

CSC205 section 1 Spring 2015
Homework 4

How to Submit:

Please submit your solutions (parts A and B separately) through Blackboard. Remember to put your name and homework number on all the documents that you submit as attachments.

Total possible points in this homework: 4 for Part B

(You receive 1 bonus point towards Part A if you get all Part A questions correct.)

Part A

1. Answer the following questions regarding sequential logic:

Complete the following table describing the output Q of the JK flip-flop, at time $t+1$, with respect to its inputs, J and K , at time t .

| Time t | $J(t)$ | $K(t)$ | $Q(t)$ | Reason: |
|----------|--------|--------|--------|--|
| 0 | 0 | 0 | 0 | <i>Initial value of Q</i> |
| 1 | 1 | 1 | | |
| 2 | 0 | 1 | | |
| 3 | 0 | 0 | | |
| 4 | 1 | 1 | | |
| 5 | 0 | 0 | | |
| 6 | 1 | 0 | | |
| 7 | 0 | 0 | | |

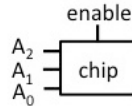
2. You are to design a mini board with the capacity of 32-byte byte-addressable memory. You are given as many of the 8-byte byte-addressable memory chips as you need.
 - a. How many 8byte chips are needed?
 - b. How many address lines go into the board?
 - c. Of the address lines that go into the board, how many go to each chip?
 - d. How many lines must be decoded for the chip-select inputs?
 - e. Specify the size of the decoder needed on the board.

Part B

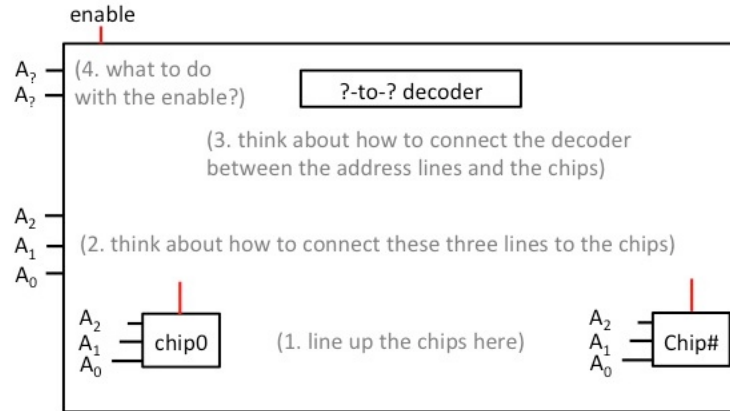
1. [1 pt] This question extends from the previous question. Suppose each 8-byte memory chip has three address pins (A_2 , A_1 , A_0) and has one enable pin. Show the circuitry of your 32-byte memory board. You may want to include an enable pin for

your board. (Normally, a chip has a read enable and a write enable, but we simplify them to just one, and ignore any clock pulse here.)

Hint: You could represent each chip with the following simple block. You could ignore the data lines since they are not the focus of this question, (but feel free to add them for completeness if you like.)

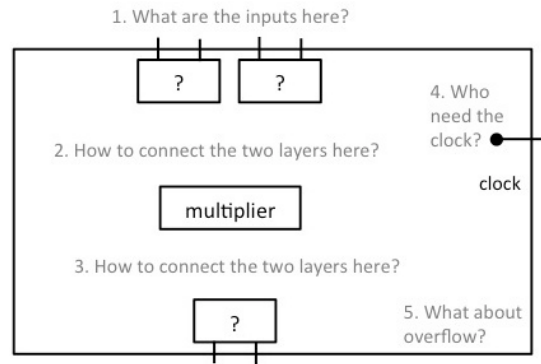


Start by drawing a board like this. And follow the steps below.



2. [Total 3 pts] This question investigates the basic circuitry in and around a *multiplier*, a unit that does multiplication. You are given the following:
 - i. a bunch of logic gates, flip-flops, and simple circuits covered in the class
 - ii. a clock;
 - iii. two 2-bit registers, RegA and RegB, storing inputs $A=(A_1,A_0)$ and $B=(B_1,B_0)$, which represent two unsigned integers;
 - iv. one 2-bit register, RegD.
- a. [0.5 pt] For this part, you may consider the multiplier as a black box. Show how to implement a simple system with two registers, RegA and RegB, and a *multiplier* that multiplies A and B to give the 2-bit result D to be stored in another register, RegD. An overflow line indicates whether an overflow has occurred.

Hint: Your circuit might look something like this:



- b. [0.5 pt] Would you use level-triggered or edge-triggered registers for this set up? Explain.

Hint: Recall that a flip-flop is like a camera. With an edge-triggered flip-flop, the shutter opens and shuts in a very short time (when the clock moves from low to high, for instance). With a level-triggered flip-flop, the shutter is left open as long as the clock is steadily high.

- c. [1 pt] Show the circuitry inside the multiplier.

Hints: Express the multiplication of A by B in terms of intermediates (M0, M1, M2 and M3). Express M0 to M1 as Boolean expressions in terms of inputs A and B. Then express the outputs D0 to D3 in terms of the intermediates. Finally, build your circuit based on the Boolean expressions of D0 to D3.

$$\begin{array}{r}
 \begin{array}{cc} & A1 \quad A0 \\ * & B1 \quad B0 \\ \hline & M1 \quad M0 \\ + & M3 \quad M2 \quad 0 \\ \hline D3 \quad D2 \quad D1 \quad D0 \end{array}
 \end{array}$$

- d. [0.5 pt] Show what happens to the value of the register RegD when the following inputs are supplied to the system at different times.

| Time t | RegA | | RegB | | RegD | |
|-------------|------|----|------|----|------|----|
| | A1 | A0 | B1 | B0 | D1 | D0 |
| 0 | 0 | 0 | 0 | 0 | - | - |
| 1 | 0 | 1 | 0 | 1 | 0 | 0 |
| 2 | 1 | 1 | 0 | 1 | 0 | 1 |
| 3 | 1 | 0 | 0 | 1 | 1 | 1 |
| 4 | 1 | 0 | 1 | 1 | 1 | 0 |
| 5 | 1 | 0 | 0 | 0 | 1 | 0 |

overflow

- e. [0.5 pt] We have mentioned in class that the delay in a simple combinational circuit is negligible. With large circuits, such as a multiplier that processes two 32-bit integers, the delay is no longer negligible. What constraints does the circuit impose on the CPU's clock for the instruction cycle?