

Calc 3 questions
undertext

Marcus Allen Denslow

Contents

Chapter 1	testing	Page 2
1.1	questions	2

Chapter 1

testing

1.1 questions

Oppgave

Evaluate the double integral

$$\iint_R x^2 y \, dA.$$

where R is the region bounded by $y = x^2$ and $y = 2x$.

Solution: First, find the intersection points of $y = x^2$ and $y = 2x$:

$$x^2 = 2x \implies x^2 - 2x = 0 \implies x(x - 2) = 0.$$

so $x = 0$ and $x = 2$. The region R is described by $x^2 \leq 2x$ for $0 \leq x \leq 2$.

set up the integral:

$$\iint_R x^2 y \, dA = \int_0^2 \int_{x^2}^{2x} x^2 y \, dy \, dx.$$

Evaluate the inner integral:

$$\begin{aligned} \int_{x^2}^{2x} x^2 y \, dy &= x^2 \left[\frac{y^2}{2} \right]_{x^2}^{2x} = x^2 \left(\frac{(2x)^2}{2} - \frac{(x^2)^2}{2} \right). \\ &= \frac{2(32)}{5} - \frac{128}{14} = \frac{64}{5} - \frac{64}{7} = \frac{448 - 320}{35} = \frac{128}{35}. \end{aligned}$$

Oppgave

Find the directional derivative of $f(x, y, z) = x^2 y z^3$ at the point $P(2, 1, -1)$ in the direction of the vector $\mathbf{v} = \mathbf{i} + 2\mathbf{j} - 2\mathbf{k}$