## Homework 08

## MO412 - Network Science

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May 2021

Two people are discussing accelerated growth, where  $m(t)=t^{\theta}$  links are added to the network with each new node. One person stands by the statement in the book, that accelerated growth leads to a scale-free network with exponent

$$\gamma = 3 + \frac{2\theta}{1 - \theta}$$

The other person used the rate equation and reached a different formula:

$$\gamma = 1 + \frac{2}{1+\theta}$$

Your task is to test these hypotheses for  $\theta = 1/2$ .

Person 1,  $\theta = \frac{1}{2}$ 

$$\gamma = 3 + \frac{2\theta}{1 - \theta}$$

$$\gamma = 5$$

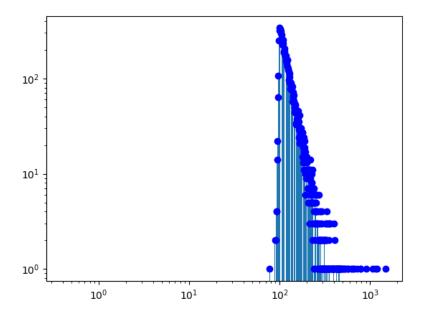
Person 2,  $\theta = \frac{1}{2}$ 

$$\gamma = 1 + \frac{2}{1+\theta}$$
 
$$\gamma = 2.33$$

(a) Start with a network with just one node at time t=0. Then, at each time step  $t\geq 1$ , add one new node to the network with  $m(t)=\lfloor \sqrt{t}\rfloor$  links to previous nodes. The other extreme of each link will be chosen by preferential attachment, that is, with a probability proportional to the degree of each node (not considering the new links). This may produce multiple edges. Let them be. Repeat until you reach N=10000.

```
\mathbf{def} \ \mathbf{m_t}(\mathbf{t}):
  return math.floor(math.sqrt(t))
def network(nodes):
  G = nx.Graph()
  G. add_node(0)
  repeated\_nodes = [0]
  t=0
  while t < nodes:
    m = m_t(t)
    choose = random.choices(rep,k=m)
    G. add_edges_from ([(t,choose[i]) for i in range(m)
        ])
    rep += choose
    rep += [t] * m
    t += 1
  return G
G = network(10000)
```

 $(b) \ \mbox{Plot}$  the degree distribution of the resulting network in log-log scale.

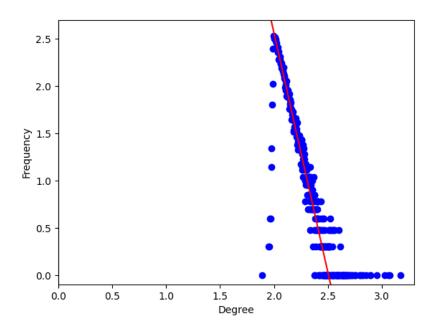


```
degree_freq = nx.degree_histogram(G)
degrees = range(len(degree_freq))

plt.loglog(degrees, degree_freq, 'bo')
plt.bar(degrees, degree_freq)
plt.show()
```

## (c) Fit a straight line to the points as best you can and estimate the $\gamma$ exponent. Did you get a value close to one of the proposed formulas?

The value of  $\gamma$  is 5.05921063, it is closer to what the first person said.



```
dee_log = []
freq_log = []

for i in range(len(degrees)):
    if(degrees[i] != 0 and degree_freq[i] != 0):
        dee_log.append(math.log10(degrees[i]))
        freq_log.append(math.log10(degree_freq[i]))

reg = linear_model.LinearRegression()
reg.fit(np.array(dee_log[10:220]).reshape(-1,1),np.
        array(freq_log[10:220]))
print("gamma :",reg.coef_)

rango = np.arange(1,3,0.1)
regression = reg.predict(rango.reshape(-1,1))
```

```
plt.xlim(0,3.3)
plt.ylim(-0.1,2.7)

plt.plot(dee_log, freq_log, 'bo')
plt.plot(rango, regression, 'r')

plt.xlabel('Degree')
plt.ylabel('Frequency')
plt.show()
```