# Package 'bayesQRsurvey'

# September 26, 2025

Title Bayesian quantile regression models for complex survey data analysis

Version 0.1.0

**Description** Bayesian quantile regression models for complex survey data analysis, both single and multiple-output are supported. To speed up the calculations, all algorithms are implemented in C++ using 'Rcpp', 'RcppArmadillo', and 'RcppEigen', and called from R.

```
License MIT + file LICENSE
Encoding UTF-8
Roxygen list(markdown = TRUE)
RoxygenNote 7.3.2
LinkingTo Rcpp,
     RcppArmadillo,
     RcppEigen
Imports Rcpp,
     stats,
     graphics,
     methods,
     plotly,
     geometry,
     pracma,
     ggplot2,
     rlang,
     posterior
Suggests MASS,
     knitr,
     rmarkdown,
     grDevices,
     testthat (>= 3.0.0)
VignetteBuilder knitr
Config/testthat/edition 3
SystemRequirements BLAS, LAPACK
URL https://github.com/torodriguezt/bayesQRsurvey
BugReports https://github.com/torodriguezt/bayesQRsurvey/issues
```

2 bqr.svy

# **Contents**

									 						2
									 						4
									 						6
									 						8
									 						8
									 						10

Index 12

bqr.svy

Bayesian quantile regression for complex survey data

## **Description**

bqr.svy implements Bayesian methods for estimating quantile regression models for complex survey data analysis regarding single (univariate) outputs. To improve computational efficiency, the Markov Chain Monte Carlo (MCMC) algorithms are implemented in C++.

# Usage

```
bqr.svy(
  formula,
  weights = NULL,
  data = NULL,
  quantile = 0.5,
  method = c("ald", "score", "approximate"),
  prior = NULL,
  niter = 50000,
  burnin = 10000,
  thin = 1,
  verbose = TRUE
)
```

# **Arguments**

formula	a symbolic description of the model to be fit.
weights	an optional numerical vector containing the survey weights. If NULL, equal weights are used.
data	an optional data frame containing the variables in the model.
quantile	numerical scalar or vector containing quantile(s) of interest (default=0.5).
method	one of "ald", "score" and "approximate" (default="ald").
prior	a bqr_prior object of class "prior". If omitted, a vague prior is assumed (see prior).
niter	number of MCMC draws.
burnin	number of initial MCMC draws to be discarded.
thin	thinning parameter, i.e., keep every keepth draw (default=1).
verbose	logical flag indicating whether to print progress messages (default=TRUE).

bqr.svy 3

#### **Details**

The function bqr.svy can estimate three types of models, depending on method specification.

- "ald" asymmetric Laplace working likelihood
- "score" score based working likelihood function
- "approximate" pseudolikelihood function based on a Gaussian approximation

#### Value

An object of class "bqr.svy", containing:

beta Posterior mean estimates of regression coefficients.

draws Posterior draws from the MCMC sampler.

accept\_rate Average acceptance rate (if available).

quantile The quantile(s) fitted.
prior Prior specification used.

formula, terms, model

Model specification details.

runtime Elapsed runtime in seconds.

#### References

Nascimento, M. L. & Gonçalves, K. C. M. (2024). Bayesian Quantile Regression Models for Complex Survey Data Under Informative Sampling. *Journal of Survey Statistics and Methodology*, 12(4), 1105–1130.

#### **Examples**

```
# Generate population data
set.seed(123)
    <- 10000
x1_p <- runif(N, -1, 1)
x2_p \leftarrow runif(N, -1, 1)
y_p < -2 + 1.5 * x1_p - 0.8 * x2_p + rnorm(N)
# Generate sample data
n <- 500
z_{aux} \leftarrow rnorm(N, mean = 1 + y_p, sd=.5)
p_{aux} < 1 / (1 + exp(2.5 - 0.5 * z_{aux}))
s_ind <- sample(1:N, n, replace = FALSE, prob = p_aux)</pre>
     <- y_p[s_ind]
x1_s <- x1_p[s_ind]
x2_s <- x2_p[s_ind]
      <- 1 / p_aux[s_ind]
data <- data.frame(y = y_s, x1 = x1_s, x2 = x2_s, w = w)
# Basic usage with default method ('ald') and priors (vague)
fit1 <- bqr.svy(y \sim x1 + x2, weights = w, data = data)
# Specify informative priors
prior<- prior(</pre>
beta_mean = c(2, 1.5, -0.8),
 beta_cov = diag(c(0.25, 0.25, 0.25)),
```

4 mo.bqr.svy

```
sigma_shape = 1,
sigma_rate = 1
)
fit2 <- bqr.svy(y ~ x1 + x2, weights = w, data = data, prior = prior)

# Specify different methods
fit_score <- bqr.svy(y ~ x1 + x2, weights = w, data = data, method = "score")
fit_approx <- bqr.svy(y ~ x1 + x2, weights = w, data = data, method = "approximate")</pre>
```

mo.bqr.svy

Multiple-Output Bayesian quantile regression for complex survey data

### **Description**

mo.bqr.svy implements a Bayesian approach to multiple-output quantile regression for complex survey data analysis. The method builds a quantile region based on a directional approach. To improve computational efficiency, an Expectation-Maximization (EM) algorithm is implemented instead of the usual Markov Chain Monte Carlo (MCMC).

## Usage

```
mo.bqr.svy(
  formula,
  weights = NULL,
  data = NULL,
  quantile = 0.5,
  prior = NULL,
  U = NULL,
  gamma_U = NULL,
  n_dir = NULL,
  epsilon = 1e-06,
  max_iter = 1000,
  verbose = FALSE
)
```

## **Arguments**

formula	a symbolic description of the model to be fit.
weights	an optional numerical vector containing the survey weights. If NULL, equal weights are used.
data	an optional data frame containing the variables in the model.
quantile	numerical scalar or vector containing quantile(s) of interest (default=0.5).
prior	a bqr_prior object of class "prior". If omitted, a vague prior is assumed (see prior).
U	an optional $d \times K$ -matrix of directions, where $d$ indicates the response variable dimension and $K$ indicates indicates the number of directions.
gamma_U	an optional list with length equal to $K$ for which each element corresponds to $d \times (d-1)$ -matrix of ortoghonal basis for each row of ${\sf U}$ .

mo.bqr.svy 5

n\_dir

numerical scalar corresponding to the number of directions (if U and gamma\_U are not supplied).

epsilon

numerical scalar indicating the convergence tolerance for the EM algorithm (default = 1e-6).

max\_iter

numerical scalar indicating maximum number of EM iterations (default = 1000).

verbose

logical flag indicating whether to print progress messages (default=FALSE).

#### Value

An object of class "mo.bqr.svy" containing:

call The matched call formula The model formula terms The terms object

quantile Vector of fitted quantiles

prior List of priors used for each quantile

fit List of fitted results for each quantile, each containing one sub-list per direction

coefficients Coefficients from the first quantile

n\_dir Number of directions

U Matrix of projection directions  $(d \times K)$ 

Gamma\_list List of orthogonal complement bases, one per direction

n\_obsn\_warsNumber of observationsNumber of covariates

 ${\tt response\_dim} \qquad {\tt Dimension} \ \ {\tt of} \ \ {\tt the} \ \ {\tt response} \ d$ 

# **Examples**

```
library(MASS)
# Generate population data
set.seed(123)
     <- 10000
data <- mvrnorm(N, rep(0,3), matrix(c(4,0,2,0,1,1.5,2,1.5,9),3,3))
x_p <- as.matrix(data[,1])</pre>
y_p \leftarrow data[,2:3]+cbind(rep(0,N),x_p)
# Generate sample data
n <- 500
z_{aux} < rnorm(N, mean = 1 + y_p, sd=.5)
p_{aux} < 1 / (1 + exp(2.5 - 0.5 * z_{aux}))
s_ind <- sample(1:N, n, replace = FALSE, prob = p_aux)</pre>
y_s \leftarrow y_p[s_ind,]
x_s \leftarrow x_p[s_ind,]
   <- 1 / p_aux[s_ind]
data_s < - data.frame(y1 = y_s[,1], y2 = y_s[,2], x1 = x_s, w = w)
# Basic usage with default priors when U and gamma_U are given
fit1 <- mo.bqr.svy(cbind(y1, y2) \sim x1, weights = w, data = data_s, quantile = c(0.1, 0.2),
 U = matrix(c(0,1,1/sqrt(2),1/sqrt(2)),2),
 gamma_U = list(c(1,0),c(1/sqrt(2),-1/sqrt(2))))
```

6 plot.bqr.svy

```
# Basic usage with default priors when n_dir is given fit2 <- mo.bqr.svy(cbind(y1, y2) \sim x1, weights = w, data = data_s, quantile = c(0.1, 0.2), n_dir=2)
```

plot.bqr.svy

Plot Method for Bayesian Weighted Quantile Regression (Survey)

## **Description**

Plot method for objects of class bqr.svy produced by bqr.svy(). It can display fitted quantile curves, coefficient—quantile profiles, MCMC trace plots, and posterior densities.

# Usage

```
## S3 method for class 'bqr.svy'
plot(
  х,
  y = NULL,
  type = c("fit", "quantile", "trace", "density"),
  predictor = NULL,
  tau = NULL,
  which = NULL,
  add_points = TRUE,
  combine = TRUE,
  show_ci = FALSE,
  ci_probs = c(0.1, 0.9),
  at = NULL,
  grid_length = 200,
  points_alpha = 0.4,
  point_size = 1.5,
  line_size = 1.2,
  main = NULL,
  use_ggplot = TRUE,
  theme_style = c("minimal", "classic", "bw", "light"),
  color_palette = c("viridis", "plasma", "set2", "dark2"),
  add_h0 = TRUE,
  add_ols = FALSE,
  ols_fit = NULL,
  ols_weights = NULL,
)
## S3 method for class 'bwqr_fit'
plot(x, ...)
## S3 method for class 'bwqr_fit_multi'
plot(x, ...)
```

#### **Arguments**

Х

Object of class bqr.svy.

plot.bgr.svy 7

y Ignored (S3 signature).

type One of "fit", "quantile", "trace", "density".

predictor (fit) Name of a numeric predictor; if NULL, the first numeric predictor (excluding

the response) is used.

tau Quantile(s) to plot; must appear in x\$quantile. If NULL, all available are used.

which (quantile/trace/density) Coefficient name or index to display.

add\_points (fit) Logical; overlay observed data points.

combine (fit) Logical; if multiple tau: TRUE overlays curves in one panel; FALSE uses one

panel per quantile.

show\_ci (fit) Logical; draw credible bands.

ci\_probs (fit) Length-2 numeric vector with lower/upper probabilities for credible bands.

at (fit) Named list of fixed values for non-predictor covariates (see Details).

grid\_length (fit) Integer; number of points in the predictor grid.

points\_alpha (fit) Point transparency in [0,1].

point\_size (fit) Point size.

line\_size (fit/quantile) Line width for fitted/summary lines.

main Optional main title.

use\_ggplot Logical; if TRUE, return a ggplot object.

theme\_style (ggplot) One of "minimal", "classic", "bw", "light". color\_palette (ggplot) One of "viridis", "plasma", "set2", "dark2". add\_h0 (quantile) Logical; add a horizontal reference at y=0.

add\_ols (quantile) Logical; add the OLS estimate (dotted line) for the selected coeffi-

cient.

ols\_fit (quantile) Optional precomputed lm object; if NULL, an lm() is fitted internally

using x\$model and x\$terms.

ols\_weights (quantile) Optional numeric vector of weights when fitting OLS internally (length

must match nrow(x\$model)).

... Accepted for compatibility; ignored by internal plotting code.

#### **Details**

### Supported plot types:

- type = "fit": Fitted quantile curves versus a single numeric predictor. Optionally overlay observed points and credible bands. Other covariates can be held fixed via at.
- type = "quantile": A single coefficient as a function of the quantile  $\tau$ . Optionally add a reference line at 0 and the corresponding OLS estimate.
- type = "trace": MCMC trace for one selected coefficient at a chosen  $\tau$ .
- type = "density": Posterior density for one selected coefficient at a chosen  $\tau$ .

#### Notes:

- tau must be included in x\$quantile. If NULL, all available quantiles in the object are used.
- For type = "fit", predictor must be a numeric column in the original model. If NULL, the first numeric predictor (different from the response) is chosen automatically.

8 prior

• For type = "fit", at is a named list (list(var = value, ...)) used to fix other covariates while plotting versus predictor. Provide valid levels for factors.

• When use\_ggplot = TRUE, a ggplot object is returned and the appearance is controlled by theme\_style and color\_palette. Otherwise, base graphics are used and the function returns invisible(NULL).

#### Value

invisible(NULL) for base R graphics, or a ggplot object if use\_ggplot = TRUE.

## **Examples**

print.bayesQRsurvey

Print methods for bayesQRsurvey model objects

# Description

print.bayesQRsurvey is an S3 method that prints the content of an S3 object of class bqr.svy or mo.bqr.svy to the console.

# Usage

```
## S3 method for class 'bqr.svy'
print(x, digits = 3, ...)
## S3 method for class 'mo.bqr.svy'
print(x, digits = 3, ...)
```

prior

Create prior for Bayesian quantile regression models for complex survey data

#### **Description**

prior creates prior distributions for both single (bqr.svy) and multiple-output (mo.bqr.svy) Bayesian quantile regression models for complex survey data.

prior 9

### Usage

```
prior(
  beta_x_mean = NULL,
  beta_x_cov = NULL,
  sigma_shape = 0.001,
  sigma_rate = 0.001,
  beta_y_mean = NULL,
  beta_y_cov = NULL
)
```

#### **Arguments**

```
beta_x_mean vector of prior means for the regression coefficients. (default = NULL). beta_x_cov prior covariance matrix for the regression coefficients. (default = NULL). sigma_shape shape parameter for inverse Gamma prior for \sigma^2. (default = 0.001). rate parameter for inverse Gamma prior for \sigma^2. (default = 0.001). prior means for the coefficients related to the variables that emerge from the product between the orthogonal basis and the outputs (default = NULL). beta_y_cov prior covariance matrix for the coefficients related to the variables that emerge from the product between the orthogonal basis and the outputs. (default = NULL).
```

#### **Details**

The function prior builds prior distributions for the three methods implemented in the function bqr.svy and for the multiple-output quantile regression implemented in the function mo.bqr.svy. Every nonspecified prior parameter will get the default value.

- method = "ald" in function bqr.svy allow the specification of hyperparameters beta\_x\_mean, beta\_x\_cov, sigma\_shape, and sigma\_rate.
- method = "score" in function bqr.svy allow the specification of hyperparameters beta\_x\_mean and beta\_x\_cov.
- method = "approximate" in function bqr.svy allow the specification of hyperparameters beta\_x\_mean and beta\_x\_cov.
- In function mo.bqr.svy, the specification of hyperparameters beta\_x\_mean,beta\_x\_cov, sigma\_shape, sigma\_rate, beta\_y\_mean, and beta\_y\_cov are allowed.

# Value

An object of class "prior".

#### See Also

```
bqr.svy, mo.bqr.svy, summary
```

#### **Examples**

```
# Create informative prior objects regarding the single-output methods prior_ald <- prior( beta_x_mean = c(2, 1.5, -0.8), beta_x_cov = diag(c(0.25, 0.25, 0.25)),
```

```
sigma_shape = 3,
  sigma_rate = 2
prior_score <- prior(</pre>
 beta_x_mean = c(2, 1.5, -0.8),
 beta_x_cov = diag(c(0.25, 0.25, 0.25))
prior_approximate <- prior(</pre>
 beta_x_mean = c(2, 1.5, -0.8),
  beta_x_cov = diag(c(0.25, 0.25, 0.25))
# Estimate the model parameters with informative prior
fit_ald <- bqr.svy(y ~ x1 + x2, weights = w, data = mydata, prior = prior_ald)</pre>
fit_scr <- bqr.svy(y ~ x1 + x2, weights = w, data = mydata, method = "score", prior = prior_score)
fit_apx \leftarrow bqr.svy(y \sim x1 + x2, weights = w, data = mydata, method = "approximate", prior = prior_approximate)
# Create an informative prior object regarding the multiple-output method
prior_mo <- prior(</pre>
  beta_x_mean = c(2, 1.5, -0.8),
  beta_x_{cov} = diag(c(0.25, 0.25, 0.25)),
  sigma_shape = 3,
  sigma_rate = 2,
 beta_y_mean = 1,
 beta_y_cov = 0.25
# Estimate the model parameters with informative prior
fit_mo <- mo.bqr.svy(cbind(y1, y2) ~ x1 + x2, weights = w, data = mydata, prior = prior_mo, n_dir = 10)
```

summary.bayesQRsurvey Summary methods for bayesQRsurvey

#### Description

summary.bayesQRsurvey is an S3 method that summarizes the output of the bqr.svy or mo.bqr.svy function. For the bqr.svy the posterior mean, posterior credible interval and convergence diagnostics are calculated. For the mo.bqr.svy the iterations for convergence, the MAP and the direction are calculated.

# Usage

```
## S3 method for class 'bqr.svy'
summary(object, probs = c(0.025, 0.975), digits = 2, ...)
## S3 method for class 'mo.bqr.svy'
summary(object, digits = 4, ...)
```

# Arguments

object An object of class mo.bqr.svy.

probs Two-element numeric vector with credible interval probabilities. Default c(0.025,

0.975).

digits Integer; number of decimals used by printing helpers. Default 4.

... Unused.

## Value

An object of class summary.bqr.svy with one block per  $\tau.$ 

An object of class summary.mo.bqr.svy.

# **Index**

```
bqr.svy, 2, 9

mo.bqr.svy, 4, 9

plot(plot.bqr.svy), 6

plot.bqr.svy, 6

print.bayesQRsurvey, 8

print.bqr.svy(print.bayesQRsurvey), 8

prior, 2, 4, 8

summary, 9

summary.bayesQRsurvey, 10

summary.bqr.svy

(summary.bayesQRsurvey), 10

summary.mo.bqr.svy

(summary.bayesQRsurvey), 10
```