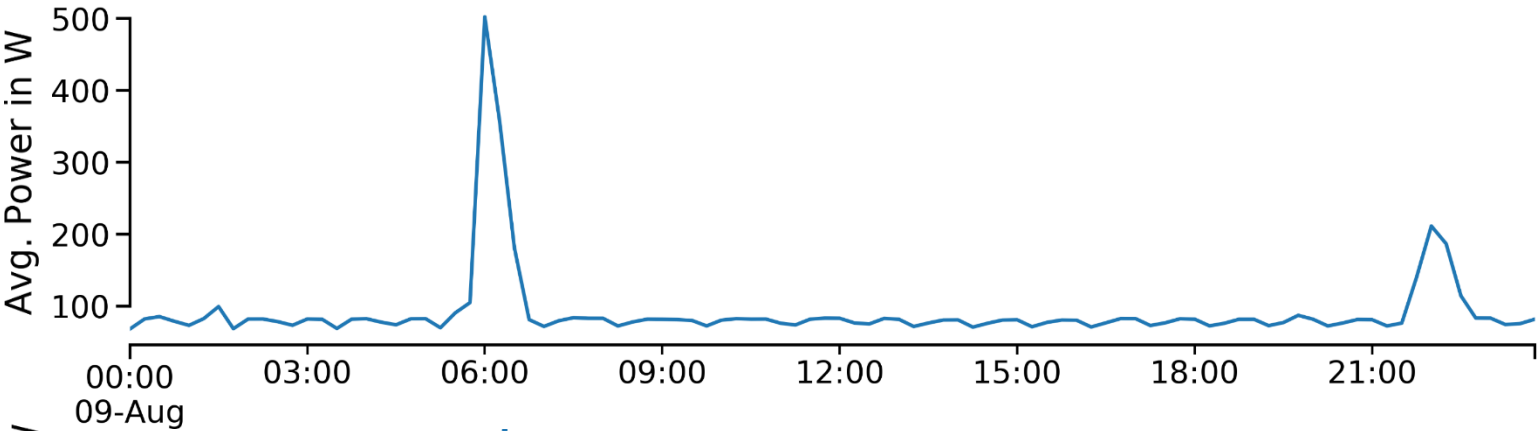
## A household-level electric load profile in 15-minute resolution



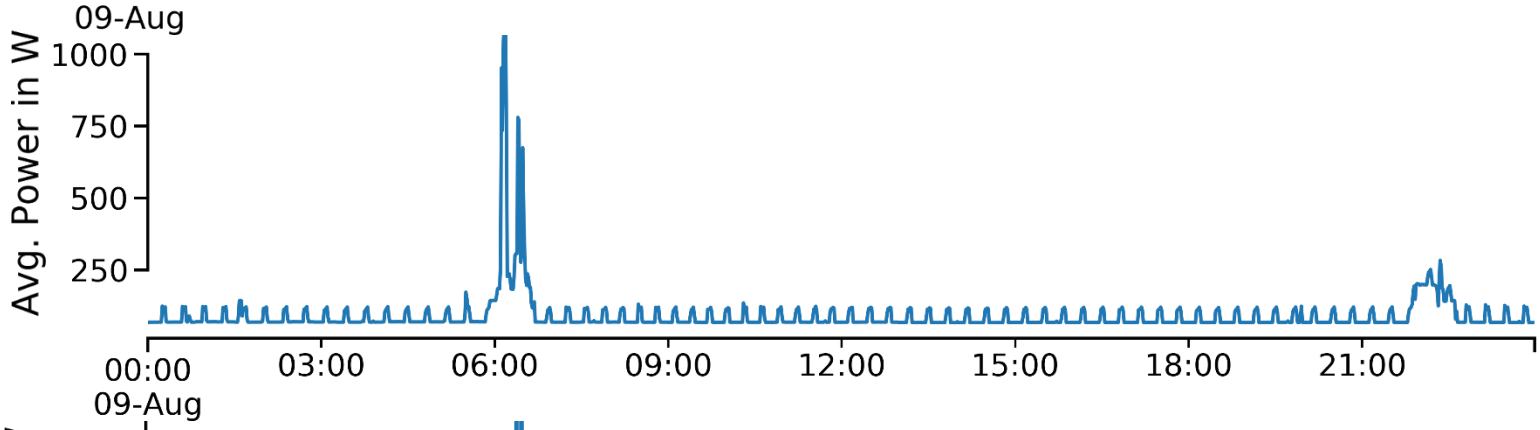
# A household-level electric load profile in higher resolutions



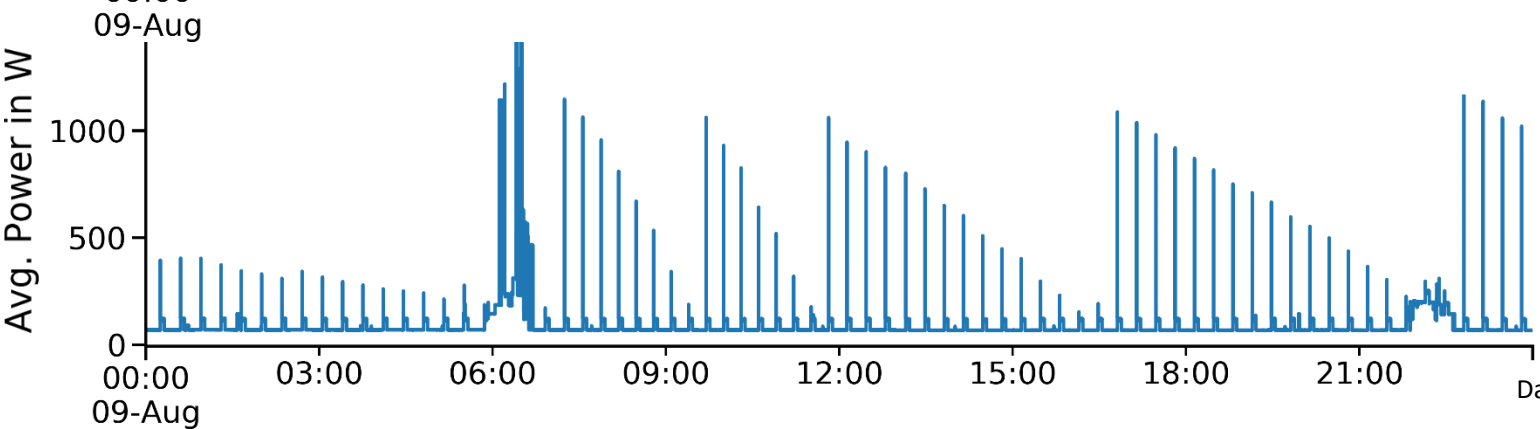
15-minute  
resolution



1-minute  
resolution



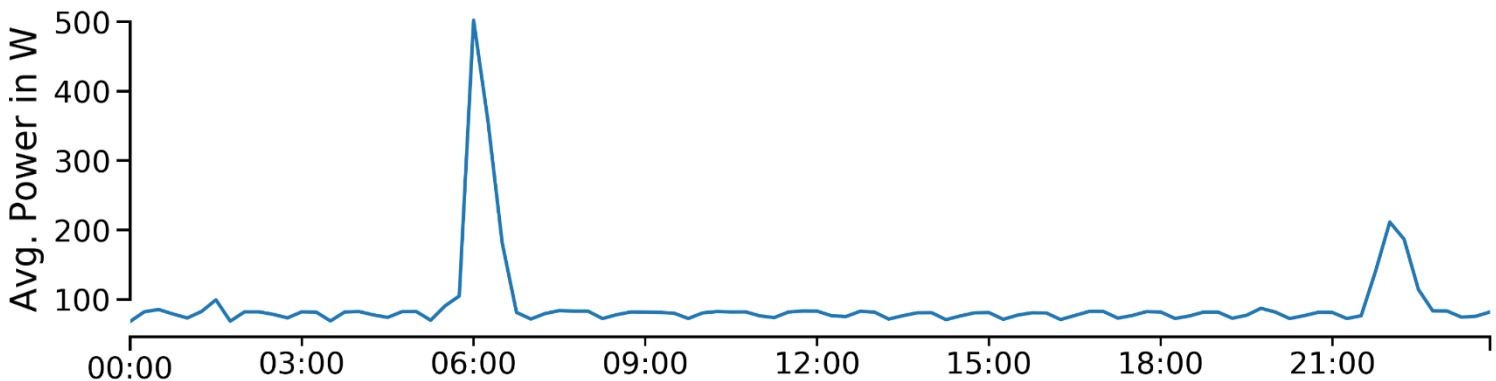
1-second  
resolution



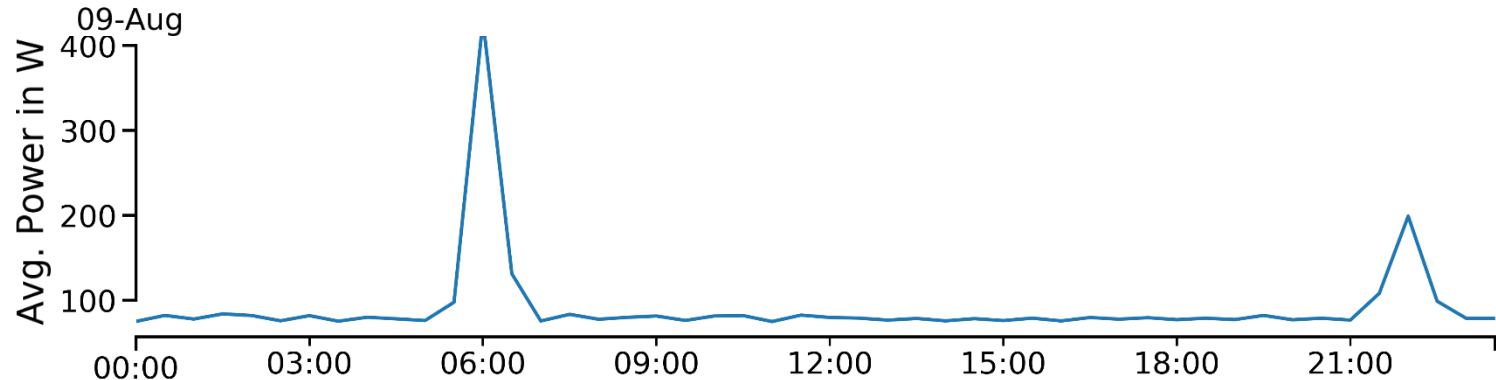
# A household-level electric load profile in lower resolutions



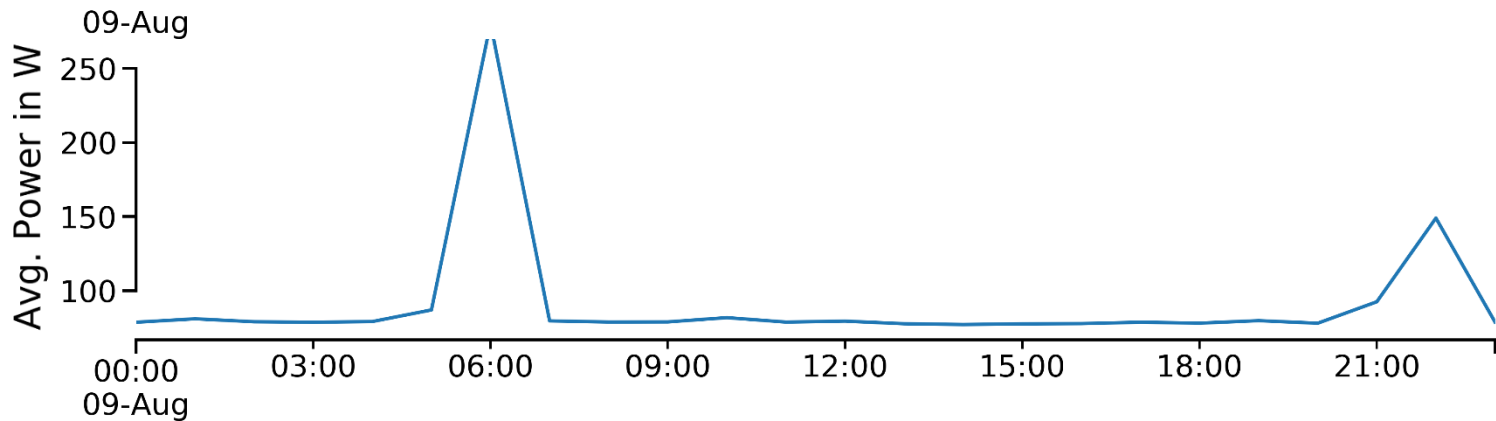
15-minute  
resolution



30-minute  
resolution



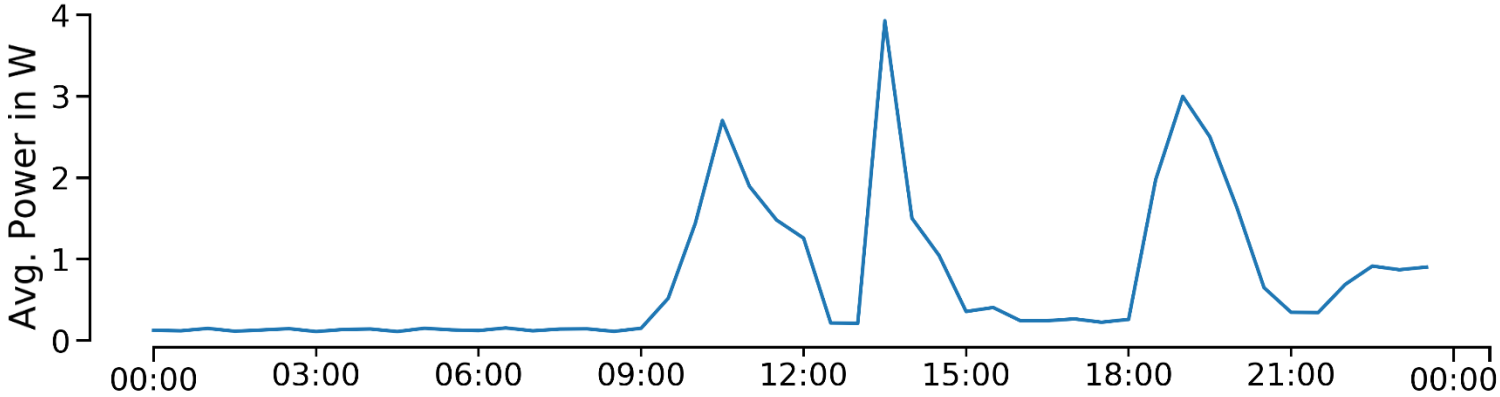
60-minute  
resolution



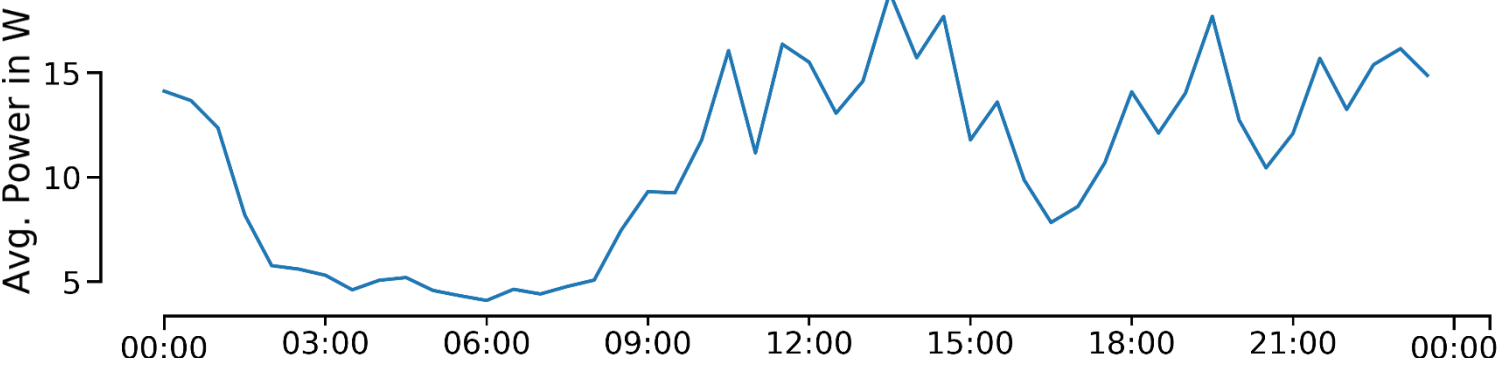
# A household-level electric load profile in higher aggregations



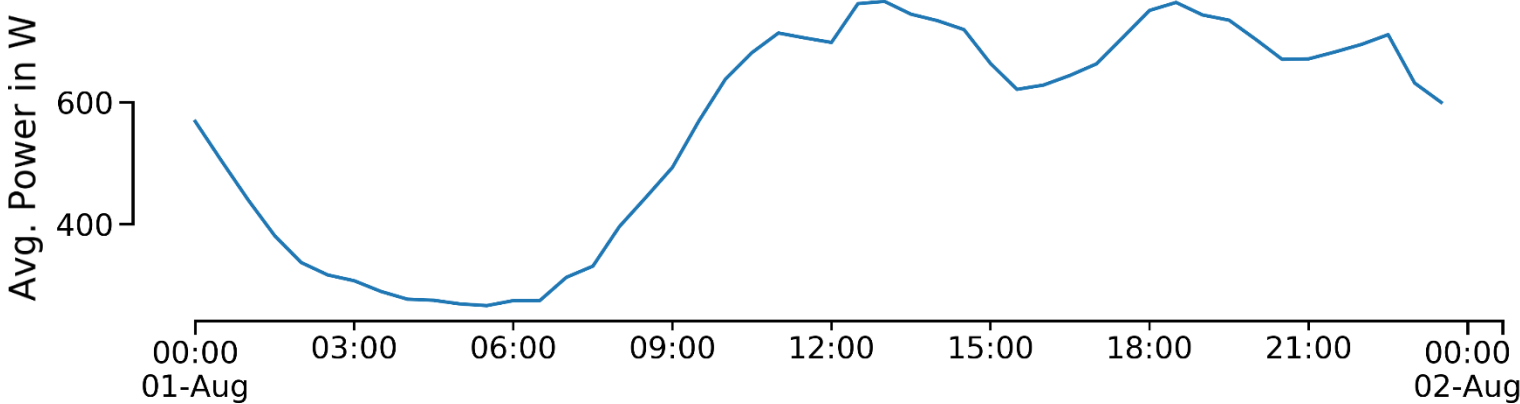
1 household



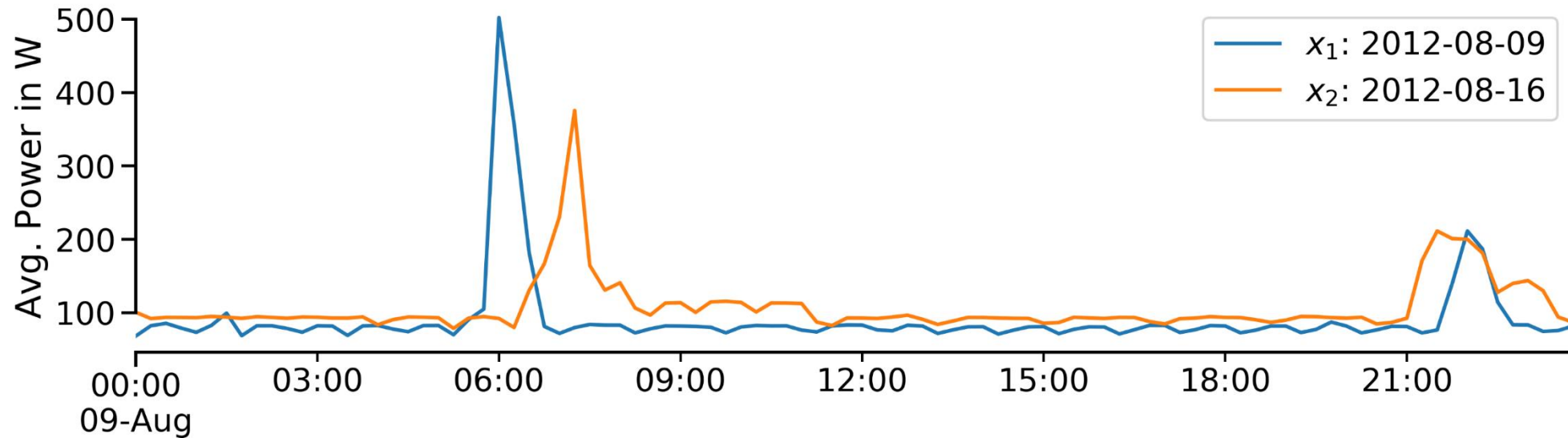
20 households



1000 households



## When are two load profiles similar?



Euclidean distance:

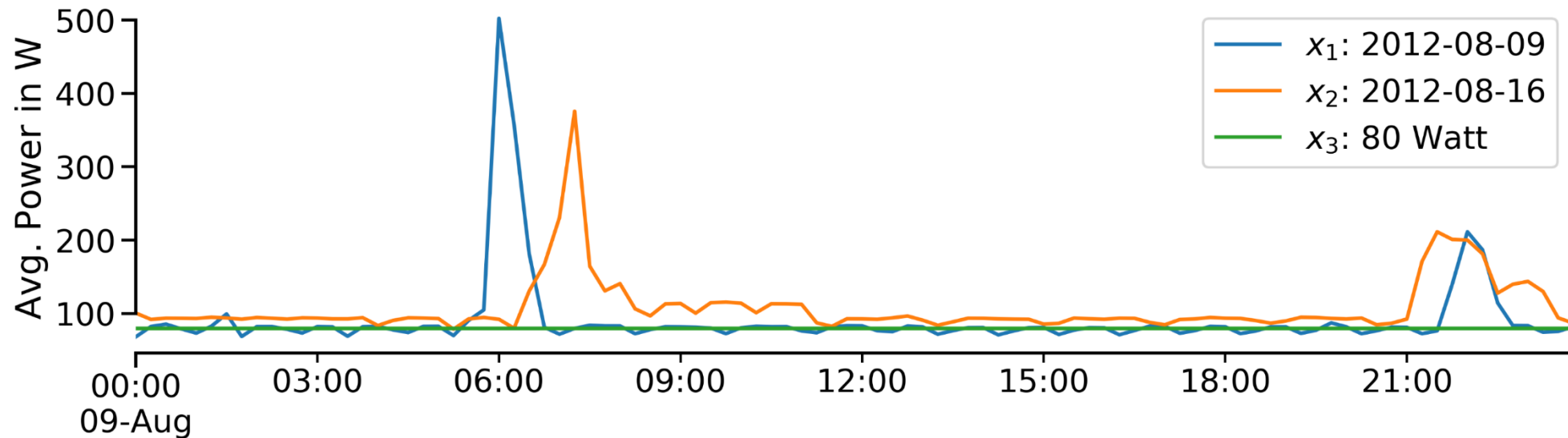
$$d(\mathbf{f}, \mathbf{x}) = \|\mathbf{f} - \mathbf{x}\|_2 = \sqrt{\sum_{i=1}^n (f_i - x_i)^2}$$

Forecast Error:

$$RMSE = \sqrt{\frac{\sum_{i=1}^n (f_i - x_i)^2}{n}}$$

$d(\mathbf{x}_1, \mathbf{x}_2)$ : 668,7 W

## When are two load profiles similar?



Euclidean distance:

$$d(\mathbf{f}, \mathbf{x}) = \|\mathbf{f} - \mathbf{x}\|_2 = \sqrt{\sum_{i=1}^n (f_i - x_i)^2}$$

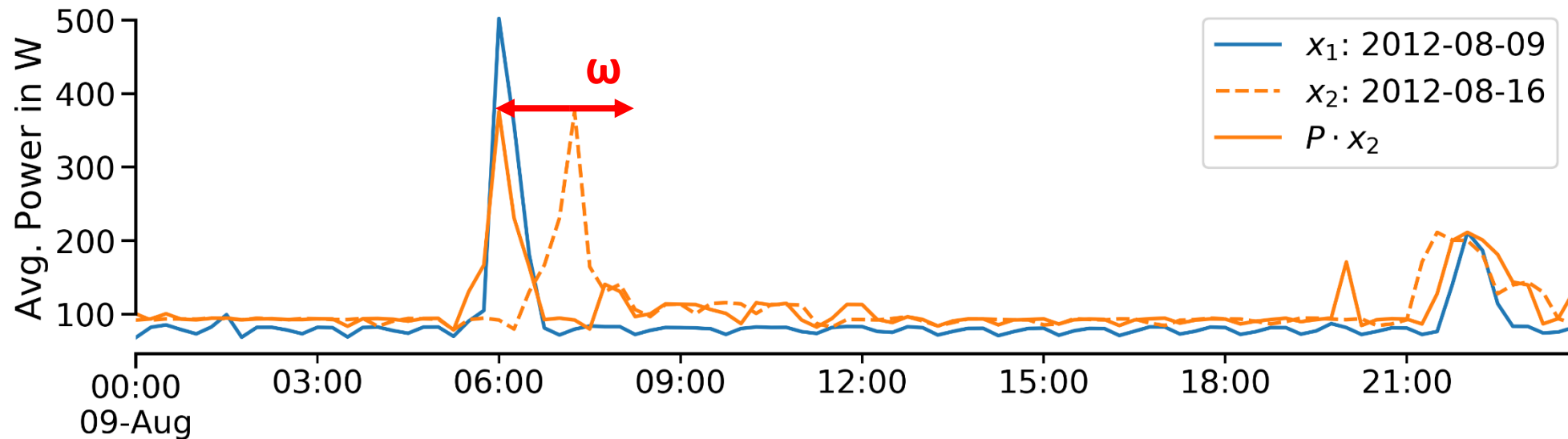
Forecast Error:

$$RMSE = \sqrt{\frac{\sum_{i=1}^n (f_i - x_i)^2}{n}}$$

$d(\mathbf{x}_1, \mathbf{x}_2)$ : 668,7 W

$d(\mathbf{x}_2, \mathbf{x}_3)$ : 549,6 W

## When are two load profiles similar?



LPI-Distance (based on Adjusted Error of [Haben2014]):

$$LPI(\mathbf{f}, \mathbf{x}; \omega) = \min_{P \in \mathcal{L}_n^\omega} \|P\mathbf{f} - \mathbf{x}\|_2$$

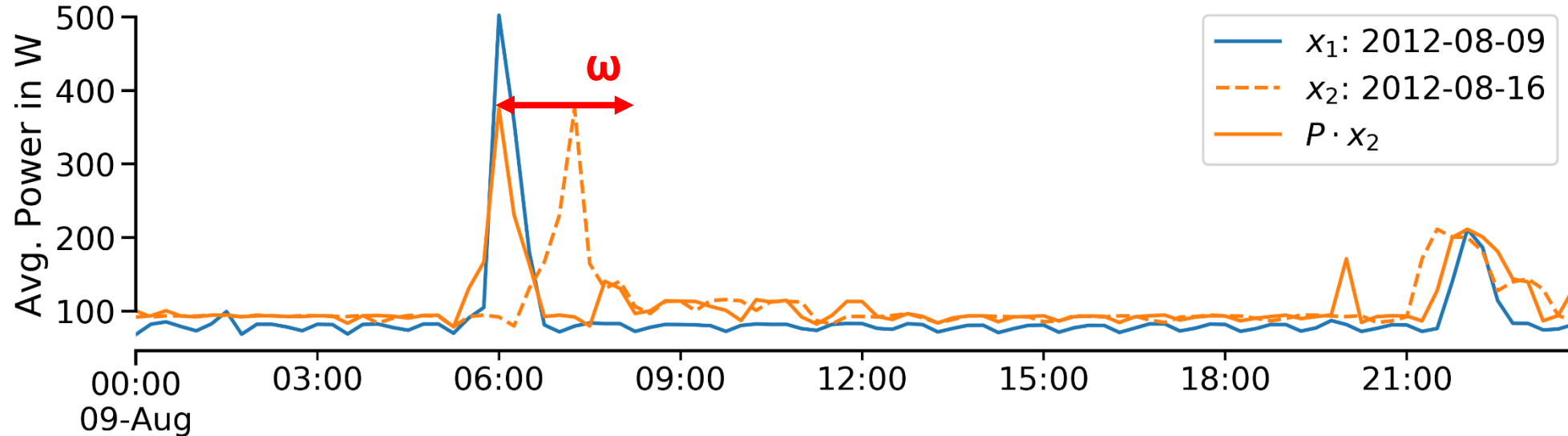
Forecast Error

$$\varepsilon_\omega = \frac{1}{\sqrt{n}} LPI(\mathbf{y}, \mathbf{x}; \omega)$$

$\omega$  Bandwidth parameter.  
 $\mathcal{L}_n^\omega$  Set of by  $\omega$  restricted permutation matrices of size  $n$ .  
 $P$  p-norm minimizing permutation matrix.



When are two load profiles similar?



$d(x_1, x_2)$ : 668,7 W

$d(x_2, x_3)$ : 549,6 W

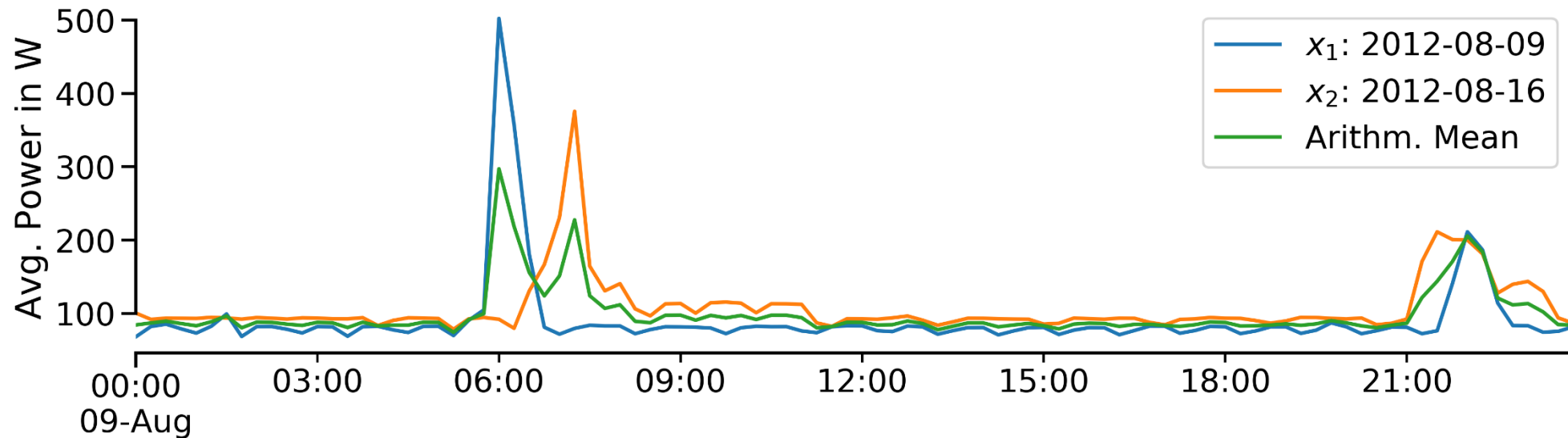


$LPI(x_1, x_2; \omega=5)$ : 308,3 W

$LPI(x_2, x_3; \omega=5)$ : 549,6 W

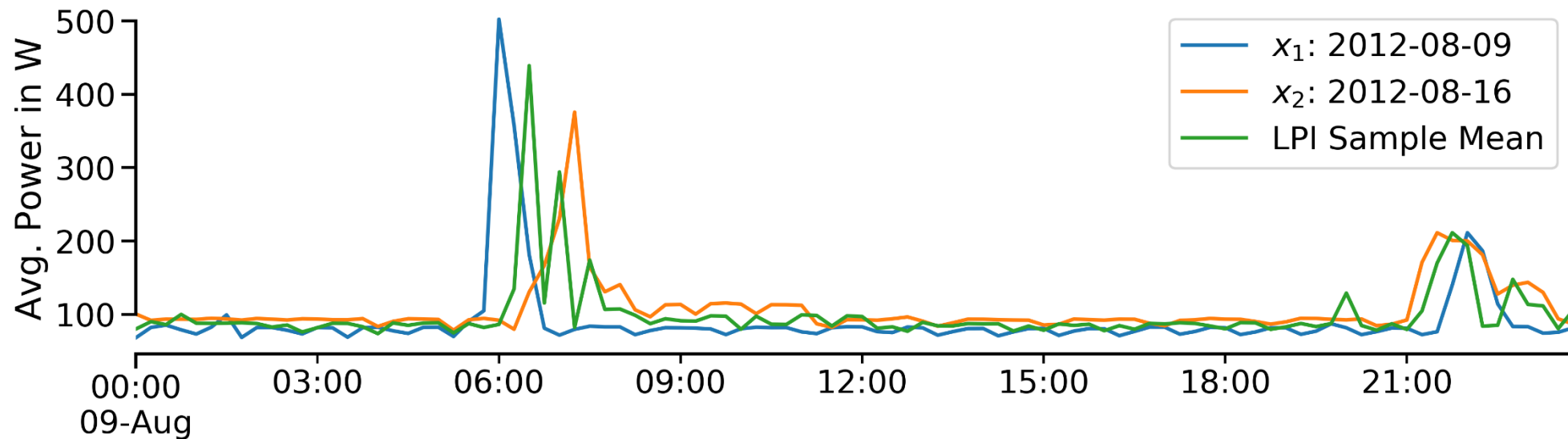
## What is a good average of household load profiles?

- ▶ The sample mean  $\bar{x}$  of a set of  $n$  profiles is a profile with minimal distance to each of the profiles.
- ▶ The arithmetic mean minimizes the Euclidean distance.

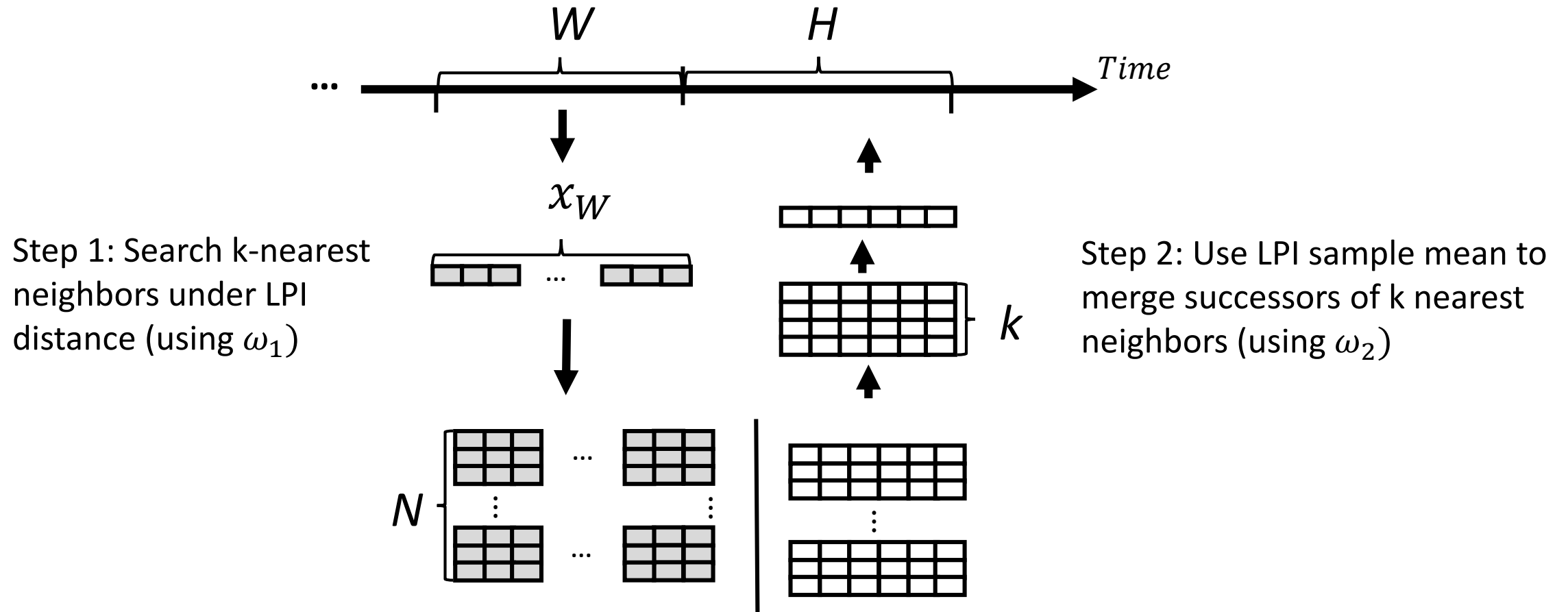


## What is a good average of household load profiles?

The LPI mean is the a sample mean under the Local Permutation Invariant (LPI) distance.

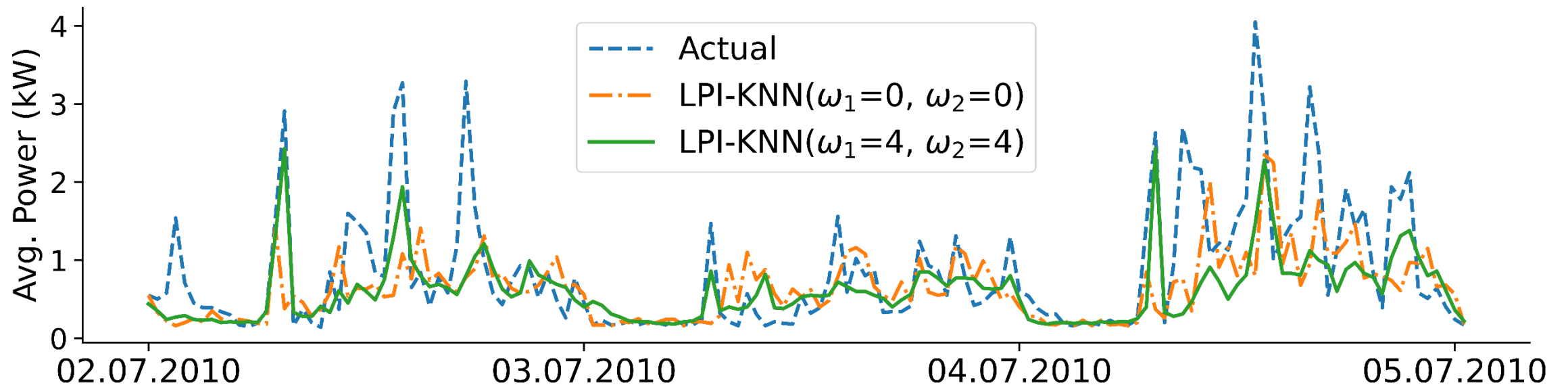


## Adjusted kNN – Load forecasting for lowly-aggregated load



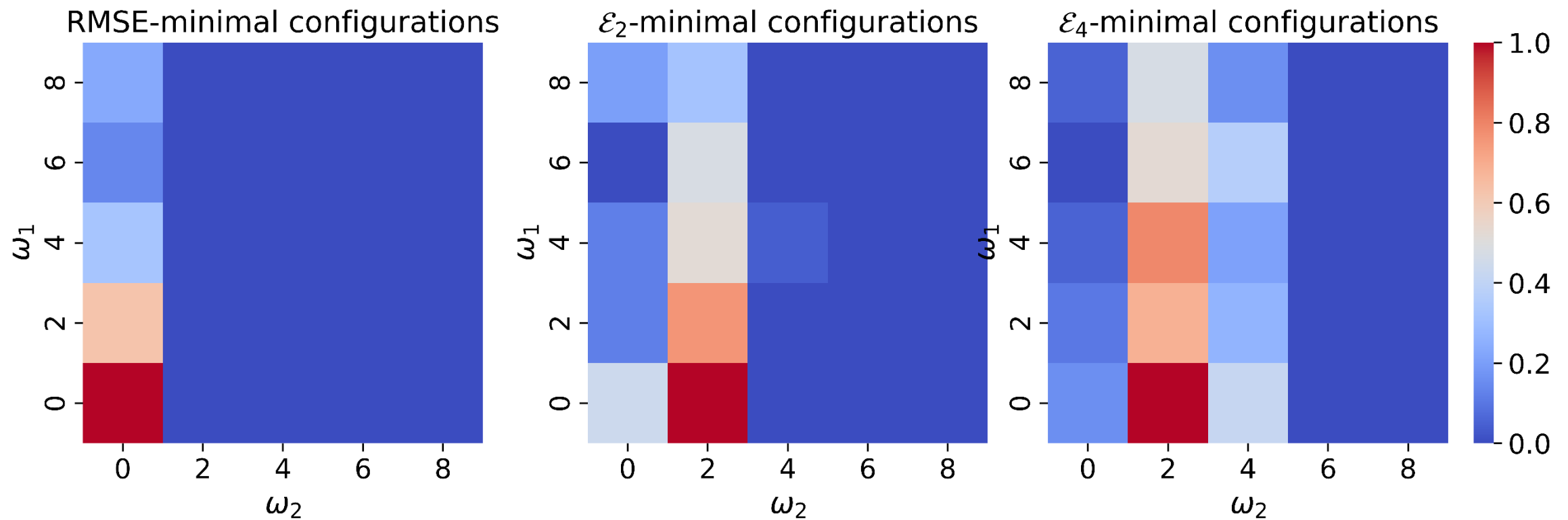
## Comparison of forecasts by RMSE-minimizing KNN and $\mathcal{E}_5$ minimizing LPI-KNN

Example traces of a household from the CER dataset [CER2012].



## Comparison of configurations of RMSE-minimizing KNN and $\mathcal{E}_5$ minimizing LPI-KNN

Distribution of the best configurations for the 100 households of the CER dataset [CER2012].



## How to establish ground truth in load forecasting?

Objective 1 Minimize Cost:

$$O_{Cost}: \min \sum_{t=1}^H c_{Utility}(t) \cdot P_{Utility}(t) \cdot \tau - p_{Feedin}(t) \cdot P_{Feedin}(t) \cdot \tau$$

Objective 2 Max. Autarky:

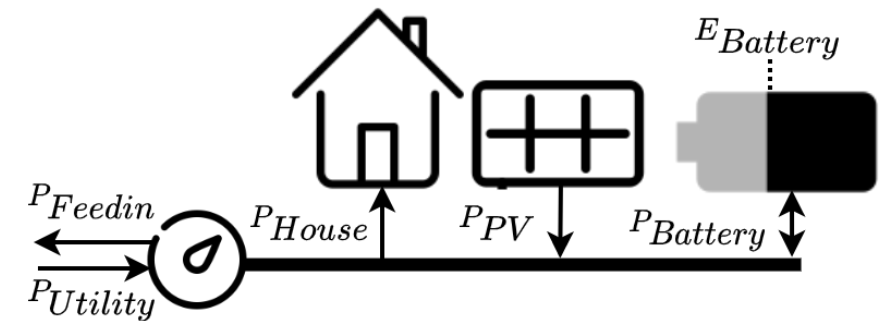
$$O_{Autarky}: \min \sum_{t=1}^H P_{Utility}(t)$$

Objective 3 Min. Peak

$$O_{Peak}: \min \sum_{t=1}^H \varepsilon$$

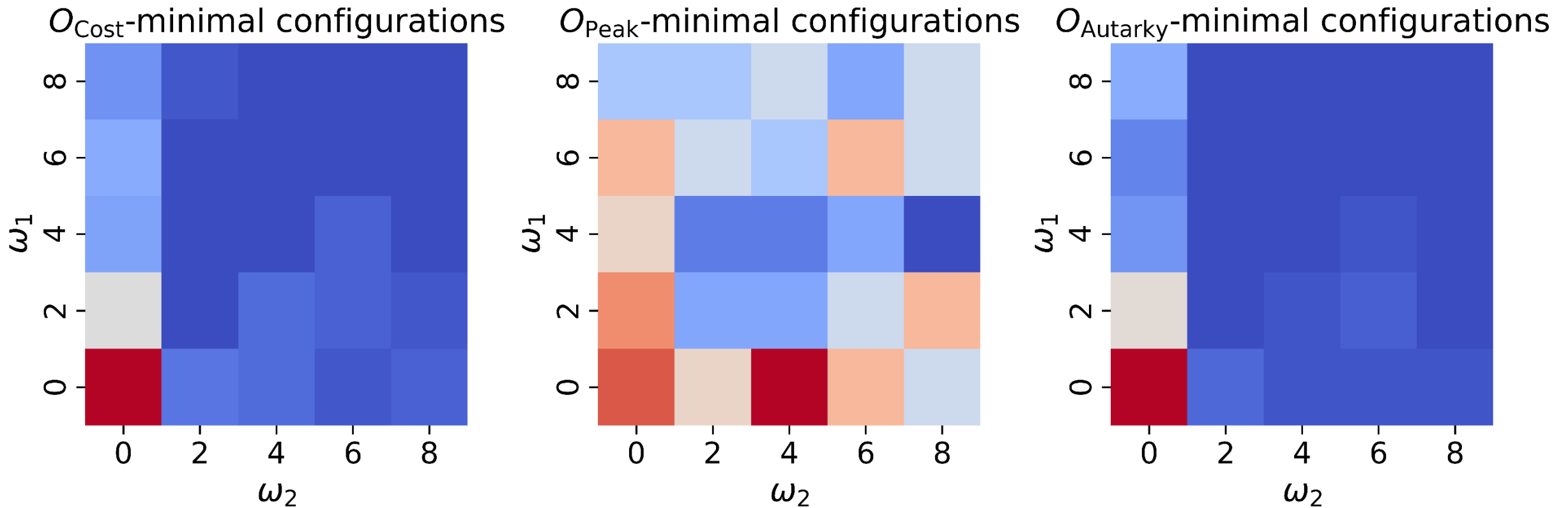
$$s. t. \quad \varepsilon \geq P_{Utility}(t) - P_{Bill}$$

$\varepsilon$  is the amount that the peak demand within the horizon  $H$  is expected to exceed the highest peak of the current billing period  $P_{Bill}$ .



## Comparison of configurations of respective objective-minimizing KNN

Distribution of the best configurations for the 100 households of the CER dataset [CER2012].



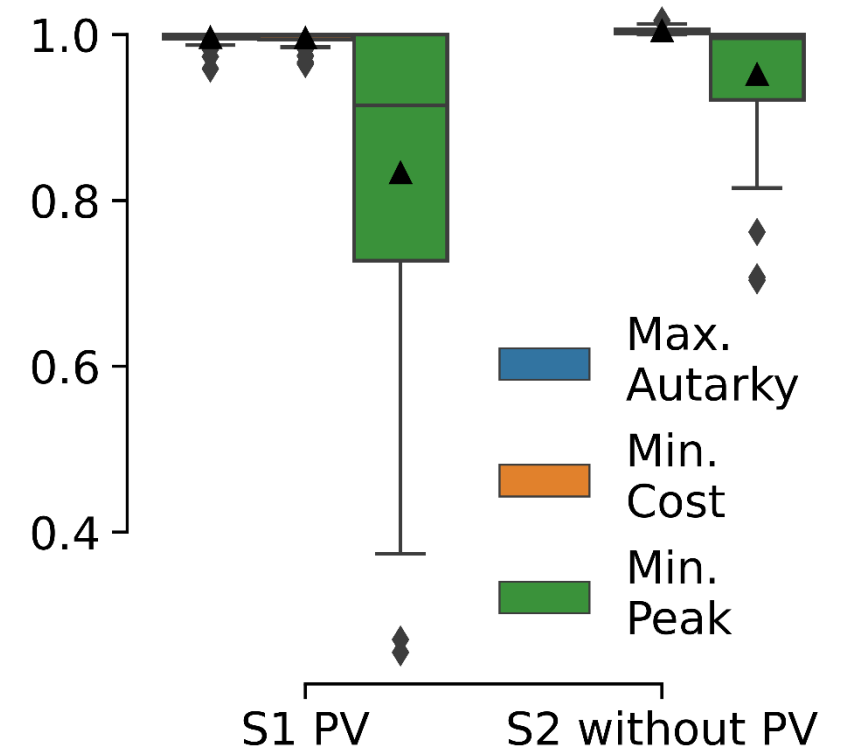


## Conclusion

- ▶ Low aggregated load profiles at high resolutions and low aggregations are intermittent and have few structure to be exploited by data mining.
- ▶ The LPI distance and adjusted error measure can be alternatives to the standard Euclidean distance and RMSE for comparing low-voltage load profiles.
- ▶ We showed how this can be done by establishing a *ground truth*, by considering the forecast error in the context of the energy management optimization goal (here: minimum cost, minimum long-term peak load, maximum autarky).
- ▶ Peak reduction by average of 22.5% using optimal configuration over RMSE-minimizing forecasting model.

### Current Work/Future Work:

- ▶ Analyze the choice of distances for clustering and other data analytics tasks on smart meter data.
- ▶ Compare the LPI distance (adjusted error) more thoroughly to DTW.
- ▶ Standard LAP scales in  $O(n^3)$  and the choice of the implementation makes a big different. Currently, I develop a heuristic with good accuracy on minute resolution.





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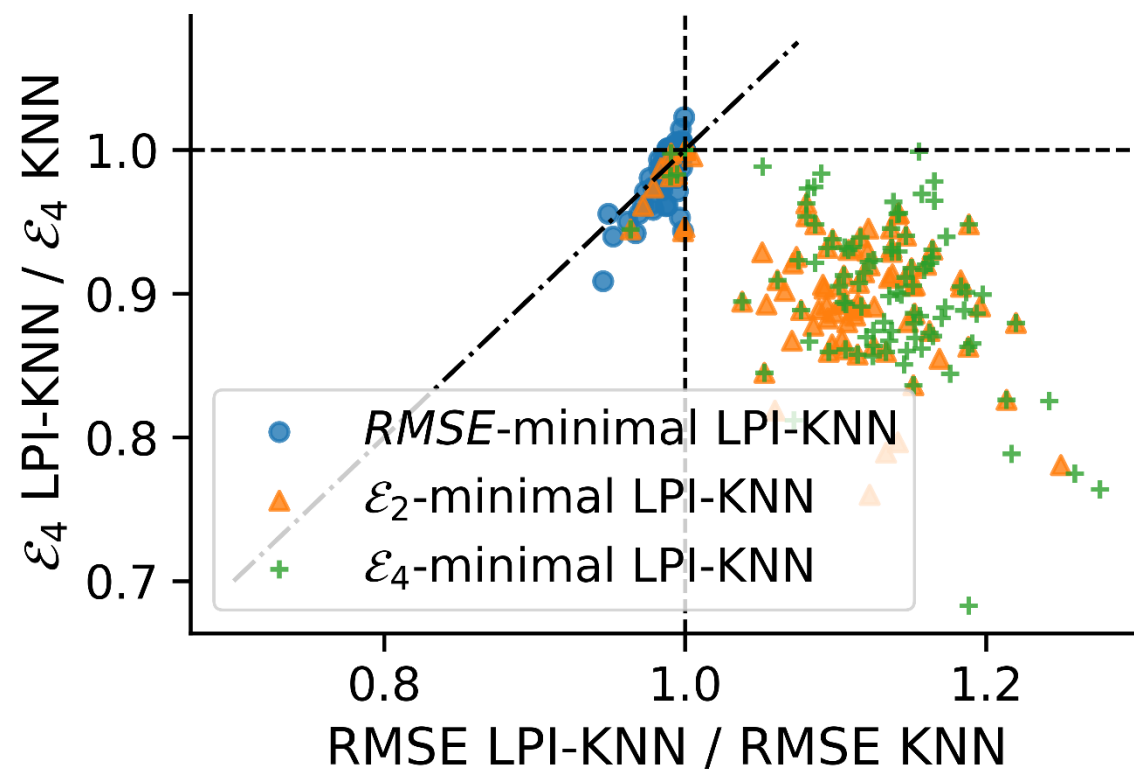
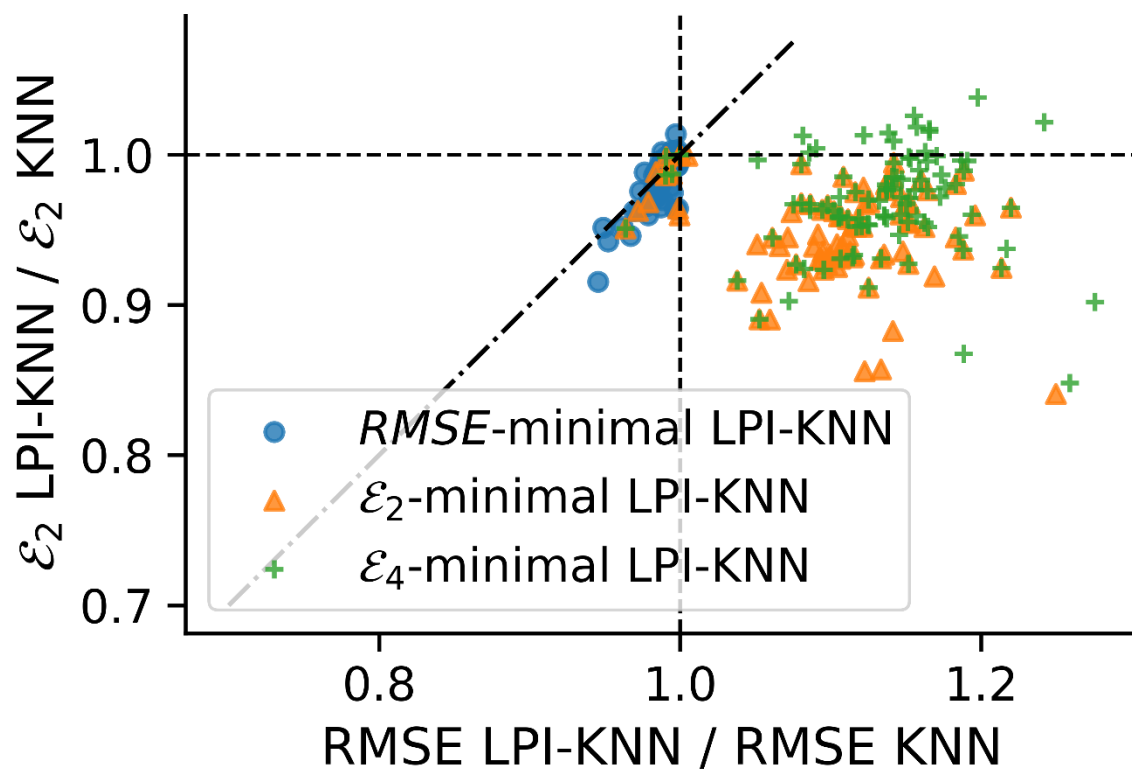
Marcus Voß



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## Comparison of forecasts by RMSE-minimizing KNN and $\mathcal{E}_5$ minimizing LPI-KNN

Results for 100 households of the CER dataset [CER2012].



## Comparison of forecasts by respective objective-minimizing KNN

Results for 100 households of the CER dataset [CER2012].

