

Rotating a vector in R2

Lua 5.2 Rotation angle in degree.

Assigned with quick input `tVar.q('\\theta=90',true)`

$$\theta = \text{rad}(\theta) = \text{rad}(45.000) = 0.785 \quad (1)$$

Rotation matrix in R2

$$\mathbf{A} = \begin{pmatrix} \cos(\theta) & (-\sin(\theta)) \\ \sin(\theta) & \cos(\theta) \end{pmatrix} = \begin{pmatrix} 0.707 & (-0.707) \\ 0.707 & 0.707 \end{pmatrix} \quad (2)$$

$$\vec{e}_x = \begin{pmatrix} 1.000 \\ 0.000 \end{pmatrix} \quad (3)$$

$$\vec{e'} = \mathbf{A} \cdot \vec{e}_x = \begin{pmatrix} 0.707 & (-0.707) \\ 0.707 & 0.707 \end{pmatrix} \cdot \begin{pmatrix} 1.000 \\ 0.000 \end{pmatrix} = \begin{pmatrix} 0.707 \\ 0.707 \end{pmatrix} \quad (4)$$