

Classical Maxwell Fields

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2026-02-06

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1.1 Rationalized Heaviside-Lorentz Units

The SI units are based on a unit of length of the order of human size originally related to the size of the earth, a unit of time approximately equal to the time between heartbeats, and a unit of mass related to the length unit and the mass of water. None of these depend on any even nearly fundamental physical quantities. Therefore many important physical equations end up with extra (needless) constants in them like c . Even with the three basic units defined, we could have chosen the unit of charge correctly to make ϵ_0 and μ_0 unnecessary but instead a very arbitrary choice was made $\mu_0 = 4\pi \times 10^{-7}$ and the Ampere is defined by the current in parallel wires at one meter distance from each other that gives a force of 2×10^{-7} Newtons per meter. The Coulomb is set so that the Ampere is one Coulomb per second. With these choices SI units make Maxwell's equations and our field theory look very messy.

In Rationalized Heaviside-Lorentz units we decrease the field strength by a factor of $\sqrt{4\pi}$ and increase the charges by the same factor, leaving the force unchanged.

Physicists have more often used CGS units in which the unit of charge and definition of the field units are set so that $\epsilon_0 = 1$ and $\mu_0 = 1$ so they need to show up in the equations. The CGS units are not perfect, however, and we will want to change them slightly to make our theory of the Maxwell Field simple. The mistake made in defining CGS units was in removing the 4π that show up in Coulombs law. Coulombs law is not fundamental and the 4π belonged there. We will correct this little mistake and move to Rationalized Heaviside-Lorentz Units by making a minor modification to the unit of charge and the units of fields. With this modification, our field theory will have few constants to carry around. As the name of the system of units suggests, the problem with CGS had been with π . We don't need to change the centimeter, gram or second to fix the problem.

$$\vec{E} \rightarrow \frac{\vec{E}}{\sqrt{4\pi}}$$