

Adaptive preprocessing methods

Global-aware

Input Time-Series

$$\mathbf{X}^{(i)} = \begin{bmatrix} x_{1,1}^{(i)} & \cdots & x_{1,j}^{(i)} & \cdots & x_{1,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ x_{t,1}^{(i)} & \cdots & x_{t,j}^{(i)} & \cdots & x_{t,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ x_{T,1}^{(i)} & \cdots & x_{T,j}^{(i)} & \cdots & x_{T,d}^{(i)} \end{bmatrix}$$

Normalization
Parameters
 $\theta \in \mathbb{R}^d$

$$\tilde{x}_{t,j}^{(i)} = f(x_{t,j}^{(i)}; \theta_j)$$

$\forall t = 1, 2, \dots, T$

$$\tilde{\mathbf{X}}^{(i)} = \begin{bmatrix} \tilde{x}_{1,1}^{(i)} & \cdots & \tilde{x}_{1,j}^{(i)} & \cdots & \tilde{x}_{1,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ \tilde{x}_{t,1}^{(i)} & \cdots & \tilde{x}_{t,j}^{(i)} & \cdots & \tilde{x}_{t,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ \tilde{x}_{T,1}^{(i)} & \cdots & \tilde{x}_{T,j}^{(i)} & \cdots & \tilde{x}_{T,d}^{(i)} \end{bmatrix}$$

Normalized Time-Series

Local-aware

Input Time-Series

$$\mathbf{X}^{(i)} = \begin{bmatrix} x_{1,1}^{(i)} & \cdots & x_{1,j}^{(i)} & \cdots & x_{1,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ x_{t,1}^{(i)} & \cdots & x_{t,j}^{(i)} & \cdots & x_{t,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ x_{T,1}^{(i)} & \cdots & x_{T,j}^{(i)} & \cdots & x_{T,d}^{(i)} \end{bmatrix}$$

Summary
Statistics
 $\lambda^{(i)} \in \mathbb{R}^d$

Normalization
Parameters
 $\theta \in \mathbb{R}^d$

$$\tilde{x}_{t,j}^{(i)} = f(x_{t,j}^{(i)}; \lambda_j^{(i)}, \theta_j)$$

$\forall t = 1, 2, \dots, T$

$$\tilde{\mathbf{X}}^{(i)} = \begin{bmatrix} \tilde{x}_{1,1}^{(i)} & \cdots & \tilde{x}_{1,j}^{(i)} & \cdots & \tilde{x}_{1,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ \tilde{x}_{t,1}^{(i)} & \cdots & \tilde{x}_{t,j}^{(i)} & \cdots & \tilde{x}_{t,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ \tilde{x}_{T,1}^{(i)} & \cdots & \tilde{x}_{T,j}^{(i)} & \cdots & \tilde{x}_{T,d}^{(i)} \end{bmatrix}$$

Normalized Time-Series

Static preprocessing methods

Preprocessing across time

Input Time-Series

Training dataset



$$\mathbf{X}^{(i)} = \begin{bmatrix} x_{1,1}^{(i)} & \cdots & x_{1,j}^{(i)} & \cdots & x_{1,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ x_{t,1}^{(i)} & \cdots & x_{t,j}^{(i)} & \cdots & x_{t,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ x_{T,1}^{(i)} & \cdots & x_{T,j}^{(i)} & \cdots & x_{T,d}^{(i)} \end{bmatrix}$$

Normalization
Statistics
 $\lambda \in \mathbb{R}^d$

$$\tilde{x}_{t,j}^{(i)} = f(x_{t,j}^{(i)}; \lambda_j)$$

$\forall t = 1, 2, \dots, T$

$$\tilde{\mathbf{X}}^{(i)} = \begin{bmatrix} \tilde{x}_{1,1}^{(i)} & \cdots & \tilde{x}_{1,j}^{(i)} & \cdots & \tilde{x}_{1,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ \tilde{x}_{t,1}^{(i)} & \cdots & \tilde{x}_{t,j}^{(i)} & \cdots & \tilde{x}_{t,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ \tilde{x}_{T,1}^{(i)} & \cdots & \tilde{x}_{T,j}^{(i)} & \cdots & \tilde{x}_{T,d}^{(i)} \end{bmatrix}$$

Normalized Time-Series

Preprocessing with time- and dimension-axis

Input Time-Series

Training dataset



$$\mathbf{X}^{(i)} = \begin{bmatrix} x_{1,1}^{(i)} & \cdots & x_{1,j}^{(i)} & \cdots & x_{1,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ x_{t,1}^{(i)} & \cdots & x_{t,j}^{(i)} & \cdots & x_{t,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ x_{T,1}^{(i)} & \cdots & x_{T,j}^{(i)} & \cdots & x_{T,d}^{(i)} \end{bmatrix}$$

Normalization
Statistics
 $\lambda \in \mathbb{R}^{d \times T}$

$$\tilde{x}_{t,j}^{(i)} = f(x_{t,j}^{(i)}; \lambda_{t,j}^{(i)})$$

$$\tilde{\mathbf{X}}^{(i)} = \begin{bmatrix} \tilde{x}_{1,1}^{(i)} & \cdots & \tilde{x}_{1,j}^{(i)} & \cdots & \tilde{x}_{1,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ \tilde{x}_{t,1}^{(i)} & \cdots & \tilde{x}_{t,j}^{(i)} & \cdots & \tilde{x}_{t,d}^{(i)} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ \tilde{x}_{T,1}^{(i)} & \cdots & \tilde{x}_{T,j}^{(i)} & \cdots & \tilde{x}_{T,d}^{(i)} \end{bmatrix}$$

Normalized Time-Series