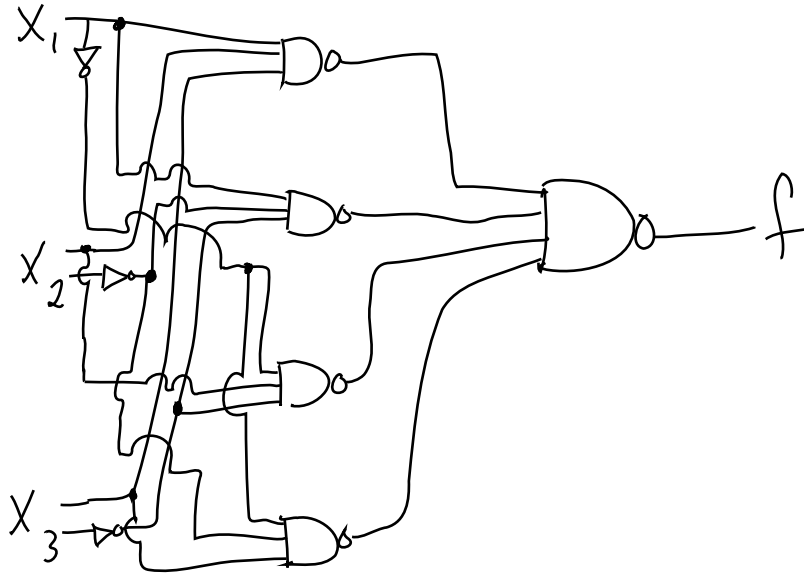


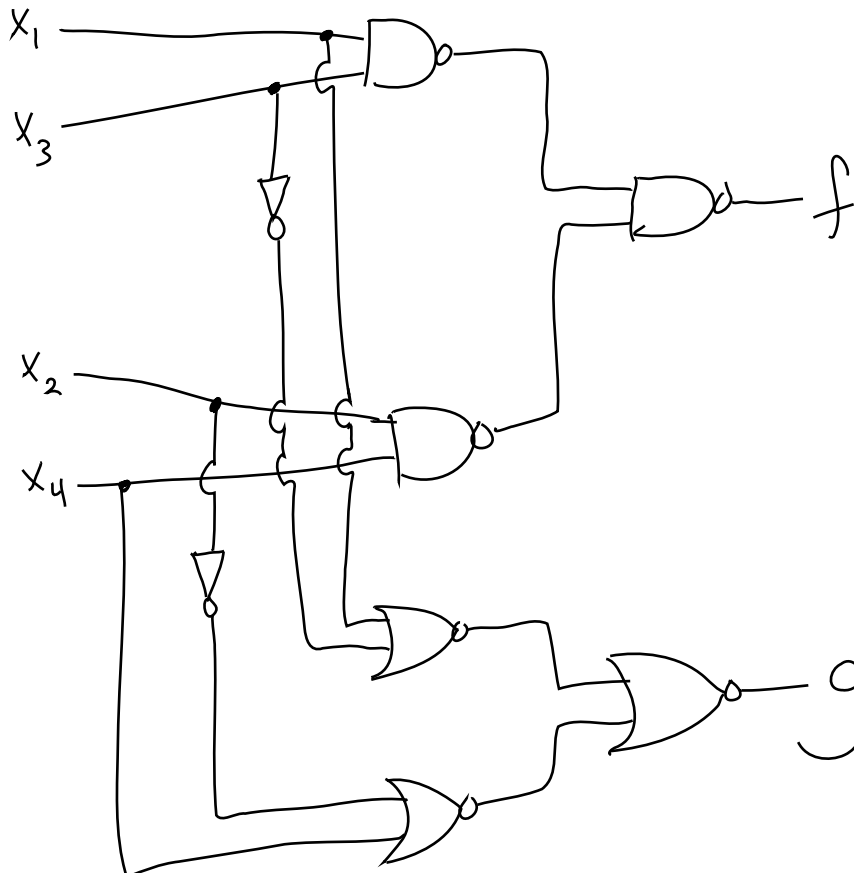
$$\begin{aligned}\mathbf{2.20:} \quad f(x_1, x_2, x_3) &= \sum m(3,4,6,7) = \overline{x_1}x_2x_3 + x_1\overline{x_2}\overline{x_3} + x_1x_2\overline{x_3} + x_1x_2x_3 \\ &= x_2x_3(\overline{x_1} + x_1) + x_1\overline{x_3}(\overline{x_2} + x_2) \\ &= x_2x_3 + x_1\overline{x_3}\end{aligned}$$

$$\begin{aligned}\mathbf{2.23:} \quad f(x_1, x_2, x_3) &= \prod M(0,1,5,7) \\ &= (x_1 + x_2 + x_3) \cdot (x_1 + x_2 + \overline{x_3}) \cdot (\overline{x_1} + x_2 + \overline{x_3}) \cdot (\overline{x_1} + \overline{x_2} + \overline{x_3}) \\ &= (x_1 + x_2 + x_3\overline{x_3}) \cdot (\overline{x_1} + x_2\overline{x_2} + \overline{x_3}) \\ &= (x_1 + x_2) \cdot (\overline{x_1} + \overline{x_3})\end{aligned}$$

2.37: $f(x_1, x_2, x_4, x_7) = \sum m(1, 2, 4, 7) = \overline{x_1}x_2x_3 + \overline{x_1}x_2\overline{x_3} + x_1\overline{x_2}x_3 + x_1x_2x_3$



2.39:



2.45: $f = \overline{x_1 x_2} x_3 + x_1 x_3 + x_2 x_3 + x_1 x_2 \overline{x_3}$

$$= x_3 (\overline{x_1 x_2} + x_1) + x_2 (x_3 + x_1 \overline{x_3})$$

$$= x_3 (\overline{x_2} + x_1) + x_2 (x_3 + x_1)$$

$$= \overline{x_2} x_3 + x_1 x_3 + x_2 x_3 + x_1 x_2$$

$$= x_3 (\overline{x_2} + x_2) + x_1 x_3 + x_1 x_2$$

$$= x_3 + x_1 x_3 + x_1 x_2 = x_3 + x_1 x_2$$

$$(\text{use } (x \cdot (x + y)) = x)$$